Causality

Macartan Humphreys

Section 1

Causality. What's a cause?

Subsection 1

Potential outcomes and the counterfactual approach

Potential outcomes and the counterfactual approach

Causation as difference making

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Motivation

The intervention based motivation for understanding causal effects:

- We want to know if a particular intervention (like aid) caused a particular outcome (like reduced corruption).
- We need to know:
 - What happened?
 - 2 What would the outcome have been if there were no intervention?
- The problem:
 - 1 ... this is hard
 - 2 ... this is impossible

The problem in 2 is that you need to know what would have happened if things were different. You need information on a **counterfactual**.

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- For each unit, we assume that there are two **post-treatment** outcomes: $Y_i(1)$ and $Y_i(0)$.
- ullet For example, Y(1) is the outcome that would obtain if the unit received the treatment.
- The causal effect of Treatment (relative to Control) is: $\tau_i = Y_i(1) - Y_i(0)$
- Note:
 - The causal effect is defined at the individual level.
 - There is no "data generating process" or functional form.
 - The causal effect is defined relative to something else, so a counterfactual must be conceivable (did Germany cause the second world war?).
 - Are there any substantive assumptions made here so far?

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Idea: A causal claim is (in part) a claim about something that did not happen. This makes it metaphysical.

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Now that we have a concept of causal effects available, let's answer two **questions**:

• TRANSITIVITY: If for a given unit A causes B and B causes C, does that mean that A causes C?

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Now that we have a concept of causal effects available, let's answer two **questions**:

- TRANSITIVITY: If for a given unit A causes B and B causes C, does that mean that A causes C?
- A boulder is flying down a mountain. You duck. This saves your life.
- So the boulder caused the ducking and the ducking caused you to survive.
- So: did the boulder cause you to survive?

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CONNECTEDNESS Say A causes B — does that mean that there is a spatiotemporally continuous sequence of causal intermediates?

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CONNECTEDNESS Say A causes B — does that mean that there is a spatiotemporally continuous sequence of causal intermediates?

 Person A is planning some action Y; Person B sets out to stop them; person X intervenes and prevents person B from stopping person A. In this case Person A may complete their action, producing Y, without any knowledge that B and X even exist; in particular B and X need not be anywhere close to the action. So: did X cause Y?

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The counterfactual model is all about contribution, not attribution, except in a very conditional sense.

- Focus is on non-rival contributions
- Not: what caused Y but what is the effect of X?
- At most it provides a conditional account

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Consider an outcome Y that might depend on two causes X_1 and X_2 :

$$Y(0,0) = 0$$
$$Y(1,0) = 0$$

$$Y(0,1)=0$$

$$Y(1,1) = 1$$

What caused Y? Which cause was most important?

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The counterfactual model is about attribution in a very conditional sense.

- Focus is on non-rival contributions
- Not: what caused Y but what is the effect of X?
- At most it provides a conditional account
- \bullet This is problem for research programs that define "explanation" in terms of figuring out the things that cause Y
- Real difficulties conceptualizing what it means to say one cause is more important than another cause. What does that mean?

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Erdogan's increasing authoritarianism was the most important reason for the attempted coup

- More important than Turkey's history of coups?
- What does that mean?

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Causal claims: No causation without manipulation

- Some seemingly causal claims not admissible.
- To get the definition off the ground, manipulation must be imaginable (whether practical or not)
- This renders thinking about effects of race and gender difficult
- What does it mean to say that Aunt Pat voted for Brexit because she is old?

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Causal claims: No causation without manipulation

- Some seemingly causal claims not admissible.
- To get the definition off the ground, manipulation must be imaginable (whether practical or not)
- This renders thinking about effects of race and gender difficult
- Compare: What does it mean to say that Southern counties voted for Brexit because they have many old people?

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Causal claims: Causal claims are everywhere

- Jack exploited Jill
- It's Jill's fault that bucket fell
- Jack is the most obstructionist member of Congress
- Melania Trump stole from Michelle Obama's speech
- Activists need causal claims

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Causal claims: What is actually seen?

- We have talked about what's potential, now what do we *observe*?
- Say Z_i indicates whether the unit i is assigned to treatment $(Z_i=1)$ or not $(Z_i=0)$. It describes the treatment process. Then what we observe is:

$$Y_i = Z_i Y_i(1) + (1-Z_i) Y_i(0) \label{eq:Yi}$$

This is sometimes called a "switching equation"

In ${\tt DeclareDesign}\ Y$ is realised from potential outcomes and assignment in this way using ${\tt reveal_outcomes}$

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Causal claims: What is actually seen?

