

Data Management – AA 2019/20
Solutions for the exam of 11/06/2020

Problem 1

If S is a schedule on transactions T_1, \dots, T_n , then the *partial precedence graph* $\text{PPG}(S)$ associated to S is a graph that has the transactions in S as nodes, and has an edge from T_i to T_j if and only if S contains two actions of different types (i.e., one read and one write) $a_i(x)$ in T_i and $a_j(x)$ in T_j on the same element x such that $a_i(x)$ precedes (not necessarily directly) $a_j(x)$ in S . Also, the *write-on graph* $\text{WOG}(S)$ associated to S is a graph that has the transactions in S as nodes, and has an edge from T_i to T_j if and only if there is an x such that $w_j(x)$ is followed by $w_i(x)$ in S , and there is no write action on x in S between $w_j(x)$ and $w_i(x)$. Prove or disprove the following claims:

1. If both $\text{PPG}(S)$ and $\text{WOG}(S)$ are acyclic, then S is view-serializable.
2. If $\text{PPG}(S)$ is acyclic, and $\text{WOG}(S)$ has no edges, then S is conflict-serializable.

Solution to problem 1

1. The claim can be disproved, for instance, by means of the following counterexample S_1 :

$$r_1(x) w_2(x) w_2(y) w_1(y)$$

S_1 is not view-serializable and is such that both $\text{PPG}(S_1)$ and $\text{WOG}(S_1)$ are acyclic. Observe that this example shows that even though both $\text{PPG}(S_1)$ and $\text{WOG}(S_1)$ are acyclic, their union may contain a cycle. Now, it is easy to see that the union of the partial precedence graph associated to S and the write-on graph associated to S is a subset of the precedence graph associated to S . This implies that if the union of the two graphs contains a cycle, such cycle appears also in the precedence graph associated to S , and therefore S is not conflict-serializable, and can even be non view-serializable, as the counterexample S_1 shows.

2. The claim can be proved by showing that, in the case where $\text{WOG}(S)$ has no edges, the partial precedence graph $\text{PPG}(S)$ associated to S coincides with the precedence graph associated to S . In order to show this property, we observe the following for S :

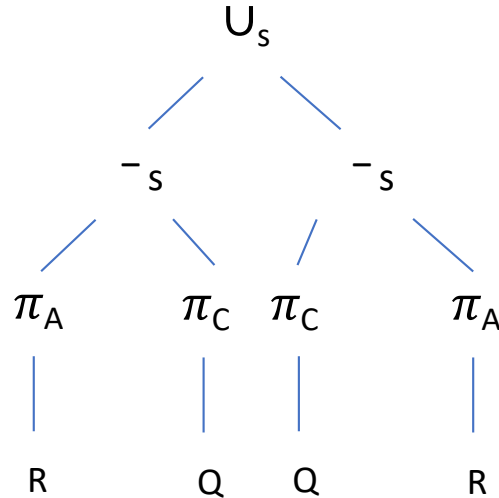
- It is immediate to note that $\text{PPG}(S)$ and the precedence graph associated to S have the same nodes.
- It is also immediate to see that the set of edges in $\text{PPG}(S)$ is a subset of the set of edges in the precedence graph associated to S .
- In the case where $\text{WOG}(S)$ has no edges, an edge from T_i to T_j exists in the precedence graph associated to S if and only if S contains two actions of different types (i.e., one read and one write) $a_i(x)$ in T_i and $a_j(x)$ in T_j on the same element x such that $a_i(x)$ precedes (not necessarily directly) $a_j(x)$ in S . This immediately implies that, if $\text{WOG}(S)$ has no edges, then every edge in the precedence graph associated to S is also an edge in $\text{PPG}(S)$.

Being $\text{PPG}(S)$ equal to the precedence graph associated to S , the acyclicity of $\text{PPG}(S)$ implies that S is conflict-serializable.

physical query plan you would choose for executing the query efficiently. Also, tell which is the cost (in terms of number of page accesses) of executing the query according to the chosen physical query plan.

Solution to problem 3

The logical query plan associated to the query, which is also the logical query plan chosen, is shown below.

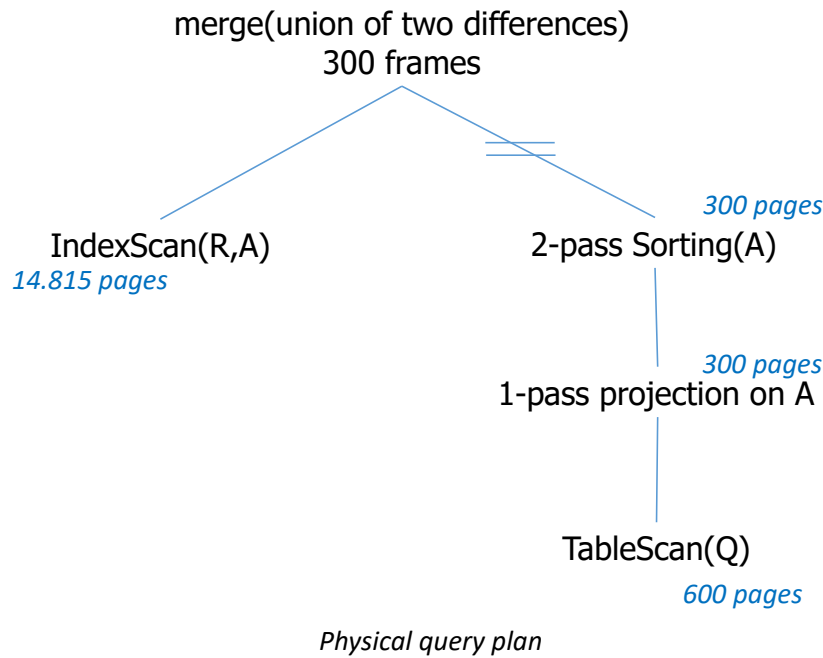


Logical query plan

If a page contains 20 tuples, each with 6 attributes, then it has space for 40 data entries. Taking into account the 67% rule, we know that each leaf contains 27 data entries. This means that the index has $400.000 / 27 = 14.815$ leaves.

To decide the physical query plan, we observe that what we have to compute is the set V_1 of values that are in $\pi_A(R)$ but not in $\pi_C(Q)$, union the set V_2 of values that are in $\pi_C(Q)$, but not in $\pi_A(R)$. Note that V_1 and V_2 are disjoint, and therefore we can ignore duplicate elimination during the union.

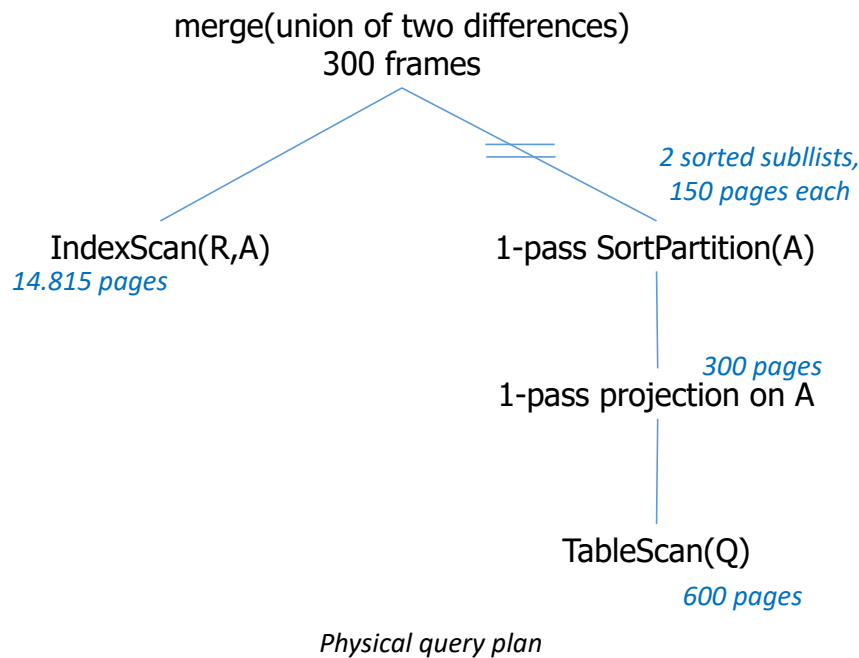
Observe that having the values of $\pi_A(R)$ sorted, and having the values of $\pi_C(Q)$ sorted would definitely help in computing the union of the two differences. Indeed, one could simply perform a kind of merge step, by scanning the sorted files, copying to the output both the values in $\pi_A(R)$ that are not in $\pi_C(Q)$, and the values in $\pi_C(Q)$ that are not in $\pi_A(R)$. Note also that the values in $\pi_A(R)$ already sorted are exactly in the leaves of the index. One could then decide to sort $\pi_C(Q)$ and then perform the merging step. However, this implies to sort the 300 pages of $\pi_C(Q)$ in two passes (since the buffer has 150 frames) and to materialize the results. The corresponding physical query plan is as follows:



The cost in terms of the number of page accesses is 14.815 (index scan) + 600 (reading of Q) + 900 (sorting of $\pi_C(Q)$) + 300 (reading of the sorted $\pi_C(Q)$) = 16.615.

