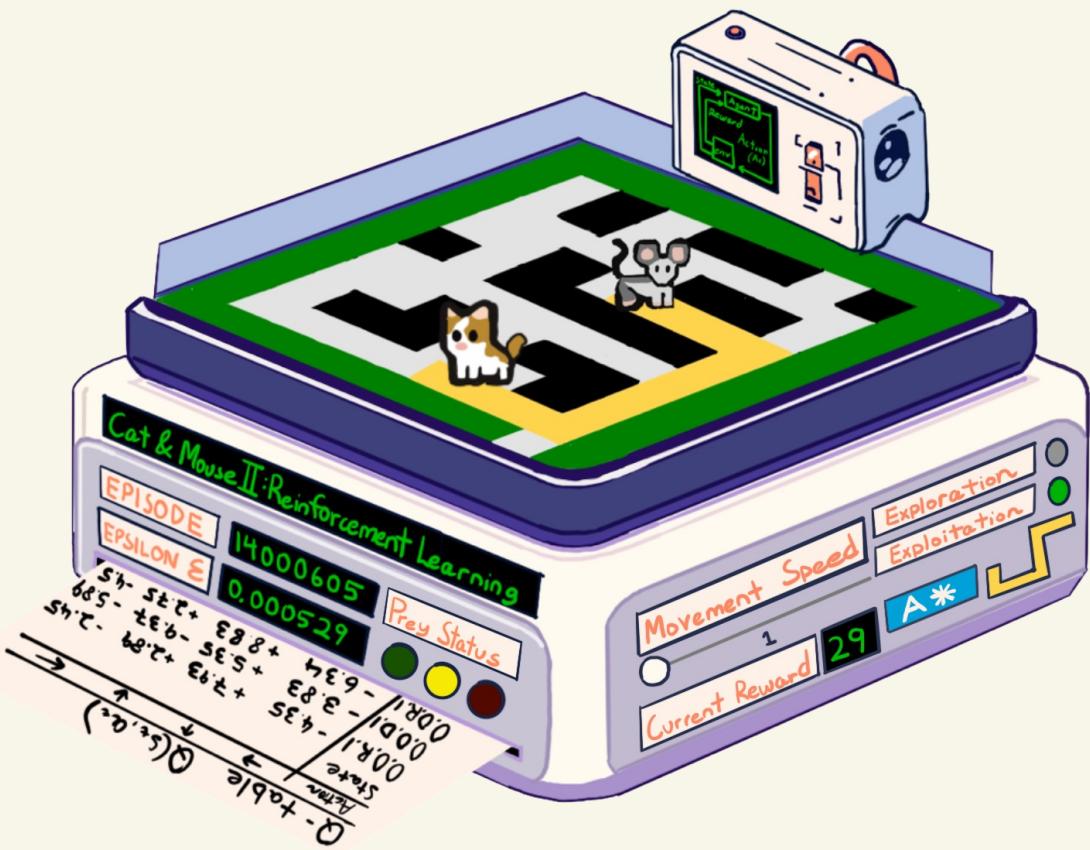


CAT AND MOUSE 2: Reinforcement Learning

A Project by Joseph Ma

Full guide page is currently in the works- this document serves as a preliminary guide, providing an overview of the projects core concepts, logic and implementation.



The first page allows you to select a character for training and select the map size. Note that larger map size means longer training time.

Cat and Mouse 2: Reinforcement Learning Training Configuration

A Project by Joseph Ma

Choose Cat Character:

Regular Cat

Choose Mouse Character:

Regular Mouse

Maze Dimensions:

10 x 10

Design Your Own Map

The next page allows you to design your own map for the training environment. Place walls down as you would like (in black).

Cat and Mouse 2: Reinforcement Learning Training Map Configuration

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Selected Cat: **Regular Cat**
Selected Mouse: **Regular Mouse**
Selected Dimensions: **10**
Map Validity (Ensure all paths are connectable from one another):

Start Game Clear Map

Note that if a portion of the map is disconnected from the others this will invalidate it. Ensure all paths are connectable from one another. There should also be at least one path from entrance to exit.

