Barlow Twins: Self-Supervised Learning via Redundancy Reduction

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Abstract

Self-supervised learning (SSL) is rapidly closing the gap with supervised methods on large computer vision benchmarks. A successful approach to SSL is to learn representations which are invariant to distortions of the input sample. However, a recurring issue with this approach is the existence of trivial constant representations. Most current methods avoid such collapsed solutions by careful implementation details. We propose an objective function that naturally avoids such collapse by measuring the cross-correlation matrix between the outputs of two identical networks fed with distorted versions of a sample, and making it as close to the identity matrix as possible. This causes the representation vectors of distorted versions of a sample to be similar, while minimizing the redundancy between the components of these vectors. The method is called BARLOW TWINS, owing to neuroscientist H. Barlow's *redundancy-reduction principle* applied to a pair of identical networks. BARLOW TWINS does not require large batches nor asymmetry between the network twins such as a predictor network, gradient stopping, or a moving average on the weight updates. It allows the use of very high-dimensional output vectors. BARLOW TWINS outperforms previous methods on ImageNet for semi-supervised classification in the low-data regime, and is on par with current state of the art for ImageNet classification with a linear classifier head, and for transfer tasks of classification and object detection. [1]
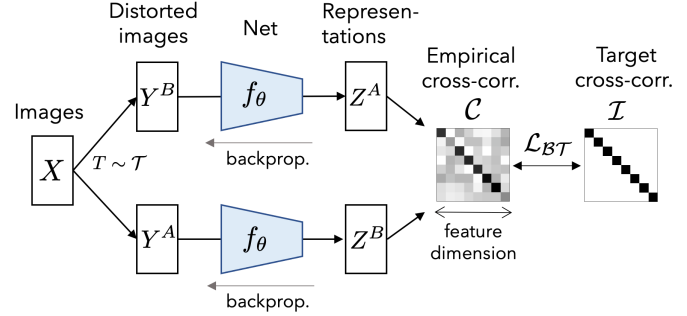
Figure 1. BARLOW TWINS's objective function measures the cross-correlation matrix between the output features of two identical networks fed with distorted versions of a batch of samples, and tries to make this matrix close to the identity. This causes the representation vectors of distorted versions of a sample to be similar, while minimizing the redundancy between the components of these vectors. BARLOW TWINS is competitive with state-of-the-art methods for self-supervised learning while being conceptually simpler, naturally avoiding trivial constant (i.e. collapsed representations), and being robust to the training batch size.

1. Introduction

Self-supervised learning aims to learn useful representations of the input data without relying on human annotations. Recent advances in self-supervised learning for visual data (Caron et al., 2020; Chen et al., 2020a; Grill et al., 2020; He et al., 2019; Misra & van der Maaten, 2019) show that it is possible to learn self-supervised representations that are competitive with supervised representations. A common underlying theme that unites these methods is that they all aim to learn representations that are invariant under different distortions (also referred to as 'data augmentations'). This is typically achieved by maximizing similarity of representations obtained from different distorted versions of a sample using a variant of Siamese networks (Hadsell et al., 2006). As there are trivial solutions to this problem, like a constant representation, these methods rely on different mechanisms to learn useful representations.

Contrastive methods like SIMCLR (Chen et al., 2020a) define 'positive' and 'negative' sample pairs which are treated differently in the loss function. Additionally, they can also use asymmetric learning updates wherein momentum encoders (He et al., 2019) are updated separately from the main network. Clustering methods use one distorted sample to compute 'targets' for the loss, and another distorted ver-

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[1]Code and pre-trained models (in PyTorch) coming soon at https://github.com/facebookresearch/barlowtwins

sion of the sample to predict these targets, followed by an alternate optimization scheme like k-means in DEEPCLUS-TER (Caron et al., 2018) or non-differentiable operators in SWAV (Caron et al., 2020) and SELA (Asano et al., 2020). In another recent line of work, BYOL (Grill et al., 2020) and SIMSIAM (Chen & He, 2020), both the network architecture and parameter updates are modified to introduce asymmetry. The network architecture is modified to be asymmetric using a special 'predictor' network and the parameter updates are asymmetric such that the model parameters are only updated using one distorted version of the input, while the representations from another distorted version are used as a fixed target. (Chen & He, 2020) conclude that the asymmetry of the learning update, 'stop-gradient', is critical to preventing trivial solutions.

In this paper, we propose a new method, BARLOW TWINS, which applies *redundancy-reduction* — a principle first proposed in neuroscience — to self-supervised learning. In his influential article *Possible Principles Underlying the Transformation of Sensory Messages* (Barlow, 1961), neuroscientist H. Barlow hypothesized that the goal of sensory processing is to recode highly redundant sensory inputs into a factorial code (a code with statistically independent components). This principle has been fruitful in explaining the organization of the visual system, from the retina to cortical areas (see (Barlow, 2001) for a review and (Lindsey et al., 2020; Ocko et al., 2018; Schwartz & Simoncelli, 2001) for recent efforts), and has led to a number of algorithms for supervised and unsupervised learning (Ballé et al., 2017; Deco & Parra, 1997; Földiák, 1990; Linsker, 1988; Redlich, 1993a;b; Schmidhuber et al., 1996). Based on this principle, we propose an objective function which tries to make the cross-correlation matrix computed from twin representations as close to the identity matrix as possible. BARLOW TWINS is conceptually simple, easy to implement and learns useful representations as opposed to trivial solutions. Compared to other methods, it does not require large batches (Chen et al., 2020a), nor does it require any asymmetric mechanisms like prediction networks (Grill et al., 2020), momentum encoders (He et al., 2019), non-differentiable operators (Caron et al., 2020) or stop-gradients (Chen & He, 2020). Intriguingly, BARLOW TWINS strongly benefits from the use of very high-dimensional representations. BARLOW TWINS outperforms previous methods on ImageNet for semi-supervised classification in the low-data regime (55% top-1 accuracy for 1% labels), and is on par with current state of the art for ImageNet classification with a linear classifier head, as well as for a number of transfer tasks of classification and object detection.

