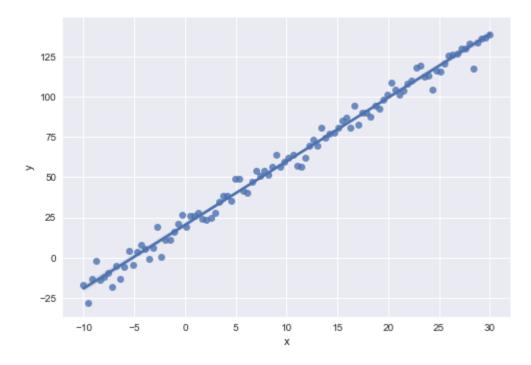
Maximum Likelihood Estimation

```
In [24]: import numpy as np
         import pandas as pd
         from matplotlib import pyplot as plt
         import seaborn as sns
         from statsmodels import api
         from scipy import stats
         from scipy.optimize import minimize
In [25]: # generate an independent variable
         x = np.linspace(-10, 30, 100)
         # generate a normally distributed residual
         e = np.random.normal(10, 5, 100)
         # generate ground truth
         y = 10 + 4*x + e
         df = pd.DataFrame({'x':x, 'y':y})
         df.head()
Out[25]:
                               у
         0 -10.000000 -16.789727
         1 -9.595960 -28.273278
         2 -9.191919 -13.206354
         3 -8.787879 -2.159996
         4 -8.383838 -13.658483
In [26]: sns.regplot(x='x', y='y', data = df)
```

plt.show()



```
In [28]: def MLE_Norm(parameters):
            # extract parameters
            const, beta, std_dev = parameters
            # predict the output
            pred = const + beta*x
            # Calculate the log-likelihood for normal distribution
            LL = np.sum(stats.norm.logpdf(y, pred, std_dev))
            # Calculate the negative log-likelihood
            neg_LL = -1*LL
            return neg_LL
In [29]: mle_model = minimize(MLE_Norm, np.array([2,2,2]), method='L-BFGS-B')
         mle_model
               fun: 299.16131301125677
Out[29]:
          hess_inv: <3x3 LbfgsInvHessProduct with dtype=float64>
               jac: array([ 1.13686828e-05,  8.52651288e-05, -2.27373677e-05])
           message: 'CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH'</pre>
              nfev: 136
               nit: 28
              njev: 34
            status: 0
           success: True
                 x: array([20.36984056, 3.95324845, 4.81951892])
```

In []: