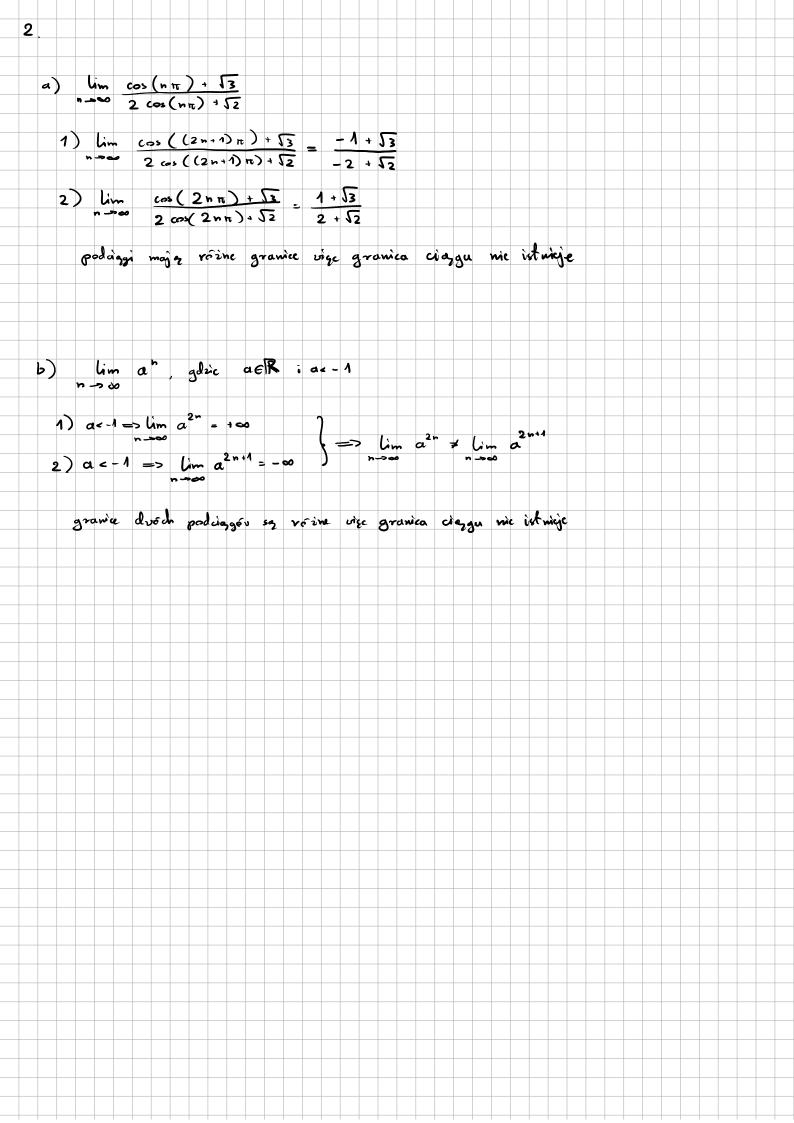


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e) \lim_{n\to\infty} \sqrt{\frac{1}{n^2}} \cdot 4^n + n \cdot 3^n + 5n^3 = 4 2 to icrollema o 3 chargech
\sqrt{\frac{1}{n^2}} 6^n \le \sqrt{\frac{1}{n^2}} 6^n + n \cdot 3^n + 5n^3 \le \sqrt{n^3 6^n + n^3 6^n} + n^3 6^n
            a_n = \binom{n+2}{n} = \frac{(n+2)(n+1)}{2} = \frac{(n+2)(n+1)}{2}
            b_n = 1 + 2 + 3 + \dots + n = \frac{1+n}{2} \cdot n = \frac{(n+1) \cdot n}{2}
   \lim_{n \to \infty} \frac{(n+2)(n+1)}{2} = \lim_{n \to \infty} \frac{n+1}{n} = \lim_{n \to \infty} \frac{1+\frac{1}{n}}{n} = 1
3) \lim_{n\to\infty} \left(1+\frac{1}{\sqrt{n}}\right)^n = \lim_{n\to\infty} \left(1+\frac{1}{\sqrt{n}}\right)^{\sqrt{n}} = \left[e^{\infty}\right] = \infty
      \lim_{n\to\infty} \int_{n} = +\infty \implies \lim_{n\to\infty} \left(1 + \frac{1}{\sqrt{n}}\right) = e
h) \lim_{n\to\infty} \left(\frac{2n^2+2n+1}{2n^2+2}\right)^{n+1} = \lim_{n\to\infty} \left(\frac{2n^2+2+2n+1-2}{2n^2+2}\right)^{n+1}
                                                                                                                                    (2n-1)(n+1) = 2n^2+2n-n-1
 \lim_{n\to\infty} \left(1 + \frac{2n-1}{2n^{2+1}}\right) = \lim_{n\to\infty} \left(1 + \frac{1}{2n^{2+2}}\right)^{n+1}
                                                                                                                                \lim_{n \to \infty} \frac{2n^2 + n - 1}{2n^2 + 2} = 1
 \lim_{n \to \infty} \left( 1 + \frac{2n^2 + 2}{2n^2 + 2} \right) \frac{2n - 1}{2n^2 + 2} = e^1 = e