- ullet Say Z is a random variable, then this is a sort of data generating process. BUT the key thing to note is
 - Y_i is random but the randomness comes from Z_i the potential outcomes, $Y_i(1)$, $Y_i(0)$ are fixed
 - \bullet Compare this to a regression approach in which Y is random but the X's are fixed. eg:

$$Y \sim N(\beta X, \sigma^2)$$
 or $Y = \alpha + \beta X + \epsilon, \epsilon \sim N(0, \sigma^2)$

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Causal claims: The estimand and the rub

The causal effect of Treatment (relative to Control) is:

$$\tau_i = Y_i(1) - Y_i(0)$$

- This is what we want to estimate.
- BUT: We never can observe both $Y_i(1)$ and $Y_i(0)$!
- This is the **fundamental problem** (@holland1986statistics)

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Causal claims: The rub and the solution

• Now for some magic. We really want to estimate:

$$\tau_i = Y_i(1) - Y_i(0)$$

- BUT: We never can observe both $Y_i(1)$ and $Y_i(0)$
- Say we lower our sights and try to estimate an average treatment effect:

$$\tau = \mathbb{E}[Y(1) - Y(0)]$$

Now make use of the fact that

$$\mathbb{E}[Y(1)-Y(0)] = \mathbb{E}[Y(1)] - \mathbb{E}[Y(0)]$$

- In words: The average of differences is equal to the difference of averages; here, the average treatment effect is equal to the difference in average outcomes in treatment and control units.
- The magic is that while we can't hope to measure the differences; we Macartan Humphreys Causality 22 / 92

Causal claims: The rub and the solution

- So we want to estimate $\mathbb{E}[Y(1)]$ and $\mathbb{E}[Y(0)]$.
- We know that we can estimate averages of a quantity by taking the average value from a random sample of units
- ullet To do this here we need to select a random sample of the Y(1) values and a random sample of the Y(0) values, in other words, we randomly assign subjects to treatment and control conditions.
- When we do that we can in fact estimate:

$$\mathbb{E}_N[Y_i(1)|Z_i=1) - \mathbb{E}_N(Y_i(0)|Z_i=0]$$

which in expectation equals:

$$\mathbb{E}[Y_i(1)|Z_i=1 \text{ or } Z_i=0] - \mathbb{E}[Y_i(0)|Z_i=1 \text{ or } Z_i=0]$$

 This highlights a deep connection between random assignment and random sampling: when we do random assignment we are in fact randomly sampling from different possible worlds.

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Causal claims: The rub and the solution

This provides a **positive argument** for causal inference from randomization, rather than simply saying with randomization "everything else is controlled for"

Let's discuss:

- Does the fact that an estimate is unbiased mean that it is right?
- Can a randomization "fail"?
- Where are the covariates?

Idea: random assignment is random sampling from potential worlds: to understand anything you find, you need to know the sampling weights

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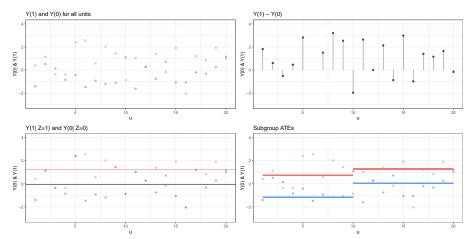
Reflection

Idea: We now have a *positive* argument for claiming unbiased estimation of the average treatment effect following random assignment

But is the average treatment effect a quantity of social scientific interest?

Potential outcomes: why randomization works

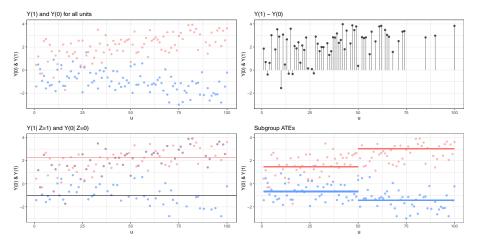
The average of the differences \approx difference of averages



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Potential outcomes: heterogeneous effects

The average of the differences \approx difference of averages



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Potential outcomes: heterogeneous effects

Question: \approx or =?

