

14-7b

DC Circuits

Ohm's Law

$$V = IR$$

44.22

Resistors in Series:

$$R_S = R_1 + R_2 + \dots + R_n$$

44 4

Resistors in Parallel:

$$R_P = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}}$$

44.5

Equivalent resistance of two resistors in parallel:

$$R_P = \frac{R_1 R_2}{R_1 + R_2}$$

44.6

Resistive Power

$$P = VI = \frac{V^2}{R} = I^2 R$$

44.7

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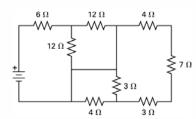
Direct Current Electricity

14-7c

DC Circuits

Example (FEIM):

What is the resistance of the following circuit as seen from the battery?



No current will flow through the two 4 Ω resistors, the two 3 Ω resistors, or the 7 Ω resistor. The circuit reduces to one 6 Ω in series with two 12 Ω in parallel.

 $R = 6 \Omega + 6 \Omega = 12 \Omega$

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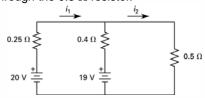
Direct Current Electricity	14-7d
DC Circuits	
Kirchhoff's Laws	
Voltage Law (KVL)	
$\sum V_{ m rises} = \sum V_{ m drops}$ [closed path] 44.24	
Current Law (KCL)	
$\sum I_{\rm in} = \sum I_{\rm out}$ [closed surface] 44.23	
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Direct Current Electricity DC Circuits Loop Current Circuit Analysis 1. Select one less than the total number of loops. 2. Write Kirchhoff's voltage equation for each loop. 3. Use the simultaneous equations to solve for the current you want.

14-7f

DC Circuits
Example (FEIM):

Find the current through the 0.5 Ω resistor.



The voltage sources around the left loop are equal to the voltage drops across the resistances.

20 V - 19 V = 0.25
$$\Omega$$
 i_1 + 0.4 Ω $(i_1 - i_2)$

The same is true for the right loop.

19 V = 0.4
$$\Omega$$
 ($i_2 - i_1$) + 0.5 Ω i_2

Solve—two equations and two unknowns.

$$0.65 \Omega i_1 - 0.4 \Omega i_2 = 1 \text{ V}$$

$$-0.4 \Omega i_1 + 0.9 \Omega i_2 = 19 \text{ V}$$

$$i_1 = 20 \text{ A}$$

 $i_2 = 30 \text{ A}$

The current through the 0.5 Ω resistor is 30 A.

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14-7g

DC Circuits

Node Voltage Circuit Analysis

- 1. Convert all current sources to voltage sources.
- 2. Choose one node as reference (usually ground).
- 3. Identify unknown voltages at other nodes compared to reference.
- 4. Write Kirchhoff's current equation for all unknown nodes except reference node.
- 5. Write all currents in terms of voltage drops.
- 6. Write all voltage drops in terms of the node voltages.

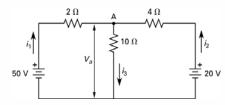
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14-7h

DC Circuits

Example (FEIM):

Find the voltage potential at point A and the current i_1 .



$$i_{1} + i_{2} = i_{3}$$

$$\frac{50 \text{ V} - V_{A}}{2 \Omega} + \frac{20 \text{ V} - V_{A}}{4 \Omega} = \frac{V_{A} - 0}{10 \Omega}$$

$$V_{A} = 35.3 \text{ V}$$

$$i_{1} = \frac{50 \text{ V} - V_{A}}{2 \Omega} = \frac{50 \text{ V} - 35.3 \text{ V}}{2 \Omega}$$

$$= 7.35 \text{ A}$$

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14-8a

Voltage Divider

The voltage across a resistor R in a loop with total resistance R_{total} with a voltage source V is

$$V_R = \frac{R}{R_{\text{total}}} V$$

In the general case, the voltage on impedance Z_i in a loop with total impedance Z_{total} with a voltage source v is

$$V_i = \frac{Z_i}{Z_{\text{total}}} v$$

NOTE: Each symbol is a complex number in the general case.

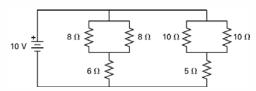
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14-8b

Voltage Divider

Example (FEIM):

What is the voltage across the 6 Ω resistor?



- (A) 5 V
- (B) 6 V
- (C) 8 V
- (D) 10 V

Two 8 Ω resistors in parallel equal 4 Ω .

The voltage across the 6 Ω resistor is

$$(10 \text{ V}) \left(\frac{6 \Omega}{6 \Omega + 4 \Omega} \right) = 6 \text{ V}$$

Therefore, the answer is (B).

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14-9a

Current Divider

The current through a resistor R in parallel with another resistance R_{parallel} and a current into the node of I is:

$$I_{\scriptscriptstyle R} = \frac{R_{\scriptscriptstyle \text{parallel}}}{R_{\scriptscriptstyle \text{total}}} \ I \quad \text{(Resistance R does not appear explicitly. $R_{\scriptscriptstyle \text{total}}$}$$
 is the sum of the resistances in parallel.)

In the general case, the current through impedance Z_i connected to a node in parallel with total impedance Z_{total} with a current i into the node is:

$$i_{z_i} = \frac{Z_{\text{parallel}}}{Z_{\text{total}}} i$$
 (Z_{total} is the sum of the impedances in parallel.)

NOTE: Each symbol is a complex number in the general case.

Procedure:

- 1. Identify the component you want the current through.
- 2. Simplify the circuit.
- 3. Determine the current into the node that is connected to the component of interest.
- 4. Allocate current in proportion to the reciprocal of resistance.

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14-9b

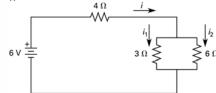
Current Divider

Example (FEIM):

What is the current through the 6 Ω resistor?

- (A) 1/10 A
- (B) 1/3 A
- (C) 1/2 A
- (D) 1 A

$$i = i_1 + i_2$$



Simplify the circuit.

3 Ω in parallel with 6 Ω = 2 Ω

2 Ω in series with 4 Ω = 6 Ω

$$i = \frac{6 \text{ V}}{6 \Omega} = 1 \text{ A}$$

$$R_{\text{parallel}} = 3 \ \Omega$$

$$R_{\text{total}} = 3 \Omega + 6 \Omega = 9 \Omega$$

$$i = (1 \text{ A}) \left(\frac{3 \Omega}{3 \Omega + 6 \Omega} \right) = 1/3 \text{ A}$$

Therefore, the answer is (B).

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14-10a

Superposition Theorem

The net current/voltage is the sum of the current/voltage caused by each current/voltage source.

Procedure:

- 1. Short all voltage sources, and open all current sources, then turn on only one source at a time.
- 2. Simplify the circuit to get the current/voltage of interest.
- 3. Repeat until all sources have been used.
- 4. Add the results for the answer.

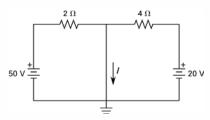
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14-10b

Superposition Theorem

Example (FEIM):

Determine the current through the center leg of the circuit.



Short the 20 V source. $I = 50 \frac{V}{2} \Omega = 25 \text{ A}$

Short the 50 V source. $I = 20 \frac{V}{4} \Omega = 5 \text{ A}$

$$I_{\text{total}} = 25 \text{ A} + 5 \text{ A} = 30 \text{ A}$$

-

14-11b

Norton Equivalent

Example (FEIM):

Find the Norton equivalent current and resistance of the circuit as seen by the 10 Ω resistor.



With the 10 Ω resistor open circuited, and the voltage sources shorted, the circuit is 4.0 Ω and 2.0 Ω in parallel.

$$R_{\rm N} = (2\,\Omega) \left(\frac{4\,\Omega}{2\,\Omega + 4\,\Omega} \right) = 1.33\,\Omega$$

With the 10 Ω resistor shorted, the circuit looks just like the previous example.

$$I_{\rm N} = 30 {\rm A}$$

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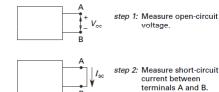
FER

Direct Current Electricity

14-12a

Thevenin Equivalent

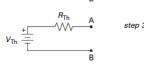
Figure 44.3 Thevenin Equivalent Circuit





$$R_{\rm N}=R_{\rm Th}$$
 44.3
 $V_{\rm Th}=I_{\rm N}R_{\rm N}$ 44.3

$$I_{\rm N} = \frac{V_{\rm Th}}{R_{\rm Th}}$$
 44.40



step 3: Draw the Thevenin equivalent.
$$R_{Th} = R_{eq}$$

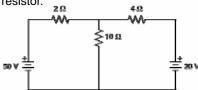
$$V_{Th} = V_{-1}$$

14-12b

Thevenin Equivalent

Example (FEIM):

Find the Thevenin equivalent voltage and resistance of the circuit as seen by the 10 Ω resistor.



