Machine Learning Exercises (chapter3)
2. Part 1: We define Sasa training set of Xx {0,1}. If the training set contain
a posetive instance (9ct), the algorithm returns hat, otherwise, it
ceturns ho which is an ERM (we assume the fact that there can be
at most a point with lable 1) > Ls(hs)=0
2. Part 2: (PAC lear nability) - Assume that get \$5, if D(fy+4) < € then
L(D,f)(h) < & for all h in H. Suppose that D(f4+3)>E,
then: triex st. 9/# 2 -> D(frig) <1-E. then we have:
{S x: L(D,f)(hs) > ε} = {S x: 2+ ≠ S x · D((2+2) > ε} =
= 951x: 4x'ES1x D(5x') <1-E}
> Dm (f 3 x: L(0, f)(hs) > Et) = Dm(fs) x: 4x' (s x D(fx'4) < 1-Et)
< (1-€) ^m < e-€m
Let $8 \in (0,1)$ st. $e^{-\epsilon m} = m = log(\frac{1}{8})$ Hence H is PAC leanable with $m_H \leq log(\frac{1}{8})$

3. Assume that ERM algorithm A takes S as training set and it returns the tightest circle that contains all posetive instances. Define his as output function and its radius by rs, we having Realizability assumption (existing at EH that its radius is r*) Now Let E, SE(0,1), we suppose that there is a rwhich rxx* then: Dx (fx: r < 11911 < r * }) = E / E = f & P(LD(hs)>E) = P(4; ES s.t. 4 E) = M: (1-P(x; EE = (1-E)m < em E 8 eme 38 Now let SE (0,1), the we have sa m> log(1/8) Hence His PAC-leanable and MH(E, 8) (log (1/8)

5. Hp: set of bad hypotheses / we suppose the help s.t. L(Dm, f) (h) > E $P[L(S+)(h)=0] = \prod_{i=1}^{m} P_{X\sim 0_i}[f(x)=h(x)] =$ $= \prod_{i=2}^{m} P_{x \sim 0_i} [f(x) - h(x)] \leq \left(\prod_{m=2}^{m} P_{x \sim 0_i} [f(x) - h(x)] \right) =$ (by the geometric arithmetic) $= \left(\left[P_{N-D\bar{m}} \left[f(x) = h(x) \right] \right)^{m} \leq (1-\epsilon)^{m} \leq e^{-\epsilon m}$ Therefore we have, P[3h EH: L(0,1)(h)>E, L(s,1)(h)=0] < |HB|e < HL-E,

6. We define hs:= A(s), D: distribution over Xxf0,14 then we
have: Dm (} Slx: Lo(hs) > min Lo(h) + Eq) < 8
Suppose &EH: f is a true labeling function.
(determine probability of 91 over y.)
If m/m+(8,8), A(s) will perform and out pat h. then:
Darif S: Lou, (h) > E1) <s his="" pac-lernable<="" td=""></s>
with realizability: min Lp(h) =0, hence A is a PAC leamer of H

7. Suppose & EX and P: conditional probability of a positive lable
given &, then we have:
P[fo(x) + Y X = x] = P[Y=0 X=x]1[P> = 1 X=x]1[P<=] P[Y=1 X=x]1[P<=]
$= (1-\rho) 1_{\left[\rho\right>\frac{1}{2}\right]} + \rho. 1_{\left[\rho<\frac{1}{2}\right]}$
=min {P, 1-P}
suppose that g is classifier g: X-10,19:
P[g(x) + Y x=x] = P[g(x)=0 X=x]P[Y=1 X=n]+P[g(x)=1 X=n]
+P[Y=0 X=91]=
= $P[X=9]p+P[g(x)=1 X=n](1-p)$
> P[g(x)=0 X=4]minfp,1-p3+P[g(x)=1 X=4]min
$= \min\{p, 1-p\}$
Therefore:
[9)= E(x, Y) ~ [1 [9(x) + Y]] = E x ~ Pm [E Y ~ DY x [1 [9(x) + Y] X - 9]] >
> Exmon[E[1[fo(m) *Y] X.M] = E[1[fo(x) *Y]] - Lp(fo)
Heree:
$L_D(f_0) \leq L_D(g)$
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Machine Learning Exercises (chapter 5)

5.2 - a) pros and cons: (Algorithm A)

Pros: It has small Eest, because of less complemity (less prone to overfiting)
This Algorithm can easily interpret models in a plot (dim: 2d)

cons: Inductive bias might be too large (high Eapp) and we can't use A, P, I in our model

(Algorithm B)

Pros: Smaller Mann inductive bias, reducing risk of under fitting.

Bhas

These small Eapp.

cons: It has larger Eest. because of that our model may lead to over fitting

2b) Increasing size of sitraing data set) leads to Ls(hs) is a better estimate of Lp(hs). It means lower & Eest, becase of that B is better than A.

Eapp can be reduced by choosing Algorithm B (complenity)

Eest can be decreased with the size of S.