Cat and Mouse 2: Reinforcement Learning Training Map Configuration

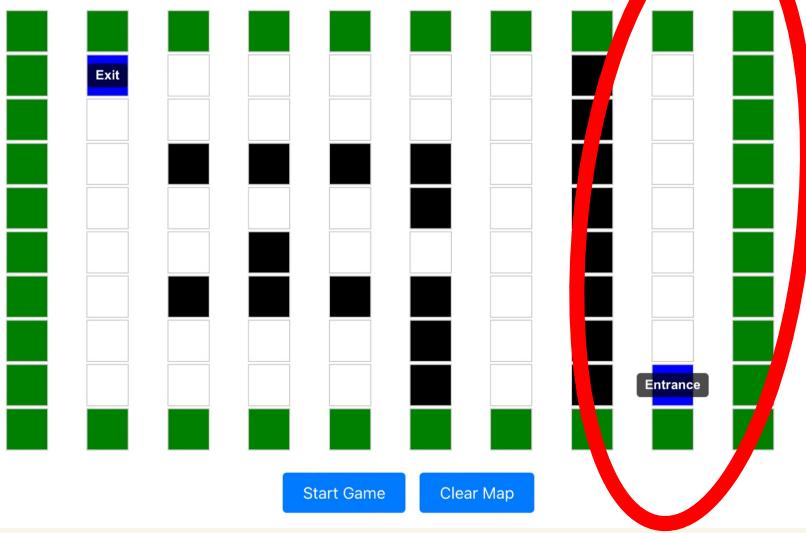
A Project by Joseph Ma

Selected Cat: Regular Cat

Selected Mouse: Regular Mouse

Selected Dimensions: 10

Map Validity (Ensure all paths are connectable from one another): ●

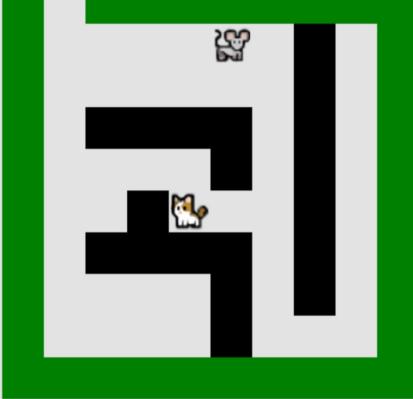


Let's begin training

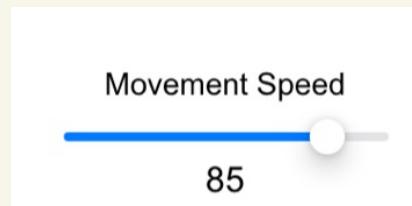
Cat and Mouse 2: Reinforcement Learning - a Project by Joseph Ma

Movement Speed: 85 Current Epsilon: 0.884084 Current Training Episode: 5 Current Reward: 26 Cumulative Episode Rewards: 26 Exploration / Exploitation: ● ● Prey Status: ● ● ●

Dead End Status: ● Phase: Training Show A* Shortest Path: Toggle



Adjust the speed at which the episodes play out



We use the greedy epsilon strategy, this is the chance the mouse chooses the best action to take. And $1 - \text{epsilon}$ the chance the mouse chooses a random action.

Current Epsilon
0.884084

The current reward is a reflection of how “good” the mouse’s action is. The more positive the better, and the more negative the worse.

Current Reward
26

The total rewards accumulated through the current episode.

Cumulative Episode Reward:
-318

Indicates whether the most recent action by the mouse was exploration or exploitation

Exploration / Exploitation



Prey status: Green will light up at the most left if mouse escapes, Yellow will light up in the middle if mouse is still alive, Red will light up at the most right if mouse gets caught by the cat

Prey Status



Click toggle to show the A* shortest path calculated by the cat to reach the mouse. The cat always takes the shortest path to the mouse.

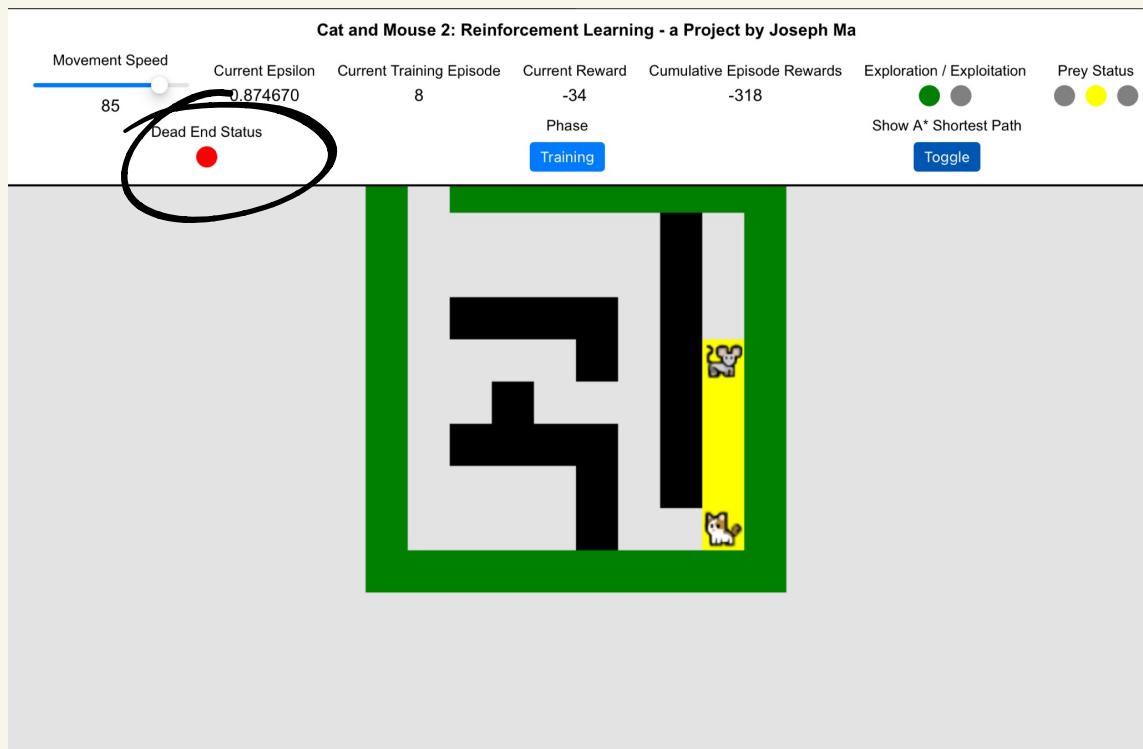
Cat and Mouse 2: Reinforcement Learning - a Project by Joseph Ma

Movement Speed: 85 Current Epsilon: 0.874670 Current Training Episode: 8 Current Reward: -34 Cumulative Episode Rewards: -318 Exploration / Exploitation: Show A* Shortest Path Prey Status: Training