                                                                                                                              \lim_{n\to\infty}\frac{2n^2+2}{2n-1}=\infty
i) \lim_{n\to\infty} \left(\frac{n+1}{n}\right)^{20/9} = \lim_{n\to\infty} \left(1+\frac{1}{n}\right)^{20/9} = \lim_{n\to\infty} \left(1+\frac{1}{n}\right)^{3/9} = 1

\frac{1}{3} \lim_{n\to\infty} n \cdot \left[ \ln(n+3) - \ln(n) \right] = \lim_{n\to\infty} n \ln\left(\frac{n+3}{n}\right) = \lim_{n\to\infty} \ln\left(\left(1+\frac{3}{n}\right)^n\right)

       = \ln \left( \lim_{n \to \infty} \left( 1 + \frac{3}{n} \right)^n \right) = \ln \left( \lim_{n \to \infty} \left( 1 + \frac{1}{n} \right)^{\frac{n}{3} \cdot 3} \right) = \ln \left( e^3 \right) = 3
```



3. a) 
$$\lim_{N\to\infty} \frac{1-\cos(4x)}{x^2} = \lim_{N\to\infty} \frac{1-(1-2x/\sqrt{2x})}{x^2} = \lim_{N\to\infty} \frac{2x/\sqrt{2x}}{x^2}$$

$$\lim_{N\to\infty} \frac{x}{x^2} + \lim_{N\to\infty} \frac{1-\sin(2x)}{x^2} = \frac{1}{x^2} + \frac{1}{x^2} = \frac{1}{x^2}$$

$$\lim_{N\to\infty} \frac{x}{x^2} + \lim_{N\to\infty} \frac{1-\sin(2x)}{x^2} = \lim_{N\to\infty} \frac{1-\sin(2x)}{x^2} + \frac{1}{x^2} = \frac{1}{x^2}$$

b)  $\lim_{N\to\infty} \frac{x}{x^2} + \lim_{N\to\infty} \frac{1-\sin(2x)}{x^2} = \lim_{N\to\infty} \frac{1-\sin(2x)}{x^2} + \frac{1}{x^2} = \frac{1}{x^2}$ 

$$\lim_{N\to\infty} \frac{1-\cos(4x)}{x^2} = \lim_{N\to\infty} \frac{1-\sin(2x)}{x^2} + \frac{\sin(2x)}{x^2} + \frac{1}{x^2} = \frac{1}{x^2}$$

c)  $\lim_{N\to\infty} \left( \frac{1-\sin(2x)}{x^2} + \frac{1}{x^2} + \frac{1}{x^2}$ 

