

Assignment-02

Q1
void fun (int n)
{ int j=1, i=0;
while (i < n)
{ j = i+j;
j++;
}

n=5
i j
0 1
0+1 2
0+1+2 3
0+1+2+3

$$O\left(\frac{n(n+1)}{2}\right)$$

$$\{O(n^2)\}$$

Q2
~~void~~ int fibonacci (int n)
a=0, b=1
if (n <= 1 ~~// n == 2~~)
return 1;
fibonacci (n-1) + fib (n-2);

$$T(n) = T(n-1) + T(n-2) + 1$$

$$T(n) = 1 + 2 + 4 + 8 + \dots + 2^{n-1}$$

$$= \frac{2^{n+1} - 1}{2 - 1} = 2^n \cdot 2 - 1$$

$$O(2^n)$$

Time complexity of this fun is $O(n)$.
 It has n stack frame, $f(n), f(n-1), f(n-2), \dots, f(1)$,
 and $O(1)$ space per stack frame to store arg. (n) .

ii) $O(n \log n)$ -

```
void fun(int n)
{
  int c = 0;
  for(i = 0; i < n; i++)
  {
    for(j = 0; j < n; j += 2)
    {
      c++;
    }
  }
}
```

ii) $O(n^3)$ -

```
void fun(int n)
{
  int c = 0;
  for(i = 0; i < n; i++)
  {
    for(j = 0; j < n; j++)
    {
      for(k = 0; k < n; k++)
      {
        c++;
      }
    }
  }
}
```

iii) $O(\log(\log n))$:-

```
for(i = 2; i <= n; i = Pow(i, c))
{
  // some  $O(1)$  exprs
}
```

Q4

$$T(n) = T(n/4) + T(n/2) + cn^2$$

Q5

$$O(n^3)$$

Q6

$$O(\log(\log n))$$

Q7