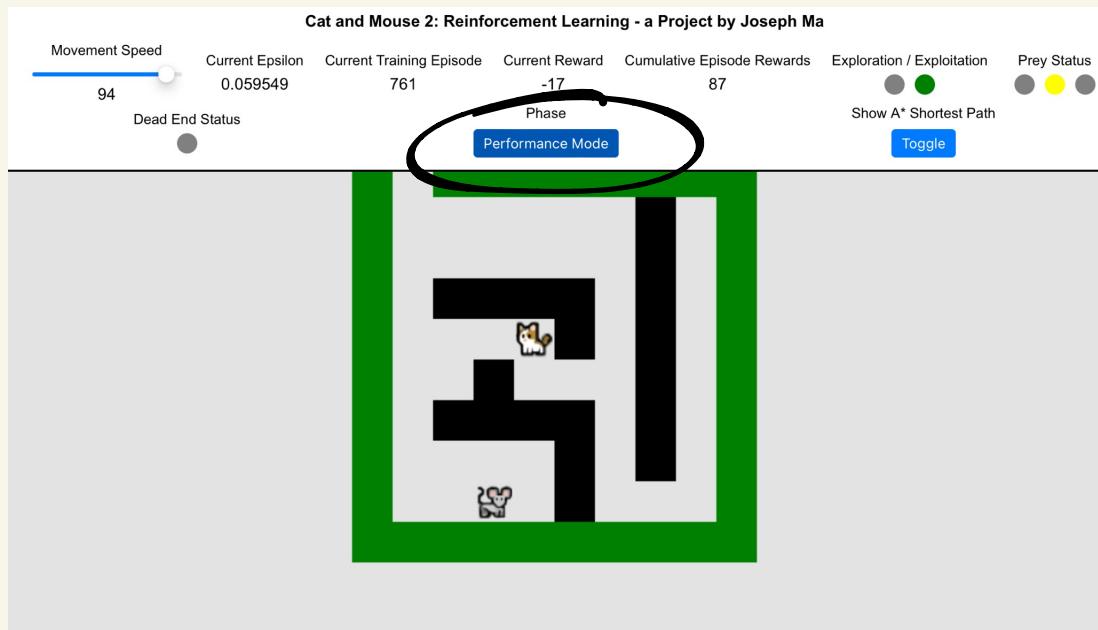
Dead End Status: ●

Show A* Shortest Path Toggle

If the mouse finds itself cornered by the cat, the dead end status will light up. A double DFS algorithm was written to check for this.



Once epsilon has decayed, toggle the training button. This will cause the mouse to take the best action in each move. In other words it will exploit every action. In this mode, the Qtable and epsilon will remain frozen until we return to regular training mode. This mode is to visualize how intelligent the mouse has gotten.



Reward function

NOTE: MAX_DISTANCE is defined as an estimate of the longest possible distance from one point of the grid to the other.

| Condition (IF-ELSE-IF) | Reward | Explanation |
|--|--|---|
| Dead End: False Maintained Distance from Cat: True Got Closer to Exit: True | MAX_DISTANCE | The mouse maintains distance from the cat and gets closer to the exit. |
| Dead End: False Maintained Distance from Cat: False (The cat got closer by 1 unit) Got Closer to Exit: False Exit Distance to Mouse < Exit Distance to Cat | $-(\text{MAX_DISTANCE} - \text{DISTANCE_TO_CAT})$ | Given that the cat got closer by 1 unit, that implies the mouse has not made a meaningful move. Since the cat uses A*, a decrease of 1 unit between the cat and mouse means the mouse did not move while the cat did. The fact that the mouse is closer to the exit than the cat means it can move towards the exit without fear of getting caught. |
| Dead End: False Maintained Distance from Cat: True Got Closer to Exit: False (The direction the cat was previously coming from != The previous direction from mouse -> exit) OR (The new distance to exit < distance from cat to exit) | $-(\text{MAX_DISTANCE} - \text{DISTANCE_TO_CAT})$ | The mouse was close enough to the exit (that is it could have reached it before the cat), but it decided not to move towards it. Basically, the mouse is wasting time. |
| Dead End: False Maintained Distance from Cat: True Got Closer to Exit: False | MAX_DISTANCE / 2 | The mouse maintains distance from the cat but gets further from the exit. In this case the cat was likely closer to the exit than the mouse was so it makes sense the mouse moves further away. |
| Dead End: False Got Closer to Exit: True Exit Distance to Mouse < Exit Distance to Cat | MAX_DISTANCE | The mouse is closer to the exit than the cat is. We can disregard the cat and move closer to the exit without worry. |

| | | |
|---|---|--|
| Dead End: False Above conditions not met | $-(\text{MAX_DISTANCE} - \text{DISTANCE_TO_CAT})$ | The cat got closer to us. That is terrifying. 😰😱 |
| Dead End: True Maintained Distance from Cat: True | $-(\text{MAX_DISTANCE} - \text{DISTANCE_TO_CAT}) - 0.5 * \text{MAX_DISTANCE}$ | The mouse is cornered in a dead end and moves inwards towards the dead end leading it closer to its inevitable death. |
| Dead End: True Maintained Distance from Cat: False (The cat got closer by 1 unit) | $-(\text{MAX_DISTANCE} - \text{DISTANCE_TO_CAT}) - 0.5 * \text{MAX_DISTANCE}$ | Any time the cat got closer by unit this means the mouse is idle. A* guarantees the Cat will either stay the same distance or get closer. Mouse is waiting to get eaten. |
| Dead End: True Maintained Distance from Cat: False (The cat got closer by 2 units) | $(\text{MAX_DISTANCE} - \text{DISTANCE_TO_CAT}) + 0.5 * \text{MAX_DISTANCE}$ | We might think that the cat getting closer by the maximum amount (2 units) is a bad thing. But when the mouse is in a dead end, this is the best thing it can do. Move towards the cat until we are out of the dead end! |
| We switched from Dead End: True -> Dead End: False | $1.5 * \text{MAX_DISTANCE}$ | Well done! We successfully got out of the dead end. |
| We switched from Dead End: False -> Dead End: True | $-1.5 * \text{MAX_DISTANCE}$ | This is not good. The mouse just wandered into a dead end. |
| Dead End: True We got Caught | 0 | If the mouse did all it could to escape (defined by the above conditions) sometimes getting caught is inevitable |
| Dead End: True We got Caught | $-1.5 * \text{MAX_DISTANCE}$ | You dead 😞 |
| Dead End: False We got Caught | $1.5 * \text{MAX_DISTANCE}$ | Well done mouse escaped 😊 |