2. Method

2.1. Description of BARLOW TWINS

Like other methods for SSL (Caron et al., 2020; Chen et al., 2020a; Grill et al., 2020; He et al., 2019; Misra & van der Maaten, 2019), BARLOW TWINS operates on a joint embedding of distorted images (Fig. 1). More specifically, it produces two distorted views for all images of a batch X sampled from a dataset. The distorted views are obtained via a distribution of data augmentations $\mathcal{T}$. The two batches of distorted views Y^A and Y^B are then fed to a function f_θ, typically a deep network with trainable parameters θ, producing batches of representations Z^A and Z^B respectively. To simplify notations, Z^A and Z^B are assumed to be mean-centered along the batch dimension, such that each unit has mean output 0 over the batch.

BARLOW TWINS distinguishes itself from other methods by its innovative loss function $\mathcal{L}_{\mathcal{BT}}$:

$$\mathcal{L}_{\mathcal{BT}} \triangleq \underbrace{\sum_i (1 - \mathcal{C}_{ii})^2}_{\text{invariance term}} + \; \lambda \underbrace{\sum_i \sum_{j \neq i} \mathcal{C}_{ij}{}^2}_{\text{redundancy reduction term}} \quad (1)$$

where λ is a positive constant trading off the importance of the first and second terms of the loss, and where $\mathcal{C}$ is the cross-correlation matrix computed between the outputs of the two identical networks along the batch dimension:

$$\mathcal{C}_{ij} \triangleq \frac{\sum_b z_{b,i}^A z_{b,j}^B}{\sqrt{\sum_b \left(z_{b,i}^A\right)^2} \sqrt{\sum_b \left(z_{b,j}^B\right)^2}} \quad (2)$$

where b indexes batch samples and i, j index the vector dimension of the networks' outputs. $\mathcal{C}$ is a square matrix with size the dimensionality of the network's output, and with values comprised between -1 (i.e. perfect anti-correlation) and 1 (i.e. perfect correlation).

Intuitively, the *invariance term* of the objective, by trying to equate the diagonal elements of the cross-correlation matrix to 1, makes the representation invariant to the distortions applied. The *redundancy reduction term*, by trying to equate the off-diagonal elements of the cross-correlation matrix to 0, decorrelates the different vector components of the representation. This decorrelation reduces the redundancy between output units, so that the output units contain non-redundant information about the sample.

More formally, BARLOW TWINS's objective function can be understood through the lens of information theory, and specifically as an instanciation of the *Information Bottleneck (IB)* objective (Tishby & Zaslavsky, 2015; Tishby et al., 2000). Applied to self-supervised learning, the IB objective consists in finding a representation that conserves as much

Algorithm 1 PyTorch-style pseudocode for Barlow Twins.

```
# f: encoder network
# lambda: weight on the off-diagonal terms
# N: batch size
# D: dimensionality of the representation
#
# mm: matrix-matrix multiplication
# off_diagonal: off-diagonal elements of a matrix
# eye: identity matrix

for x in loader: # load a batch with N samples
    # two randomly augmented versions of x
    y_a, y_b = augment(x)

    # compute representations
    z_a = f(y_a) # NxD
    z_b = f(y_b) # NxD

    # normalize repr. along the batch dimension
    z_a_norm = (z_a - z_a.mean(0)) / z_a.std(0) # NxD
    z_b_norm = (z_b - z_b.mean(0)) / z_b.std(0) # NxD

    # cross-correlation matrix
    c = mm(z_a_norm.T, z_b_norm) / N # DxD

    # loss
    c_diff = (c - eye(D)).pow(2) # DxD
    # multiply off-diagonal elems of c_diff by lambda
    off_diagonal(c_diff).mul_(lambda)
    loss = c_diff.sum()

    # optimization step
    loss.backward()
    optimizer.step()
```

information about the sample as possible while being the *least* possible informative about the specific distortions applied to that sample. The mathematical connection between BARLOW TWINS's objective function and the IB principle is explored in Appendix A.

BARLOW TWINS' objective function has similarities with existing objective functions for SSL. For example, the redundancy reduction term plays a role similar to the *contrastive term* in the INFONCE objective (Oord et al., 2018), as discussed in detail in Section 5. However, important conceptual differences in these objective functions result in practical advantages of our method compared to INFONCE-based methods, namely that (1) our method does not require a large number of negative samples and can thus operate on small batches (2) our method can take advantage of very high-dimensional representations. Alternatively, the redundancy reduction term can be viewed as a *soft-whitening* constraint on the representations, connecting our method to a recently proposed method performing a *hard-whitening* operation on the representations (Ermolov et al., 2020), as discussed in Section 5. However, our method performs better than current hard-whitening methods.

The pseudocode for BARLOW TWINS is shown as Algorithm 1.

2.2. Implementation Details

Image augmentations   Each input image is transformed twice to produce the two distorted views shown in Figure 1.

The image augmentation pipeline consists of the following transformations: random cropping, resizing to 224×224, horizontal flipping, color jittering, converting to grayscale, Gaussian blurring, and solarization. The first two transformations (cropping and resizing) are always applied, while the last five are applied randomly, with some probability. This probability is different for the two distorted views in the last two transformations (blurring and solarization). We use the same augmentation parameters as BYOL (Grill et al., 2020).

