Circuit Design Equations

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I. SINUSOIDAL SIGNALS

$$V(t) = V_{pk}\sin(\omega t + \phi)$$
 $I(t) = I_{pk}\sin(\omega t + \phi)$ (1)

II. SIGNAL VOLTAGE, CURRENT, & POWER

$$P = \int_{T} \frac{V^{2}(t)}{RT} dt \qquad P = \int_{T} \frac{RI^{2}(t)}{T} dt$$
 (2)

Sub (1) in (2) & solving:

$$P = \frac{V_{pk}^2}{2R} \qquad P = \frac{RI_{pk}^2}{2}$$

RMS Voltage & Current,

$$V_{RMS} \triangleq \sqrt{RP} = \frac{V_{pk}}{\sqrt{2}}$$
 $I_{RMS} \triangleq \sqrt{\frac{P}{R}} = \frac{I_{pk}}{\sqrt{2}}$

III. DECIBELS & NEPERS

Power (Decibels),

$$\begin{split} P_{\mathrm{dB}} &\triangleq 10 \log_{10} \frac{P_{1}}{P_{2}} \left[\mathrm{dB} \right] &\Leftrightarrow \frac{P_{1}}{P_{2}} = 10^{\frac{P_{\mathrm{dB}}}{10}} \\ &= 10 \log_{10} \frac{V_{1}^{2} R_{2}}{V_{2}^{2} R_{1}} \left[\mathrm{dB} \right] &\Leftrightarrow \frac{V_{1}}{V_{2}} \sqrt{\frac{R_{2}}{R_{1}}} = 10^{\frac{P_{\mathrm{dB}}}{20}} \\ &= 10 \log_{10} \frac{I_{1}^{2} R_{2}}{I_{2}^{2} R_{2}} \left[\mathrm{dB} \right] &\Leftrightarrow \frac{I_{1}}{I_{2}} \sqrt{\frac{R_{1}}{R_{2}}} = 10^{\frac{P_{\mathrm{dB}}}{20}} \end{split}$$

Power (Nepers),

$$\begin{split} P_{\mathrm{Np}} &\triangleq \frac{1}{2} \ln \frac{P_{1}}{P_{2}} \left[\mathrm{Np} \right] \quad \Leftrightarrow \quad \frac{P_{1}}{P_{2}} = e^{2P_{\mathrm{Np}}} \\ &= \ln \frac{V_{1} \sqrt{R_{2}}}{V_{2} \sqrt{R_{1}}} \left[\mathrm{Np} \right] \quad \Leftrightarrow \quad \frac{V_{1}}{V_{2}} \sqrt{\frac{R_{2}}{R_{1}}} = e^{P_{\mathrm{Np}}} \\ &= \ln \frac{I_{1} \sqrt{R_{1}}}{I_{2} \sqrt{R_{2}}} \left[\mathrm{Np} \right] \quad \Leftrightarrow \quad \frac{I_{1}}{I_{2}} \sqrt{\frac{R_{1}}{R_{2}}} = e^{P_{\mathrm{Np}}} \end{split}$$

Decibels ⇔ Nepers,

$$\begin{split} e^{2P_{\rm Np}} &= \frac{P_1}{P_2} = 10^{\frac{P_{\rm dB}}{10}} \\ P_{\rm dB} &= \frac{20}{\ln 10} P_{\rm Np} = (20 \log_{10} e) P_{\rm Np} \\ &1 \, [{\rm Np}] \approx 8.686 \, [{\rm dB}] \end{split}$$