The Thevenin resistance is the same as the Norton resistance in the previous example, which is 1.3 Ω . With the 10 Ω resistor open-circuited, apply the Kirchhoff voltage law around the loop and find V_{TH} = 40 V.

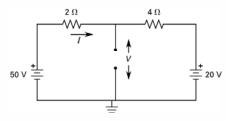
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14-12c

Thevenin Equivalent



$$(50 \text{ V} - 20 \text{ V}) = I(2 \Omega + 4 \Omega)$$

$$I = 5 \text{ A}$$

$$V = 50 \text{ V} - I(2 \Omega)$$

$$= 50 \text{ V} - (5 \text{ A})(2 \Omega)$$

$$= 40 \text{ V}$$

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14-13a

Capacitors

$$q_C(t) = C v_C(t)$$

$$C = \frac{q_C(t)}{v_C(t)} \quad \text{[varying } v(t) \text{]}$$

$$\textbf{44.9}$$

energy =
$$\frac{Cv_C^2}{2} = \frac{q_C^2}{2C}$$
$$= \frac{q_Cv_C}{2}$$
 44.13

Parallel Plate Capacitors

$$C = \frac{\epsilon A}{d}$$
 44.10

• Capacitance in Parallel:

$$C_P = C_1 + C_2 + \dots + C_n$$
 44.19

• Capacitance in Series:

$$C_S = \frac{1}{\frac{1}{C_1} + \frac{1}{C_2} + \dots + \frac{1}{C_n}}$$
 44.18

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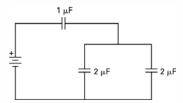
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14-13b

Capacitors

Example 1 (FEIM):

What is the capacitance seen by the battery?



The two 2 μF capacitors in parallel are equivalent to 4 μF . The 1 μF capacitor in series with the equivalent 4 μF capacitance will add as resistors in parallel.

$$C = \frac{C_1 C_2}{C_1 + C_2}$$
$$= \frac{(1 \mu F)(1 \mu F)}{1 \mu F + 4 \mu F}$$
$$= 4/5 \mu F$$

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14-13c

Capacitors

Example 2 (FEIM):

A 10 μF capacitor has been connected to a potential source of 150 V. The energy stored in the capacitor in 10 time constants is most nearly

- (A) $1.0 \times 10^{-7} \text{ J}$
- (B) 9.0 x 10⁻³ J
- (C) 1.1 x 10⁻¹ J
- (D) $9.0 \times 10^{1} J$

Energy =
$$\frac{(10 \times 10^{-6} \text{ F})(150 \text{ V})^2}{2}$$

$$= 0.11 \text{ J} (1.1 \times 10^{-1} \text{ J})$$

Therefore, the answer is (C).

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14-14a

Inductors

$$u = \frac{N\phi}{i\tau}$$
 44.

$$v_L(t) = L \frac{di_L}{dt}$$
 44.15

$$i_L(t) = i_L(0) + \frac{1}{L} \int_0^{t_0} v_L(t) dt$$
 44.16

- Inductance in Series:
 - $L_S = L_1 + L_2 + \dots + L_n$ 44.20
- Inductance in Parallel:

$$L_P = \frac{1}{\frac{1}{L_1} + \frac{1}{L_2} + \dots + \frac{1}{L_n}}$$
 44.21

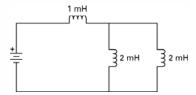
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14-14b

Inductors

Example (FEIM):

Find the inductance as seen from the battery.



The two 2 mH inductors in parallel will add as resistors in parallel.

$$L = \frac{L_1 L_2}{L_1 + L_2} = \frac{(2 \text{ mH})(2 \text{ mH})}{2 \text{ mH} + 2 \text{ mH}} = 1 \text{ mH}$$

The 1 mH inductor in series with the equivalent 1 mH inductance will combine for 2 mH total inductance.

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Direct Current Electricity RC Transients Figure 44.5 RC Transient Circuit $v_C(t) = v_C(0)e^{-t/RC} + V(1 - e^{-t/RC})$ (a) series-RC, discharging (energy source(s) disconnected) $v_C(t) = v_C(0)e^{-t/RC} + V(1 - e^{-t/RC})$ $v_C(t) = v_C(0)e^{-t/RC} +$

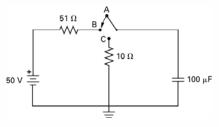
14-15b

RC Transients

Example (FEIM):

At t = 0, the capacitor is discharged, and the switch is moved from A to B. At t = 6 s, the switch is moved to C.

