

STAT 662 Homework 3

45.5/50

Liangjian Yao

1253177

- Question 1
- Question 2
- Question 3
- SAS code & output

Question 1

- a) Factor A: water Amount ✓
 Factor B: Autolyse time
 $N = abn = 2 \times 4 \times 3 = 24$

$a = 2$
 $b = 4$
 $n = 3$

Factor levels

b) Provide the specific factor levels, not the number of levels. (0.5)

- c) 8 treatment groups = 315 grams & 30 mins
 315 grams & 60 mins
 315 grams & 90 mins
 315 grams & 120 mins 320 grams & 30 mins
 320 grams & 60 mins
 320 grams & 90 mins
 320 grams & 120 mins ✓

d) define

$$Y_{ijk} = \mu + \tau_i + \beta_j + (\tau\beta)_{ij} + \epsilon_{ijk}$$

μ : overall population mean of loaf heights

τ_i : effect of i th level of Water Amount ($i = 1, 2$)

(0.5)

β_j : effect of j th level of Autolyse time ($j = 1, 2, 3, 4$)

$(\tau\beta)_{ij}$: the interaction effect of i th level of water Amount and j th level of Autolyse time,
 $(i=1, 2)$
 $(j=1, 2, 3, 4)$

ϵ_{ijk} : random error of k th experiment from i th level of Water Amount and j th level of Autolyse time

($i = 1, 2$; $j = 1, 2, 3, 4$; $k = 1, 2, 3$)

e) Constraints: $\sum_{i=1}^a \tau_i = 0$

$$\sum_{j=1}^b \beta_j = 0$$

✓

$$\sum_{i=1}^a (\tau\beta)_{ij} = 0, j = 1, 2, 3, 4$$

$$\sum_{j=1}^b (\tau\beta)_{ij} = 0, i = 1, 2$$

f) Assumptions: $E_{ijk} \sim N(0, \sigma^2)$ ✓

Normality

Independent

Constant Variance

$$g) \mu = \bar{y}_{...} = 10.60$$

$$\bar{z}_i = \bar{y}_{i..} - \bar{y}_{...}$$

| Factor A | $\bar{y}_{i..}$ | \bar{z}_i |
|-----------|-----------------|------------------------|
| 315 grams | 10.10 | $10.10 - 10.60 = -0.5$ |
| 320 grams | 11.10 | $11.10 - 10.60 = 0.5$ |

$$\beta_j = \bar{y}_{.-j} - \bar{y}_{...}$$

| Factor B | 30 min | 60 min | 90 min | 120 min |
|-----------------|--------|--------|--------|---------|
| $\bar{y}_{.-j}$ | 9.40 | 10.75 | 11.10 | 11.15 |
| β_j | -1.2 | 0.15 | 0.5 | 0.55 |

$$(\bar{\tau}\beta)_{ij} = \bar{y}_{ij.} - \bar{y}_{i..} - \bar{y}_{.-j} + \bar{y}_{...}$$

$$(\bar{\tau}\beta)_{11} = 8.5 - 9.4 - 10.10 + 10.60 = -0.4$$

$$(\bar{\tau}\beta)_{12} = 9.4 - 10.75 - 10.10 + 10.60 = -0.85$$

$$(\bar{\tau}\beta)_{13} = 10.50 - 11.10 - 10.10 + 10.60 = -0.1$$

$$(\bar{\tau}\beta)_{14} = 12.00 - 11.15 - 10.10 + 10.60 = 1.35$$

$$(\bar{\tau}\beta)_{21} = 10.30 - 9.4 - 11.10 + 10.60 = 0.4$$

$$(\bar{\tau}\beta)_{22} = 12.10 - 10.75 - 11.10 + 10.60 = 0.85$$

$$(\bar{\tau}\beta)_{23} = 11.70 - 11.10 - 11.10 + 10.60 = 0.1$$

$$(\bar{\tau}\beta)_{24} = 10.30 - 11.15 - 11.10 + 10.60 = -1.35$$

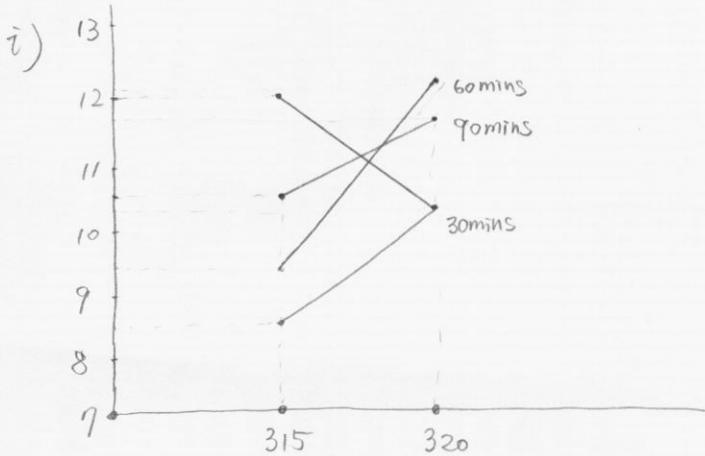
✓

$$h) i=1, j=3$$

$$\bar{y}_{13.} = 10.50 \quad \leftarrow \text{Fitted value}$$

$$y_{13.} = 10.1 \quad \leftarrow \text{Actual}$$

$$\epsilon_{13.} = y_{13.} - \bar{y}_{13.} = 10.1 - 10.50 = -0.4$$



Interaction plot:

The lines are not parallel, which means there's ^{likely an} interaction between the two factors.

j.) ANOVA Table

$$SS_A = bn \sum_{i=1}^a (\bar{y}_{i..} - \bar{y}_{...})^2$$

$$= 4 \times 3 \times [(10.10 - 10.60)^2 + (11.10 - 10.60)^2]$$

$$= 6$$

$$SS_B = an \sum_{j=1}^b (\bar{y}_{.j.} - \bar{y}_{...})^2$$

$$= 2 \times 3 \times [(9.40 - 10.60)^2 + (10.75 - 10.60)^2 + (11.10 - 10.60)^2 + (11.15 - 10.60)^2]$$

$$= 12.09$$

$$SS_{AB} = n \sum_{i=1}^a \sum_{j=1}^b (\bar{y}_{ij.} - \bar{y}_{i..} - \bar{y}_{.j.} + \bar{y}_{...})^2$$

$$= 3 \times [(18.5 - 10.10 - 9.4 + 10.6)^2 + (10.3 - 11.1 - 9.4 + 10.6)^2 +$$

$$(9.4 - 10.10 - 10.75 + 10.6)^2 + (12.10 - 11.1 - 10.75 + 10.6)^2 +$$

$$(10.5 - 10.10 - 11.10 + 10.6)^2 + (11.70 - 11.1 - 11.1 + 10.6)^2 +$$

$$(12.00 - 10.10 - 11.15 + 10.6)^2 + (10.30 - 11.10 - 11.15 + 10.6)^2]$$

$$= 3 \times 5.43$$

$$= 16.29$$

| | df | SS | MS | F |
|-------|----|-------|-------|-------|
| A | 1 | 6 | 6 | 5.581 |
| B | 3 | 12.09 | 4.03 | 3.749 |
| AB | 3 | 16.29 | 5.43 | 5.098 |
| Error | 16 | 17.2 | 1.075 | |
| Total | 23 | 51.58 | | |

k.) $\sigma^2 = MSE = 1.075$

4) test for interaction effects:

$$H_0: (\tau\beta)_{ij} = 0 \quad \forall (i,j)$$

$$H_a: (\tau\beta)_{ij} \neq 0 \text{ for at least one } (i,j)$$

$$F_{AB} = 5.098$$

$$\text{Critical value: } F(3, 16, 0.05) = 3.24$$



Reject H_0 if $F_{AB} \geq$ critical value

$$F_{AB} = 5.098 > 3.24,$$

Thus, Reject H_0 .

There's sufficient evidence to conclude that at least one $(\tau\beta)_{ij} \neq 0$, which means there's interaction effects.

test for Water Amount (Main effect)

$$H_0: \tau_1 = \tau_2 = 0 \quad H_a: \text{at least one } \tau_i \neq 0$$

$$F_{OA} = 5.581$$

$$\text{Critical value: } F(1, 16, 0.05) = 4.49$$

Reject H_0 if $F_{OA} \geq$ critical value.



$$F_{OA} = 5.581 > 4.49$$

Thus, Reject H_0 .

There's sufficient evidence to claim $H_a: \text{at least one } \tau_i \neq 0$.

test for Autolyse time (main effect)

$$H_0: \beta_1 = \beta_2 = \beta_3 = \beta_4 = 0, \quad H_a: \text{at least one } \beta_i \neq 0$$

$$F_{OB} = 3.749$$

$$\text{Critical value: } F(3, 16, 0.05) = 3.24$$



Reject H_0 if $F_{OB} \geq$ critical value.

$$F_{OB} = 3.749 > 3.24$$

Thus, Reject H_0 .

