



# **Evaluating the benefit of grid-based weather information in energy forecasting**

Bachelors's Thesis of

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I declare that I have developed and written the enclosed thesis completely by myself, and have not used sources or means without declaration in the text.

**Karlsruhe, 2019/10/31**

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(Marcel Herm)



# Abstract

As the share of electricity from regenerative sources is growing constantly, the weather becomes an increasingly important factor in the analysis of electricity markets. Hence, this thesis uses local weather data to predict electricity spot prices. More precisely, we include wind speed and temperature from individual German weather stations into time series and statistical learning models. However, as the available weather information is vast and renewable power is not generated everywhere, we use random forests and Bayesian structural time series to perform a feature selection. Overall, we manage to improve our forecasting accuracy of the EPEX electricity prices by up to 7.69 % in terms of root mean squared error and up to 8.19 % in terms of mean absolute error.



# Contents

<b>1. Introduction</b>	<b>1</b>
<b>2. Related Work</b>	<b>3</b>
<b>3. Methodology</b>	<b>9</b>
3.1. Forecasting methods . . . . .	9
3.2. Feature selection techniques . . . . .	10
3.3. Forecast Evaluation . . . . .	11
<b>4. Evaluation</b>	<b>13</b>
4.1. Data . . . . .	13
4.1.1. ECMWF . . . . .	13
4.1.2. Load data . . . . .	15
4.1.3. Population . . . . .	18
4.2. Implementation . . . . .	19
4.3. Results . . . . .	19
<b>5. Discussion</b>	<b>25</b>
<b>6. Conclusion</b>	<b>27</b>
<b>Terms and abbreviations</b>	<b>29</b>
<b>Bibliography</b>	<b>33</b>
<b>A. Appendix</b>	<b>35</b>





# List of Figures

4.1.	Four maps showing the four times with the highest two metre temperature variance in Germany, where top left is the highest, top right the second highest, bottom left the third highest and bottom right the fourth highest variance. . . . .	14
4.2.	2D boolean numpy.ndarray (left) used to filter grid squares that are within Germany. It was created by using a shapefile of Germany from Eurostat and checking for each point of the grid if it is within the shapefile. When applied to the weather data, only relevant data within Germany is obtained (right). . . . .	15
4.3.	Load curve with mean of 2 metre measured temperature in Germany as color from 2015/1/1 to 2018/12/31 with one single point per day at 12 AM UTC time respectively. . . . .	17
4.4.	Population of Germany for each region respectively using a log scale for better distinction. . . . .	18
4.5.	Autocorrelation (a) and Partial Autocorrelation (b) plots used to select the order of ARMA and ARMAX models. . . . .	20
4.6.	An example forecast from 2017/12/31 01:00 to 2018/12/31 00:00 for an ARMAX(1,0) using load data from 2015/01/08 00:00 to 2017/12/31 00:00 performing one step ahead forecasts for each step, which equals 1 hour forecasts due to the 1 hour resolution of the data. . . . .	21
4.7.	An example forecast from 2017/12/31 01:00 to 2018/12/31 00:00 for an ARMAX(1,0) using load data from 2015/01/08 00:00 to 2017/12/31 00:00 and seven dummy variables each for one week day as exogenous input, performing one step ahead forecasts for each step, which equals one hour forecasts due to the one hour resolution of the data. . . . .	22

4.8.	An example forecast from 2017/12/31 01:00 to 2018/12/31 00:00 for an ARMAX(1,0) using load data from 2015/01/08 00:00 to 2017/12/31 00:00 and the load data shifted back in time by one week as exogenous input, performing one step ahead forecasts for each step, which equals one hour forecasts due to the one hour resolution of the data. . . . .	23
A.1.	Load curve with mean of 2 meter height measured temperature in germany as color from 2015/1/1 to 2018/12/31 with one single point per day at 12am utc time respectively. . . . .	36

# List of Tables

2.1.	List of related works regarding the type of the used weather data, used methods, place of origin of the data, forecast horizon and forecast time series. . . . .	7
4.1.	List of exogenous weather variables used to forecast the load including min, max values from ECMWF. . . . .	15
4.2.	Information Criteria for ARMA models without exogenous inputs using training data from 2015/01/01 to 2017/12/31. . . . .	20
4.3.	ARMAX results. . . . .	20



# 1. Introduction

TODO mention that the idea for this thesis originated from Nicole Ludwig<sup>1</sup>

According to Li et al. (2009), especially temperature and perceived temperature have a great impact on energy demand. Consequently, several authors combine forecasting energy time series using weather data. They mostly either focus on forecasting photovoltaic (PV) electricity generation as in Bofinger and Heilscher (2014) and Sperati et al. (2016) or on electricity generation from wind as in Davò et al. (2016) and Alessandrini et al. (2015).

It is notable, that works using station-based data often try to do some sort of geographic interpolation to be able to obtain values for every possible position. Considering this thesis, there is no such problem, as the used grid-based data already provides such distributed values. Thus, when using grid-based data, the step of interpolation can be omitted, and therefore, less effort is required. Some works also regard only forecasting for specific locations or accumulated values for bigger areas. With grid-based data, more general predictions can be made regarding the target location, as there is no binding to a certain locality.

Another interesting point is, that the works that forecast weather related time series all used grid-based data, though some of them also used station-based data to refine their forecasts. Among the papers that aimed for forecasting power or similar often only station-based data is used which leads to the assumption that less effort has been made in these fields, as it is still more complex to acquire grid-based data. However, there remains the possibility that station-based data is more suitable, even though this means a trade-off in terms of flexibility. Of course it is also possible that this has to do with the fact, that there is no grid-based power data available as this may harm privacy issues.

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<sup>1</sup>[https://www.iai.kit.edu/2154\\_2161.php](https://www.iai.kit.edu/2154_2161.php)



## 2. Related Work

This chapter gives an overview of related work in the field of energy forecasting considering grid-based data. After describing the general approach of search, there are some sources presented in ascending order of degree of relation to this thesis.

In order to find relevant literature, arXiv<sup>1</sup>, Google Scholar<sup>2</sup> and BASE<sup>3</sup> are used.

In the process of search, the following criteria are applied to identify relevant literature:

- The title of the paper suggests that the authors work with geographic or grid-based data
- The title of the paper implies that the subject of the paper is being situated in the field of energy networks
- The title of the paper suggests that the authors aim at forecasting values
- The abstract or introduction of the paper suggests that the authors work with geographic or grid-based data
- The abstract or introduction of the paper suggests that the authors aim at forecasting or rather how forecasting is done

Subsequently, there will be two papers outlined which provide useful information for related research. After that, the papers that meet above criteria are outlined and explained regarding the used type of data, the forecast time series, applied forecasting methods, the location and the forecast horizon.

There is a high correlation between internet traffic load and electricity load, as can be read in Morley et al. (2018). This is why Kamińska-Chuchmala (2014) are considered to contain valuable information. They apply Ordinary Kriging (OK) to spatially interpolate station-based data. Due to the high similarity between internet traffic load and electricity load, it

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<sup>1</sup><https://arxiv.org/>

<sup>2</sup><https://scholar.google.de/>

<sup>3</sup><https://www.base-search.net/>

has potential for related subjects and also influenced this work e. g. concerning further research. Furthermore, this work underlines the benefit of grid-based data by illustrating the necessary effort of processing station-based data. Another suitable example utilizing station-based data is Fairley et al. (2017) which investigates marine electricity generation and critically discusses implications for electricity supply. This combines localization issues and the electricity network. Unfortunately, the aim here is not to forecast, but only to examine the problem.

