

Dynamic viscosity } takes density into account

$$\nu = \frac{\mu}{\rho} = \frac{\text{dynamic viscosity}}{\text{mass density}}$$



$$\nu_{\text{air}} \approx 10^{-5} \text{ m}^2 \text{ s}^{-1}$$

$$\nu_{\text{water}} \approx 10^{-6} \text{ m}^2 \text{ s}^{-1}$$

$$\nu_{\text{honey}} \approx 10^{-2} \text{ m}^2 \text{ s}^{-1}$$

Pressure vs depth → liquids incompressible so no change in density with depth  
 ↳ gases compressible so density changes with depth

Liquid

→ Incompressible  
 ↳ density fixed

Hydrostatic equation

$$\frac{dP}{dz} = -\rho g$$

$\rho$  constant (incompressible)

$$P = P_0 + \rho g h$$



$P_0$   
 $P(h)$

Gases compressible but obeys gas law →  $PV = nRT = Nk_B T$

$$n_d = \text{no. density of gas} = \frac{N}{V} = \frac{P}{k_B T}$$

$$\text{mass density} \Rightarrow \rho = \frac{mN}{V} = \frac{mP}{k_B T}$$

$\rho \propto P$  and  $\propto \frac{1}{T}$

$$\frac{dP}{dz} = -\rho(z)g = -\frac{mPg}{k_B T}$$

$$\frac{dP}{dz} = -\frac{mg}{k_B T} P$$

Solve to get:

$$P(h) = P_0 e^{-\frac{mgh}{k_B T}}$$

here  $mgh \rightarrow$  energy at height  $h$  due to gravitational potential

$$\Rightarrow e^{-\frac{E}{k_B T}}$$

↳ Boltzmann Factor

More energetic states less probable than less energetic states