There's sufficient evidence to claim $H_a: \text{at least one } \beta_i \neq 0$.

m) ANOVA Table $F = 5.581$ for autolyse indicates significant,
 (iv) then it is appropriate to investigate contrasts of interest or
 compare the means of the different factor levels.

Tukey's Method (in chapter 3)

$$T_\alpha = q_\alpha(a, f) \cdot \sqrt{\frac{MSE}{n}}$$

$$= q_{0.05}(4, 20) \cdot \sqrt{\frac{1.075}{3}}$$

$$= 4.24 \times \sqrt{\frac{1.075}{3}}$$

$$= 2.538$$

a: factor level of autolyse time: 4

$$f = N - a = 24 - 4 = 20$$

$$MSE = 1.075$$

$$n = 3$$

$$H_0: \mu_i = \mu_j \quad H_a: \mu_i \neq \mu_j$$

Reject H_0 if $|\bar{y}_{i\cdot} - \bar{y}_{j\cdot}| \geq T_\alpha$

$$|\bar{y}_{1\cdot} - \bar{y}_{2\cdot}| = |9.4 - 10.75| = 1.35 < T_\alpha$$

$$|\bar{y}_{1\cdot} - \bar{y}_{3\cdot}| = |9.40 - 11.10| = 1.7 < T_\alpha$$

$$|\bar{y}_{1\cdot} - \bar{y}_{4\cdot}| = |9.40 - 11.15| = 1.75 < T_\alpha$$

$$|\bar{y}_{2\cdot} - \bar{y}_{3\cdot}| = |10.75 - 11.10| = 0.35 < T_\alpha$$

$$|\bar{y}_{2\cdot} - \bar{y}_{4\cdot}| = |10.75 - 11.15| = 0.4 < T_\alpha$$

$$|\bar{y}_{3\cdot} - \bar{y}_{4\cdot}| = |11.10 - 11.15| = 0.05 < T_\alpha$$

| Autolyse Time | 30min | 60min | 90min | 120min |
|---------------|--------------------|-------|-------|--------|
| | $\bar{y}_{j\cdot}$ | 9.40 | 10.75 | 11.10 |

Fail to Reject H_0 .

There's No enough evidence to claim H_a : $\mu_i \neq \mu_j$, which mean that there's different effects of all levels of Autolyse time.

ii) By ANOVA Table $F=5.098$ for interaction effects indicates significant.

$$\begin{aligned} T_\alpha &= q_{\alpha}(ab, ab(n-1)) \cdot \sqrt{\frac{MS_E}{n}} \\ &= q_{0.05}(8, 16) \cdot \sqrt{\frac{1.075}{3}} \\ &= 4.90 \times \sqrt{\frac{1.075}{3}} \\ &= 2.93 \checkmark \end{aligned}$$

$$\begin{aligned} n &= 3 \\ a &= 2 \\ b &= 4 \\ ab &= 8 \\ ab(n-1) &= 16 \end{aligned}$$

$$H_0: \mu_{ij} - \mu_{kl} = 0 \quad H_a: \mu_{ij} - \mu_{kl} \neq 0$$

Reject H_0 if $|\bar{y}_{ij.} - \bar{y}_{kl.}| \geq T_\alpha$

$$|8.5 - 9.4| = 0.9$$

$$|8.5 - 10.5| = 2$$

$$|\bar{y}_{11.} - \bar{y}_{14.}| = |8.5 - 12.0| = 3.5 > T_\alpha$$

$$|8.5 - 10.30| = 1.8$$

$$|\bar{y}_{11.} - \bar{y}_{22.}| = |8.5 - 12.10| = 3.6 > T_\alpha$$

$$|\bar{y}_{11.} - \bar{y}_{23.}| = |8.5 - 11.7| = 3.2 > T_\alpha$$

$$|8.5 - 10.30| = 1.8$$

$$|9.4 - 10.50| = 1.1$$

$$|9.4 - 12.0| = 2.6$$

$$|9.4 - 10.3| = 0.9$$

$$|9.4 - 12.1| = 2.7$$

$$|9.4 - 11.7| = 2.3$$

$$|9.4 - 10.3| = 0.9$$

$$|10.5 - 12.0| = 1.5$$

$$|10.5 - 10.3| = 0.2$$

$$|10.5 - 12.1| = 1.6$$

$$|10.5 - 11.7| = 1.2$$

$$|10.5 - 10.3| = 0.2$$

$$|12.0 - 10.3| = 1.7$$

$$|12.0 - 12.1| = 0.1$$

$$|12.0 - 11.7| = 0.3$$

$$|12.0 - 10.3| = 1.7$$

$$|10.3 - 12.1| = 1.8$$

$$|10.3 - 11.7| = 1.4$$

$$|10.3 - 10.3| = 0$$

$$|12.1 - 11.7| = 0.4$$

$$|12.1 - 10.3| = 1.8$$

$$|11.7 - 10.3| = 1.4$$

For the treatment groups of $\bar{y}_{11.} - \bar{y}_{14.}$

✓ Reject H_0 .
 There's sufficient evidence to claim that means among these treatment groups.

For the other treatment groups ($< T_\alpha$):

Fail to reject H_0 .

There's no sufficient evidence to claim $H_a: \mu_{ij} - \mu_{kl} \neq 0$, which indicates that there's no different effects among these treatment groups.

0).

Treatments: 8 groups total

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|-------|------|------|------|------|------|------|------|------|
| Day 1 | | | | | | | | |
| Day 2 | | | | | | | | |
| Day 3 | | | | | | | | |
| | 8.50 | 9.40 | 10.5 | 12.0 | 10.3 | 12.1 | 11.7 | 10.3 |

Blocking: df = 2

| | df | SS | MS | F |
|-------|----|-------|-------|-----------------------|
| A | 1 | 6 | 6 | $6/1.164 = 5.155$ |
| B | 3 | 12.09 | 4.03 | $4.03/1.164 = 3.462$ |
| AB | 3 | 16.29 | 5.43 | $5.43/1.164 = 4.665$ |
| Block | 2 | 0.91 | 0.455 | $0.455/1.164 = 0.391$ |
| Error | 14 | 16.29 | 1.164 | |
| Total | 23 | 51.58 | | |

$$df = 8-1=7$$

$$\text{total SS} = 34.38$$

SAME as j.)

$$(8-1) \times (3-1) = 14$$

df of Error

Subtraction for SSE ✓

$$= 51.58 - 34.38 - 0.91$$

$$= 16.29$$

Question 2. → Graded on completion except for SAS code/output

a) ANOVA Table checked

b) Model Assumptions:

$$\epsilon_{ijk} \sim iid N(0, \sigma^2)$$

Normality by Q-Q plot: All data aligned to one straight line.
Normality satisfied.

Constant Variance by plot of residuals vs. fitted values:

All data are sparsely & averagely scattered.
Satisfied.

Independent error by plot of residuals vs. run order and by residuals vs. fitted values:
averagely scattered.
Satisfied.

c) $y = b_0 + b_1 x_1 + b_2 x_2 + b_3 x_2^2 + b_4 x_2^3 + b_5 x_1 x_2 + b_6 x_1 x_2^2 + b_7 x_1 x_2^3 + \epsilon$

i) $y = 11.006 + 1.094x_1 + 0.481x_2 - 0.731x_2^2 + 0.394x_2^3 - 1.156x_1x_2 - 1.069x_1x_2^2 + 0.281x_1x_2^3$

ii) $x_1 = \frac{317 - 317.5}{2.5} = -0.2$

$x_2 = \frac{100 - 75}{45} = 0.556$

$$y = 11.006 + 1.094 \times (-0.2) + 0.481 \times 0.556 - 0.731 \times 0.556^2 + 0.394 \times 0.556^3 - 1.156 \times (-0.2) \times 0.556 - 1.069 \times (-0.2) \times 0.556^2 + 0.281 \times (-0.2) \times 0.556^3 \\ = 11.081 \doteq 11.08$$

iii) $x_1 = \frac{300 - 317.5}{2.5} = -7$

$x_2 = \frac{80 - 75}{45} = 0.111$

Is there any difference between ii) and iii)?
But they are asked in different ways

$$y = 11.006 + 1.094 \times (-7) + 0.481 \times 0.111 - 0.731 \times 0.111^2 + 0.394 \times 0.111^3 - 1.156 \times (-7) \times 0.111 - 1.069 \times (-7) \times 0.111^2 + 0.281 \times (-7) \times 0.111^3 \\ = 4.381$$

iv) $x_1 = \frac{319 - 317.5}{2.5} = 0.6$

$$y = 11.006 + 1.094 \times 0.6 + 0.481x_2 - 0.731x_2^2 + 0.394x_2^3 - 1.156 \times 0.6x_2 - 1.069 \times 0.6x_2^2 + 0.281 \times 0.6x_2^3 \\ = 11.662 + 0.481x_2 - 0.731x_2^2 + 0.394x_2^3 - 0.694x_2 - 0.641x_2^2 + 0.169x_2^3 \\ = 11.662 - 0.213x_2 - 1.312x_2^2 + 0.563x_2^3$$

QUESTION 3:

- a) Plant types as banker = Verbena \times hybrida cv. Tapien plant (V.)
 (Factor A)
- Scaevola aemula plant (S.) ✓
 a = 2
- Flower with/without = with without
 (Factor B)
- b) a = 2
 b = 2
- Diagram showing a 2x2 factorial design:
- ```

 graph TD
 A[Factor A] --> V[V. plant]
 A --> S[S. plant]
 B[Factor B] --> W[with]
 B --> NW[without]
 V --> W
 V --> NW
 S --> W
 S --> NW

```

|  |  | Factor B    |                |
|--|--|-------------|----------------|
|  |  | with Flower | without Flower |
|  |  | V. plant    | S. plant       |
|  |  |             |                |
|  |  |             |                |

- c) V. plant & flower, V. plant & without flower ✓  
 S. plant & flower, S. plant & without flower

- d) N. tenuis adults

\* (not sure whether necessary to specify further for different response variables in e)

- e) egg development time

Nymphal development time

Female Fecundity

$r_m$  (Intrinsic rate of increase)

Sugar of plants

Answers should be specific  
to two-way ANOVA

- f) in Materials and methods section:

for egg development, newly emerged females and males were reared on potted V. plant or S. plant;  
 which are randomly selected (Although Random is not mentioned in paper)  
 then mature, presumed mated N. tenuis females were collected from the cage  
 and released into another cage to obtain 40 eggs.

By the description for all different response variable measurement,  
 the process is randomized. -0.5

You can't claim randomization if  
it is not mentioned in article

- g). Yes. there are many N. tenuis female adults as experiment unit.

eggs are many for egg development

-0.5 per treatment group

nymphs are many for nymphal development

N. tenuis female are many for female fecundity.

Plant samples are many for sugar analysis.

the experiment has replication.

h) Blocking is not used.

the experimental units are randomly assigned to treatments,  
the experiments are not blocking on any other factors.

i) the objective of this study is to study the life history parameters and reproductive potential of a Japanese *N. tenuis* strain on Verbena and Scaevola with and without flowers.

y as  $\gamma_m$  for reproductive potential / egg development time / nymphal development time /

$$Y = \mu + \tau_i + \beta_j + (\tau\beta)_{ij} + \epsilon_{ijk}$$

$\mu$ : overall population mean ~~of y~~

**fecundity**

$k = ?$

$\tau_i$ : effect of plant type  $i=1, 2$

$\beta_j$ : effect of flower  $j=1, 2$

$(\tau\beta)_{ij}$ : interaction effect of  $i$ th level of plant types and  $j$ th level of flower with/without

$\epsilon_{ijk}$ : random error of the  $k$ th ~~experimental unit~~

from  $i$ th level of plant types and  $j$ th level of flower with/without.

\* (not sure whether need to specify  $y$  for different response variables in e).

# Result Section

## j) Sample Statistics

✓

egg development time

|    | with F.       | without F. |
|----|---------------|------------|
| V. | $9.4 \pm 0.1$ | -          |
| S. | $9.1 \pm 0.1$ | -          |

$$H_0: \mu_V = \mu_S, H_a: \mu_V \neq \mu_S$$

$$t = -1.37$$

$$df = 82$$

$$P\text{-value} = 0.173 > 0.05$$

DO NOT Reject  $H_0$ .  
not significant.

Nymphal development time

|    | with F.        | without F. |
|----|----------------|------------|
| V. | $16.1 \pm 0.3$ | -          |
| S. | $16.5 \pm 0.3$ | -          |

$$H_0: \mu_V = \mu_S, H_a: \mu_V \neq \mu_S$$

$$t = -0.807$$

$$df = 55$$

$$P\text{-value} = 0.423 > 0.05$$

DO NOT Reject  $H_0$ .  
not significant.

Female oviposition

Two-Way ANOVA

what do these values represent? -0.5

Female survival rate

Two-way ANOVA

|    | with F.        | without F.    |
|----|----------------|---------------|
| V. | $54.1 \pm 1.3$ | $4.4 \pm 1.7$ |
| S. | $50.3 \pm 6.8$ | $1.1 \pm 0.7$ |

|    | with F. | without F. |
|----|---------|------------|
| V. | 81.3    | 6.3        |
| S. | 60.0    | 12.5       |

Effect of plants with flower:

$$F = 4.38 \quad \checkmark$$

Effect of plant without flower:

$$F = 2.35$$

provide info for interaction -0.5

effect of flowers:

$$Z = -4.36$$

effect of plant

$$Z = 0.75$$

$$P\text{-value} = 0.0406 < 0.05$$

Reject  $H_0$ .  
Significant ✓

$$P\text{-value} < 0.001 < 0.05$$

Reject  $H_0$ .  
Significant

Ym

|    | with Flower           | without |
|----|-----------------------|---------|
| V. | $0.0884 \pm 0.00052$  | -       |
| S. | $0.08098 \pm 0.00018$ | -       |

$$\chi^2 = 22.5$$

$$df = 1$$

$$P\text{-value} < 0.001$$

Reject  $H_0$ . Significant.

$$P\text{-value} = 0.450 > 0.05$$

Not significant.  
Fail to reject  $H_0$ .

$$P\text{-value} < 0.001$$

Reject  $H_0$ .  
Significant.

Sugar

|           | Fructose | Glucose |
|-----------|----------|---------|
| V. plants | 1        |         |
| S. plants | 2        |         |

Friedman Test

$$H_0: M_1 = M_2$$

$$\chi^2 = 12.0$$

$$df = 2$$

$$P\text{-value} = 0.002 < 0.05$$

Significant  
Reject  $H_0$ .

|           | Fructose | Glucose | Sucrose |
|-----------|----------|---------|---------|
| V. plants | 1        |         |         |
| S. plants | 2        |         |         |

Friedman

$$H_0: M_1 = M_2 = M_3$$

$$\chi^2 = 9.56$$

$$df = 2$$

$$P\text{-value} = 0.008 < 0.05$$

Significant  
Reject  $H_0$ .

Fructose in V. S. Mann Whitney  $H_0: \mu_V = \mu_S$   
Glucose in V. S. Mann Whitney  $H_0: \mu_V = \mu_S$

$$V = 54.0$$

$$V = 53.0$$

$$P\text{-value} = 0.0004 < 0.05$$

Significant Reject  $H_0$ .

$$P\text{-value} = 0.0008 < 0.05$$

Significant Reject  $H_0$ .

m)  
conclusion on significance

l)  
P-value

✓

k)  
test statistic

✓

l)  
P-value

m)  
conclusion on significance

m) the objective of this study was to study the life history parameters and reproductive potential of a Japanese *N. tenuis* Strain on Verbena and Scaevola with and without flowers and analyzed sugars in the flowers of these two plant species.

\* See solutions  
-0.5

|          |          | Factor B    |                |
|----------|----------|-------------|----------------|
|          |          | with Flower | without Flower |
| Factor A | V. plant |             |                |
|          | S. plant |             |                |

The intrinsic rate of increase  $r_m$  is widely used to evaluate reproductive potential.

$r_m$  values on Verbena and Scaevola with flowers were 0.0884 and 0.08098.

Flowers are essential for the positive effects of these species as banker plants.