The first group of related work utilizes grid-based, station-based or both types of data to forecast various, not necessarily electricity generation related, time series. In the first paper elaborated by Ludwig et al. (2015), the use of station-based weather data from Deutscher Wetterdienst (DWD) for electricity price forecasting in Germany is investigated. The price history is obtained from European Power Exchange (EPEX SPOT). The work compares Least Absolute Shrinkage Selection Operation (LASSO) and Random Forests (RF) in addition to Autoregressive-Moving Average (ARMA) and Autoregressive-Moving Average with Exogenous Inputs (ARMAX) models. A desirable side effect from RF is the output of the variable importance which is useful in order to filter variables by order of their relevance. As this work has a focus on short-term forecasts, the forecast time series here is the electricity price for the next day, thus having a forecast horizon of 24 hours. Another example of this group is Salcedo-Sanz et al. (2018), where grid-based weather data is used to forecast solar radiation in Australia. The evaluated methods are combinations of Coral Reefs Optimization (CRO), Extreme Learning Machine (ELM), Grouping Genetic Algorithm (GGA), Multivariate Adaptive Regression Splines (MARS), Support Vector Regression (SVR) for a forecast horizon of 24 hours. Similarly, Diagne et al. (2013) utilizes grid-based weather data for solar radiation forecasting. Different data sources are compared, specifically European Centre of Medium-Range Weather Forecasts (ECMWF), Fifth-generation Mesoscale Model (MM5) and Weather Research and Forecasting Model (WRF). The paper focuses on Autoregressive (AR) methods including ARMA, Autoregressive Integrated Moving Average (ARIMA) and Coupled Autoregressive and Dynamical System (CARDS), Neural Networks (NN) and Wavelet Neural Networks (WNN) considering short time ranges from 5 min up to 6h.

The second group of related work forecasts electricity generation and makes use of station-based data. E. g. Aguiar et al. (2016) utilize both, grid-based and station-based weather data to improve Global Horizontal Solar Irradiance (GHI) forecasts on Gran Canaria Island. GHI is similar to solar radiation that is forecast in the last paper of the previous group. In order



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to obtain the desired results, NN are applied. As the authors consider intra-day forecasting, the forecast horizon is limited to a range from 1 up to 6 hours in this case. Bofinger and Heilscher (2014) acquire data only from local weather stations to forecast solar power generation. The data is then refined with grid-based data from ECMWF by applying Model Output Statistics (MOS) and Inverse Distance Weighting (IDW), spatially interpolated and then simulated for Germany in order to predict a temporal range of 24-120 hours. In a work, that has been published by Haben et al. (2018), station-based weather data is applied to forecast low voltage load in the United Kingdom. They implement Kernel Density Estimation (KDE), Simple Seasonal Linear Regression (SSLR), Autoregressive model using an average weekly profile (ARWD), Autoregressive model using an average weekly profile including annual seasonality (ARWDY) and Holt-Winters-Taylor Exponential Smoothing Method (HWT-ESM) and compare them for forecast horizons of up to 4 days. Alessandrini et al. (2015) utilize non-gridded wind and power data from a wind farm in northern Sicily in Italy, with which they forecast generated wind power. Here, a novel approach, an Analog Ensemble (AnEn), is applied to the data to retain a probabilistic prediction for the next 0-132 hours. This method originally is used for meteorological ensemble forecasts.

The last group of related work forecasts electricity generation, but in contrast to the first two groups, only uses grid-based data. An application of grid-based data from ECMWF is proposed in Sperati et al. (2016) for solar power prediction in Italy. They implement a Probability Density Function (PDF) combined with NN, Variance Deficit (VD), Ensemble Model Output Statistics (EMOS) and Persistence Ensemble (PE). The time series forecast includes a range of 0-72 hours. Similar to this thesis, De Felice et al. (2015) use grid-based data from ECMWF to forecast the electricity demand, though for Italy. Linear Regression (LR) and a Support Vector Machines (SVM) are applied. Given that power prediction is a rather complex problem, the non-linear SVM performs better than a simple LR. The last, and therefore most relevant paper presented, is Davò et al. (2016) who utilize grid-based wind speed data generated by applying the Regional Atmospheric Modelling System (RAMS) with boundary conditions from ECMWF. Furthermore, they acquire grid-based data of solar radiation energy per square meter as one of the two forecast time series is the solar irradiance. The data is coming from National Oceanic and Atmospheric Administration - Earth System Research Laboratory (NOAA/ESRL) and was provided for an online competition hosted by Kaggle<sup>4</sup>, an online community for data scientists providing competitions which are mainly based on machine learning tasks. Reference power data is

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<sup>4</sup><https://www.kaggle.com/>

obtained from Terna<sup>5</sup>, one of the main European electricity transmission grid operators, since the other predicted time series is the wind power produced over Sicily. A Principal Component Analysis (PCA) is employed, as grid-based data is even more prone to the curse of dimensionality because of the two additional dimensions. In terms of forecasting, they apply NN and an AnEn. The forecast horizon has a range of 0 to 72 hours and the output is a prediction of both, wind power and solar radiation.

Comparing the works above to this thesis, it is notable that none of them focuses on the exact issue of evaluating the benefit of grid-based data to forecast energy time series. This is why other papers containing similar subjects are consulted as information sources in order to solve this problem. Table 4.2 provides an overview about the mentioned related works regarding the type of the used weather data, used methods, the place of origin of the data, the forecast horizon and the forecast time series.

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<sup>5</sup><https://www.terna.it/>

<b>paper</b>	<b>type of weather data</b>	<b>forecast time series</b>	<b>location</b>	<b>methods</b>	<b>forecast horizon</b>
Ludwig et al. (2015)	station-based	energy prices	Germany	ARMA,ARMAX,LASSO,RF	24h
Salcedo-Sanz et al. (2018)	grid-based	solar radiation	Australia	ELM,CRO,MARS, MLR,SVR,GGA	24h
Diagne et al. (2013)	grid-based	solar radiation	-	ARMA,ARIMA,CARDS, NN,WNN	5 min-6h
Aguilar et al. (2016)	mixed	solar radiation	Gran Canaria Island	NN	1-6h
Böfinger and Heitscher (2014)	mixed	solar power	Germany	MOS,JDW	24-120h
Haben et al. (2018)	station-based	low voltage electricity load	United Kingdom	KDE,SLR,ARWD, ARWDY,HWT-ESM	up to 4 days
Alessandrini et al. (2015)	station-based	wind power	Sicily	AnEn	0-132h
Sperati et al. (2016)	grid-based	solar power	Italy	PDF,NN,VD,EMOS,PE	0-72h
De Felice et al. (2015)	grid-based	electricity demand	Italy	LR,SVM	1-2 months
Davò et al. (2016)	grid-based	wind power,solar radiation	Sicily	PCA,AnEn,NN	0-72h
<b>This thesis</b>	grid-based	electricity load	Germany	LR,ARMA,ARMAX,PCA	1h

**Table 2.1.** List of related works regarding the type of the used weather data, used methods, place of origin of the data, forecast horizon and forecast time series.