Architecture   The encoder f_θ consists of a ResNet-50 network (He et al., 2016) (without the final classification layer) followed by a projector network. The projector network has three linear layers, each with 8192 output units. The first two layers of the projector are followed by a batch normalization layer and rectified linear units.

Optimization   We follow the optimization protocol described in BYOL (Grill et al., 2020). We use the LARS optimizer (You et al., 2017) and train for 1000 epochs with a batch size of 2048. We however emphasize that our model works well with batches as small as 256 (see Ablations). The learning rate starts at 0 and is linearly increased to 0.2 in the first 10 epochs of training, after which it is decreased to 0.002 using a cosine decay schedule (Loshchilov & Hutter, 2016). We ran a search for the trade-off parameter λ of the loss function and found the best results for $\lambda = 5 \cdot 10^{-3}$. We use a weight decay parameter of $1.5 \cdot 10^{-6}$. The biases and batch normalization parameters are excluded from LARS adaptation and weight decay. Training is distributed across 32 V100 GPUs and takes approximately 124 hours. For comparison, our reimplementation of BYOL trained with a batch size of 4096 takes 113 hours on the same hardware.

3. Results

We follow standard practice (Goyal et al., 2019) and evaluate our representations by transfer learning to different datasets and tasks in computer vision. Our network is pretrained using self-supervised learning on the training set of the ImageNet ILSVRC-2012 dataset (Deng et al., 2009) (without labels). We evaluate our model on a variety of tasks such as image classification and object detection, and using fixed representations from the network or finetuning it. We provide the hyperparameters for all the transfer learning experiments in the Appendix.

3.1. Linear and Semi-Supervised Evaluations on ImageNet

Linear evaluation on ImageNet   We train a linear classifier on ImageNet on top of fixed representations of a ResNet-50 pretrained with our method. The top-1 and top-5 accu-

racies obtained on the ImageNet validation set are reported in Table 1. Our method obtains a top-1 accuracy of 73.2% which is comparable to the state-of-the-art methods.

Table 1. **Top-1 and top-5 accuracies (in %) under linear evaluation on ImageNet**. All models use a ResNet-50 encoder. Top-3 best self-supervised methods are underlined.

Method	Top-1	Top-5
Supervised	76.5	
MoCo	60.6	
PIRL	63.6	-
SimCLR	69.3	89.0
MoCo v2	71.1	90.1
SimSiam	71.3	-
SwAV	71.8	-
BYOL	74.3	91.6
SwAV (w/ multi-crop)	75.3	-
Barlow Twins (ours)	73.2	91.0

Semi-supervised training on ImageNet We fine-tune a ResNet-50 pretrained with our method on a subset of ImageNet. We use subsets of size 1% and 10% using the same split as SimCLR. The semi-supervised results obtained on the ImageNet validation set are reported in Table 2. Our method is either on par (when using 10% of the data) or slightly better (when using 1% of the data) than competing methods.

Table 2. **Semi-supervised learning on ImageNet** using 1% and 10% training examples. Results for the supervised method are from (Zhai et al., 2019). Best results are in **bold**.

Method	Top-1		Top-5	
	1%	10%	1%	10%
Supervised	25.4	56.4	48.4	80.4
PIRL	-	-	57.2	83.8
SimCLR	48.3	65.6	75.5	87.8
BYOL	53.2	68.8	78.4	89.0
SwAV (w/ multi-crop)	53.9	**70.2**	78.5	**89.9**
Barlow Twins (ours)	**55.0**	69.7	**79.2**	89.3

3.2. Transfer to other datasets and tasks

Image classification with fixed features We follow the setup from (Misra & van der Maaten, 2019) and train a linear classifier on fixed image representations, *i.e.*, the parameters of the ConvNet remain unchanged. We use a diverse set of datasets for this evaluation - Places-205 (Zhou et al., 2014) for scene classification, VOC07 (Everingham

Table 3. **Transfer learning: image classification.** We benchmark learned representations on the image classification task by training linear classifiers on fixed features. We report top-1 accuracy on Places-205 and iNat18 datasets, and classification mAP on VOC07. Top-3 best self-supervised methods are underlined.

Method	Places-205	VOC07	iNat18
Supervised	53.2	87.5	46.7
SimCLR	52.5	85.5	37.2
MoCo-v2	51.8	86.4	38.6
SwAV	52.8	86.4	39.5
SwAV (w/ multi-crop)	56.7	88.9	48.6
BYOL	54.0	86.6	47.6
Barlow Twins (ours)	54.1	86.2	46.5

et al., 2010) for multi-label image classification, and iNaturalist2018 (Van Horn et al., 2018) for fine-grained image classification. We report our results in Table 3. Barlow Twins performs competitively against prior work, and outperforms SimCLR and MoCo-v2 across all datasets.

Object Detection and Instance Segmentation We evaluate our representations for the localization based tasks of object detection and instance segmentation. We use the VOC07+12 (Everingham et al., 2010) and COCO (Lin et al., 2014) datasets following the setup in (He et al., 2019) which finetunes the ConvNet parameters. Our results in Table 4 indicate that Barlow Twins performs comparably or better than state-of-the-art representation learning methods for these localization tasks.

Table 4. **Transfer learning: object detection and instance segmentation.** We benchmark learned representations on the object detection task on VOC07+12 using Faster R-CNN (Ren et al., 2015) and on the detection and instance segmentation task on COCO using Mask R-CNN (He et al., 2017). All methods use the C4 backbone variant (Wu et al., 2019) and models on COCO are finetuned using the $1\times$ schedule. Best results are in **bold**.