\* Answer in last page also can specify this question.

```

ods rtf file='hw3_output.rtf' startpage=NO;

data loaf;
infile 'sourdough.csv' firsttobs=2 dsd;
input day water autolyse height x1 x2 x22 x23 x1x2 x1x22 x1x23;
run;

proc print data=loaf;
run;

title 'Homework3: Two-Factor Factorial ANOVA';

/*Insert SAS code for Homework 3 here (i.e., before the "ods rtf close;" command) */
proc glm data=loaf plots=all;
class water autolyse;
model height= water autolyse water*autolyse;
lsmeans water*autolyse/cl pdiff adjust=tukey;
run;

title 'Homework3: Response Curve Analysis';

proc reg data=loaf;
model height=x1 x2 x22 x23 x1x2 x1x22 x1x23/ssl;
run;

title 'Homework3: Two-Factor Factorial with blocking ANOVA';

proc glm data=loaf plots=all;
class water autolyse day;
model height=day water autolyse water*autolyse;
run;

ods rtf close;

```

### The SAS System

| <b>Obs</b> | <b>day</b> | <b>water</b> | <b>autolyse</b> | <b>height</b> | <b>x1</b> | <b>x2</b> | <b>x22</b> | <b>x23</b> | <b>x1x2</b> | <b>x1x22</b> | <b>x1x23</b> |
|------------|------------|--------------|-----------------|---------------|-----------|-----------|------------|------------|-------------|--------------|--------------|
| <b>1</b>   | 12         | 315          | 30              | 8.5           | -1        | -1.00000  | 1.00000    | -1.00000   | 1.00000     | -1.00000     | 1.00000      |
| <b>2</b>   | 1          | 315          | 30              | 7.4           | -1        | -1.00000  | 1.00000    | -1.00000   | 1.00000     | -1.00000     | 1.00000      |
| <b>3</b>   | 5          | 315          | 30              | 9.6           | -1        | -1.00000  | 1.00000    | -1.00000   | 1.00000     | -1.00000     | 1.00000      |
| <b>4</b>   | 10         | 315          | 60              | 9.3           | -1        | -0.33333  | 0.11111    | -0.03704   | 0.33333     | -0.11111     | 0.03704      |
| <b>5</b>   | 15         | 315          | 60              | 9.7           | -1        | -0.33333  | 0.11111    | -0.03704   | 0.33333     | -0.11111     | 0.03704      |
| <b>6</b>   | 11         | 315          | 60              | 9.2           | -1        | -0.33333  | 0.11111    | -0.03704   | 0.33333     | -0.11111     | 0.03704      |
| <b>7</b>   | 2          | 315          | 90              | 9.4           | -1        | 0.33333   | 0.11111    | 0.03704    | -0.33333    | -0.11111     | -0.03704     |
| <b>8</b>   | 23         | 315          | 90              | 12.0          | -1        | 0.33333   | 0.11111    | 0.03704    | -0.33333    | -0.11111     | -0.03704     |
| <b>9</b>   | 18         | 315          | 90              | 10.1          | -1        | 0.33333   | 0.11111    | 0.03704    | -0.33333    | -0.11111     | -0.03704     |
| <b>10</b>  | 24         | 315          | 120             | 13.9          | -1        | 1.00000   | 1.00000    | 1.00000    | -1.00000    | -1.00000     | -1.00000     |
| <b>11</b>  | 13         | 315          | 120             | 11.5          | -1        | 1.00000   | 1.00000    | 1.00000    | -1.00000    | -1.00000     | -1.00000     |
| <b>12</b>  | 6          | 315          | 120             | 10.6          | -1        | 1.00000   | 1.00000    | 1.00000    | -1.00000    | -1.00000     | -1.00000     |
| <b>13</b>  | 3          | 320          | 30              | 10.4          | 1         | -1.00000  | 1.00000    | -1.00000   | -1.00000    | 1.00000      | -1.00000     |
| <b>14</b>  | 8          | 320          | 30              | 9.6           | 1         | -1.00000  | 1.00000    | -1.00000   | -1.00000    | 1.00000      | -1.00000     |
| <b>15</b>  | 7          | 320          | 30              | 10.9          | 1         | -1.00000  | 1.00000    | -1.00000   | -1.00000    | 1.00000      | -1.00000     |
| <b>16</b>  | 22         | 320          | 60              | 10.9          | 1         | -0.33333  | 0.11111    | -0.03704   | -0.33333    | 0.11111      | -0.03704     |
| <b>17</b>  | 20         | 320          | 60              | 12.1          | 1         | -0.33333  | 0.11111    | -0.03704   | -0.33333    | 0.11111      | -0.03704     |
| <b>18</b>  | 16         | 320          | 60              | 13.3          | 1         | -0.33333  | 0.11111    | -0.03704   | -0.33333    | 0.11111      | -0.03704     |
| <b>19</b>  | 9          | 320          | 90              | 11.5          | 1         | 0.33333   | 0.11111    | 0.03704    | 0.33333     | 0.11111      | 0.03704      |
| <b>20</b>  | 19         | 320          | 90              | 11.1          | 1         | 0.33333   | 0.11111    | 0.03704    | 0.33333     | 0.11111      | 0.03704      |
| <b>21</b>  | 21         | 320          | 90              | 12.5          | 1         | 0.33333   | 0.11111    | 0.03704    | 0.33333     | 0.11111      | 0.03704      |
| <b>22</b>  | 17         | 320          | 120             | 9.9           | 1         | 1.00000   | 1.00000    | 1.00000    | 1.00000     | 1.00000      | 1.00000      |
| <b>23</b>  | 4          | 320          | 120             | 10.2          | 1         | 1.00000   | 1.00000    | 1.00000    | 1.00000     | 1.00000      | 1.00000      |
| <b>24</b>  | 14         | 320          | 120             | 10.8          | 1         | 1.00000   | 1.00000    | 1.00000    | 1.00000     | 1.00000      | 1.00000      |

### The GLM Procedure

| Class Level Information |        |              |
|-------------------------|--------|--------------|
| Class                   | Levels | Values       |
| <b>water</b>            | 2      | 315 320      |
| <b>autolyse</b>         | 4      | 30 60 90 120 |

|                                    |    |
|------------------------------------|----|
| <b>Number of Observations Read</b> | 24 |
| <b>Number of Observations Used</b> | 24 |

### The GLM Procedure

### **Homework3: Two-Factor Factorial ANOVA**

*Dependent Variable: height*

ANOVA  
Table

| Source                 | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|------------------------|----|----------------|-------------|---------|--------|
| <b>Model</b>           | 7  | 34.38000000    | 4.91142857  | 4.57    | 0.0057 |
| <b>Error</b>           | 16 | 17.20000000    | 1.07500000  |         |        |
| <b>Corrected Total</b> | 23 | 51.58000000    |             |         |        |

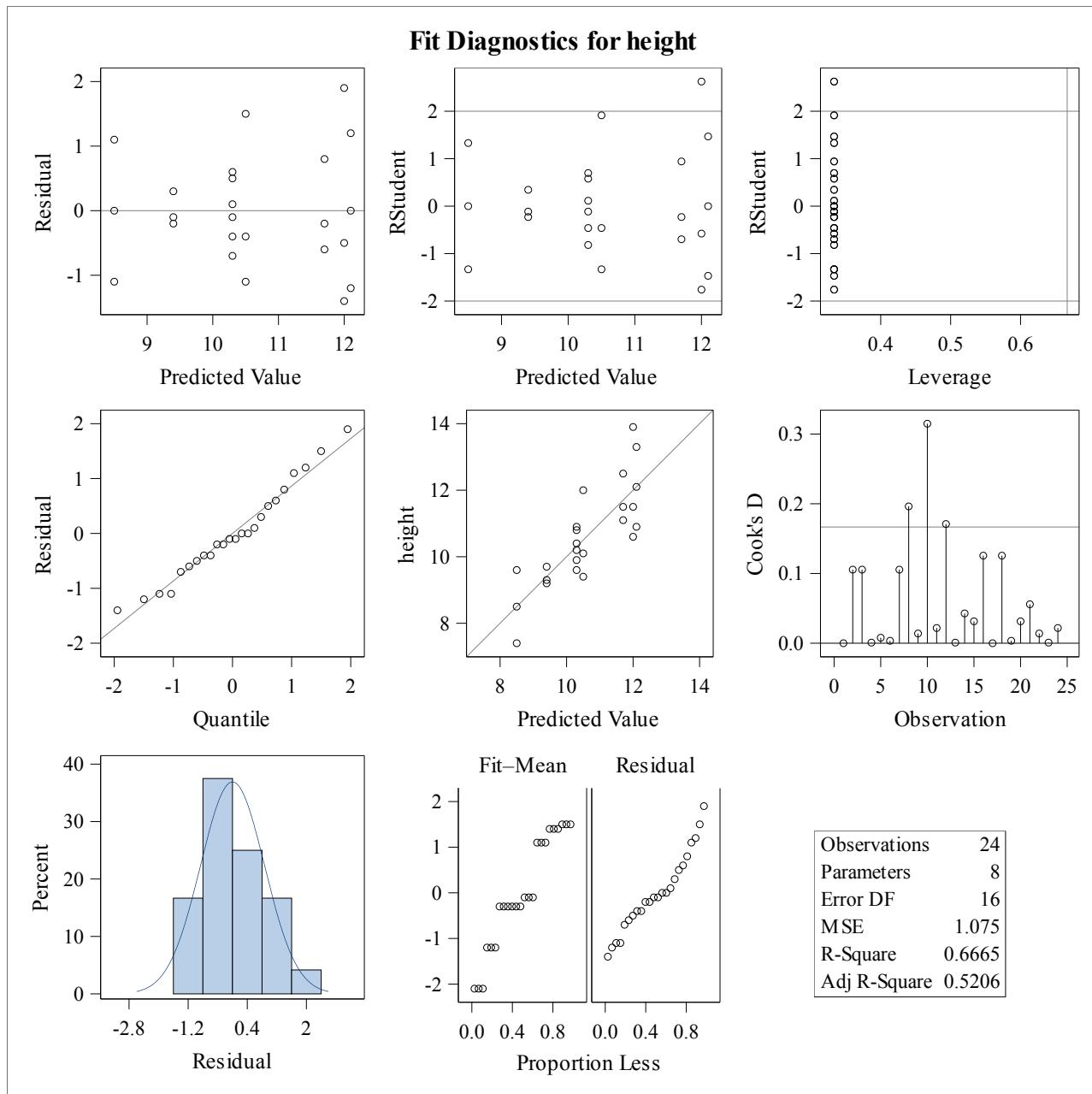
| R-Square | Coeff Var | Root MSE | height Mean |
|----------|-----------|----------|-------------|
| 0.666537 | 9.781340  | 1.036822 | 10.60000    |