## 3. Methodology

This chapter introduces the methods that are applied in this thesis. The first group of methods comprises the used forecasting methods, the second group involves feature selection techniques and the last group covers methods that are used to evaluate forecasts.

### 3.1. Forecasting methods

For time series forecasting, often used methods are e. g. ARMA models as mentioned in Hyndman and Athanasopoulos (2018). This sections will introduce the methods that are applied in this thesis to forecast the electricity load.

#### ARMA

The ARMA model is a combination of Autoregressive (AR) and Moving Average (MA) terms. The formal description is given by

$$y_t = c + \sum_{i=1}^p \phi_i y_{t-i} + \sum_{j=1}^q \rho_j \epsilon_{t-j} + \epsilon_t , \quad (3.1)$$

with  $c$  as a constant,  $\epsilon_t$  as noise term with respect to time  $t$ ,  $p$  as size of the AR part,  $q$  as size of the MA part,  $\phi$  and  $\rho$  for the AR and MA coefficients respectively and  $y_t$  as the response variable.

#### ARMAX

An extension of ARMA is ARMAX, which includes an additional term for exogenous variables. This term can be used to include relations to external factors that do not depend

on the endogenous data. It is formally described as

$$y_t = c + \sum_{i=1}^p \phi_i y_{t-i} + \sum_{j=1}^q \rho_j \epsilon_{t-j} + \sum_{k=1}^n \eta_k x_k + \epsilon_t . \quad (3.2)$$

The only difference between Equation (3.2) and Equation (3.1) is the additional term  $\sum_{k=1}^n \eta_k x_k$  for the ARMAX for  $n$  included exogenous variables  $x$  with  $\eta$  as the respective coefficients.

## 3.2. Feature selection techniques

Because the used weather data is grid-based, there are two more dimensions than usual, where only one value per time step exists for a variable. This is why feature selection here is more important in order to obtain a reasonable computation time. In the following, the used methods for feature selection are presented.

### Naive approach

First, naive techniques are presented, that are used to reduce the huge amount of grid-based weather data. They are reduced along the two spatial dimensions, longitude and latitude, for each step in time, respectively. These are simple functions such as the maximum or the mean. An exemplary formula for reducing the data along longitude and latitude using the mean is given as

$$x_t = \frac{1}{l \times m} \sum_{i=1}^l \sum_{j=1}^m x_{ij} , \quad (3.3)$$

where  $x_t$  is the calculated mean for time  $t$ ,  $l$  and  $m$  are the size of the data along the axis of the longitude and latitude and  $x_{ij}$  is the value of a weather variable at the grid point with longitude  $i$  and latitude  $j$ .

### Using population data

Another method involves population data from Eurostat<sup>1</sup>. It contains the population of NUTS 3 level regions. The regions are sorted by population and those with the highest population are used to filter the respective grid points that are then used as exogenous variables.

## 3.3. Forecast Evaluation

In order to estimate whether the used model performs well, it is important to apply suitable metrics to evaluate the results. In the following, the four used metrics are introduced, where for each metric,  $k$  is the number of forecast values,  $y$  the actual values and  $\hat{y}$  the predicted values.

### Root Mean Squared Error

The first metric is the Root-Mean-Square Error (RMSE), which is an often used, scale-dependent accuracy measure that calculates the root of the squared mean of the differences between the forecast and the actual values. It is described by

$$RMSE = \sqrt{\frac{1}{k} \sum_{i=1}^k (y_i - \hat{y}_i)^2} . \quad (3.4)$$

### Mean Absolute Error

The second metric is the Mean Absolute Error (MAE), which is another scale-dependent accuracy measure that averages absolute errors. The equation for the MAE is described by

$$MAE = \frac{1}{k} \sum_{i=1}^k |y_i - \hat{y}_i| . \quad (3.5)$$

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<sup>1</sup><https://ec.europa.eu/eurostat/data/database>

#### Mean Percentage Error

The third metric is the Mean Percentage Error (MPE), which is a relative measure of the prediction accuracy. Since it is multiplied by 100 after dividing it by the size of the predictions, it is called a percentage error. The equation is

$$MPE = \frac{100}{k} \sum_{i=1}^k \frac{y_i - \hat{y}_i}{y_i} . \quad (3.6)$$

#### Mean Absolute Percentage Error

The fourth metric is the Mean Absolute Percentage Error (MAPE), which is similar to the MPE, but takes the absolute value of each single error instead. The equation for the MAPE is given by

$$MAPE = \frac{1}{k} \times 100 \sum_{i=1}^k \left| \frac{y_i - \hat{y}_i}{y_i} \right| . \quad (3.7)$$



## 4. Evaluation

This chapter provides information about the input data acquired from different sources, the methods that were used to forecast electricity load and other statistical methods and also evaluates them regarding performance and the quality of the output.

### 4.1. Data

In this section, the different types of data that are used within this thesis are presented. After that, the process of data preprocessing is briefly examined.

#### 4.1.1. ECMWF

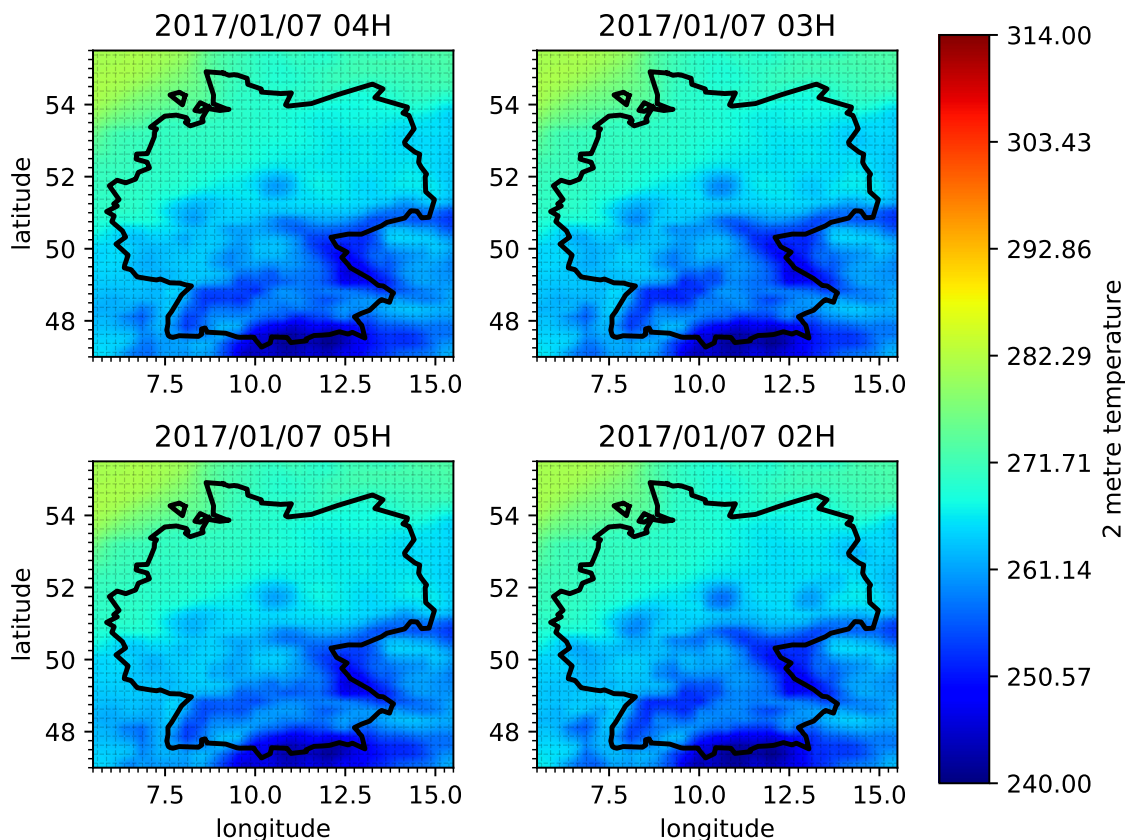
The data used in this thesis originates from ECMWF, which is a research institute that produces global numerical weather predictions and other data.