Method	VOC07+12 det			COCO det			COCO instance seg		
	AP_{all}	AP_{50}	AP_{75}	AP^{bb}	AP^{bb}_{50}	AP^{bb}_{75}	AP^{mk}	AP^{mk}_{50}	AP^{mk}_{75}
Sup.	53.5	81.3	58.8	38.2	58.2	41.2	33.3	54.7	35.2
MoCo-v2	**57.4**	82.5	**64.0**	**39.3**	58.9	**42.5**	**34.4**	55.8	36.5
SwAV	56.1	**82.6**	62.7	38.4	58.6	41.3	33.8	55.2	35.9
SimSiam	57	82.4	63.7	39.2	**59.3**	42.1	**34.4**	**56.0**	**36.7**
BT (ours)	56.8	**82.6**	63.4	39.2	59.0	**42.5**	34.3	**56.0**	36.5

4. Ablations

For all ablation studies, Barlow Twins was trained for 300 epochs instead of 1000 epochs in the previous section. A linear evaluation on ImageNet of this baseline model yielded a 71.4% top-1 accuracy and a 90.2% top-5 accu-

racy. For all the ablations presented we report the top-1 and top-5 accuracy of training linear classifiers on the 2048 dimensional `res5` features using the ImageNet train set.

Loss Function Ablations We alter our loss function (eqn. 1) in several ways to test the necessity of each term of the loss function, and to experiment with different practices popular in other loss functions for SSL, such as INFONCE. Table 5 recapitulates the different loss functions tested along with their results on a linear evaluation benchmark of Imagenet. First we find that removing the invariance term (on-diagonal term) or the redundancy reduction term (off-diagonal term) of our loss function leads to worse/collapsed solutions, as expected. We then study the effect of different normalization strategies. We first try to normalize the representations along the feature dimension so that they lie on the unit sphere, as it is common practice for losses measuring a cosine similarity (Chen et al., 2020a; Grill et al., 2020; Wang & Isola, 2020). Specifically, we first normalize the representations along the batch dimension (with mean subtraction), then normalize the representations along the feature dimension (without mean subtraction), and finally we measure the (unnormalized) covariance matrix instead of the (normalized) cross-correlation matrix in eqn. 2. The performance is slightly reduced. Second, we try to remove batch-normalization operations in the two hidden layers of the projector network MLP. The performance is barely affected. Third, in addition to removing the batch-normalization in the hidden layers, we replace the cross-correlation matrix in eqn. 2 by the cross-covariance matrix (which means the features are no longer normalized along the batch dimension). The performance is substantially reduced. We finally try a cross-entropy loss with temperature, for which the on-diagonal term and off-diagonal term is controlled by a temperature hyperparameter τ and coefficient λ: $\mathcal{L} = -\log \sum_i \exp(\mathcal{C}_{ii}/\tau) + \lambda \log \sum_i \sum_{j\neq i} \exp(\max(\mathcal{C}_{ij}, 0)/\tau)$. The performance is reduced.

Robustness to Batch Size The INFONCE loss that draws negative examples from the minibatch suffer performance drops when the batch size is reduced (e.g. SIMCLR (Chen et al., 2020a)). We thus sought to test the robustness of BARLOW TWINS to small batch sizes. In order to adapt our model to different batch sizes, we performed a grid search on LARS learning rates for each batch size. We find that, unlike SIMCLR, our model is robust to small batch sizes (Fig. 2), with a performance almost unaffected for a batch as small as 256. In comparison the accuracy for SimCLR drops about 4 p.p. for batch size 256. This robustness to small batch size, also found in non-contrastive methods such as BYOL, further demonstrates that our method is not only conceptually (see Discussion) but also empirically different than the INFONCE objective.

Table 5. **Loss function explorations**. We ablate the invariance and redundancy terms in our proposed loss and observe that both terms are necessary for good performance. We also experiment with different normalization schemes and a cross-entropy loss and observe reduced performance.

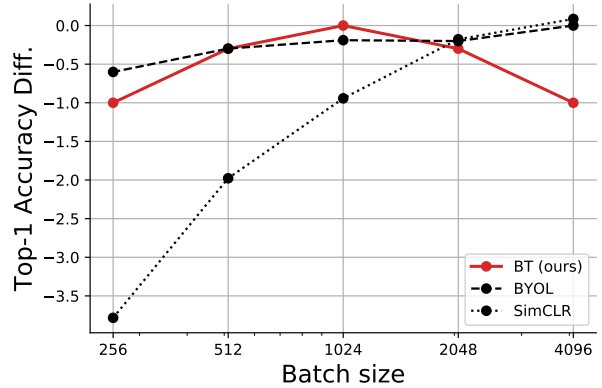| Loss function	Top-1	Top-5
Baseline	71.4	90.2
Only invariance term (on-diag term)	57.3	80.5
Only red. red. term (off-diag term)	0.1	0.5
Normalization along feature dim.	69.8	88.8
No BN in MLP	71.2	89.7
No BN in MLP + no Normalization	53.4	76.7
Cross-entropy with temp.	63.3	85.7

Figure 2. Effect of batch size. To compare the effect of the batch size across methods, for each method we report the difference between the top-1 accuracy at a given batch size and the best obtained accuracy among all batch size tested. BYOL: best accuracy is 72.5% for a batch size of 4096 (data from (Grill et al., 2020) fig. 3A). SIMCLR: best accuracy is 67.1% for a batch size of 4096 (data from (Chen et al., 2020a) fig. 9, model trained for 300 epochs). BARLOW TWINS: best accuracy is 71.7% for a batch size of 1024.

Effect of Removing Augmentations We find that our model is not robust to removing some types of data augmentations, like SIMCLR but unlike BYOL (Fig. 3). While this can be seen as a disadvantage of our method compared to BYOL, it can also be argued that the representations learned by our method are better controlled by the specific set of distortions used, as opposed to BYOL for which the invariances learned seem generic and intriguingly independent of the specific distortions used.