The Markov Decision Process

$$Q(s, a) \leftarrow Q(s, a) + \alpha(r + \gamma \max_{a'} Q(s', a') - Q(s, a))$$

TD error

Discount Rate ($0 \sim 1$)

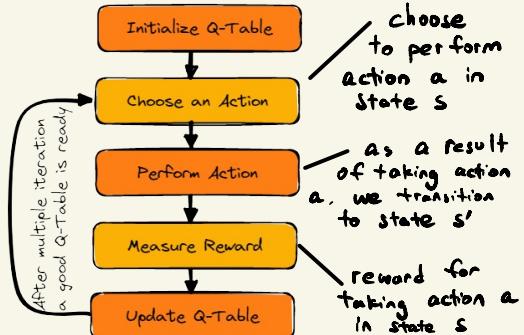
Maximum Q value of transition destination state

Old Q Value Reward Learning Rate ($0 \sim 1$) New Q Value

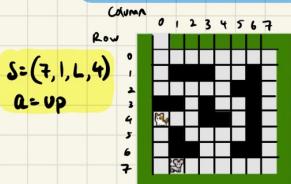


| possible states | possible actions | | | |
|-----------------|------------------|----------------|----------------|-----------------|
| | up | down | left | right |
| s_0 | $Q(s_0, up)$ | $Q(s_0, down)$ | $Q(s_0, left)$ | $Q(s_0, right)$ |
| s_1 | $Q(s_1, up)$ | $Q(s_1, down)$ | $Q(s_1, left)$ | $Q(s_1, right)$ |
| s_2 | $Q(s_2, up)$ | $Q(s_2, down)$ | $Q(s_2, left)$ | $Q(s_2, right)$ |
| : | : | : | : | : |
| s_n | $Q(s_n, up)$ | $Q(s_n, down)$ | $Q(s_n, left)$ | $Q(s_n, right)$ |

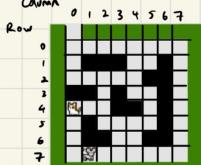
Assuming N states



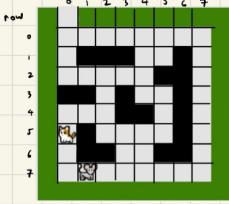
State $(7, 1, L, 4)$



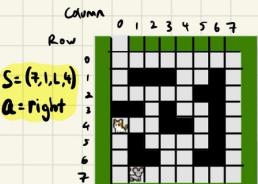
Random Action \downarrow UP



$s' = (7, 1, L, 3)$ \downarrow State $(7, 1, L, 3)$



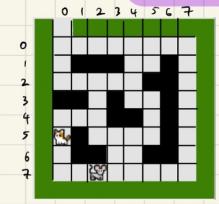
State $(7, 1, L, 4)$



Best Action \downarrow Right



$s' = (7, 2, L, 4)$ \downarrow State $(7, 2, L, 4)$



Qtable Actions

| States | up | down | left | right |
|--------------|----------|----------|----------|----------|
| $0, 0, R, 1$ | +5 | +3 | -10 | -13 |
| $0, 0, R, 2$ | +4.5 | +3.3 | -11 | -15 |
| $0, 0, R, 3$ | +6.3 | +2.7 | -14 | -14.5 |
| \vdots | \vdots | \vdots | \vdots | \vdots |
| $7, 1, L, 1$ | -2.7 | -1.8 | -28.3 | +12 |
| $7, 1, L, 2$ | -4.5 | -3.9 | -15.4 | +11.5 |
| $7, 1, L, 3$ | -2.7 | -4.4 | -27.5 | +9.3 |
| $7, 1, L, 4$ | -1.3 | -4.5 | -33.3 | +3.7 |
| \vdots | \vdots | \vdots | \vdots | \vdots |
| $7, 2, L, 1$ | -12.8 | -14.3 | -47.3 | +17.4 |
| $7, 2, L, 2$ | -13.4 | -13.5 | -34.3 | +15.7 |
| $7, 2, L, 3$ | -14.5 | -13.8 | -29.8 | +16.3 |
| $7, 2, L, 4$ | -13.6 | -14.5 | -33.5 | +16.5 |
| $7, 2, L, 5$ | -13.8 | -14.3 | -35.7 | +18.4 |

$\gamma = 0.95$ $s = (7, 1, L, 4)$ $a = \text{up}$

$\gamma = 0.95$

\downarrow

$s' = (7, 1, L, 3)$

| State | up | down | left | right |
|--------------|------|------|-------|-------|
| $7, 1, L, 3$ | -2.7 | -4.4 | -27.5 | +9.3 |

$$\text{Max } Q(s', a') = +9.3$$

| State | up | down | left | right |
|--------------|------|------|-------|-------|
| $7, 1, L, 4$ | -1.3 | -4.5 | -33.3 | +3.7 |

$$Q(s, a) = -1.3$$

Any other case

-(Maximum distance - distance from cat to mouse) = -(15 - 3) = -12

$$r = -(15 - 3) = -12$$

$$Q(s, a) = (1 - 0.95)(-1.3) + 0.95(-12) + 0.95(9.3) = -2.28$$

| State | up | down | left | right |
|--------------|-------|------|-------|-------|
| $7, 1, L, 4$ | -2.28 | -4.5 | -33.3 | +3.7 |