It is time series based and for each timestamp there is a 2-dimensional array referred to by longitude and latitude respectively.

It must be mentioned, that, as the data used has been reanalysed, so the expected error is likely to be smaller than if working with real-time data.

As data parameters, there are also longitude and latitude, where the longitude is chosen to be from 5.5 to 15.5 and the latitude from 47 to 55.5. As the resolution of the used grid is at  $0.25^\circ$ , this results in a total of 1435 grid points per timestamp. As the range of the data from ECMWF extends from 2015/1/1 to 2018/12/31, there is a total of 1461 days with each 24 timestamps due to the 1 hours frequency and thus 35064 timestamps. Considering that there is a value for each point in the grid and every timestamp, there are 50316840 values for each variable and thus 654118920 values for 13 variables.

Figure 4.1 shows four plots of the data on a map of Germany and Figure 4.2. In this case the temperature measured at 2 metres is visualized.

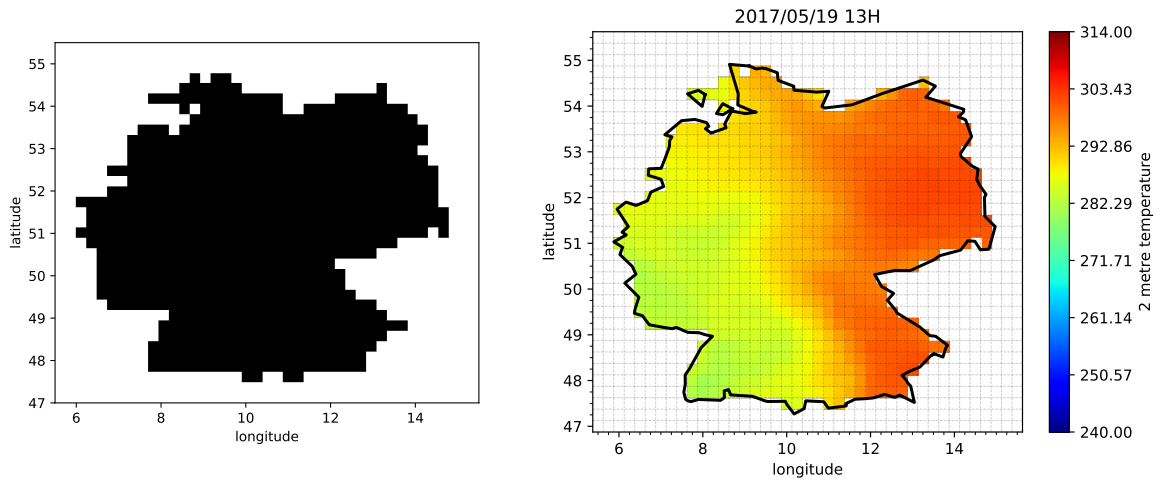


**Figure 4.1.** Four maps showing the four times with the highest two metre temperature variance in Germany, where top left is the highest, top right the second highest, bottom left the third highest and bottom right the fourth highest variance.

In order to reduce complexity, a shapefile of the NUTS dataset was used. The shapefile contains all countries in the EU. The shape of Germany was filtered from this data and each point in the dataset is checked whether it is within Germany or not. The result can be seen in Section 4.1.1. The filtered map first is saved in a `numpy.ndarray` and then applied on the data to mask unwanted data visualized in Section 4.1.1.

The initial dataset contains a set of variables listed in Table 4.1 where also the units, min and max are shown for each variable respectively.

<sup>1</sup><https://ec.europa.eu/eurostat/de/web/gisco/geodata/reference-data/administrative-units-statistical-units/nuts>



**Figure 4.2.** 2D boolean numpy.ndarray (left) used to filter grid squares that are within germany. It was created by using a shapefile of Germany from Eurostat<sup>1</sup> and checking for each point of the grid whether it is within the shape. When applied to the weather data, only relevant data within Germany is obtained (right).

variable name	units	min	max
10 metre U wind component	$m s^{-1}$	-18.56	21.92
10 metre V wind component	$m s^{-1}$	-21.51	20.00
2 metre temperature	$K$	240.97	313.26
Leaf area index, high vegetation	$m^2 m^{-2}$	0.00	4.90
Leaf area index, low vegetation	$m^2 m^{-2}$	0.00	3.84
Low cloud cover	(0 – 1)	0.00	1.00
Soil temperature level 1	$K$	257.91	313.64
Surface latent heat flux	$J m^{-2}$	-2203977.00	359411.00
Surface net thermal radiation	$J m^{-2}$	-663417.00	142945.02
Surface sensible heat flux	$J m^{-2}$	-1703159.00	801354.00
Total cloud cover	(0 – 1)	0.00	1.00
Total column rain water	$kg m^{-2}$	0.00	2.73
Total sky direct solar radiation at surface	$J m^{-2}$	-0.12	3088320.00

**Table 4.1.** List of exogenous weather variables used to forecast the load including min, max values from ECMWF<sup>2</sup>.

#### 4.1.2. Load data

Besides weather data used to refine the forecasting results, also historic load data was needed. Therefore data has been retained from Open Power System Data<sup>3</sup>. Figure 4.3 shows the distribution of loads over time with one point per day at 12 am UTC time. The color shows the mean temperature measured at 2 metres. The same data in a single plot is added in the Appendix as Figure A.1, it is shown here in two plots for better distinction of