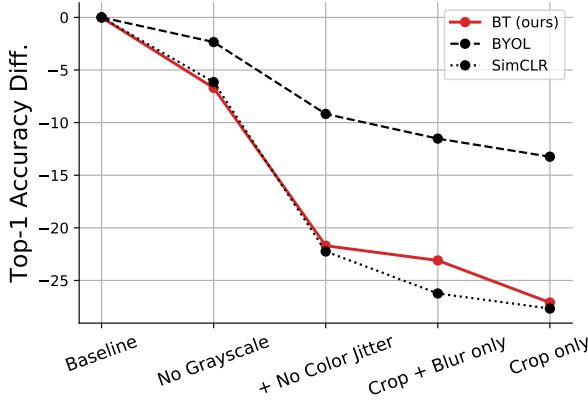**Projector Network Depth & Width** For other SSL methods, such as BYOL and SIMCLR, the projector network

Figure 3. Effect of progressively removing data augmentations. Data for BYOL and SIMCLR (repro) is from (Grill et al., 2020) fig 3b.

drastically reduces the dimensionality of the ResNet output. In stark contrast, we find that BARLOW TWINS performs better when the dimensionality of the projector network output is very large. Other methods rapidly saturate when the dimensionality of the output increases, but our method keeps improving with all output dimensionality tested (Fig. 4). This result is quite surprising because the output of the ResNet is kept fixed to 2048, which acts as a dimensionality bottleneck in our model and sets the limit of the intrinsic dimensionality of the representation. In addition, similarly to other methods, we find that our model performs better when the projector network has more layers, with a saturation of the performance for 3 layers.
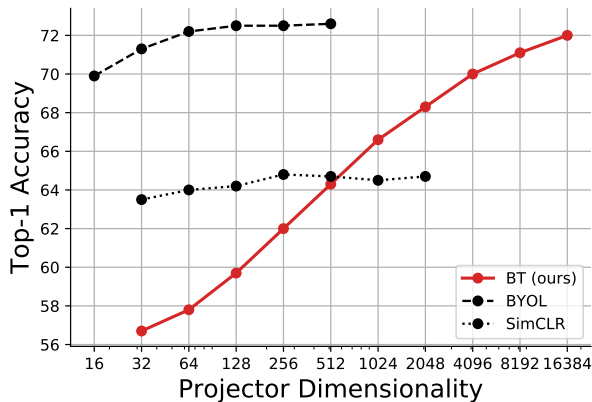

Figure 4. Effect of the dimensionality of the last layer of the projector network on performance. Data for SIMCLR is from (Chen et al., 2020a) fig 8; Data for BYOL is from (Grill et al., 2020) Table 14b.

Breaking Symmetry Many SSL methods (e.g. BYOL, SIMSIAM, SWAV) rely on different symmetry-breaking mechanisms to avoid trivial solutions. Our loss function avoids these trivial solutions by construction, even in the case of symmetric networks. It is however interesting to ask whether breaking symmetry can further improve the performance of our network. Following SIMSIAM and BYOL, we experiment with adding a predictor network composed of 2 fully connected layers of size 8192 to one of the network (with batch normalization followed by a ReLU nonlinearity in the hidden layer) and/or a stop-gradient mechanism on the other network. We find that these asymmetries slightly decrease the performance of our network (see Table 6).

Table 6. Effect of asymmetric settings

case	stop-gradient	predictor	Top-1	Top-5
Baseline	-	-	71.4	90.2
(a)	✓	-	70.5	89.0
(b)	-	✓	70.2	89.0
(c)	✓	✓	61.3	83.5

5. Discussion

BARLOW TWINS learns self-supervised representations through a joint embedding of distorted images, with an objective function that maximizes similarity between the embedding vectors while reducing redundancy between their components. Our method does not require large batches of samples, nor does it require any particular asymmetry in the twin network structure. We discuss next the similarities and differences between our method and prior art, both from a conceptual and an empirical standpoint. For ease of comparison, all objective functions are recast with a common set of notations. The discussion ends with future directions.

5.1. Comparison with Prior Art

infoNCE The INFONCE loss, where NCE stands for Noise-Contrastive Estimation (Gutmann & Hyvärinen, 2010), is a popular type of contrastive loss function used for self-supervised learning (e.g. (Chen et al., 2020a; He et al., 2019; Hénaff et al., 2019; Oord et al., 2018)). It can be instantiated as:

$$\mathcal{L}_{infoNCE} \triangleq - \underbrace{\sum_b \frac{\langle z_b^A, z_b^B \rangle_i}{\tau \left\| z_b^A \right\|_2 \left\| z_b^B \right\|_2}}_{\text{similarity term}}$$

$$+ \underbrace{\sum_b \log \left(\sum_{b' \neq b} \exp \left(\frac{\langle z_b^A, z_{b'}^B \rangle_i}{\tau \left\| z_b^A \right\|_2 \left\| z_{b'}^B \right\|_2} \right) \right)}_{\text{contrastive term}}$$

where z^A and z^B are the twin network outputs, b indexes the sample in a batch, i indexes the vector component of the output, and τ is a positive constant called temperature in analogy to statistical physics.