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Exercise your potential outcomes 1

Consider the following potential outcomes table:

Y(0)	Y(1)	τ_{i}
4	3	
2	3	
1	3	
1	3	
2	3	
	4 2 1 1	4 3 2 3 1 3 1 3

Questions for us: What are the unit level treatment effects? What is the average treatment effect?

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Exercise your potential outcomes 2

Consider the following potential outcomes table:

In treatment?	Y(0)	Y(1)
Yes		2
No	3	
No	1	
Yes		3
Yes		3
No	2	

Questions for us: Fill in the blanks.

- Assuming a constant treatment effect of +1
- Assuming a constant treatment effect of -1
- Assuming an average treatment effect of 0

Subsection 2

Endogeneous subgroups

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Endogeneous Subgroups

Experiments often give rise to endogenous subgroups. The potential outcomes framework can make it clear why this can cause problems.

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- Problems arise in analyses of subgroups when the categories themselves are affected by treatment
- Example from our work:
 - You want to know if an intervention affects reporting on violence against women
 - You measure the share of all subjects that experienced violence that file reports
 - The problem is that which subjects experienced violence is itself a function of treatment

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It is possible that in truth no one's reporting behavior has changed, what has changed is the propensity of people with different propensities to report to experience violence:

```
\begin{table} \scriptsize
    \centering
    \begin{tabular}{rcc|cc|cc}
        & \multicolumn{ 2}{c}{Violence(Treatment)} & \multicol
                V(0) &
                             V(1) &
                                        R(0.1) &
                                                      R(1.1) &
        &
        Type 1 (reporter) &
                                                   1 &
                                     1 &
        Type 2 (non reporter) &
```

\end{tabular}

1 &

&₹.

- Violence(Treatment)
- Reporting(Treatment, Violence)

	V(0)	V(1)	R(0,1)	R(1,1)	R(0,0)	R(1,0)
Type 1 (reporter)	1	1	1	1	0	0
Type 2 (non reporter)	1	0	0	0	0	0

Expected reporting given violence in control = Pr(Type 1)

Expected reporting given violence in treatment = 100%

Question: What is the actual effect of treatment on the propensity to report violence?

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It is possible that in truth no one's reporting behavior has changed, what has changed is the propensity of people with different propensities to report to experience violence:

	Reporters		Non reporters		
	Experience Violence		Experience Violence		
Control	No 25	Yes 25	No 25	Yes 25	% Report $\frac{25}{25+25} = 50\%$
Treatment	25	25	50	0	$\frac{25}{25+0}$ =100%

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Heterogeneous Effects with Endogeneous Categories

This problem can arise as easily in seemingly simple field experiments. Example:

- In one study we provided constituents with information about performance of politicians
- we told politicians in advance so that they could take action
- we wanted to see whether voters punished poorly performing politicians
- what's the problem?

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Heterogeneous Effects with Endogeneous Categories

Question for us:

Setting:

- * Quotas for women are randomly placed in a set of constitution
- * In year 2 these quotas are then lifted.

Questions Which problems face an endogenous subgroup issue?:

- 1 You want to estimate the likelihood that a woman will stand for reelection in treatment versus control areas in year 2.
- 2 You want to estimate how much incumbents are more likely to be reelected in treatment versus control areas in year 2.
- You want to estimate how much treatment areas have more relected incumbents in elections in year 2 compared to control.

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Heterogeneous Effects with Endogeneous Categories

In such cases you can:

- Examine the joint distribution of multiple outcomes
- Condition on pretreatment features only
- Engage in mediation analysis

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Missing data can create an endogeneous subgroup problem

- It is well known that missing data can undo the magic of random assignment.
- One seemingly promising approach is to match into pairs ex ante and drop pairs together ex post.
- Say potential outcomes looked like this (four units divided into two pairs):

Pair	I	l	П	Ш	
Unit	1	2	3	4	Average
Y(0)	0	0	0	0	
Y(1)	-3	1	1	1	
au	-3	1	1	1	

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Missing data

- Say though that cases are likely to drop out of the sample if things go badly (eg they get a negative score or die)
- Then you might see no attrition in cases in which people that are likely to drop out if treated do not get treated.
- You might assume you have no problem (after all, no attrition).
- No missing data when the normal cases happens to be selected

Pair	I	I	П	Ш	
Unit	1	2	3	4	Average
Y(0)	0		0		0
$Y(1)$ $\hat{\tau}$		1		1	1
$\hat{ au}$					1

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Missing data

- But in cases in which you have attrition, dropping the pair doesn't necessarily help.
- The problem is potential missingness still depends on potential outcomes
- The kicker is that the method can produce bias even if (in fact) there is no attrition!