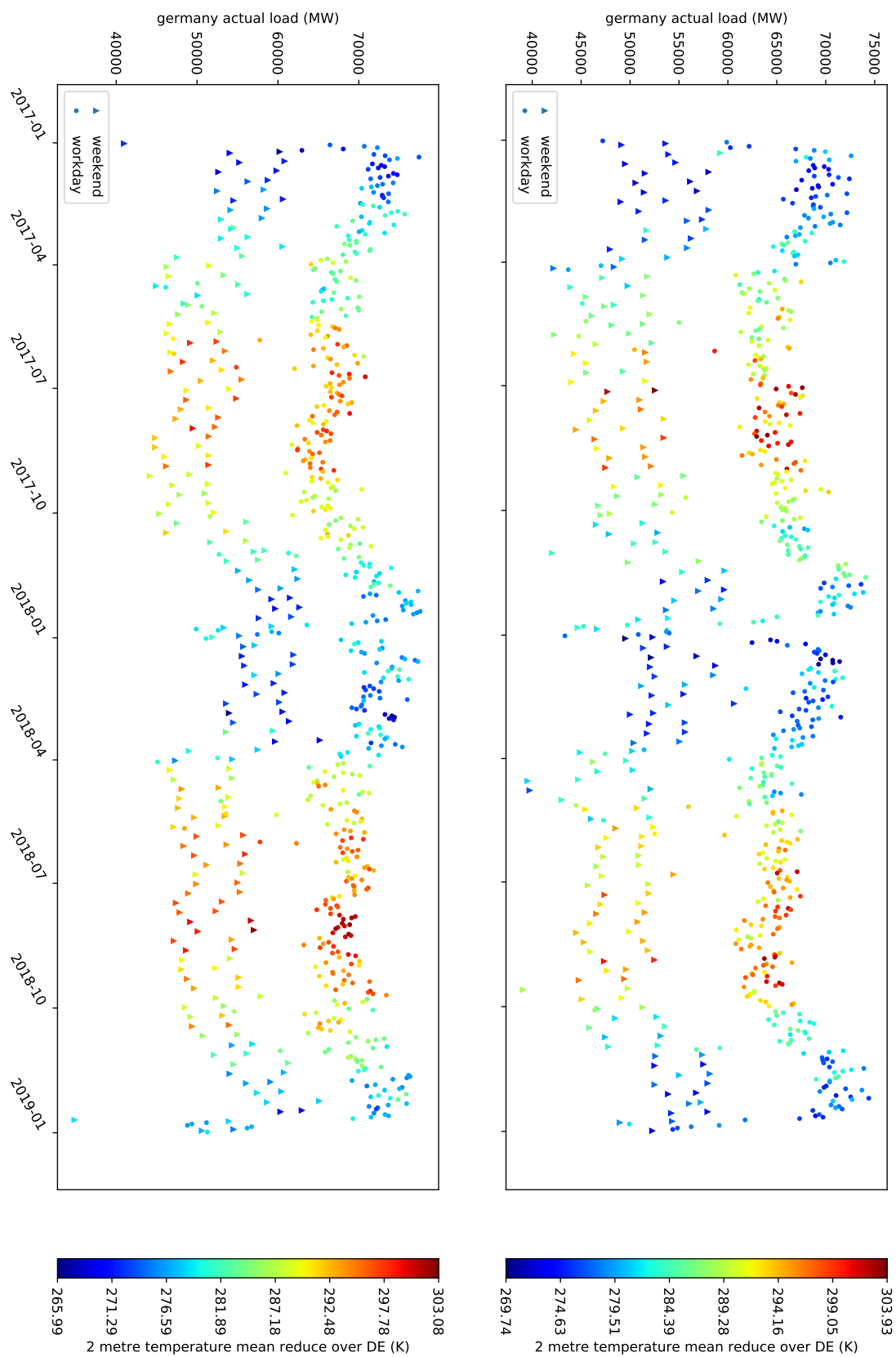
<sup>2</sup><https://www.ecmwf.int/en/forecasts/datasets/browse-reanalysis-datasets>

<sup>3</sup>[https://data.open-power-system-data.org/time\\_series/](https://data.open-power-system-data.org/time_series/)

#### 4. *Evaluation*

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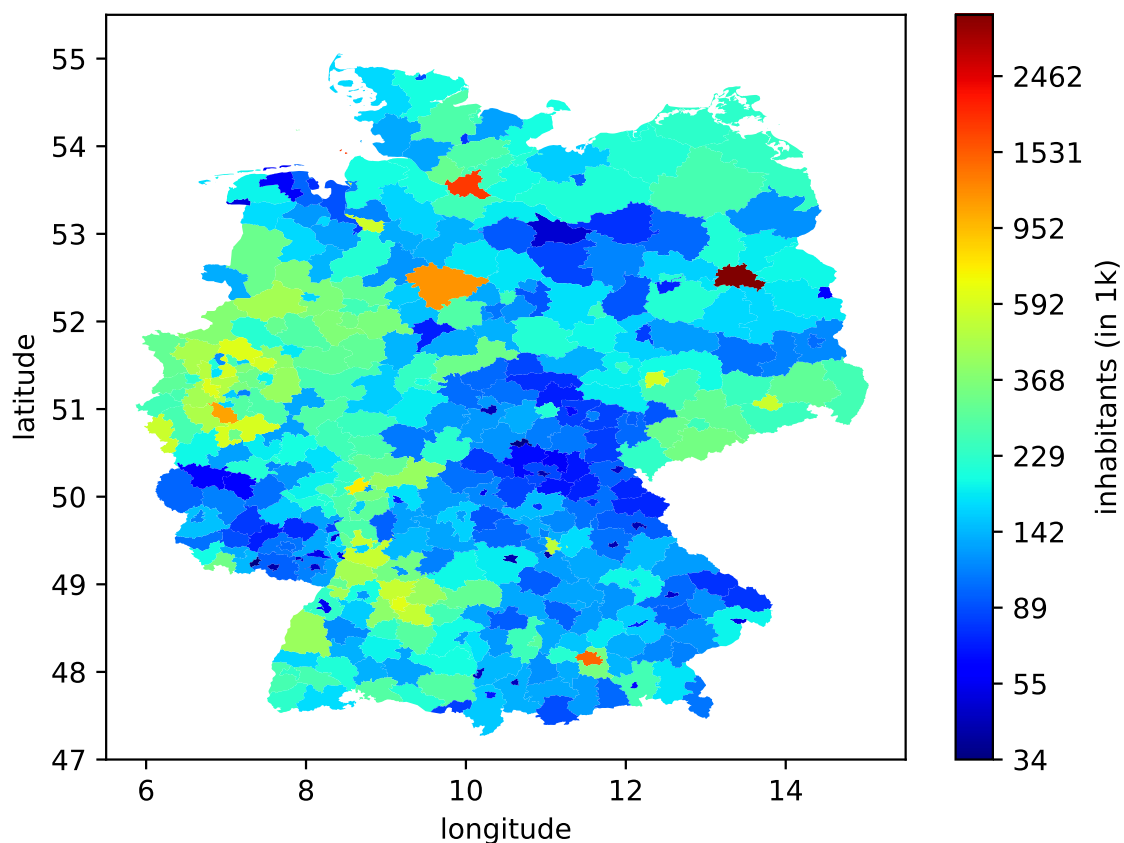
single points.



**Figure 4.3.** Load curve with mean of 2 metre measured temperature in Germany as color from 2015/1/1 to 2018/12/31 with one single point per day at 12 AM UTC time respectively.

### 4.1.3. Population

For further improvement and in order to filter important points in the grid, population data for Germany has been acquired from Eurostat<sup>4</sup>. The data is being visualized in Figure 4.4 with a logarithmic scale to improve visual distinction of the different regions which is harder for a non-logarithmic scale.



**Figure 4.4.** Population of Germany for each region respectively using a log scale for better distinction.

## Data Preprocessing

TODO

<sup>4</sup><https://ec.europa.eu/eurostat/data/database>

## 4.2. Implementation

This section will first outline which programming language is used and why. After that there are two points about the documentation.

For the programming part, Python 3.6+ has been chosen, as there is a variety of libraries to process all used file formats and because it tends to be a time saving language, also for visualization.

In regard to coding styles, especially when it comes to docstrings, the numpy conventions were used. The three major points for this were first, that it is a popular and often used style, second, it is also a visually oriented style which means, that it is easy to read and last, it is supported by several automated documentation tools that create a PDF or HTML based documentation from existing source code with docstrings. For this purpose, the Sphinx<sup>5</sup> tool was used.

## 4.3. Results

At this point, I would like to thank Kaleb Phipps<sup>6</sup> who provided some very useful code, saving me a big cauldron of time that would have otherwise been spent for bug fixing.

