Exol

Quels sont les ss espaces du

R - 0 for est tits un ss espace!

- TR l'espace thentier aussi

Si Ectin est ss espace vectoriel

dim E = ??

dim E = ! > droite qui passe par 0

2 > plan

> 3 > hyperplan

Rappels

Soit
$$f \in -\infty \mathbb{R}$$
 whe application lineary alovs $f^{-1}(\{0\}) = \{0\}$, $f(x) = 0\}$ est as ex

1) $ext{0} = f^{-1}(\{0\})$ can $f(0) = 0$

11) Soient $ext{0}$, $ext{0} = f(x) = f(y) = 0$

Alove $f(x) + f(y) = f(x) + f(y)$ can $f(x) = 0$

11) Soient $ext{0} = 0$

11) Soient $ext{0} = 0$

11) Soient $ext{0} = 0$

11) $ext{0} = 0$

Alore $ext{0} = 0$

2) $ext{0} = 0$

Alore $ext{0} = 0$

3) $ext{0} = 0$

Alore $ext{0} = 0$

5) $ext{0} = 0$

Soient $ext{0} = 0$

11) $ext{0} = 0$

12) $ext{0} = 0$

13) $ext{0} = 0$

14) $ext{0} = 0$

15) $ext{0} = 0$

16) $ext{0} = 0$

17) $ext{0} = 0$

18) $ext{0} = 0$

19) $ext{0} = 0$

10) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

12) $ext{0} = 0$

13) $ext{0} = 0$

14) $ext{0} = 0$

15) $ext{0} = 0$

16) $ext{0} = 0$

17) $ext{0} = 0$

18) $ext{0} = 0$

19) $ext{0} = 0$

10) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

12) $ext{0} = 0$

13) $ext{0} = 0$

14) $ext{0} = 0$

15) $ext{0} = 0$

16) $ext{0} = 0$

17) $ext{0} = 0$

18) $ext{0} = 0$

19) $ext{0} = 0$

10) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

12) $ext{0} = 0$

13) $ext{0} = 0$

14) $ext{0} = 0$

15) $ext{0} = 0$

16) $ext{0} = 0$

17) $ext{0} = 0$

18) $ext{0} = 0$

19) $ext{0} = 0$

10) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

12) $ext{0} = 0$

12) $ext{0} = 0$

13) $ext{0} = 0$

14) $ext{0} = 0$

15) $ext{0} = 0$

16) $ext{0} = 0$

17) $ext{0} = 0$

18) $ext{0} = 0$

19) $ext{0} = 0$

10) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

12) $ext{0} = 0$

12) $ext{0} = 0$

13) $ext{0} = 0$

14) $ext{0} = 0$

15) $ext{0} = 0$

16) $ext{0} = 0$

17) $ext{0} = 0$

18) $ext{0} = 0$

19) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

12) $ext{0} = 0$

13) $ext{0} = 0$

14) $ext{0} = 0$

15) $ext{0} = 0$

17) $ext{0} = 0$

18) $ext{0} = 0$

19) $ext{0} = 0$

19) $ext{0} = 0$

10) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

11) $ext{0} = 0$

12) $ext{0} = 0$

111) rett x = Fin F2 similaire à venfer Exo 2

II
$$f(x,y,z) \rightarrow x+y-7z$$
 app infaire
 $E_1 = f^{-1}(3 \circ 3) \Rightarrow ss$ esp vectoriel

21
$$E_2$$
 n'est pas
 $(0,6,0) \notin E_2$ $4 \times 0 + 5\pi - 0 = 0 \neq 1$

41
$$E_4 = F_1 n F$$
 $F_1 = \{ x + y - 7z = 0 \}$
 $F = \{ x - y = 0 \} = g^{-1} \{ \{ 0 \} \}$
 $g(x, y, z) = x - z$

51 Es non
Verifier que
$$(1,-1,0) \in E_5$$
 et ??
 $(1,1,0) \in E_5$

Exo 3
$$V = \{ \}$$
 polynomes degré $\{ \} \}$
= $\{ \sum_{n=1}^{n} a_n X^n, a_n \in \mathbb{R} \}$

Ex polynômes de degrē = 1

$$P(X) = a \times +b \qquad Q(X) = c \times +d \qquad \lambda \in \mathbb{R}$$

$$III \qquad (P+Q)(X) = (a+b)X + (c+d) \Rightarrow deg \leq 1$$

$$= 0 \quad SI \quad a+b=0$$

$$IIII \qquad (\lambda P)(X) = (\lambda a)X + (\lambda b) \Rightarrow deg \leq 1$$

$$= 0 \quad SI \quad \lambda a = 0$$

1)
$$0_V = \sum_{s=0}^{d} X'$$

11) Soient $P(X) = \sum_{s=0}^{d} a_s X'$
 $Q(X) = \sum_{s=0}^{d} b_s X'$
 $M(X) = \sum_{s=0}^{d} b_s X'$
 $M(X) = \sum_{s=0}^{d} b_s X'$
 $M(X) = \sum_{s=0}^{d} a_s X'$

```
1) Montrer que P+>P(z) est app linéalite

2) Montrer que P+>P(z) est app linéalite

3) Montrer que 26F3 et faire le produit

3(-2 eF3)

4) Montrer que si f,g E -> TR |inéalite

alors f+g est linéalite aussi

Prendre fig clams 1/,2/ ci dessus
```

5/ Fo n'est pas lineaire justifier

$$(z H_6 \rightarrow C_2 H_4 + H_2)$$

Faisons une table

	CL	b	C
	C2 H6	Cz H4	Hz
С	Z	2	0
H	C	4	2

systēme Iinēaire

$$2a = 2b$$

$$6a = 4b + 2c$$

$$6a = 4a + 2C \Rightarrow 2a = 2c \Rightarrow q = C$$
Substitution $q = b$

$$a NO_2 + b H_2O = c HNO_3 + d NO$$

_	NO_2	H20	H NO3	No	
N	1	0	1	1	
0	2	1	3	1	
H	Ď	2	1	0	

système linéaire a = c +d

$$2b = c$$

=>
$$a = 3b$$
 $d = b$
 $c = 2b$

$$3NO_2 + H_2O = 2HNO_3 + NO$$

Exo 6 cont

Fe₇ S_{δ} + O_z \rightarrow Fe₃ O_4 + S O_2 3 Fe₇ S_{δ} + 38 O_z = 7 Fe₃ O_4 + 245 O_z Trouver le système lineante et verifier