| Source                | DF | Type I SS   | Mean Square | F Value | Pr > F |
|-----------------------|----|-------------|-------------|---------|--------|
| <b>water</b>          | 1  | 6.00000000  | 6.00000000  | 5.58    | 0.0312 |
| <b>autolyse</b>       | 3  | 12.09000000 | 4.03000000  | 3.75    | 0.0326 |
| <b>water*autolyse</b> | 3  | 16.29000000 | 5.43000000  | 5.05    | 0.0119 |

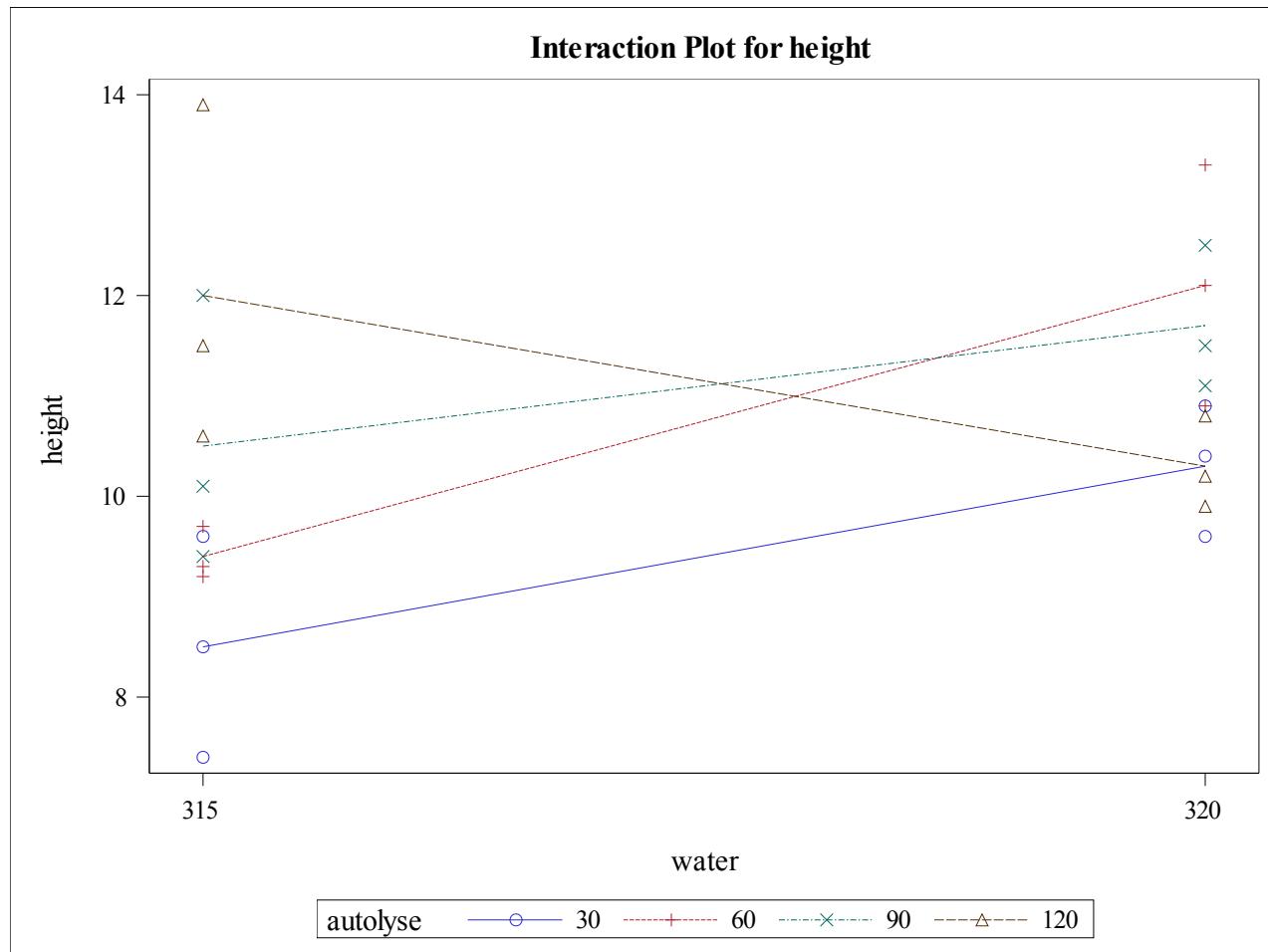
| Source                | DF | Type III SS | Mean Square | F Value | Pr > F |
|-----------------------|----|-------------|-------------|---------|--------|
| <b>water</b>          | 1  | 6.00000000  | 6.00000000  | 5.58    | 0.0312 |
| <b>autolyse</b>       | 3  | 12.09000000 | 4.03000000  | 3.75    | 0.0326 |
| <b>water*autolyse</b> | 3  | 16.29000000 | 5.43000000  | 5.05    | 0.0119 |

To check whether ASSUMPTION Satisfied.

### Homework3: Two-Factor Factorial ANOVA



### Homework3: Two-Factor Factorial ANOVA



***The GLM Procedure***  
***Least Squares Means***  
***Adjustment for Multiple Comparisons: Tukey***

| water | autolyse | height<br>LSMEAN | LSMEAN<br>Number |
|-------|----------|------------------|------------------|
| 315   | 30       | 8.5000000        | 1                |
| 315   | 60       | 9.4000000        | 2                |
| 315   | 90       | 10.5000000       | 3                |
| 315   | 120      | 12.0000000       | 4                |
| 320   | 30       | 10.3000000       | 5                |
| 320   | 60       | 12.1000000       | 6                |
| 320   | 90       | 11.7000000       | 7                |
| 320   | 120      | 10.3000000       | 8                |

**Homework3: Two-Factor Factorial ANOVA**

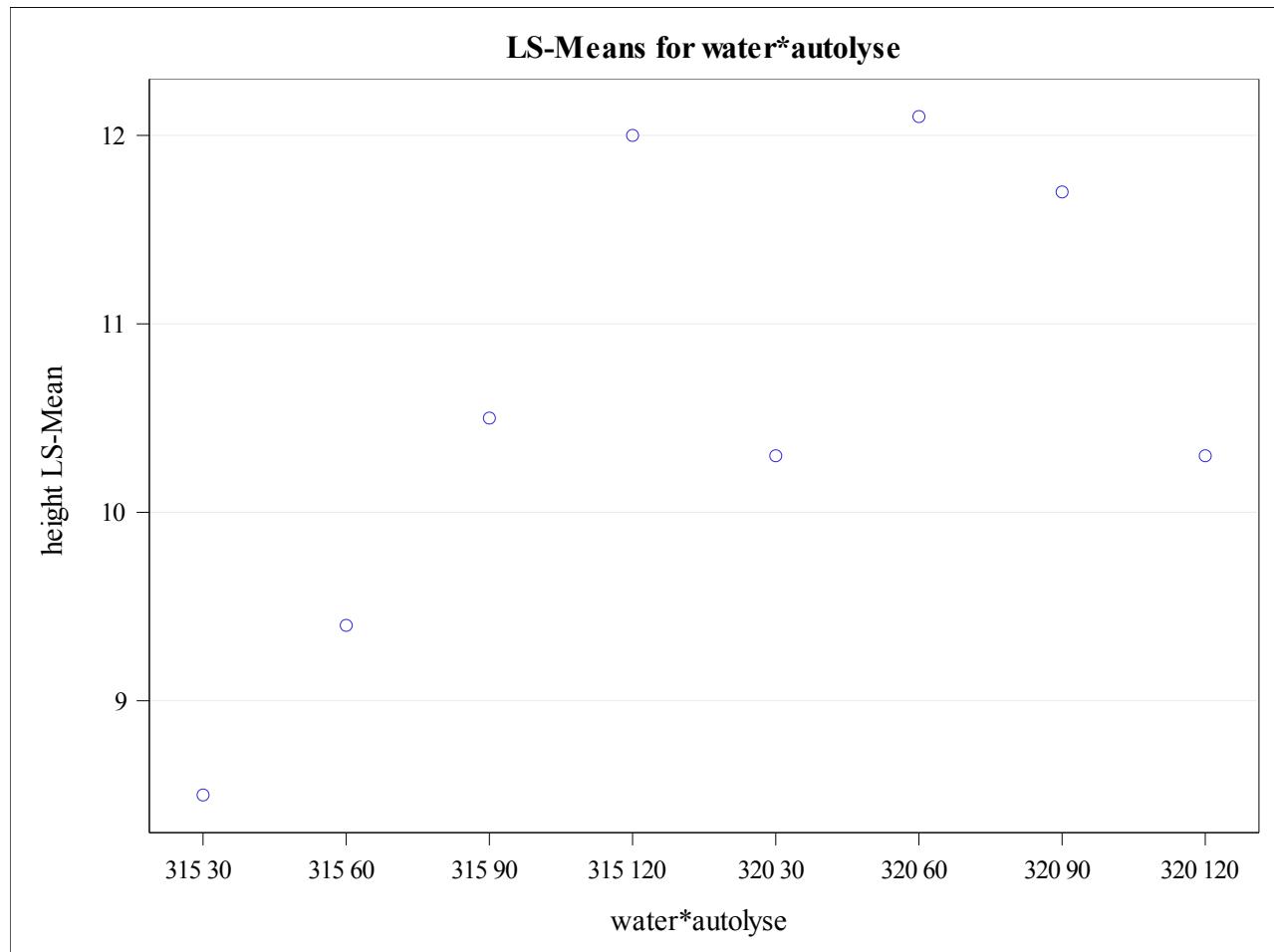
| Least Squares Means for effect water*autolyse<br>Pr >  t  for H0: LSMean(i)=LSMean(j) |        |        |        |        |        |        |        |        |
|---------------------------------------------------------------------------------------|--------|--------|--------|--------|--------|--------|--------|--------|
| i/j                                                                                   | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      |
| 1                                                                                     |        | 0.9559 | 0.3209 | 0.0138 | 0.4396 | 0.0109 | 0.0273 | 0.4396 |
| 2                                                                                     | 0.9559 |        | 0.8864 | 0.1021 | 0.9559 | 0.0826 | 0.1867 | 0.9559 |
| 3                                                                                     | 0.3209 | 0.8864 |        | 0.6454 | 1.0000 | 0.5753 | 0.8368 | 1.0000 |
| 4                                                                                     | 0.0138 | 0.1021 | 0.6454 |        | 0.5060 | 1.0000 | 0.9999 | 0.5060 |
| 5                                                                                     | 0.4396 | 0.9559 | 1.0000 | 0.5060 |        | 0.4396 | 0.7141 | 1.0000 |
| 6                                                                                     | 0.0109 | 0.0826 | 0.5753 | 1.0000 | 0.4396 |        | 0.9996 | 0.4396 |
| 7                                                                                     | 0.0273 | 0.1867 | 0.8368 | 0.9999 | 0.7141 | 0.9996 |        | 0.7141 |
| 8                                                                                     | 0.4396 | 0.9559 | 1.0000 | 0.5060 | 1.0000 | 0.4396 | 0.7141 |        |

| water | autolyse | height<br>LSMEAN | 95% Confidence<br>Limits |           |
|-------|----------|------------------|--------------------------|-----------|
| 315   | 30       | 8.500000         | 7.231005                 | 9.768995  |
| 315   | 60       | 9.400000         | 8.131005                 | 10.668995 |
| 315   | 90       | 10.500000        | 9.231005                 | 11.768995 |
| 315   | 120      | 12.000000        | 10.731005                | 13.268995 |
| 320   | 30       | 10.300000        | 9.031005                 | 11.568995 |
| 320   | 60       | 12.100000        | 10.831005                | 13.368995 |
| 320   | 90       | 11.700000        | 10.431005                | 12.968995 |
| 320   | 120      | 10.300000        | 9.031005                 | 11.568995 |

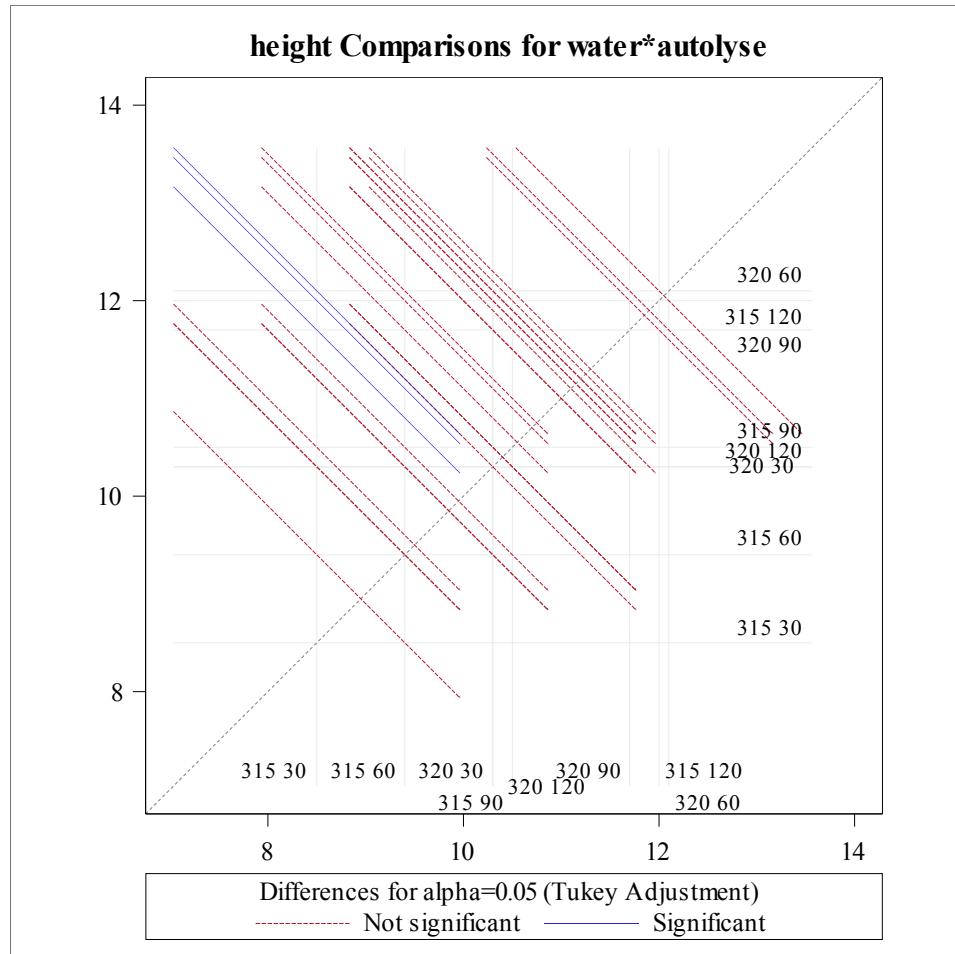
| Least Squares Means for Effect<br>water*autolyse |   |                                |                                                                  |           |
|--------------------------------------------------|---|--------------------------------|------------------------------------------------------------------|-----------|
| i                                                | j | Difference<br>Between<br>Means | Simultaneous 95%<br>Confidence Limits for<br>LSMean(i)-LSMean(j) |           |
| 1                                                | 2 | -0.900000                      | -3.830924                                                        | 2.030924  |
| 1                                                | 3 | -2.000000                      | -4.930924                                                        | 0.930924  |
| 1                                                | 4 | -3.500000                      | -6.430924                                                        | -0.569076 |
| 1                                                | 5 | -1.800000                      | -4.730924                                                        | 1.130924  |
| 1                                                | 6 | -3.600000                      | -6.530924                                                        | -0.669076 |
| 1                                                | 7 | -3.200000                      | -6.130924                                                        | -0.269076 |
| 1                                                | 8 | -1.800000                      | -4.730924                                                        | 1.130924  |
| 2                                                | 3 | -1.100000                      | -4.030924                                                        | 1.830924  |