### Model selection

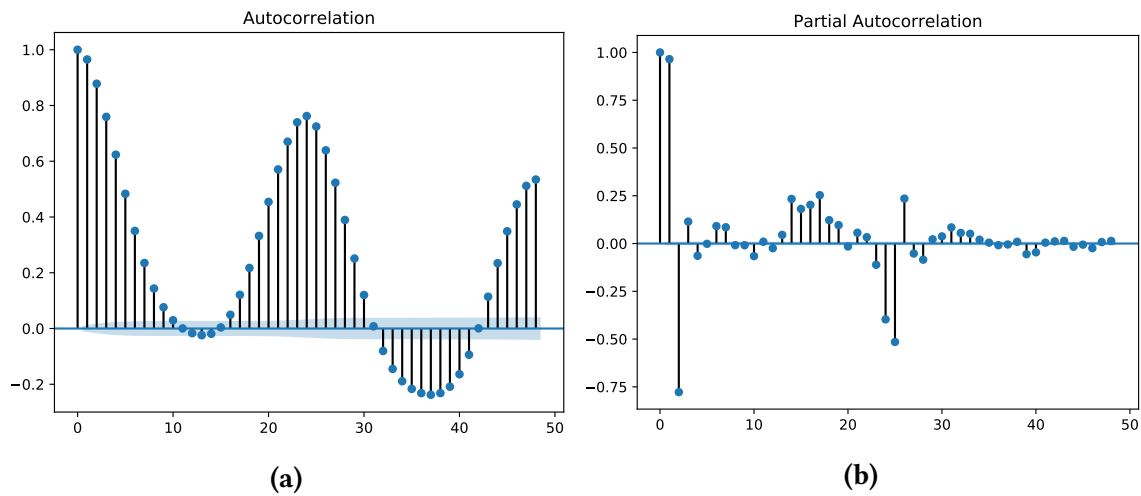
#### ARMAX

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<sup>5</sup><http://www.sphinx-doc.org>

<sup>6</sup>[https://www.iai.kit.edu/2154\\_2880.php](https://www.iai.kit.edu/2154_2880.php)

#### 4. Evaluation



**Figure 4.5.** Autocorrelation (a) and Partial Autocorrelation (b) plots used to select the order of ARMA and ARMAX models.

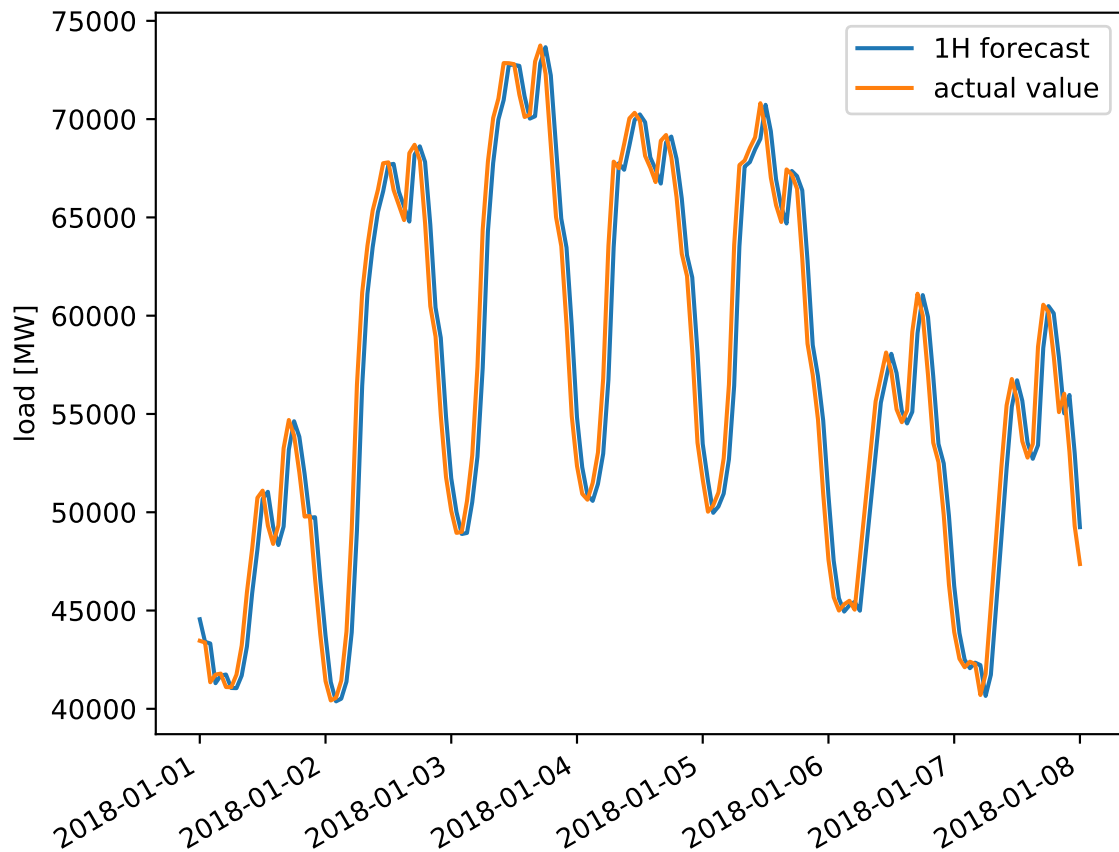
		MA(q) >	0	1	2	3	4	5
		AR(p) v						
AIC	1		489489.23	472851.05	467543.07	466091.08	465622.11	464728.34
BIC			489513.76	472883.76	467583.96	466140.14	465679.35	464793.76
HQIC			489497.15	472861.61	467556.27	466106.92	465640.59	464749.47
AIC	2		464699.50	464253.96	464204.94	464190.14	464054.46	463634.12
BIC			464732.21	464294.85	464254.01	464247.39	464119.87	463707.72
HQIC			464710.06	464267.16	464220.79	464208.63	464075.58	463657.89
AIC	3		464324.69	464226.02	464202.92	463643.15	462483.99	462271.48
BIC			464365.58	464275.09	464260.16	463708.57	462557.59	462353.25
HQIC			464337.89	464241.87	464221.4	463664.27	462507.75	462297.88
AIC	4		464171.28	464173.25	462433.17	462985.37	462149.01	-
BIC			464220.35	464230.49	462498.59	463058.97	462230.78	
HQIC			464187.13	464191.73	462454.29	463009.14	462175.41	
AIC	5		464173.18	463588.38	462944.78	-	462138.70	-
BIC			464230.42	463653.80	463018.38		462228.65	
HQIC			464191.66	463609.50	462968.54		462167.74	

**Table 4.2.** Information Criteria for ARMA models without exogenous inputs using training data from 2015/01/01 to 2017/12/31.

