Exo 1

Quels sont les ss espaces du

R - 0 {0} sest tits nn ss espace!

- TR l'espace thentier aussi

S. Ectte est ss espace vectoriel

dim E = ??

Rappels

Soit
$$f \in -\infty \mathbb{R}$$
 whe application lineary alovs $f^{-1}(\{0\}) = \{0\}$, $f(x) = 0\}$ est as ex

1) $ext{0} = f^{-1}(\{0\})$ can $f(0) = 0$

11) Soient $ext{0}$, $ext{0} = f(x) = f(y) = 0$

Alove $f(x) + f(y) = f(x) + f(y)$ can $f(x) = 0$

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111) rett x = Fin F2 similaire à venfer Exo 2

II
$$f(x,y,z) \rightarrow x+y-7z$$
 app infaire
 $E_1 = f^{-1}(3 \circ 3) \Rightarrow ss$ esp vectoriel

21
$$E_2$$
 n'est pas
 $(0,6,0) \notin E_2$ $4 \times 0 + 5\pi - 0 = 0 \neq 1$

41
$$E_4 = F_1 n F$$
 $F_1 = \{ x + y - 7z = 0 \}$
 $F = \{ x - y = 0 \} = g^{-1} \{ \{ 0 \} \}$
 $g(x, y, z) = x - z$

51 Es non
Verifier que
$$(1,-1,0) \in E_5$$
 et ??
 $(1,1,0) \in E_5$

Exo 3 $V=\{\{\}\}$ by $\{\}$ mes $\{\}$ degree $\{\}$ of $\{\}$ $\{\}$ $\{\}$ $\{\}$ $\{\}$ of $\{\}$ $\{\}$ of $\{\}$

Exo4

1/ Montrer que $P \mapsto P(z)$ est app linéalite

2/ Montrer que $P \mapsto P(z)$ est app linéalite

3/ Montrer que $z \in F_3$ et foure le produit $z \in F_3$ $z \in F_3$

4) Montrer que si f,g E -> TR Inéquire alors f+g est linéaire aussi Prendre f,q dams 1/,2/ ci dessus

5/ Fo n'est pas lineaire justifier

$$(z H_6 \rightarrow C_2 H_4 + H_2)$$

Faisons une table

	C	b	C
	C2H6	Cz H4	Hz
С	Z	2	0
H	Ľ	4	2

systēme linēaire

2a = 2b

6a = 4b + 2C

$$6a = 4a + 2C \Rightarrow 2a = 2c \Rightarrow q = C$$
substitution $q = c$

$$a NO_2 + b H_2O = c HNO_3 + d NO$$

_	NOz	H20	H NO3	No	_
N	I	0	I	1	
0	2	1	3	1	
H	٥	2	1	0	

systēme linēaire a = c +d

2a+b=3c+d

2b = c

=>
$$a = 3b$$
 $d = b$
 $c = 2b$

$$3NO_2 + H_2O = 2HNO_3 + NO$$