***Homework3: Two-Factor Factorial ANOVA***

|   |   | Least Squares Means for Effect<br>water*autolyse |                                                                  |          |
|---|---|--------------------------------------------------|------------------------------------------------------------------|----------|
| i | j | Difference<br>Between<br>Means                   | Simultaneous 95%<br>Confidence Limits for<br>LSMean(i)-LSMean(j) |          |
| 2 | 4 | -2.600000                                        | -5.530924                                                        | 0.330924 |
| 2 | 5 | -0.900000                                        | -3.830924                                                        | 2.030924 |
| 2 | 6 | -2.700000                                        | -5.630924                                                        | 0.230924 |
| 2 | 7 | -2.300000                                        | -5.230924                                                        | 0.630924 |
| 2 | 8 | -0.900000                                        | -3.830924                                                        | 2.030924 |
| 3 | 4 | -1.500000                                        | -4.430924                                                        | 1.430924 |
| 3 | 5 | 0.200000                                         | -2.730924                                                        | 3.130924 |
| 3 | 6 | -1.600000                                        | -4.530924                                                        | 1.330924 |
| 3 | 7 | -1.200000                                        | -4.130924                                                        | 1.730924 |
| 3 | 8 | 0.200000                                         | -2.730924                                                        | 3.130924 |
| 4 | 5 | 1.700000                                         | -1.230924                                                        | 4.630924 |
| 4 | 6 | -0.100000                                        | -3.030924                                                        | 2.830924 |
| 4 | 7 | 0.300000                                         | -2.630924                                                        | 3.230924 |
| 4 | 8 | 1.700000                                         | -1.230924                                                        | 4.630924 |
| 5 | 6 | -1.800000                                        | -4.730924                                                        | 1.130924 |
| 5 | 7 | -1.400000                                        | -4.330924                                                        | 1.530924 |
| 5 | 8 | 0                                                | -2.930924                                                        | 2.930924 |
| 6 | 7 | 0.400000                                         | -2.530924                                                        | 3.330924 |
| 6 | 8 | 1.800000                                         | -1.130924                                                        | 4.730924 |
| 7 | 8 | 1.400000                                         | -1.530924                                                        | 4.330924 |

**Homework3: Two-Factor Factorial ANOVA**

### Homework3: Two-Factor Factorial ANOVA



#### The REG Procedure

**Model: MODEL1**

**Dependent Variable: height**

|                             |    |
|-----------------------------|----|
| Number of Observations Read | 24 |
| Number of Observations Used | 24 |

| Analysis of Variance   |    |                |             |         |        |
|------------------------|----|----------------|-------------|---------|--------|
| Source                 | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| <b>Model</b>           | 7  | 34.38000       | 4.91143     | 4.57    | 0.0057 |
| <b>Error</b>           | 16 | 17.20000       | 1.07500     |         |        |
| <b>Corrected Total</b> | 23 | 51.58000       |             |         |        |

### *Homework3: Response Curve Analysis*

|                       |          |                 |        |
|-----------------------|----------|-----------------|--------|
| <b>Root MSE</b>       | 1.03682  | <b>R-Square</b> | 0.6665 |
| <b>Dependent Mean</b> | 10.60000 | <b>Adj R-Sq</b> | 0.5206 |
| <b>Coeff Var</b>      | 9.78134  |                 |        |

QUESTION 2

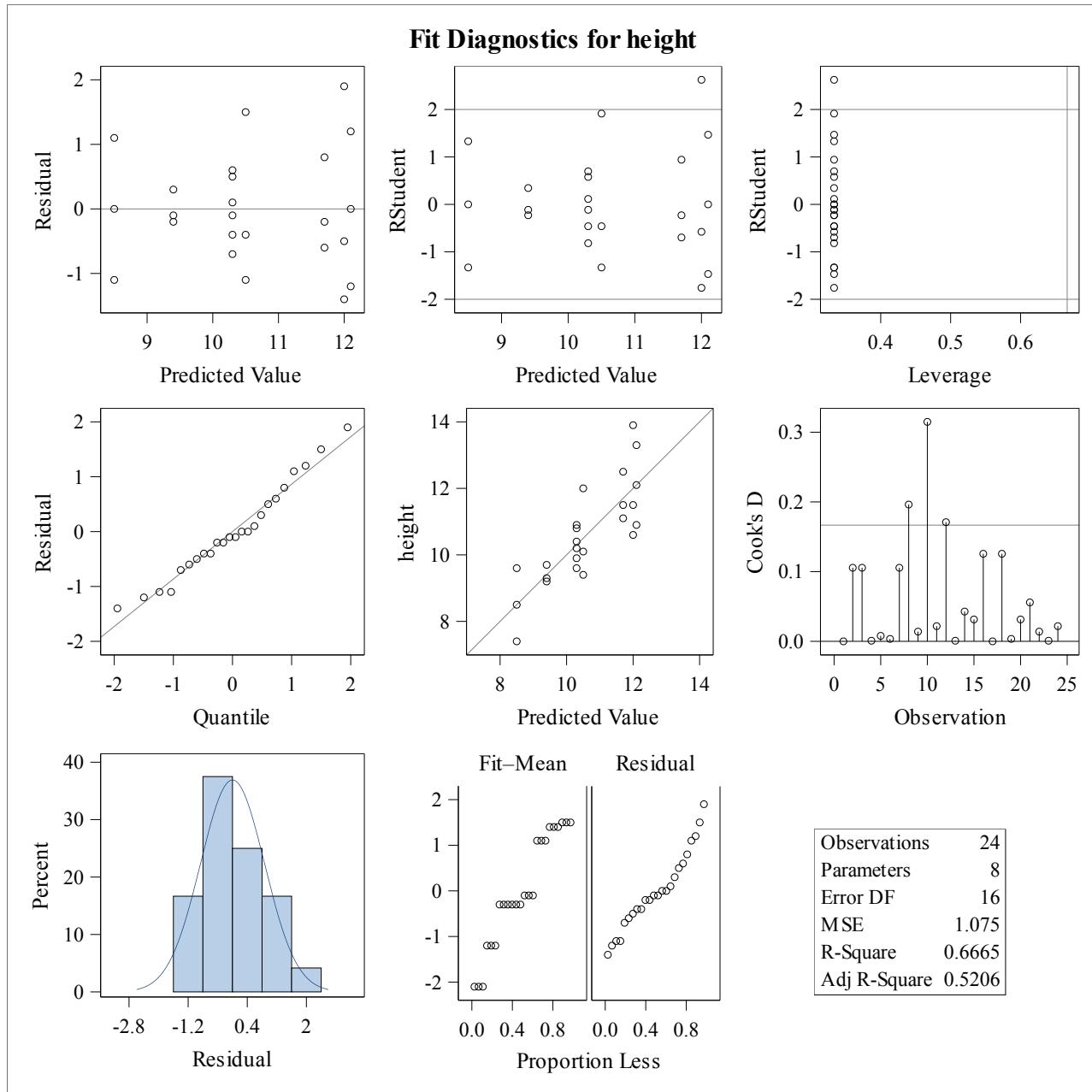
| Parameter Estimates |    |                    |                |         |         |            |
|---------------------|----|--------------------|----------------|---------|---------|------------|
| Variable            | DF | Parameter Estimate | Standard Error | t Value | Pr >  t | Type I SS  |
| <b>Intercept</b>    | 1  | 11.00625           | 0.33879        | 32.49   | <.0001  | 2696.64000 |
| <b>x1</b>           | 1  | 1.09375            | 0.33879        | 3.23    | 0.0053  | 6.00000    |
| <b>x2</b>           | 1  | 0.48125            | 1.01085        | 0.48    | 0.6404  | 9.40800    |
| <b>x22</b>          | 1  | -0.73125           | 0.47619        | -1.54   | 0.1442  | 2.53500    |
| <b>x23</b>          | 1  | 0.39375            | 1.06480        | 0.37    | 0.7164  | 0.14700    |
| <b>x1x2</b>         | 1  | -1.15625           | 1.01085        | -1.14   | 0.2695  | 10.80000   |
| <b>x1x22</b>        | 1  | -1.06875           | 0.47619        | -2.24   | 0.0393  | 5.41500    |
| <b>x1x23</b>        | 1  | 0.28125            | 1.06480        | 0.26    | 0.7950  | 0.07500    |