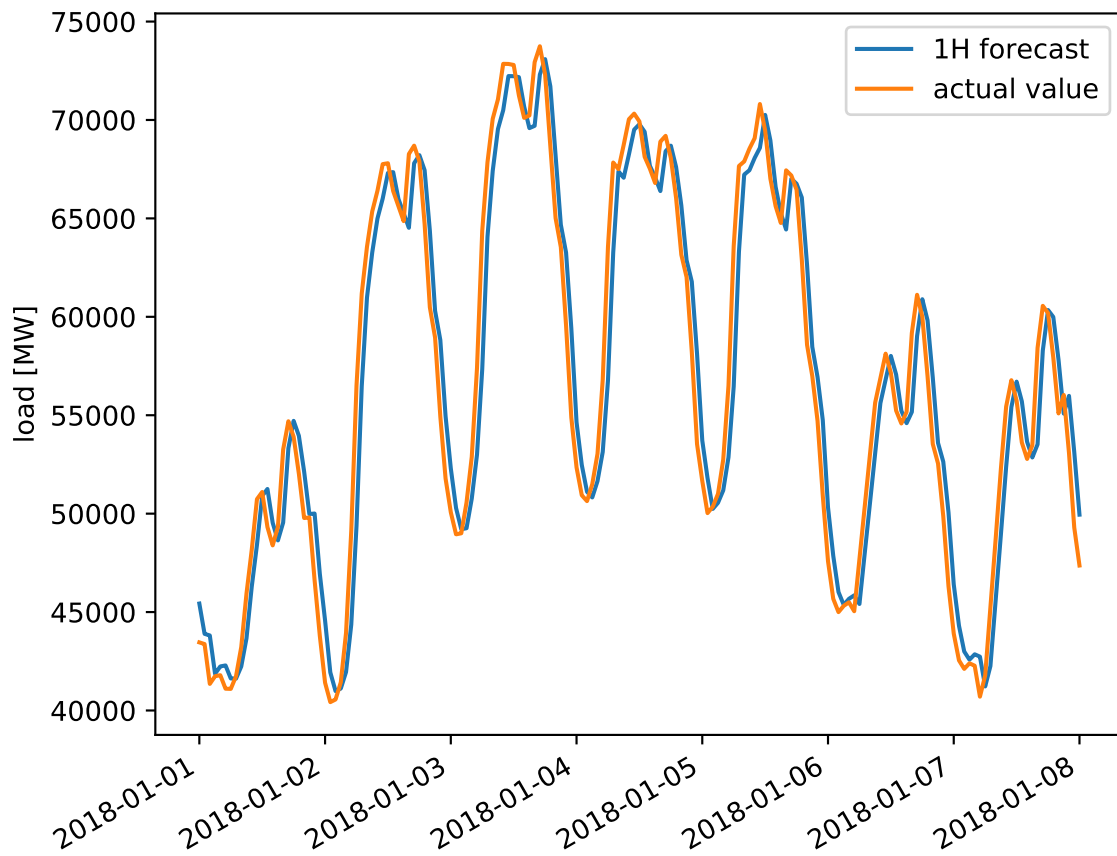
model	data	RMSE	MAE	MPE	MAPE
ARMA(1,0)	no exogenous data	67.114	66.160	0.114	0.114
ARMAX(1,0)	weekend dummy	66.913	65.963	0.114	0.114
ARMAX(1,0)	t2m mean temperature	1958.589	1930.693	3.324	3.324
ARMAX(1,0)	weekend dummy + t2m mean	4.417	4.157	-0.008	0.008
ARMAX(1,0)	t2m data of 10 regions with highest population	2381.090	2347.192	4.041	4.041
ARMAX(1,0)	t2m data of 10 regions with highest population + weekend dummy	3475.891	3426.441	5.899	5.899

**Table 4.3.** ARMAX results.

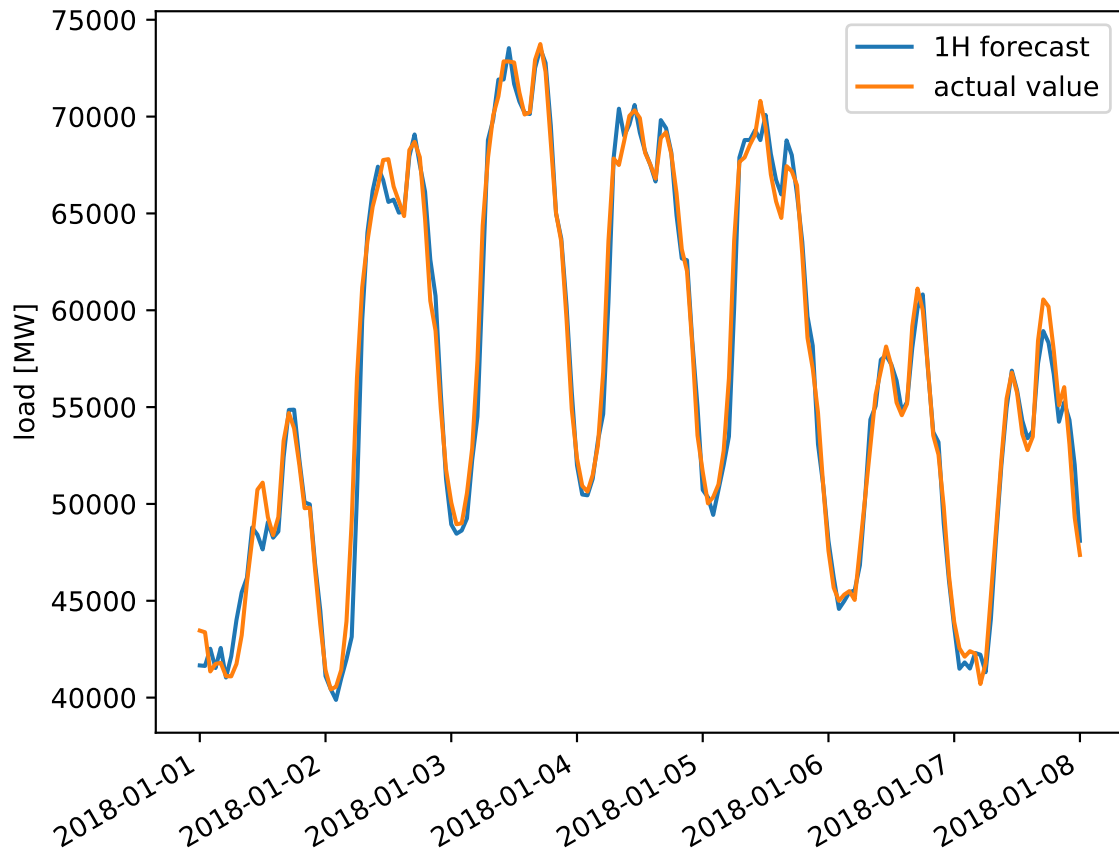




**Figure 4.6.** An example forecast from 2017/12/31 01:00 to 2018/12/31 00:00 for an ARMAX(1,0) using load data from 2015/01/08 00:00 to 2017/12/31 00:00 performing one step ahead forecasts for each step, which equals 1 hour forecasts due to the 1 hour resolution of the data.



**Figure 4.7.** An example forecast from 2017/12/31 01:00 to 2018/12/31 00:00 for an  $\text{ARMAX}(1,0)$  using load data from 2015/01/08 00:00 to 2017/12/31 00:00 and seven dummy variables each for one week day as exogenous input, performing one step ahead forecasts for each step, which equals one hour forecasts due to the one hour resolution of the data.



**Figure 4.8.** An example forecast from 2017/12/31 01:00 to 2018/12/31 00:00 for an ARMAX(1,0) using load data from 2015/01/08 00:00 to 2017/12/31 00:00 and the load data shifted back in time by one week as exogenous input, performing one step ahead forecasts for each step, which equals one hour forecasts due to the one hour resolution of the data.