For ready comparison, we rewrite BARLOW TWINS loss function with the same notations:

$$\mathcal{L}_{\mathcal{BT}} = \underbrace{\sum_i \left(1 - \frac{\langle z^A_{\cdot,i}, z^B_{\cdot,i}\rangle_b}{\left\|z^A_{\cdot,i}\right\|_2 \left\|z^B_{\cdot,i}\right\|_2}\right)^2}_{\text{invariance term}}$$
$$+ \lambda \underbrace{\sum_i \sum_{j \neq i} \left(\frac{\langle z^A_{\cdot,i}, z^B_{\cdot,j}\rangle_b}{\left\|z^A_{\cdot,i}\right\|_2 \left\|z^B_{\cdot,j}\right\|_2}\right)^2}_{\text{redundancy reduction term}}$$

Both BARLOW TWINS' and INFONCE's objective functions have two terms, the first aiming at making the representations invariant to the distortions fed to the twin networks, the second aiming at maximizing the variability of the representation learned. Another common point between the two losses is that they both rely on batch statistics to measure this variability. However, the INFONCE objective maximizes the variability of the representation by maximizing the pairwise distance between all pairs of samples, whereas our method does so by decorrelating the components of the representation vectors.

The contrastive term in INFONCE can be interpreted as a non-parametric estimation of the entropy of the distribution of representations (Wang & Isola, 2020). An issue that arises with non-parametric entropy estimators is that they are prone to the curse of dimensionality: they can only be estimated reliably in a low-dimensional setting, and they typically require a large number of samples.

In contrast, our loss can be interpreted as a *proxy* entropy estimator of the distribution of representations under *a Gaussian parametrization* (see Appendix A). Thanks to this simplified parametrization, the variability of the representation can be estimated from much fewer samples, and on very large-dimensional representations. Indeed, in the ablation studies that we perform, we find that (1) our method is robust to small batches unlike the popular INFONCE-based method SIMCLR, and (2) our method can take advantage of very large dimensional outputs, unlike INFONCE-based methods which do not see a benefit in increasing the dimensionality of the output.

Our loss presents several other interesting differences with infoNCE:

- In INFONCE, the representations are typically normalized along the feature dimension to compute a cosine similarity between embedded samples. We normalize the representations along the batch dimension instead.

- In our method, there is a parameter λ that trades off how much emphasis is put on the invariance term vs. the redundancy reduction term. This parameter can be interpreted as the trade-off parameter in the *Information Bottleneck* framework (see Appendix A). This parameter is not present in INFONCE.

- INFONCE also has a hyperparameter, the temperature, which can be interpreted as the width of the kernel in a non-parametric kernel density estimation of entropy, and practically weighs the relative importance of the hardest negative samples present in the batch (Chen et al., 2020a).

A number of alternative methods to ours have been proposed to alleviate the reliance on large batches of the INFONCE loss. For example, MoCo (Chen et al., 2020b; He et al., 2019) builds a dynamic dictionary of negative samples with a queue and a moving-averaged encoder. This enables building a large and consistent dictionary on-the-fly that facilitates contrastive unsupervised learning. MoCo typically needs to store $> 60,000$ sample embeddings. In contrast, our method does not require such a large dictionary, since it works well with a relatively small batch size (e.g. 256).

Asymmetric Twins BOOTSTRAP-YOUR-OWN-LATENT (aka BYOL) (Grill et al., 2020) and SIMSIAM (Chen & He, 2020) are two recent methods which use a simple cosine similarity between twin representations as an objective function, without *any* contrastive term:

$$\mathcal{L}_{cosine} = -\sum_b \frac{\langle z^A_b, z^B_b\rangle_i}{\left\|z^A_b\right\|_2 \left\|z^B_b\right\|_2}$$

Surprisingly, these methods successfully avoid trivial solutions by introducing some asymmetry in the architecture and learning procedure of the twin networks. For example, BYOL uses a predictor network which breaks the symmetry between the two networks, and also enforces an exponential moving average on the target network weights to slow down the progression of the weights on the target network. Combined together, these two mechanisms surprisingly avoid trivial solutions. The reasons behind this success are the subject of recent theoretical and empirical studies (Chen & He, 2020; Fetterman & Albrecht, 2020; Richemond et al., 2020; Tian et al., 2020). In particular, the ablation study (Chen & He, 2020) shows that the moving average is not necessary, but that stop-gradient on one of the branch and the presence of the predictor network are two crucial elements to avoid collapse. Other works show that batch normalization (Fetterman & Albrecht, 2020; Tian et al., 2020) or alternatively group normalization (Richemond et al., 2020) could play an important role in avoiding collapse.

Like our method, these asymmetric methods do not require large batches, since in their case there is no interaction between batch samples in the objective function.

It should be noted however that these asymmetric methods cannot be described as the optimization of an overall learning objective. Instead, there exists trivial solutions to the learning objective that these methods avoid via particular implementation choices and/or the result of non-trivial learning dynamics. In contrast, our method avoids trivial solutions by construction, making our method conceptually simpler and more principled than these alternatives (until their principle is discovered, see (Tian et al., 2021) for an early attempt).

Whitening In a concurrent work, (Ermolov et al., 2020) propose W-MSE. Acting on the representations of identical twin networks, this method performs a differentiable whitening operation (via Cholesky decomposition) of each batch of representations before computing a simple cosine similarity between the whitened representations of the twin networks. In contrast, the redundancy reduction term in our loss encourages the whitening of the batch representations as a soft constraint. The current W-MSE model achieves 66.3% top-1 accuracy on the Imagenet linear evaluation benchmark. It is an interesting direction for future studies to determine whether improved versions of this hard-whitening strategy could also lead to state-of-the-art results on these large-scale computer vision benchmarks.

Clustering These methods, such as DEEPCLUSTER (Caron et al., 2018), SwAV (Caron et al., 2020), SELA (Asano et al., 2020), perform contrastive-like comparisons without the requirement to compute all pairwise distances. Specifically, these methods simultaneously cluster the data while enforcing consistency between cluster assignments produced for different distortions of the same image, instead of comparing features directly as in contrastive learning. Clustering methods are also prone to collapse, *e.g.*, empty clusters in k-means and avoiding them relies on careful implementation details. Online clustering methods like SwAV can be trained with large and small batches but require storing features when the number of clusters is much larger than the batch size.