We can actually do better, by avoiding the materialization step as follows. We produce the sorted sublists of $\pi_C(Q)$, sorted on the basis of C, in one pass (2 sorted sublists), and then we perform a merge step using only 4 buffer frames (1 for the leaves of the index, 2 for the sublists of $\pi_C(Q)$, and 1 for the output) for computing the result. In such a merge step, a value that is both in $\pi_A(R)$ and in $\pi_C(Q)$ is ignored, whilst all other values are copied to the output.

The physical query plan is as follows:



The cost in terms of the number of page accesses is 14.815 (index scan) + 600 (reading of Q) + 300 (writing of the sorted sublists of $\pi_C(Q)$) + 300 (reading of the sorted sublists of $\pi_C(Q)$) = 16.015.

Given the two relations $R_1(A,B,C)$ and $R_2(C,D)$, the following equivalences were intended to be used during the optimization of logical query plans involving R_1 and R_2 :

- For each of the above equivalences, prove or disprove, explaining your answer in details, that it is valid, and can indeed be used in query optimization. We remind the students that δ denotes duplicate elimination, π denotes projection (without duplicate eliminations) and \bowtie denotes natural join, i.e., the join of two relations based on equality on common attributes.

1. This equivalence is valid. To show validity, we will prove that, for any R_1 (set or bag) and R_2 (set or bag), (i) $t \in \delta(R_1 \bowtie R_2)$ implies $t \in \delta(R_1) \bowtie \delta(R_2)$, and (ii) $t \in \delta(R_1) \bowtie \delta(R_2)$ implies $t \in \delta(R_1 \bowtie R_2)$.
 - (i) If a tuple $\langle x_1, x_2, x_3, x_4 \rangle$ is in $\delta(R_1 \bowtie R_2)$, then at least one occurrence of $\langle x_1, x_2, x_3, x_4 \rangle$ is in $R_1 \bowtie R_2$. By definition of natural join, we know that there exist $\langle x_1, x_2, x_3 \rangle \in R_1$, and $\langle x_3, x_4 \rangle \in R_2$. This in turn implies that there exist at least one occurrence of the tuple $\langle x_1, x_2, x_3 \rangle$ in $\delta(R_1)$ and one occurrence of the tuple $\langle x_3, x_4 \rangle$ in $\delta(R_2)$, and therefore $\langle x_1, x_2, x_3, x_4 \rangle \in \delta(R_1) \bowtie \delta(R_2)$.
 - (ii) Consider a tuple $\langle x_1, x_2, x_3, x_4 \rangle \in \delta(R_1) \bowtie \delta(R_2)$; by definition of natural join, we know that there exist $\langle x_1, x_2, x_3 \rangle \in \delta(R_1)$, and $\langle x_3, x_4 \rangle \in \delta(R_2)$, which implies that there exist at least one occurrence of the tuple $\langle x_1, x_2, x_3 \rangle$ in R_1 , and at least one occurrence of the tuple $\langle x_3, x_4 \rangle$ in R_2 . This in turn implies that at least one occurrence of $\langle x_1, x_2, x_3, x_4 \rangle$ is in $R_1 \bowtie R_2$, and therefore $\langle x_1, x_2, x_3, x_4 \rangle \in \delta(R_1 \bowtie R_2)$.
2. Clearly, this equivalence is not valid, as shown by the following counterexample: $R_1(A, B, C) = \{\langle a, b, c \rangle\}$, $R_2(C, D) = \{\langle c, d_1 \rangle, \langle c, d_2 \rangle\}$, for which we have $R_1 \bowtie R_2 = \{\langle a, b, c, d_1 \rangle, \langle a, b, c, d_2 \rangle\}$, and $\pi_{A, B, C}(R_1 \bowtie R_2) = \{\langle a, b, c \rangle, \langle a, b, c \rangle\}$, $\delta(\pi_{A, B, C}(R_1 \bowtie R_2)) = \{\langle a, b, c \rangle\}$.

Let $R_1(A, B, C, D)$ and $R_2(A, B, C, D)$ be two relations stored in two heap files with $B(R_1)$ and $B(R_2)$ pages, respectively. We know that $B(R_1) < B(R_2)$, $B(R_1) > K$, and $B(R_2) > K$, where K is the number of available frames in the buffer. We have to compute the intersection of R_1 and R_2 , in four different scenarios: (a) both R_1 and R_2 are sets; (b) R_1 is a set and R_2 is a bag; (c) R_1 is a bag and R_2 is a set; (d) both R_1 and R_2 are bags. For each of the above scenarios, tell whether the “classical block-nested loop algorithm” can be used or not; if the answer is negative, then motivate the answer in detail, and if the answer is positive, then briefly describe the algorithm and its cost (in terms of number of page accesses). We remind the students that the “classical block-nested loop algorithm” reads all the pages of the outer relation in blocks, and for each block, it reads all the pages of the inner relation, and while doing this, it does not execute any write operation other than the writes of the pages of the result.

We analyze the various cases.