Missing data when the vulnerable cases happens to be selected

Pair	I	I	Ш	Ш	
Unit	1	2	3	4	Average
Y(0)		[0]	0		0
$Y(1)$ $\hat{\tau}$	[-3]			1	1
$\hat{ au}$					1

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Missing data

Note: The right way to think about this is that bias is a property of the strategy over possible realizations of data and not normally a property of the estimator conditional on the data.

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Multistage games can also present an endogenous group problem since collections of late stage players facing a given choice have been created by early stage players.

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Question: Does **visibility** alter the extent to which subjects follow norms to punish antisocial behavior (and reward prosocial behavior)? Consider a trust game in which we are interested in how information on receivers affects their actions

Table 7: Return rates given investments under different conditions

		% invested	Average % returned		
		(average)	whenwhen		
			10% invested	50% invested	
Treatment	Masked information on respon- dents	30% (avg)	20%	40%	
	Full information on respondents	30% (avg)	0%	60%	

What do we think? Does visibility make people react more to investments?

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Imagine you could see all the potential outcomes, and they looked like this:

Table 8: Potential outcomes with (and without) identity protection

		Re	Responder's return decision (given type)						
		Nice	Nice	Nice	Mean	Mean	Mean		
		1	2	3	4	4	6		
Offerer	Invest 10%:	60%	60%	60%	0%	0%	0%	30%	
behavior	Invest 50%:	60%	60%	60%	0%	0%	0%	30%	

Conclusion: Both the offer and the information condition are **completely irrelevant** for all subjects.

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Unfortunately you only see a sample of the potential outcomes, and that looks like this:

Table 9: Outcomes when respondent is visible

		Re	Responder's return decision (given type)						
		Nice	Nice	Nice	Mean	Mean	Mean		
		1	2	3	4	4	6		
Offerer	Invest 10%:				0%	0%	0%	0%	
behavior	Invest 50%:	60%	60%	60%				60%	

False Conclusion: When not protected, responders condition behavior *strongly* on offers (because offerers can select on type accurately)

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Unfortunately you only see a sample of the potential outcomes, and that looks like this.

Table 10: Outcomes when respondent is not visible

		Re	Responder's return decision (given type) A						
		Nice	Nice	Nice	Mean	Mean	Mean		
		1	2	3	4	4	6		
Offerer	Invest 10%:			60%		0%	0%	20%	
behavior	Invest 50%:	60%	60%		0%			40%	

False Conclusion: When protected, responders condition behavior less strongly on offers (because offerers can select on type less accurately)

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What to do?

Solutions?

- Analysis could focus on the effect of treatment on respondent behavior, directly.
 - This would get the correct answer but to a different question [Does information affect the share of contributions returned by subjects on average? No]
- Strategy method can sometimes help address the problem, but that is also (a) changing the question and (b) putting demands on respondent imagination and honesty
- First mover action could be directly manipulated, but unless deception is used that is also changing the question
- First movers could be selected because they act in predictable ways (bordering on deception?)

Idea: Proceed with extreme caution when estimating effects beyond the

DAGs

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Key insight

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Key insight

The most powerful results from the study of DAGs are procedures for figuring out when conditioning aids or hinders causal identification.

- You can read off a confounding variable from a DAG.
 - You have to condition on such a variable for causal identification.
- You can read off "colliders" from a DAG
 - Sometimes you have avoid conditioning on these
- Sometimes a variable might be both, so
 - you have to condition on it
 - you have to avoid conditioning on it
 - Ouch.

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Key resource

- Pearl's book Causality is the key reference. @pearl2009causality (Though see also older work such as @pearl1985graphoids)
- There is a lot of excellent material on Pearl's page http://bayes.cs.ucla.edu/WHY/
- See also excellent material on Felix Elwert's page http://www.ssc.wisc.edu/~felwert/causality/?page id=66

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Challenge for us

- Say you don't like graphs. Fine.
- Consider this causal structure:
 - $Z = f_1(U_1, U_2)$
 - $X = f_2(U_2)$
 - $Y = f_3(X, U_1)$

Say Z is temporally prior to X; it is correlated with Y (because of U_1) and with X (because of U_2).

