

# Compiler Design

## Lab 3: Context Free Grammar

Muhammad Maaz Hasan Akhtar

ERP: 09399

Code:

<https://github.com/maazh/Compiler-Design-Labs>

Q1 (a)

$\{a, aa, aaa\} \cdot \{a^n \mid n \in [1, 3]\}$

$V_n = \{S, A\}$

$\Sigma = \{a\}$

$S = \text{start symbol}$

$F = \{A\}$

$S \rightarrow aAA$

$A \rightarrow a$

$A \rightarrow \epsilon$

(b)  $\{a, aa, aaa, \dots\}$

$\{a^n \mid n > 0\}$

$V_n = \{S, A\}$

$\Sigma = \{a\}$

$F = \{A\}$

$S \rightarrow aA$

$A \rightarrow aA$

$A \rightarrow \epsilon$

(c)  $\{\lambda, a, aa, aaa\}$

$\{a^n \mid n \in [0, 3]\}$

$V_n = \{S, A\}$

$\Sigma = \{a\}$

$F = \{A\}$

$S \rightarrow aA \mid \epsilon$

$A \rightarrow a$

$S \rightarrow aAA \mid \epsilon$

$A \rightarrow a \mid \epsilon$



Q1  
 (a)  $\{\lambda, a, aa, \dots\}$   $\{a^n / n \geq 0\}$

$$V_n = \{S, A\}$$

$$\Sigma = \{a\}$$

$$F = \{A\}$$

$$S \rightarrow aA / \epsilon$$

$$A \rightarrow aA / \epsilon$$

Q2.

(a)  $\lambda, c, cc, ccc, \dots$   $S \rightarrow \lambda$   
 $S \rightarrow A$

$$\{c^n / n \geq 0\}$$

$$A \rightarrow \{ \lambda, c, cc, ccc, cccc, \dots \}$$

$$S \rightarrow AA$$

$$\rightarrow cAA$$

$$\rightarrow ccAA$$

$$\rightarrow cccAA$$

$$\rightarrow \dots$$

(b)  $S \rightarrow \lambda / A$   
 $A \rightarrow cAd / cd$

$$\{c^n d^n / n \geq 0\}$$

$$S \rightarrow \lambda \rightarrow A$$

$$\rightarrow cd \rightarrow cAd$$

$$\rightarrow ccdd$$

$$\rightarrow c cAd$$

$$\rightarrow cc cdd \rightarrow cccAdd$$

$$\{\lambda, cd, ccd, cccdd, ccccdd, \dots\}$$

$$\rightarrow ccc cAd \rightarrow ccccdd$$

$$\rightarrow cccccAdd \rightarrow cccccdd$$

$$\rightarrow ccccc cdd \dots$$

$$\{c^n d^m / n, m \geq 0\}$$

$$n+m \geq 1$$

Ans.



Q3

Q3

P3

$$S \rightarrow \lambda / A$$

$$A \rightarrow cAd / ed \quad A \rightarrow AcA / c$$

$$S \rightarrow \lambda / A$$

$$cd. / cAd.$$

$$S \rightarrow \lambda / A$$

$$\lambda, A, A \rightarrow A$$

$$AcA$$

c

$$AcAcc$$

$$AcAccA$$

$$AcAccAcAcAcc$$

$$\{c^n \mid n \geq 0\}$$

$$A \rightarrow cAd$$

$$n \bmod 2 > 0$$

$$AcAcccccccc$$

c

all languages where 'c' is either zero, or odd in number.

Q4

P4

$$S \rightarrow cA$$

$$A \rightarrow d / cA / Td$$

$$T \rightarrow Td / d$$

$$\{c, \dots\}$$

$$cA$$

$$cd$$

$$cAcA$$

$$cTd$$

$$edd$$

$$cTd$$

$$cTdd$$

$$cTddd$$

$$ccA$$

$$ccTd$$

$$ccAcA$$

$$cTddd / cd$$

$$\{c^m d^n \mid m, n \geq 0\}$$

$$\{cd, ccd, cdd, cddd, \dots\}$$

$$\{c d d d d\}$$

c

$$cTddd$$

$$cddd$$

$$cTddd$$

Ans.

Q2 (c):

$$\left\{ e^m d^n \mid m, n \geq 0, m+n \geq 0 \right\}$$

~~$m+n \geq 0$~~

~~$m+n$~~

$$\left\{ e^m d^n \mid m, n \geq 0, m+n \neq 1 \right\}$$



Q3.

$$\begin{aligned}
 (a) \quad & P: S \rightarrow aAb \\
 & V_n = \{S, A\} \quad A \rightarrow ab \\
 & \Sigma = \{a, b\} \quad A \rightarrow aAb \mid \epsilon \\
 & \underline{S} = \\
 & F = \{A\}.
 \end{aligned}$$

$$(b) \quad \{a^n b^m \mid \underline{n > 0}, \underline{0 < m < n}\} \quad \begin{matrix} m > 0 \\ n > m \end{matrix}$$

$a^1 b^1, a^2 b^1, a^3 b^1, a^4 b^1, a^5 b^1, a^6 b^1, a^7 b^1, a^8 b^1, a^9 b^1, a^{10} b^1, \dots$

$$\begin{aligned}
 S &\rightarrow aA \\
 \underline{S} &= \\
 A &\rightarrow aB \\
 B &\rightarrow aB \mid b
 \end{aligned}$$

$$\begin{aligned}
 V_n &= \{S, A, B\} \\
 \Sigma &= \{a, b\} \\
 F &= \{B\}
 \end{aligned}$$

$$\begin{aligned}
 P: \quad & S \rightarrow A \\
 & A \rightarrow aaBb \\
 & B \rightarrow aBb \mid \epsilon \\
 & B \rightarrow aB. \\
 & B \rightarrow \epsilon
 \end{aligned}$$



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$$(c) \{ a^n b^m \mid n > 0, 0 \leq m < n \}$$

$\{ a, aab, aa, aaa \dots, aaab, aaabb \dots \}$

$$V_n = \{ S, A, B, C \}$$

$$\Sigma = \{ a, b \}$$

$$F = \{ B, C \}$$

$$P: S \rightarrow A$$

$$A \rightarrow aB$$

$$B \rightarrow aB \mid abC \mid \epsilon$$

$$C \rightarrow b \mid \epsilon$$

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