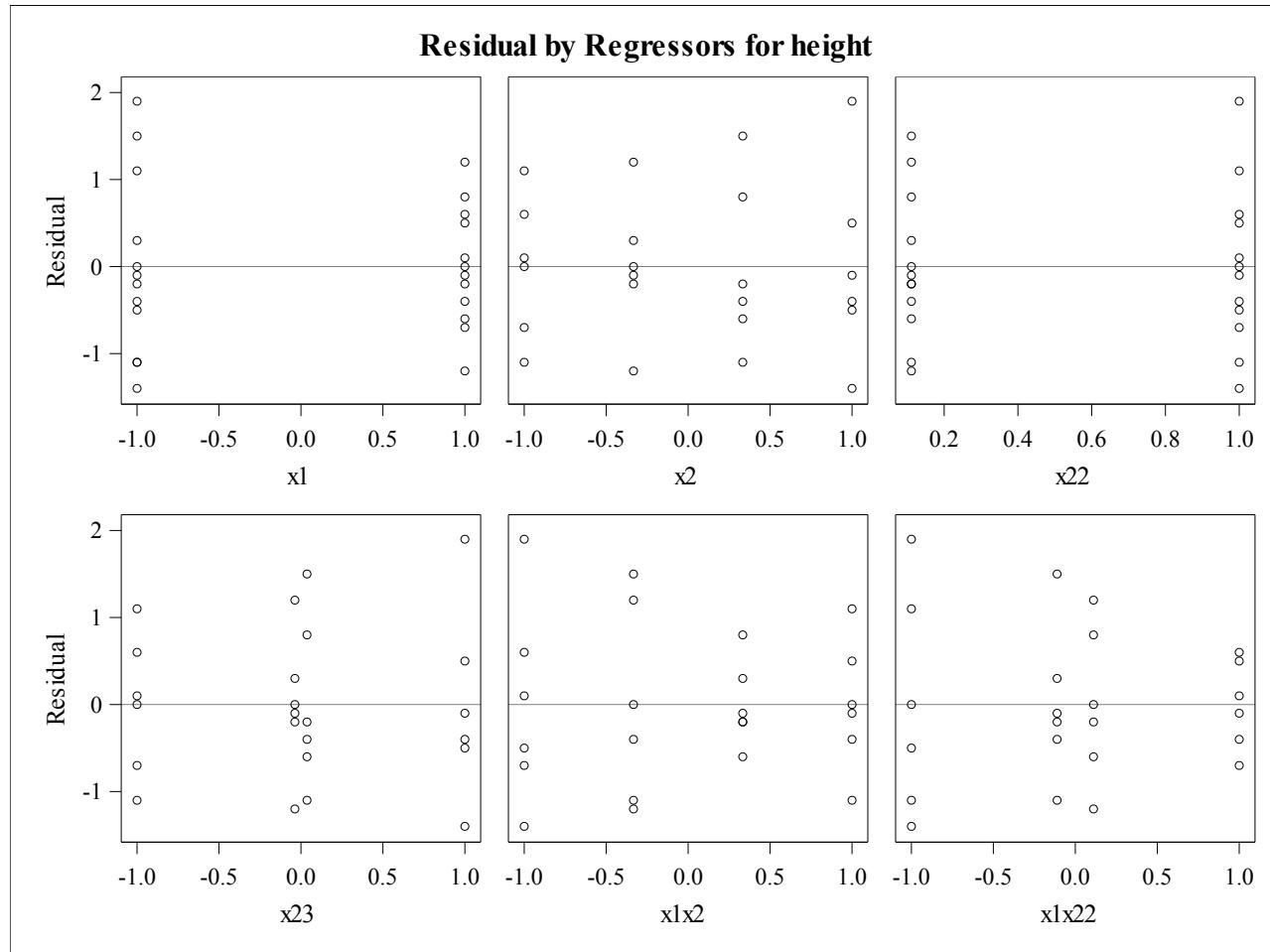
*The REG Procedure*

*Model: MODEL1*

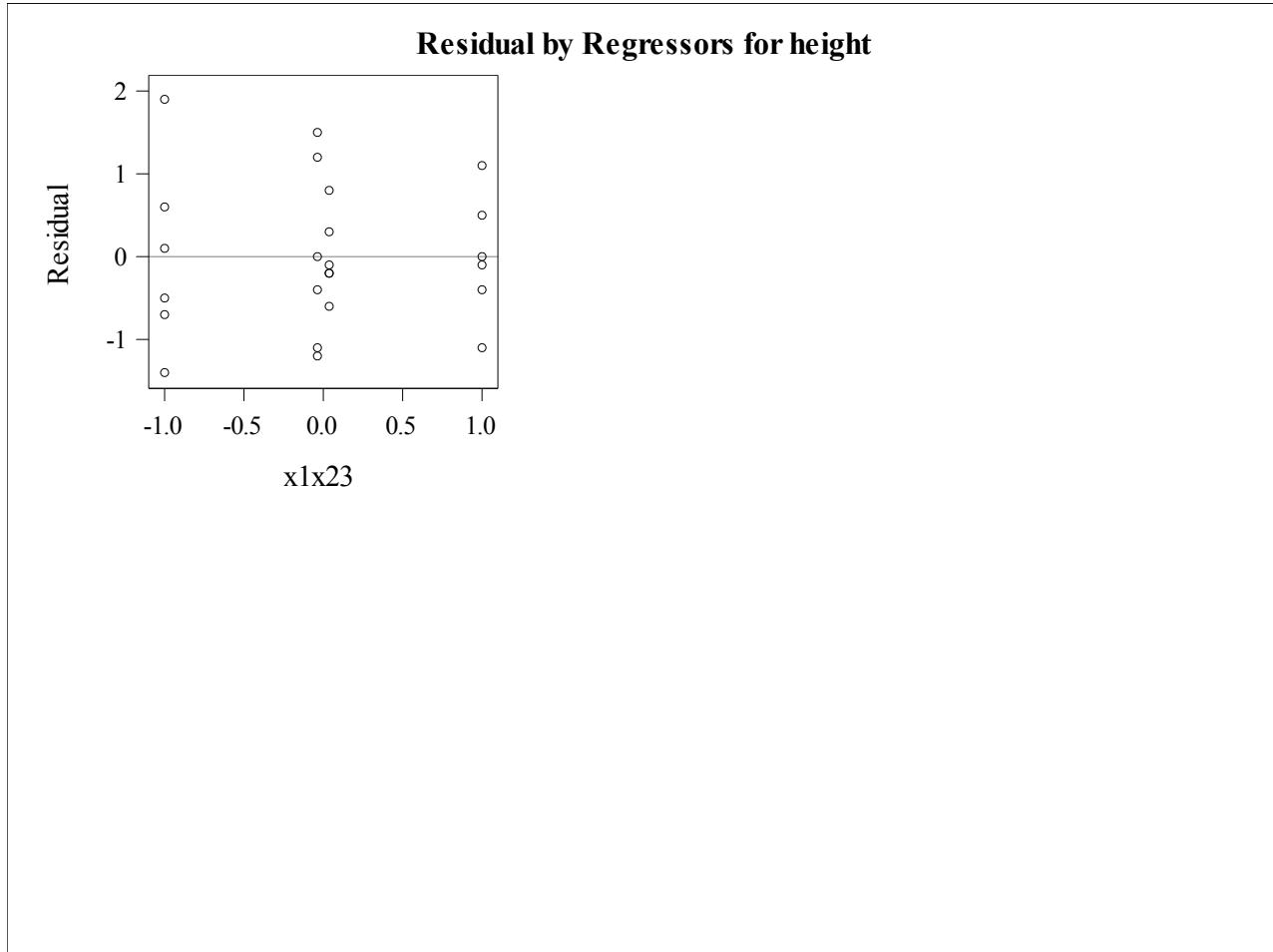
*Dependent Variable: height*

### Homework3: Response Curve Analysis



**Homework3: Response Curve Analysis**

### *Homework3: Response Curve Analysis*



#### *The GLM Procedure*

| Class Level Information |        |                                                                |
|-------------------------|--------|----------------------------------------------------------------|
| Class                   | Levels | Values                                                         |
| <b>water</b>            | 2      | 315 320                                                        |
| <b>autolyse</b>         | 4      | 30 60 90 120                                                   |
| <b>day</b>              | 24     | 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 |

|                             |    |
|-----------------------------|----|
| Number of Observations Read | 24 |
| Number of Observations Used | 24 |

#### *The GLM Procedure*

*Dependent Variable: height*

### Homework3: Two-Factor Factorial with *blocking* ANOVA

| Source          | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|----|----------------|-------------|---------|--------|
| Model           | 23 | 51.58000000    | 2.24260870  | .       | .      |
| Error           | 0  | 0.00000000     | .           | .       | .      |
| Corrected Total | 23 | 51.58000000    |             |         |        |

| R-Square | Coeff Var | Root MSE | height Mean |
|----------|-----------|----------|-------------|
| 1.000000 | .         | .        | 10.60000    |

| Source         | DF | Type I SS   | Mean Square | F Value | Pr > F |
|----------------|----|-------------|-------------|---------|--------|
| day            | 23 | 51.58000000 | 2.24260870  | .       | .      |
| water          | 0  | 0.00000000  | .           | .       | .      |
| autolyse       | 0  | 0.00000000  | .           | .       | .      |
| water*autolyse | 0  | 0.00000000  | .           | .       | .      |

| Source         | DF | Type III SS | Mean Square | F Value | Pr > F |
|----------------|----|-------------|-------------|---------|--------|
| day            | 16 | 17.20000000 | 1.07500000  | .       | .      |
| water          | 0  | 0.00000000  | .           | .       | .      |
| autolyse       | 0  | 0.00000000  | .           | .       | .      |
| water*autolyse | 0  | 0.00000000  | .           | .       | .      |

Seems like  
not working  
please ignore  
this part.

\* I didn't  
give you  
info on  
the blocking  
factor. ☺

### Homework3: Two-Factor Factorial with blocking ANOVA