Noise As Targets This method (Bojanowski & Joulin, 2017) aims at learning features by mapping them to fixed random targets on the unit sphere, which can be interpreted as a form of whitening. This objective directly works with a single network, and hence does not leverage the distortions induced by twin networks. Using a single network is prone to collapsing and this forces the method to sample predefined target samples and match the output distribution to this subset, limiting the flexibility of the representation that can be learned.

IMAX In the early days of SSL, (Becker & Hinton, 1992; Zemel & Hinton, 1990) proposed a loss function between twin networks given by:

$$\mathcal{L}_{IMAX} \triangleq \log |\mathcal{C}_{(Z^A - Z^B)}| - \log |\mathcal{C}_{(Z^A + Z^B)}|$$

where $|\;|$ denotes the determinant of a matrix, $\mathcal{C}_{(Z^A - Z^B)}$ is the covariance matrix of the sum of the outputs of the twin networks and $\mathcal{C}_{(Z^A + Z^B)}$ the covariance of the difference of these outputs. It can be shown that this objective maximizes the information between the twin network representations under the assumptions that the two representations are noisy versions of the same underlying Gaussian signal, assuming that the noise is independant, additive and Gaussian. This objective is similar to ours in the sense that there is one term that encourages the two representations to be similar and another term that encourages the units to be decorrelated. However, unlike IMAX, our objective is not directly an information quantity, and we have an extra trade-off parameter λ that trades off the two terms of our loss. The IMAX objective was used in early work so it is not clear whether it can scale to large computer vision benchmarks. Our attempts to make it work on ImageNet were not successful.

5.2. Future Directions

We observe a steady improvement of the performance of our method as we increase the dimensionality of the representation (i.e. of the last layer of the projection network). This intriguing result is in stark contrast with other popular methods for SSL, such as SIMCLR (Chen et al., 2020a) and BYOL (Grill et al., 2020), for which increasing the dimensionality of the representation rapidly saturates performance. It is a promising avenue to continue this exploration for even higher dimensional representations ($> 16,000$), but this would require the development of new methods or alternative hardware to accommodate the memory requirements of operating on such large representations.

Our method is just one possible instanciation of the *Information Bottleneck* principle applied to SSL. We believe that further refinements of the proposed loss function and algorithm could lead to more efficient solutions and even better performances. For example, the redundancy reduction term is currently computed from the off-diagonal terms of the cross-correlation matrix between the twin network representations, but alternatively it could be computed from the off-diagonal terms of the auto-correlation matrix of a single network's representation. Our preliminary analyses seem to indicate that this alternative leads to similar performances (not shown). A modified loss could also be applied to the (unnormalized) cross-covariance matrix instead of the (normalized) cross-correlation matrix (see Ablations for preliminary analyses).

Acknowledgements

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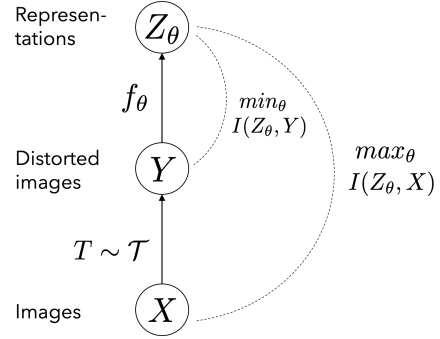## A. Connection between BARLOW TWINS and the Information Bottleneck Principle

Figure 5. The information bottleneck principle applied to self-supervised learning (SSL) posits that the objective of SSL is to learn a representation Z_θ which is informative about the image sample, but invariant (i.e. uninformative) to the specific distortions that are applied to this sample. BARLOW TWINS can be viewed as a specific instanciation of the information bottleneck objective.

We explore in this appendix the connection between BARLOW TWINS' loss function and the *Information Bottleneck* (IB) principle (Tishby & Zaslavsky, 2015; Tishby et al., 2000).

As a reminder, BARLOW TWINS' loss function is given by:

$$\mathcal{L}_{\mathcal{BT}} \triangleq \underbrace{\sum_i (1 - \mathcal{C}_{ii})^2}_{\text{invariance term}} + \lambda \underbrace{\sum_i \sum_{j \neq i} \mathcal{C}_{ij}{}^2}_{\text{redundancy reduction term}} \qquad (3)$$

where λ is a positive constant trading off the importance of the first and second terms of the loss, and where $\mathcal{C}$ is the cross-correlation matrix computed between the outputs of the two identical networks along the batch dimension :

$$\mathcal{C}_{ij} \triangleq \frac{\sum_b z^A_{b,i} z^B_{b,j}}{\sqrt{\sum_b \left(z^A_{b,i}\right)^2} \sqrt{\sum_b \left(z^B_{b,j}\right)^2}} \qquad (4)$$

where b indexes batch samples and i, j index the vector dimension of the networks' outputs. $\mathcal{C}$ is a square matrix with size the dimensionality of the network's output, and with values comprised between -1 (i.e. perfect anti-correlation) and 1 (i.e. perfect correlation).

Applied to self-supervised learning, the IB principle posits that a desirable representation should be as informative as possible about the sample represented while being as invariant (i.e. non-informative) as possible to distortions

of that sample (here the data augmentations used) (Fig. 5). This trade-off is captured by the following loss function:

$$\mathcal{IB}_\theta \triangleq I(Z_\theta, Y) - \beta I(Z_\theta, X) \qquad (5)$$

where $I(.,.)$ denotes mutual information and β is a positive scalar trading off the desideratas of preserving information and being invariant to distortions.