$\gamma = 0.95$ $s = (7, 1, L, 4)$ $a = \text{right}$

$\gamma = 0.95$

\downarrow

$s' = (7, 2, L, 4)$

| State | up | down | left | right |
|--------------|-------|-------|-------|-------|
| $7, 2, L, 4$ | -13.6 | -14.5 | -33.5 | +16.5 |

$$\text{Max } Q(s', a') = +16.5$$

| State | up | down | left | right |
|--------------|------|------|-------|-------|
| $7, 1, L, 4$ | -1.3 | -4.5 | -33.3 | +3.7 |

$$Q(s, a) = +3.7$$

Distance from cat to mouse stays the same, mouse gets closer to exit

Maximum Distance = 15

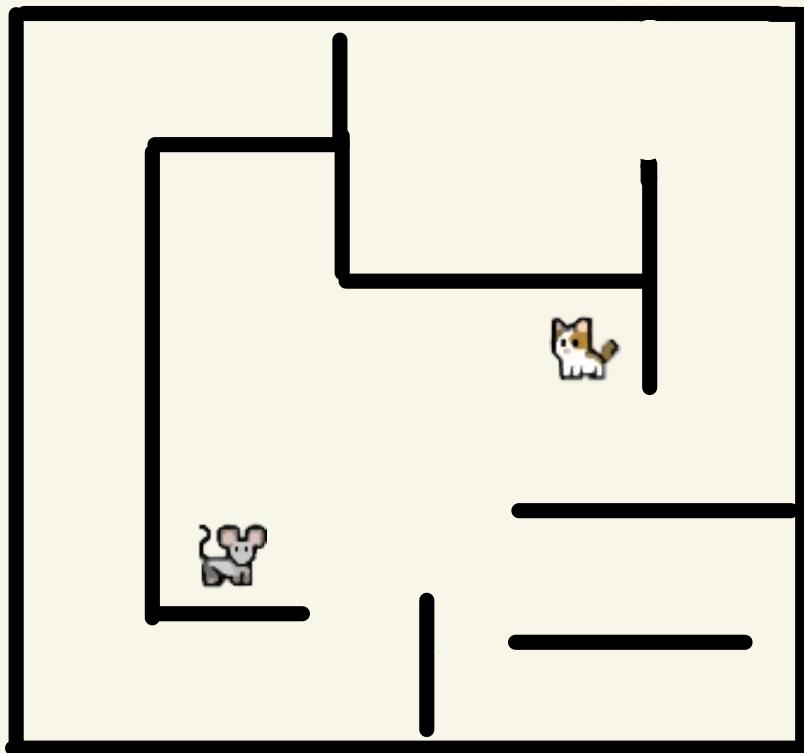
$$r = 15$$

$$Q(s, a) = (1 - 0.95)(-1.3) + 0.95(15) + 0.95(16.5) = 29.33$$

| State | up | down | left | right |
|--------------|------|------|-------|--------|
| $7, 1, L, 4$ | -1.3 | -4.5 | -33.3 | +29.33 |

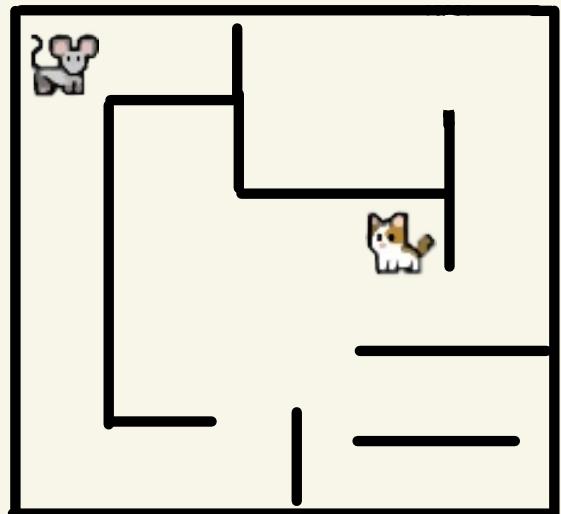
The Double DFS End Algorithm

What constitutes as a dead end?- that is any spot where we are truly cornered and will have limited mobility (just one direction). The concept seems subjective as it may depend on both the location of the cat/mouse and orientation of the maze. Here we go in depth into the double DFS dead end algorithm I came up with.

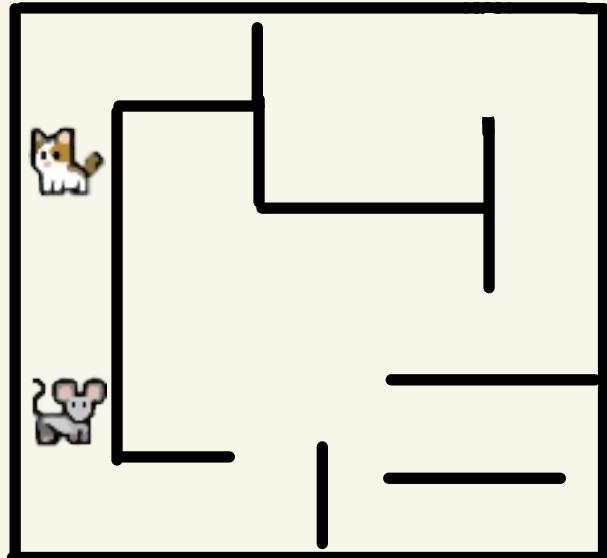


Whether we are in a dead end may also depend on our relative position to the cat

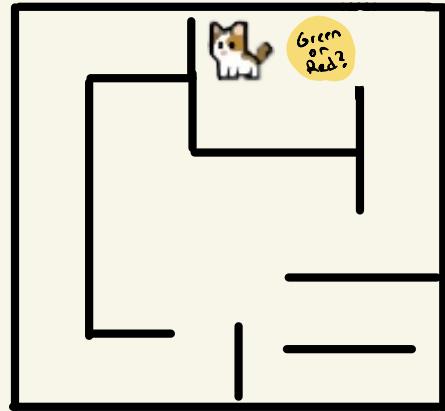
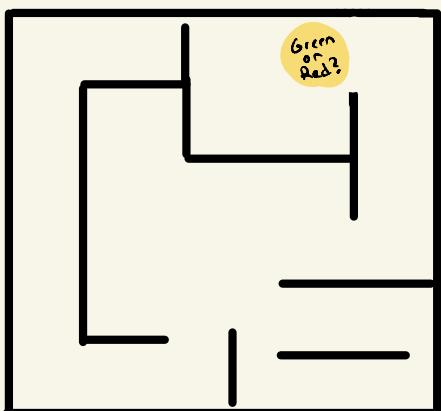
Dead end: true



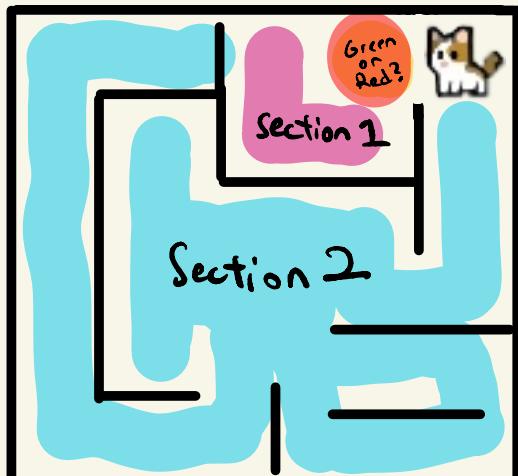
Dead end: false



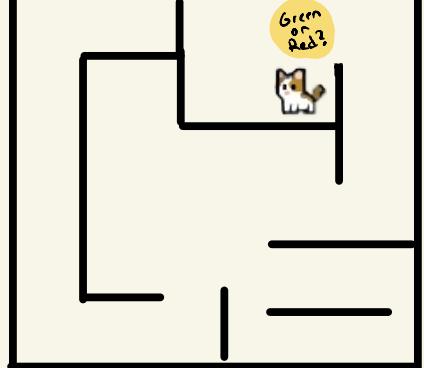
First step of the dead end algorithm: we first highlight the dots where we look in all 4 directions, placing an imaginary cat right next to that point. If the imaginary cat separates us from the rest of the map in any 4 of those points, we mark it red. Otherwise we mark it green.



Not separated from
rest of map ✓

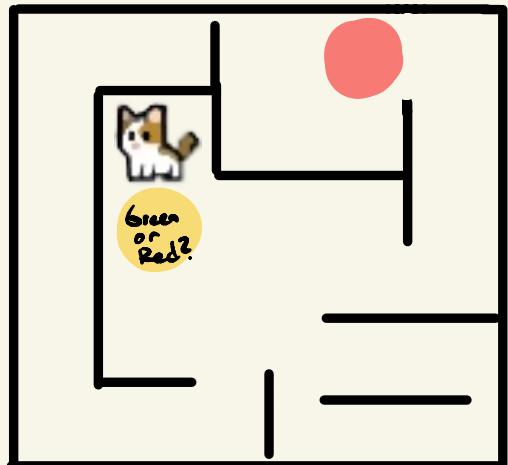
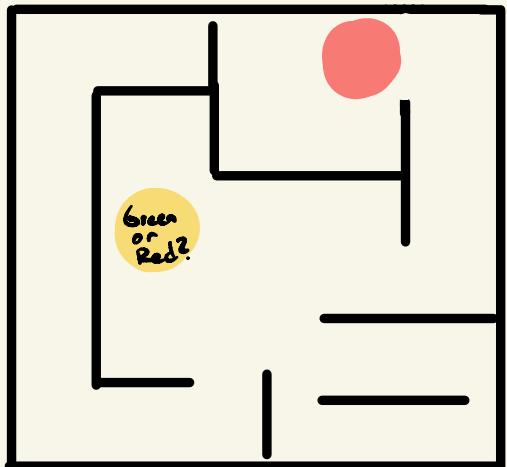


Separated!

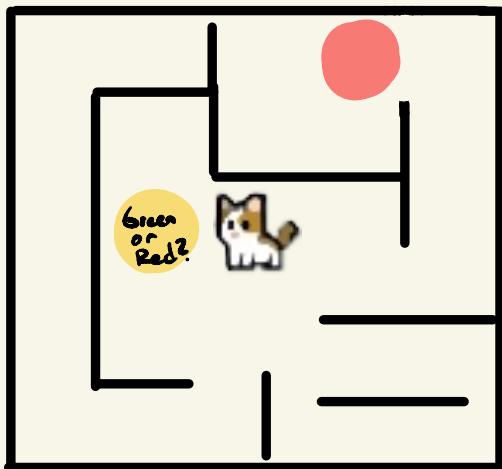
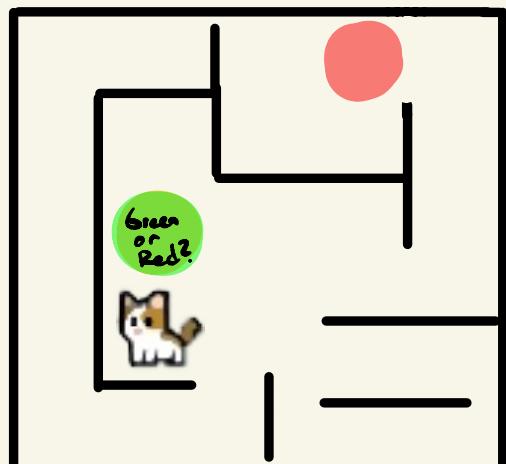


Not separated from
rest of map ✓

Let's do one more example!



