ITU, Spring 2025

## Exercise 5

Last update February 16, 2025

This exercise sheet must be handed in via LearnIt.

You solve the assignments in your groups.

Your name must be part of the filename, e.g., FP-05-<name>-<name>.fsx.

An example: FP-05-MadsAndersen-HugoHansen.fsx.

You can only upload one file and it must be of type fs or fsx.

It is important that you annotate your own code with comments. It is also important that you apply a functional style, i.e., no loops and no mutable variables.

For this hand-in you also need to consider scenarios where your solutions should return an error, i.e., an exception. The requirement is, that no matter what input you pass to your function that fulfils the function type, then the function should return the intended answer or an exception. It is up to you to define the exceptions and whether they should carry extra information, like error messages.

The exercises 5.1 to 5.3 refer to code defined on slides 30 to 32 on the slide deck from lecture 5 about finite trees. You need to look there for the definition of 'a BinTree and in-order traversal.

Exercise 5.4, 5.5 and 5.6 refer to the slides from the same slide deck, lecture 5, starting with slide 17.

## Exercise 5.1 Consider the definition of type 'a BinTree on slide 30. Write a function

```
inOrder:'a BinTree ->'a list
```

that makes an in-order traversal of the tree and collect the elements in a result list. In-order traversal is defined on slide 32.

With the value intBinTree defined on slide 30

```
let intBinTree =
   Node(43, Node(25, Node(56, Leaf, Leaf), Leaf),
        Node(562, Leaf, Node(78, Leaf, Leaf)))
```

# we get the following:

```
> inOrder intBinTree;;
val it : int list = [56; 25; 43; 562; 78]
```

#### Exercise 5.2 Write a function

```
mapInOrder: ('a -> 'b) -> 'a BinTree -> 'b BinTree
```

that makes an in-order traversal of the binary tree and apply the function on all nodes in the tree.

With the value intBinTree

```
let intBinTree =
   Node(43, Node(25, Node(56, Leaf, Leaf), Leaf),
        Node(562, Leaf, Node(78, Leaf, Leaf)))
```

we can do the following example:

```
> mapInOrder (fun x -> x+1) intBinTree;;
val it : int BinTree =
  Node
     (44,Node (26,Node (57,Leaf,Leaf),Leaf),
          Node (563,Leaf,Node (79,Leaf,Leaf)))
```

Can you give an example of why mapInOrder might give a result different from mapPostOrder, but the result tree retruned in both cases is still the same.

#### Exercise 5.3 Write a function

```
foldInOrder : ('a -> 'b -> 'b) -> 'b -> 'a BinTree -> 'b
```

that makes an in-order traversal of the tree and folds over the elements.

For instance, given the tree

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**Exercise 5.4** Complete the program skeleton for the interpreter presented on slide 28 in the slide deck from the lecture 5 about finite trees.

The declaration for the abstract syntax for arithmetic expressions follows the grammar (slide 23):

The declaration of the abstract syntax for boolean expressions is defined as follows (slide 25).

The conjunction of two boolean values returns true if both values are true.

The abstract syntax for the statements are defined as below (slide 26):

Define 5 examples and evaluate them.

For instance, consider the example stmt0 and initial state state0 below.

```
let stmt0 = Ass("res", (Add(N 10, N 30)))
let state0 = Map.empty
```

You can then run the example as follows

```
> I stmt0 state0;;
val it : Map<string,int> = map [("res", 40)]
```

and get the result state with variable res assigned the value 40 (as expected).

**Exercise 5.5** Extend the abstract syntax and the interpreter with *if-then* and *repeat-until* statements.

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Again we refer to slide 28 in the slide deck from the lecture 5.

Hint: The if-then statement is similar to the if-then-else statement when you do a Skip statement in the else branch.

Hint: Slide 29 provides an example of running the fac example program with a state mapping x to 4.

**Exercise 5.6** Suppose that an *expression* of the form inc(x) is added to the abstract syntax. It adds one to the value of x in the current state, and the value of the expression is this new value of x. The expression inc(x) should be added to the type aExp.

How would you refine the interpreter to cope with this construct?

Again we refer to slide 28 in the slide deck from the lecture 5

Hint: Adding inc(x) to aExp, means that evaluating an expression may also update the state. Hense the state must be returned which has a rippling effect on the evaluation functions.

This task is only to describe how you would solve the task. There is no code to hand-in.