## **5. Discussion**

This chapter is supposed to discuss your results. Point out what your results mean. What are the limitations of your approach, managerial implications or future impact?

Explain the broader picture but be critical with your methods.



## **6. Conclusion**

It needs to be clarified, that in contrast to most of the presented works, this thesis uses reanalysed data from ECMWF as weather predictions which means, that the forecasts might behave differently from forecasts in other works as what here is assumed to be a weather forecast is more accurate than usually. This also means that results from this thesis may not exactly match results using the same procedure with real-time data.





# Terms and abbreviations

**AnEn** Analog Ensemble. 5–7

**AR** Autoregressive. 4, 9

**ARIMA** Autoregressive Integrated Moving Average. 4, 7

**ARMA** Autoregressive-Moving Average. v, 4, 7, 9, 20

**ARMAX** Autoregressive-Moving Average with Exogenous Inputs. v, 4, 7, 9, 10, 20

**ARWD** Autoregressive model using an average weekly profile. 5, 7

**ARWDY** Autoregressive model using an average weekly profile including annual seasonality. 5, 7

**CARDS** Coupled Autoregressive and Dynamical System. 4, 7

**CRO** Coral Reefs Optimization. 4, 7

**DWD** Deutscher Wetterdienst. 4

**ECMWF** European Centre of Medium-Range Weather Forecasts. vii, 4, 5, 13, 15, 25

**ELM** Extreme Learning Machine. 4, 7

**EMOS** Ensemble Model Output Statistics. 5, 7

**EPEX SPOT** European Power Exchange. 4

**GGA** Grouping Genetic Algorithm. 4, 7

**GHI** Global Horizontal Solar Irradiance. 4

**HWT-ESM** Holt-Winters-Taylor Exponential Smoothing Method. 5, 7

- IDW** Inverse Distance Weighting. 5, 7
- KDE** Kernel Density Estimation. 5, 7
- LASSO** Least Absolute Shrinkage Selection Operation. 4, 7
- LR** Linear Regression. 5, 7
- MA** Moving Average. 9
- MAE** Mean Absolute Error. 11, 19
- MAPE** Mean Absolute Percentage Error. 12, 19
- MARS** Multivariate Adaptive Regression Splines. 4, 7
- MLR** Multiple Linear Regression. 7
- MM5** Fifth-generation Mesoscale Model. 4
- MOS** Model Output Statistics. 5, 7
- MPE** Mean Percentage Error. 12, 19
- NN** Neural Networks. 4–7
- NOAA/ESRL** National Oceanic and Atmospheric Administration - Earth System Research Laboratory. 5
- NUTS** Nomenclature des Unités territoriales statistiques. 14
- OK** Ordinary Kriging. 3
- PCA** Principal Component Analysis. 6, 7
- PDF** Probability Density Function. 5, 7
- PE** Persistence Ensemble. 5, 7
- PV** photovoltaic. 1
- RAMS** Regional Atmospheric Modelling System. 5
- RF** Random Forests. 4, 7

**RMSE** Root-Mean-Square Error. 11, 19

**SSLR** Simple Seasonal Linear Regression. 5, 7

**SVM** Support Vector Machines. 5, 7

**SVR** Support Vector Regression. 4, 7

**VD** Variance Deficit. 5, 7

**WNN** Wavelet Neural Networks. 4, 7

**WRF** Weather Research and Forecasting Model. 4

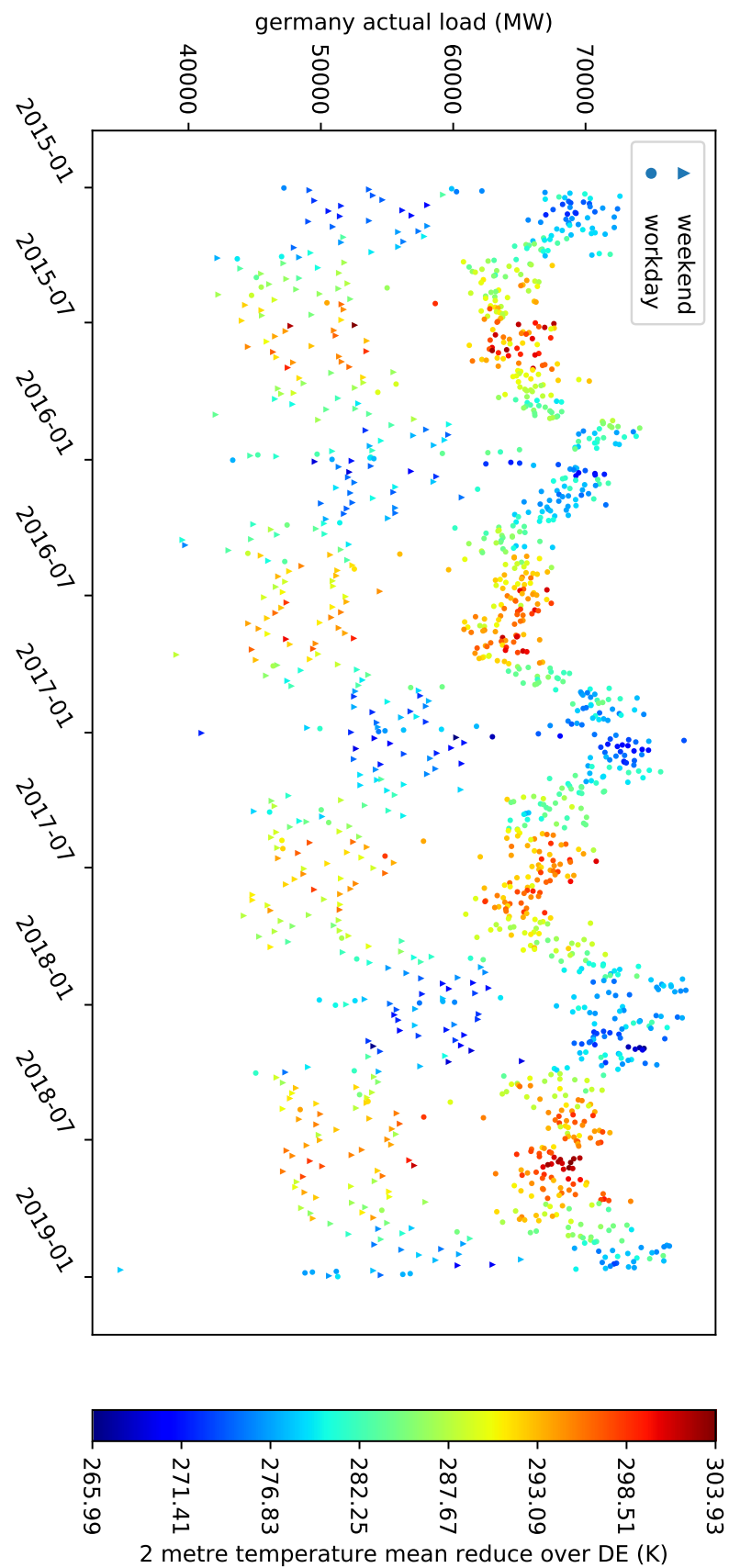


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## **A. Appendix**



**Figure A.1.** Load curve with mean of 2 meter height measured temperature in germany as color from 2015/1/1 to 2018/12/31 with one single point per day at 12am 360utc time respectively.