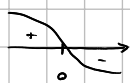


$$1. \lim_{x \rightarrow 0^+} x^2 e^{-\frac{4}{x}} = \lim_{x \rightarrow 0^+} \frac{e^{-\frac{4}{x}}}{x^{-2}} \stackrel{\frac{\infty}{\infty}}{=} \lim_{x \rightarrow 0^+} \frac{4x^2 e^{-\frac{4}{x}}}{-2x^{-3}} = \lim_{x \rightarrow 0^+} \frac{2e^{-\frac{4}{x}}}{-x^{-1}} \stackrel{\frac{\infty}{\infty}}{=} \lim_{x \rightarrow 0^+} \frac{2 \cdot 4x^4 e^{-\frac{4}{x}}}{x^{-2}} = \lim_{x \rightarrow 0^+} 8 \cdot e^{-\frac{4}{x}} = \left\{ 8 \cdot e^{-\frac{4}{x}} = 8e^{-\infty} \right\} = 0$$

$$\frac{d}{dx} e^{-\frac{4}{x}} = e^{-\frac{4}{x}} \cdot \frac{d}{dx} \frac{-4}{x} = -4e^{-\frac{4}{x}} \cdot \frac{d}{dx} x^{-1} = -4e^{-\frac{4}{x}} (-1)x^{-2} = 4e^{-\frac{4}{x}} x^{-2}$$

$$2. f(x) = e^{-4x^2+3}$$

$$f'(x) = -8x e^{-4x^2+3}$$



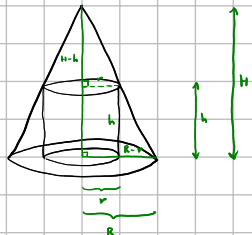
$$f' \nearrow \cup (-\infty, 0]$$

$$f' \searrow \cup [0, +\infty)$$

$$\forall t \in \mathbb{R} e^t > 0$$

$$\text{maximum lokale } f(0) = e^3$$

3.



$$V = \pi r^2 h \quad r \in (0, R)$$

$$\frac{r}{H-h} = \frac{R-r}{h}$$

$$rh = RH - Rh - rH + rh$$

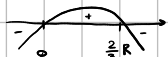
$$0 = RH - Rh - rH$$

$$Rh = RH - rH$$

$$h = \frac{RH - rH}{R} = H \frac{R-r}{R} = H \left(1 - \frac{r}{R}\right)$$

$$V = \pi H r^2 \left(1 - \frac{r}{R}\right) = \pi H r^2 - \frac{\pi H}{R} r^3$$

$$\frac{dV}{dr} = 2\pi H r - 3 \frac{\pi H}{R} r^2 = \pi H r \left(2 - \frac{3}{R} r\right) = \frac{3\pi H}{R} r \left(\frac{2R}{3} - r\right)$$



$$V \nearrow \cup \left(0, \frac{2}{3}R\right]$$

$$V \searrow \cup \left[\frac{2}{3}R, R\right)$$

$$\text{maximum} \text{ da } r = \frac{2}{3}R \quad h = H \left(1 - \frac{\frac{2}{3}R}{R}\right) = \frac{1}{3}H$$

$$4. f(x) = \frac{1}{9}x^4 - \frac{7}{2}x^2 + 6x$$

$$f'(x) = x^3 - 7x + 6 = (x-1)(x^2+x-6) = (x-1)(x-2)(x+3)$$

$$\begin{array}{r} x^2 + x - 6 \\ x^3 \quad -7x + 6 \end{array} \begin{array}{l} x-1 \\ \hline \end{array}$$

$$\Delta = 1 - 4(-6) = 25 \quad \sqrt{\Delta} = 5$$

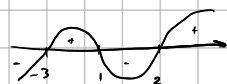
$$x_1 = \frac{-1+5}{2} = 2 \quad x_2 = -3$$

$$\ominus \frac{x^3 - x^2}{x^2 - 7x}$$

$$\ominus \frac{x^2 - x}{x^2 - 7x}$$

$$\ominus \frac{x^2 - x}{-6x + 6}$$

$$\ominus \frac{-6x + 6}{-6x + 6}$$



$$f \nearrow \cup [-3, 1], [2, +\infty)$$

$$f \searrow \cup (-\infty, -3], [1, 2]$$

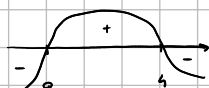
$$\text{maximum } \cup x=1 \quad f(1) = \frac{1}{9} - \frac{7}{2} + 6 = 2\frac{2}{9}$$

$$\text{minimum } \cup x=-3 \quad ; \quad x=2$$

$$5. f(x) = x^4 e^{-x}$$

$$f'(x) = 4x^3 e^{-x} - x^4 e^{-x} = x^3 e^{-x} (4-x) = -x^3 (x-4) e^{-x}$$

$$\forall x \in \mathbb{R} e^{-x} > 0$$



$$f \nearrow \cup [0, 4]$$

$$f \searrow \cup (-\infty, 0], [4, +\infty)$$

$$\text{minimum } \cup x=0 \quad f(0) = 0$$

$$\text{maximum } \cup x=4 \quad f(4) = 256 e^{-4}$$