Question: Would it be useful to "control" for Z when trying to estimate the effect of X on Y?

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Challenge for us

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Challenge for us

- Say you don't like graphs. Fine.
- Consider this causal structure:
 - $Z = f_1(U_1, U_2)$
 - $X = f_2(U_2)$
 - $Y = f_3(X, U_1)$

Question: Would it be useful to "control" for Z when trying to estimate the effect of X on Y?

Answer: Hopefully by the end of today you should see that that the answer is obviously (or at least, plausibly) "no."

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Conditional independence

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Conditional independence

Variable sets A and B are conditionally independent, given C if for all $a,\,b,\,c$:

$$Pr(A = a | C = c) = Pr(A = a | B = b, C = c)$$

Informally; given C, knowing B tells you nothing more about A.

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- Consider a situation with variables $X_1, X_2, ... X_n$
- ullet The probability of outcome x can always be written in the form $P(X_1 = x_1)P(X_2 = x_2|X_1 = x_1)(X_3 = x_3|X_1 = x_1, X_2 = x_2)...$
- This can be done with any ordering of variables.
- However the representation can be greatly simplified if you can make use of a set of "parentage" relationships
- ullet Given an ordering of variables, the **Markovian parents** of variable X_i are the minimal set of variables such that when you condition on these, X_i is independent of all other prior variables in the ordering
- In this case we can write: $P(x) = \prod_i (x_i | pa_i)$
- No graphs yet

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Causal graphs basics 2

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- We want to use causal graphs to represent these relations of conditional independence.
- Informally, an arrow, $A \to B$ means that A is a cause of B: that is, under some conditions, a change in A produces a change in B.
 - Arrows carry no information about the type of effect; e.g. sign, size, or whether different causes are complements or substitutes
- We say that arrows point from parents to children, and by extension from ancestors to descendants.
- These are parents on the graph; but we will connect them to Markovian parents in a probability distribution P.

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Causal graphs basics 2

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- A DAG is just a graph in which some or all nodes are connected by directed edges (arrows) and there are no cyclical paths along these directed edges.
- Consider a DAG, G, and consider the ancestry relations implied by G: the distribution P is Markov relative to the graph G if every variable is independent of its nondescendants (in G) conditional on its parents (in G).
 - This is the Markov condition: conditional on its parents, a variable is independent of its non-descendants.
- OK now we have a link from probability distributions to graphs. But we have not talked about causality.

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We want the graphs to be able to represent the effects of interventions.

Pearl uses do notation to capture this idea.

$$\Pr(X_1, X_2, \dots | do(X_j = x_j))$$

or

$$\Pr(X_1, X_2, \dots | \hat{x}_i)$$

denotes the distribution of X when a particular node (or set of nodes) is intervened upon and forced to a particular level, x_i .

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Causal graphs basics 3

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Note, in general:

$$\Pr(X_1,X_2,\dots|do(X_j=x_j'))\neq\Pr(X_1,X_2,\dots|X_j=x_j')$$

as an example we might imagine a situation where for men binary X always causes Y=1 and for women Y=1 regardless of X. We imagine that X=1 for men only.

In that case
$$\Pr(Y=1|X=1)=1$$
 but $\Pr(Y=1|do(X=1))=.5$

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Causal graphs basics 3

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- Let P_z denote the resulting distribution on all variables that arises when vector Z is "set" (forced, controlled...) to the value z. That is when we have do (Z=z).
- ullet Let P_* denote the set of all such distributions that can result from any set of interventions on variables.
- A DAG, G, is a causal Bayesian network compatible with P_* iff, for all interventions z:
 - $oldsymbol{0}$ P_z is Markov relative to G
 - 2 $P_z(x_i) = 1$ for all x_i consistent with z
 - $\ \, \textbf{0} \ \, P_z(x_j|pa_j) = P(x_j|pa_j) \text{ for all } x_j \not\in Z \text{ when } pa_j \text{ is consistent with } z$

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Causal graphs basics 3

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Causal graphs basics 3

 That all means that the probability distribution resulting from setting some set X_i to $\hat{x'}_i$ (i.e. do(X=x')) is:

$$P_{\hat{x}_i} = P(x_1, x_2, \dots x_n | \hat{x}_i) = \prod_{-i} P(x_j | pa_j) \mathbb{1}(x_i = x_i')$$

This means that there is only probability mass on vectors in which $x_i = x_i'$ (reflecting the success of control) and all other variables are determined by their parents, given the values that have been set for x_i .