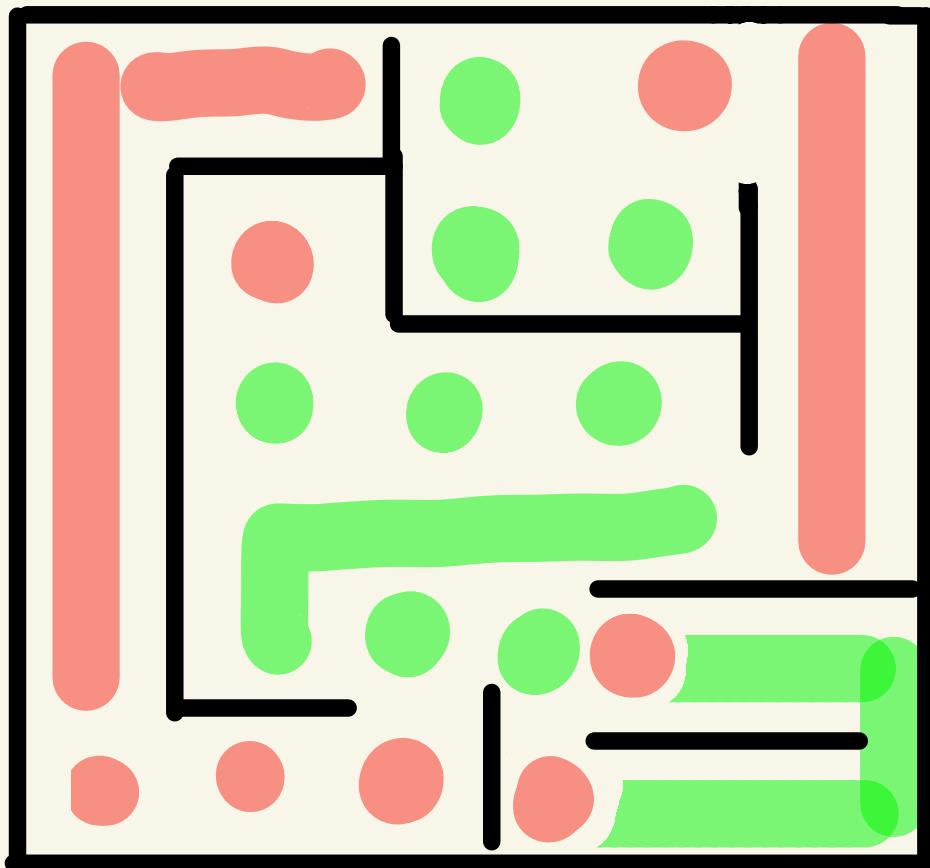
Not separated from
rest of map ✓



Not separated from
rest of map ✓

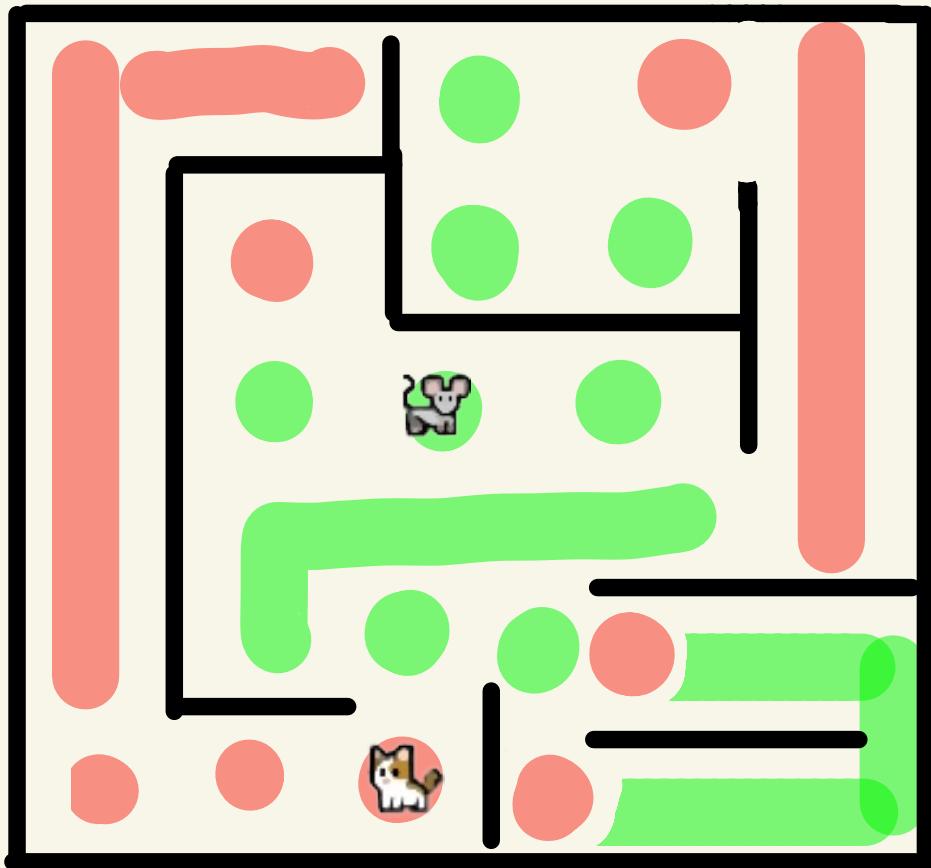
Not separated from
rest of map ✓

Result:



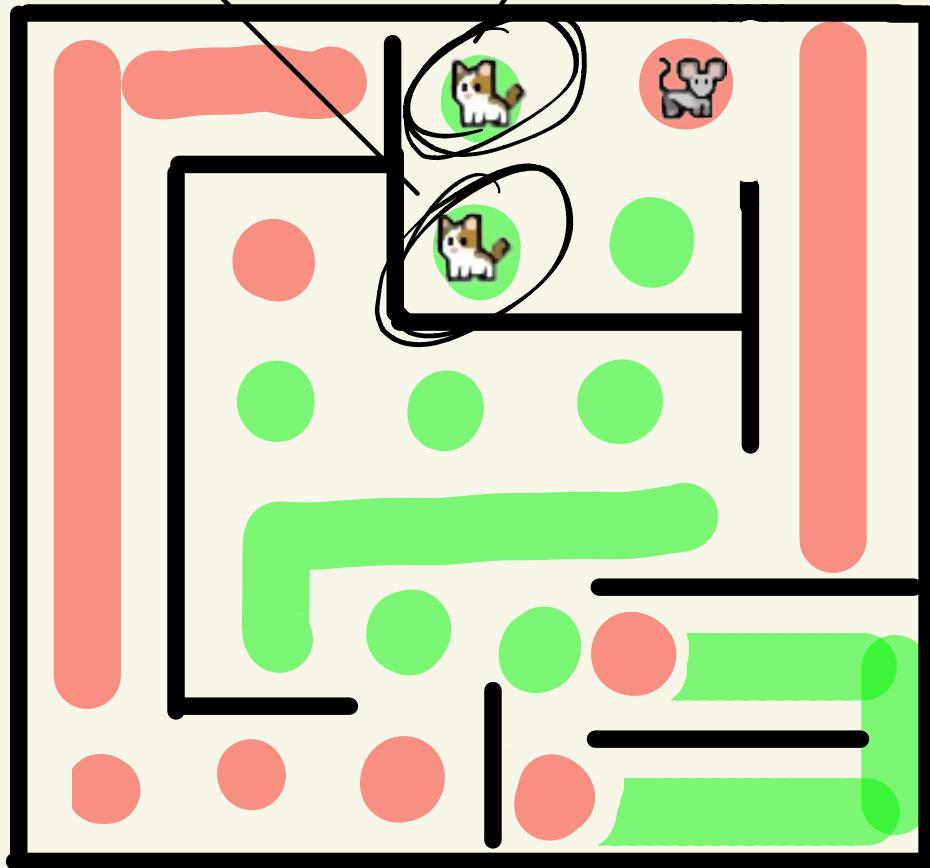
Second step of the dead end algorithm: for each evaluation of whether the mouse is in a dead end, if the mouse is on a green tile, we are NOT in a dead end. If the mouse is on a red tile we place an imaginary cat right next to the mouse (that is an imaginary cat from the direction the cat is coming from). If the imaginary cat does not separate us from the rest of the map, we are NOT in a dead end. If the imaginary cat separates us from the rest of the map, check whether we are connected to any green tiles. If we are connected to green tiles, we are NOT in a dead end. Otherwise if we are only connected to red tiles we are in a dead end.

We are on a green tile. DEAD END: FALSE



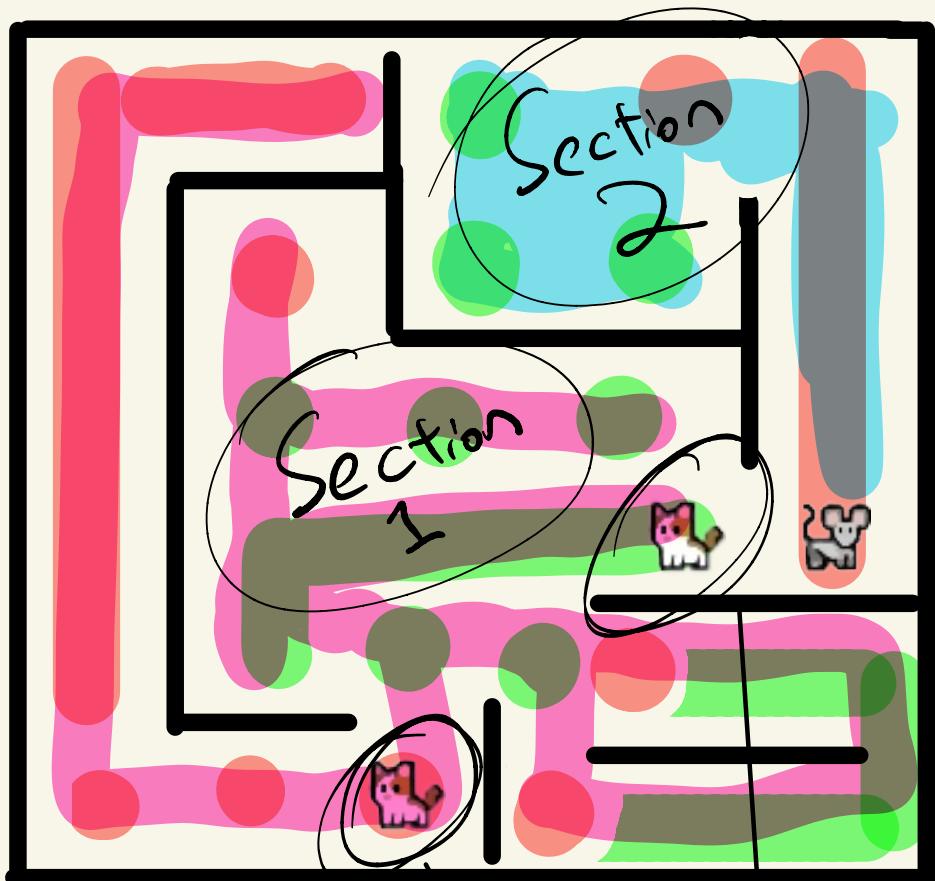
Real Cat

Imaginary
Cat



Since the mouse is not separated from the rest of the map due to the imaginary cat- DEAD END: FALSE

The imaginary cat separates us from the rest of the map but we are connected to green tiles-
DEAD END: FALSE



The imaginary cat separates us from the rest of the map AND we are NOT connected to green tiles- DEAD END: TRUE