Using a classical identity for mutual information, we can rewrite equation 5 as:

$$\mathcal{IB}_\theta = [H(Z_\theta) - \overset{0}{\cancel{H(Z_\theta|Y)}}] - \beta[H(Z_\theta) - H(Z_\theta|X)] \quad (6)$$

where $H(.)$ denotes entropy. The conditional entropy $H(Z_\theta|Y)$ —the entropy of the representation conditioned on a specific distorted sample— cancels to 0 because the function f_θ is deterministic, and so the representation Z_θ conditioned on the input sample Y is perfectly known and has zero entropy. Since the overall scaling factor of the loss function is not important, we can rearrange equation 6 as:

$$\mathcal{IB}_\theta = H(Z_\theta|X) + \frac{1-\beta}{\beta} H(Z_\theta) \qquad (7)$$

Measuring the entropy of a high-dimensional signal generally requires vast amounts of data, much larger than the size of a single batch. In order to circumvent this difficulty, we make the simplifying assumption that the representation Z is distributed as a Gaussian. The entropy of a Gaussian distribution is simply given by the logarithm of the determinant of its covariance function (up to a constant corresponding to the assumed discretization level that we ignore here) (Cai et al., 2015). The loss function becomes:

$$\mathcal{IB}_\theta = \mathbb{E}_X \log |\mathcal{C}_{Z_\theta|X}| + \frac{1-\beta}{\beta} \log |\mathcal{C}_{Z_\theta}| \qquad (8)$$

This equation is still not exactly the one we optimize for in practice (see eqn. 3 and 4). Indeed, our loss function is only connected to the IB loss given by eqn. 8 through the following simplifications and approximations:

- In the case where $\beta <= 1$, it is easy to see from eqn. 8 that the best solution to the IB trade-off is to set the representation to a constant that does not depend on the input. This trade-off thus does not lead to interesting representations and can be ignored. When $\beta > 1$, we note that the second term of eqn. 8 is preceded by a negative constant. We can thus simply replace $\frac{1-\beta}{\beta}$ by a new positive constant λ, preceded by a negative sign.

- In practice, we find that directly optimizing the determinant of the covariance matrices does not lead to SoTA solutions. Instead, we replace the second term of the loss in eqn. 8 (maximizing the information about samples), by the proxy which consist in simply minimizing the Frobenius norm of the cross-correlation matrix. If the representations are assumed to be rescaled to 1 along the batch dimension before entering the loss (an assumption we are free to make since the cross-correlation matrix is invariant to this re-scaling), this minimization only affects the off-diagonal terms of the covariance matrix (the diagonal terms being fixed to 1 by the re-scaling) and encourages them to be as close to 0 as possible. It is clear that this surrogate objective, which consists in decorrelating all output units, has the same global optimum than the original information maximization objective.

- For consistency with eqn. 8, the second term in BAR-LOW TWINS' loss should be computed from the auto-correlation matrix of one of the twin networks, instead of the cross-correlation matrix between twin networks. In practice, we do not see a strong difference in performance between these alternatives.

- Similarly, it can easily be shown that the first term of eqn. 8 (minimizing the information the representation contains about the distortions) has the same global optimum than the first term of eqn. 3, which maximizes the alignment between representations of pairs of distorted samples.

B. Evaluations on ImageNet

B.1. Linear evaluation on ImageNet

The linear classifier is trained for 100 epochs with a learning rate of 0.3 and a cosine learning rate schedule. We minimize the cross-entropy loss with the SGD optimizer with momentum and weight decay of 10^{-6}. We use a batch size of 256. At training time we augment an input image by taking a random crop, resizing it to 224×224, and optionally flipping the image horizontally. At test time we resize the image to 256×256 and center-crop it to a size of 224×224.

B.2. Semi-supervised training on ImageNet

We train for 20 epochs with a learning rate of 0.002 for the ResNet-50 and 0.5 for the final classification layer. The learning rate is multiplied by a factor of 0.2 after the 12th and 16th epoch. We minimize the cross-entropy loss with the SGD optimizer with momentum and do not use weight decay. We use a batch size of 256. The image augmentations are the same as in the linear evaluation setting.

C. Transfer Learning

C.1. Linear evaluation

We follow the exact settings from PIRL (Misra & van der Maaten, 2019) for evaluating linear classifiers on the Places-205, VOC07 and iNaturalist2018 datasets. For Places-205 and iNaturalist2018 we train a linear classifier with SGD (14 epochs on Places-205, 84 epochs on iNaturalist2018) with a learning rate of 0.01 reduced by a factor of 10 at two equally spaced intervals, a weight decay of 5×10^{-4} and SGD momentum of 0.9. We train SVM classifiers on the VOC07 dataset where the C values are computed using cross-validation.

C.2. Object Detection and Instance Segmentation

We use the detectron2 library (Wu et al., 2019) for training the detection models and closely follow the evaluation settings from (He et al., 2019). The backbone ResNet50 network for Faster R-CNN (Ren et al., 2015) and Mask R-CNN (He et al., 2017) is initialized using our BARLOW TWINS pretrained model.

VOC07+12 We use the VOC07+12 `trainval` set of $16K$ images for training a Faster R-CNN (Ren et al., 2015) C-4 backbone for $24K$ iterations using a batch size of 16 across 8 GPUs using SyncBatchNorm. The initial learning rate for the model is 0.1 which is reduced by a factor of 10 after $18K$ and $22K$ iterations. We use linear warmup (Goyal et al., 2017) with a slope of 0.333 for 1000 iterations.

COCO We train Mask R-CNN (He et al., 2017) C-4 backbone on the COCO 2017 `train` split and report results on the `val` split. We use a learning rate of 0.03 and keep the other parameters the same as in the $1\times$ schedule in detectron2.