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Conditional Independence and d-separation

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Conditional Independence and d-separation

- We now have a well defined sense in which the arrows on a graph represent a causal structure and capture the conditional independence relations implied by the causal structure.
- Of course any graph might represent many different probability distributions P
- We can now start reading off from a graph when there is or is not conditional independence between sets of variables

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Conditional independence on paths

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Conditional independence on paths

(1) A path of arrows pointing in the same direction



(2) A forked path



(3) An inverted fork (collision)



Figure 1: Three elemental relations of conditional independence.

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Conditional independence

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Conditional independence

A and B are conditionally independent, given C if on every path between A and B:

• there is some chain $(\bullet \to \bullet \to \bullet \text{ or } \bullet \leftarrow \bullet \leftarrow \bullet)$ or fork $(\bullet \leftarrow \bullet \to \bullet)$ with the central element in C,

or

ullet there is an inverted fork (ullet o ullet o) with the central element (and its descendants) not in C

Notes:

- In this case we say that A and B are d-separated by C.
- A, B, and C can all be sets
- Note that a path can involve arrows pointing any direction

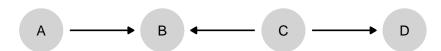
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 o o o o o o

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Test yourself

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Test yourself



Are A and D unconditionally independent:

- if you do not condition on anything?
- if you condition on B?
- if you condition on C?

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Back to this example

Back to this example

- $* $Z = f_1(U_1, U_2)$$ * \$X = f 2(U 2)\$ $* $Y = f_3(X, U 1)$$
 - Let's graph this
 - 2 Now: say we removed the arrow from X to Y
 - ullet Would you expect to see a correlation between X and Y if you did not control for Z
 - Would you expect to see a correlation between X and Y if you did control for Z

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From graphs to Causal Models

From graphs to Causal Models

A "causal model" is:

- 1.1: An ordered list of n endogenous nodes, $\mathcal{V} = (V^1, V^2, \dots, V^n)$, with a specification of a range for each of them
- 1.2: A list of n exogenous nodes, $\Theta = (\theta^1, \theta^2, \dots, \theta^n)$
- 2: A list of n functions $\mathcal{F} = (f^1, f^2, \dots, f^n)$, one for each element of \mathcal{V} such that each f^i takes as arguments θ^i as well as elements of $\mathcal V$ that are prior to V^i in the ordering

and

3: A probability distribution over Θ

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From graphs to Causal Models

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A model of inequality's effect on democratization

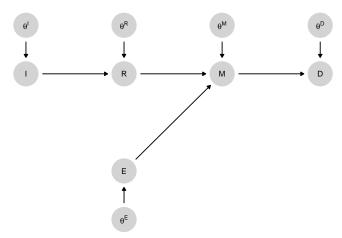


Figure 2: A simple causal model in which high inequality (I) affects democratization (D) via redistributive demands (R) and mass mobilization (M) Macartan Humphreys Causality

Effects on a DAG

Learning about effects given a model means learning about F and also the distribution of shocks (Θ) .

For discrete data this can be reduced to a question about learning about the distribution of Θ only.

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Recap: Key features of graphs

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Recap: Key features of graphs

- Directed
- Acyclic
- The missing arcs are the really important ones
- Implicitly there are shocks going into every node
- These graphs represent Nonparametric structural equation models **NPSEMs**
- But you cannot read off the size or direction of effects from a DAG

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Recap: Ten things you need to know about causal inference

- A causal claim is a statement about what didn't happen.
- There is a fundamental problem of causal inference.
- You can estimate average causal effects even if you cannot observe any individual causal effects.
- If you know that A causes B and that B causes C, this does not mean that you know that A causes C.
- The counterfactual model is primarily about contribution, and about attribution in a limited sense.
- \bullet X can cause Y even if there is no "causal path" connecting X and Y.
- Correlation is not causation.
- lacktriangle X can cause Y even if X is not a necessary condition or a sufficient condition for Y.
- Estimating average causal effects does not require that treatment and control groups are identical.
- There is no causation without manipulation.