- (a) What is the capacitor voltage at t = 6 s?
- (b) What is the current at t = 10 s?
- (c) When (after 6 s) is the voltage across the capacitor equal to 10 V?



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14-15c

RC Transients

(a) From time = 0 to 6 s,

$$V_c\left(0\right)=0$$

$$V = 50 \text{ V}$$

 $RC = (51 \times 10^3 \Omega)(100 \times 10^{-6} \text{ F}) = 5.1 \text{ s}$

$$v_c(6 \text{ s}) = 0e^{-\frac{6 \text{ s}}{5.1 \text{ s}}} + 50 \text{ V} \left(1 - e^{-\frac{6 \text{ s}}{5.1 \text{ s}}}\right) = 34.58 \text{ V}$$

So 34.58 V is the peak voltage the capacitor reaches before it starts to discharge.

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14-15d

RC Transients

(b) From time = 6 s on,
$$V_c$$
 (6 s) = 34.58 V

$$V = 0 V$$

$$RC = (10 \times 10^3 \Omega)(100 \times 10^{-6} \text{ F}) = 1 \text{ s}$$

$$i(10 \text{ s}) = \left(\frac{0 - 34.58 \text{ V}}{10 \times 10^3 \Omega}\right) e^{-\frac{10 \text{ s} - 6 \text{ s}}{1}} = -6.3 \times 10^{-6} \text{ A}$$

(c)
$$V_c(t) = 34.58 \text{ Ve}^{-\frac{t-6 \text{ s}}{1 \text{ s}}} + 0 \left(1 - e^{-\frac{t-6 \text{ s}}{1 \text{ s}}}\right) = 10 \text{ V}$$

Take the natural logarithm of both sides of the equation

$$ln34.58 \ V \ e^{-(t-6s)} = ln10$$

$$ln e^{-(t-6s)} + ln 34.58 V = ln 10$$

$$-(t-6 s) = ln10 - ln34.58 V$$

$$t - 6 s = 1.24 s$$

$$t = 7.24 \text{ s}$$

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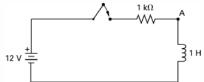
14-16a **Direct Current Electricity RL Transients** Figure 44.6 RL Transient Circuit i(t) $v_R(t) = i(t)R$ $= i(0)Re^{-Rt/L} + V(1 - e^{-Rt/L})$ 44.48 $i(t) = i(0)e^{-Rt/L} + \frac{V}{R}(1 - e^{-Rt/L})$ t = 044.49 (a) series-RL, discharging (energy source(s) disconnected) $= -i(0)Re^{-Rt/L} + Ve^{-Rt/L}$ 44.50 (b) series-RL, charging (energy source(s) connected)

14-16b

RL Transients

Example (FEIM):

Find the voltage at point A at the instant the switch is closed. The switch has been open for a long time, and there is no initial current in the inductor.



- (A) 0 V
- (B) 1 V
- (C) 3 V
- (D) 12 V

$$i(0) = 0$$

$$V = 12 \text{ V}$$
, so at $t = 0$

$$v_L(0^+) = 0Re^0 + (12 \text{ V})e^0 = 12 \text{ V}$$

Therefore, the answer is (D).

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14-17

Transducers

A transducer is any device used to convert a physical phenomenon into an electrical signal (e.g., microphone, thermocouple, and voltmeter).

Characteristics of measurement design:

- Sensitivity
- Linearity
- Accuracy
- Precision
- Stability

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14-18a

Resistance Temperature Detectors (RTDs)

Make use of changes in their resistance to determine the changes in temperature.

$$R_T = R_0 (1 + \alpha (T - T_0))$$
 49.3

Example (FEIM):

A resistance temperature detector (RTD) that is not perfectly linear is used for a temperature measurement. The temperature coefficient is $3.900\times10^{-30}C^{-1}$, the reference temperature is $0^{\circ}C$, and the reference resistance is $500.0~\Omega$. The resistance measured when the actual temperature is $400^{\circ}C$ is $1247~\Omega$. Determine the error in the temperature measurement.

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14-18b

Resistance Temperature Detectors (RTDs)

If the RTD was perfectly linear the resistance would be given by

$$R_T = R_0 \left(1 + \alpha (T - T_0) \right)$$

However, the temperature that the RTD indicates is not the actual temperature of 400° C, so rearranging the RTD equation to solve for the temperature that the RTD indicates yields

$$T = \frac{R_{\tau} - R_{0} + \alpha R_{0}T_{0}}{\alpha R_{0}}$$

$$= \frac{1247 \ \Omega - 500.0 \ \Omega + (3.900 \times 10^{-3} \ ^{\circ}\text{C}^{-1})(500 \ ^{\circ}\text{C})(0 \ ^{\circ}\text{C})}{(3.900 \times 10^{-3} \ ^{\circ}\text{C}^{-1})(500 \ ^{\circ}\Omega)}$$

$$= 383.1 \ ^{\circ}\text{C}$$

000.1 0

The error in the measurement is: Error = $383.1^{\circ}\text{C} - 400^{\circ}\text{C} = -16.9^{\circ}\text{C}$

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14-19a

Strain Gages

Metal or semiconductor foils that change resistance linearly with the strain.

$$GF = \frac{\frac{\Delta R}{R}}{\frac{\Delta L}{L}} = \frac{\frac{\Delta R}{R}}{\epsilon}$$
49.6

Example (FEIM):

A strain gage is measured to determine the gage factor. A strain gage with an initial resistance of 200.00 Ω and final resistance of 199.79 Ω when subjected to a strain that causes the gage to compress to 0.9994 cm. The initial length of the gage was 1.0000 cm. What is the gage factor?

(A) 0.15

(B) 0.42

(C) 1.8

(D) 4.0

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14-19b

Strain Gages

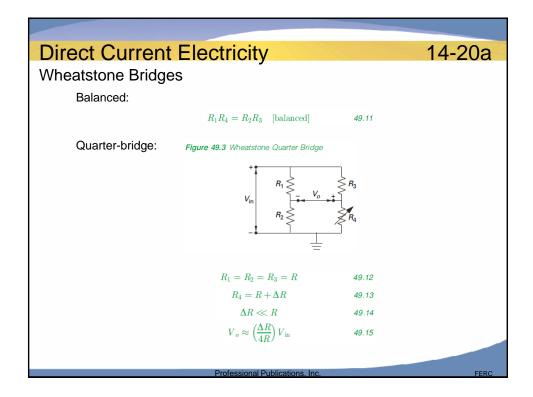
$$\mathsf{GF} = \frac{\frac{\Delta R}{R}}{\frac{\Delta L}{L}}$$

$$= \frac{\frac{199.79\,\Omega - 200.00\,\Omega}{200.00\,\Omega}}{\frac{200.00\,\Omega}{0.9994\,\text{cm} - 1.0000\,\text{cm}}}$$

= 1.75

Therefore, the answer is (C).

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14-20b

Wheatstone Bridges

Example (FEIM):

There are three high-precision resistors known to be 10.00 k Ω in a quarter bridge circuit. R_1 is a sensor with a small resistance difference from 10 k Ω . Find the resistance if $V_{\rm in} = 5.00$ V and $V_{\rm o} = 0.03$ V.

$$\Delta R = \frac{4RV_o}{V_{in}}$$

$$= \frac{(4)(10.00 \text{ k}\Omega)(0.03 \text{ V})}{5.00 \text{ V}}$$

$$= 0.24 \text{ k}\Omega$$

$$R_1 = 10.00 \text{ k}\Omega + 0.24 \Omega = 10.24 \text{ k}\Omega$$

For the strain gage quarter-bridge circuit, ΔR can be substituted.

$$V_o = \frac{1}{4} (GF) \epsilon V_{in}$$

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14-21a

Sampling

Sampling Rate or Frequency:

$$f_s = \frac{1}{\Delta t}$$

49.16

Shannon's Sampling Theorem

Determines the sampling rate to reproduce accurately in the discrete time system.

Nyquist Rate:

$$f_N = 2f_I$$

(where f_I is the frequency of interest)

Reproducible Sampling:

$$f_s > f_n$$
 [reproducible sampling]

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14-21b

Sampling

Example (FEIM):

An analog signal is to be sampled at 0.03 μs intervals. What is most nearly the highest frequency that can be accurately reproduced?

