Exo 4

1) Si A, BE Mn (TR) alovs det AB = de+A de+B

A inversible (>> det A +0

Binversible (>> det B +0

A, Binversible => detA +0 => det AB = detA detB +0
detB +0

$$(AB)^{-1} = B^{-1}A^{-1} cov \qquad (B^{-1}A^{-1}) AB = B^{-1}(A^{-1}A)B$$

$$= B^{-1} I_{\eta} B$$

$$= B^{-1} B$$

$$= I_{\eta}$$

de même AB(B'A') = In

2/ 
$$\forall A,B \in M_n(R)$$
  
on a que  ${}^{\dagger}(AB) = {}^{\dagger}B^{\dagger}A \Rightarrow T_n = {}^{\dagger}T_n = {}^{\dagger}(AA^{-1}) = {}^{\dagger}(A^{-1})^{\dagger}A$   
 $\Rightarrow ({}^{\dagger}A)^{-1} = {}^{\dagger}(A^{-1})$ 

Ex05/

1/ det M = 8  
= 
$$-(\sqrt{3}-1)(\sqrt{3}+1) 2 + (2\sqrt{3})^2$$
  
=  $-2(3-1) + 4 \times 3 = 12-4$ 

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$$M^3 = 8 I_n$$
 a venfer

3/ 
$$M^3 = 8I_n \Rightarrow M M^2 = 8I_n$$
  
 $\Rightarrow M(\frac{1}{8}M^2) = I_n$   
 $\Rightarrow M^{-1} = \frac{1}{8}M^2$ 

olet 
$$\begin{pmatrix} 2 & 3 & 6 \\ 4 & -1 & 1 \\ 6 & 2 & 7 \end{pmatrix} = 0 \Rightarrow pas inversible  $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$  perp aux colormes  $\Rightarrow lm A c \{x+y-z=0\}$$$

## Pivot de Gomss pour trouver son inverse