- (A) $4.0 \times 10^6 \text{ Hz}$
- (B) $12 \times 10^6 \text{ Hz}$
- (C) 16 × 10⁶ Hz
- (D) 18 × 10⁶ Hz

The sampling frequency is

$$f_{s} = \frac{1}{\Delta t} = \frac{1}{0.03 \times 10^{-6}}$$

$$= 33 \times 10^6 \text{ Hz}$$

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Sampling

The sampling frequency must be greater than the Nyquist rate for accurate reproduction.

$$f_{\rm s} > 2f_{\rm M}$$

The greatest frequency that can be reproduced at this sampling rate is

$$f_{N} < \frac{f_{s}}{2} = \frac{33 \times 10^{6} \text{ Hz}}{2} = 16.7 \times 10^{6} \text{ Hz}$$
 (16×10⁶ Hz)

Therefore, the answer is (C).

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14-22a

Analog-to-Digital Conversion

Voltage Resolution

The range from a high voltage, V_H , and a low voltage, V_L , is divided up into the 2^n ranges.

$$\epsilon_V = \frac{V_H - V_L}{2^n}$$
 49.19

For example, if all the bits are "1" then the analog value is somewhere between V_H and $V_H - \varepsilon_V$. To calculate the analog value from the digital value use

$$V = \epsilon_V N + V_L \tag{49.20}$$

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14-22b

Analog-to-Digital Conversion

Example (FEIM):

A 16 bit analog-to-digital conversion has a resolution of 1.52588 \times 10⁻⁴ V and the lowest voltage measured has half the magnitude of the highest voltage. Both the high and low voltages are positive. Determine the highest voltage.

$$V_H - V_L = 2^n \varepsilon_v$$

= $(2)^{16} (1.52588 \times 10^{-4} \text{ V})$
= 10.0 V

The problem statement also says that

$$|V_{H}| = |2V_{L}|$$

Since V_H and V_L are positive, this equation becomes

$$V_H = 2V_I$$

Substituting into the first equation

$$2V_{L} - V_{L} = 10 \text{ V}$$

$$V_{L} = 10^{\circ} V$$

$$V_{H} = 20 \text{ V}$$

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14-23a

Measurement Uncertainty

Kline-McClintock Equation:

A method for estimating the uncertainty in a function that depends on more than one measurement.

$$w_{R} = \sqrt{\frac{\left(w_{1} \frac{\partial f}{\partial x_{1}}\right)^{2} + \left(w_{2} \frac{\partial f}{\partial x_{2}}\right)^{2}}{+ \dots + \left(w_{n} \frac{\partial f}{\partial x_{n}}\right)^{2}}}$$

$$49.21$$

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14-23b

Measurement Uncertainty

Example (FEIM):

A function is given by $R = 5x_1 - 3x_2^2$.

Find the measurement uncertainty at (1, 2) if the uncertainty in the variables is ± 0.01 and ± 0.03 respectively.

$$\frac{\partial R}{\partial x_1} = 5 \qquad \frac{\partial R}{\partial x_2} = -6x_2$$

At the point (1, 2) the partial derivatives are

$$\frac{\partial R}{\partial x_1}\Big|_{(1,2)} = 5$$
 $\frac{\partial R}{\partial x_2}\Big|_{(1,2)} = (-6)(2) = -12$

$$w_{R} = \sqrt{\left(w_{1}\frac{\partial R}{\partial x_{1}}\Big|_{(1,2)}\right)^{2} + \left(w_{2}\frac{\partial R}{\partial x_{2}}\Big|_{(1,2)}\right)^{2}}$$
$$= \sqrt{\left((0.01)(5)\right)^{2} + \left((0.03)(-12)\right)^{2}}$$
$$= 0.36$$

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14-23c

Measurement Uncertainty

If the function *R* is the sum of the measurements,

 $R = x_1 + x_2 + x_3 + \dots + x_n$, then the Kline-McClintock method reduces to

$$W_R = \sqrt{W_1^2 + W_2^2 + \dots + W_n^2}$$

This is called the root sum square (RSS) value.

If the function R is the sum of the measurements times constants, $R = a_1x_1 + a_2x_2 + a_3x_3 + \ldots + a_nx_n$, then the Kline-McClintock method reduces to

$$W_{R} = \sqrt{a_{1}^{2} w_{1}^{2} + a_{2}^{2} w_{2}^{2} + \dots + a_{n}^{2} w_{n}^{2}}$$

This is called a weighted RSS value.

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