

---

# Machine Listening for Music and Sound Analysis

## Lecture 1 – Audio Representations

---

Dr.-Ing. Jakob Abeßer  
Fraunhofer IDMT

[Jakob.abesser@idmt.fraunhofer.de](mailto:Jakob.abesser@idmt.fraunhofer.de)

[\*\*https://www.machinelistening.de\*\*](https://www.machinelistening.de)

---

# Learning Objectives

---

- 
- Sound categories
  - Music representations
  - Audio representations
  - Audio signal decomposition
  - Audio features
-

# Sound Categories

## Environmental Sounds

- Sound sources
  - Animals, humans, machines
- Sound characteristics
  - Stationary or non-stationary, repetitive or without any predictable nature
- Sound duration
  - Very short (gun shot, door knock, shouts)
  - Very long (running machines, wind, rain)



AUD-1



Fig. 1



Fig. 2



Fig. 3

# Sound Categories

## Music Signals

- Sound sources
  - Music instruments
    - Sound production mechanisms (brass, wind, string, percussive)
  - Singing Voice
- Sound characteristics
  - Mostly well structured along
    - Frequency (pitch, overtone relationships, harmony)
    - Time (onset, rhythm, structure)



AUD-2



Fig. 4



Fig. 5

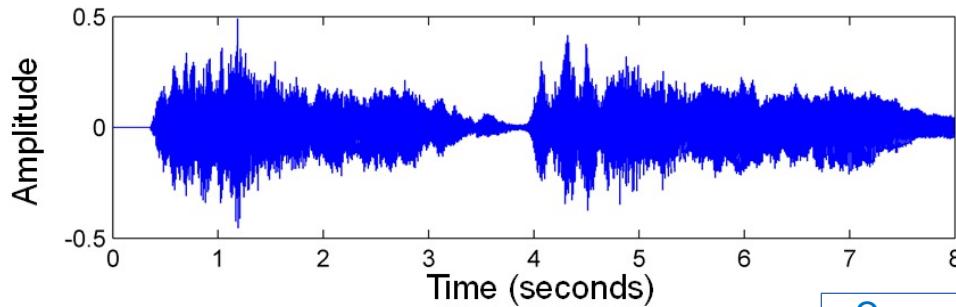


Fig. 6

# Music Representations

## Recording & Notation

### ■ Music recording (waveform)

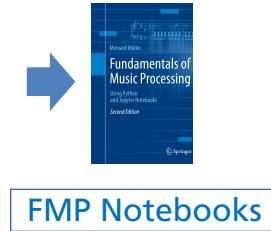


Own

### ■ Music notation (score)



Fig. 7



FMP Notebooks

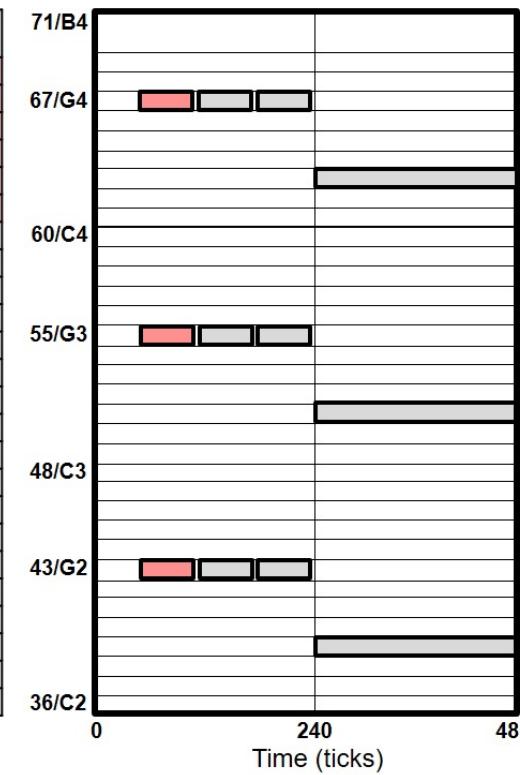
# Music Representations

## MIDI

### ■ Sequence of note events (MIDI)



Time (Ticks)	Message	Channel	Note Number	Velocity
60	NOTE ON	1	67	100
0	NOTE ON	1	55	100
0	NOTE ON	2	43	100
55	NOTE OFF	1	67	0
0	NOTE OFF	1	55	0
0	NOTE OFF	2	43	0
5	NOTE ON	1	67	100
0	NOTE ON	1	55	100
0	NOTE ON	2	43	100
55	NOTE OFF	1	67	0
0	NOTE OFF	1	55	0
0	NOTE OFF	2	43	0
5	NOTE ON	1	67	100
0	NOTE ON	1	55	100
0	NOTE ON	2	43	100
55	NOTE OFF	1	67	0
0	NOTE OFF	1	55	0
0	NOTE OFF	2	43	0
5	NOTE ON	1	63	100
0	NOTE ON	2	51	100
0	NOTE ON	2	39	100
240	NOTE OFF	1	63	0
0	NOTE OFF	2	51	0
0	NOTE OFF	2	39	0



FMP Notebooks

Fig. 8

# Music Representations

## MusicXML

- Textual description of note events (MusicXML)

```
<note>
  <pitch>
    <step>E</step>
    <alter>-1</alter>
    <octave>4</octave>
  </pitch>
  <duration>2</duration>
  <type>half</type>
</note>
```



Fig. 9

# Audio Representations

## Short-term Fourier Transform (STFT)

- Discrete Short-Term Fourier Transform (STFT)
- Windowed analysis of audio signals

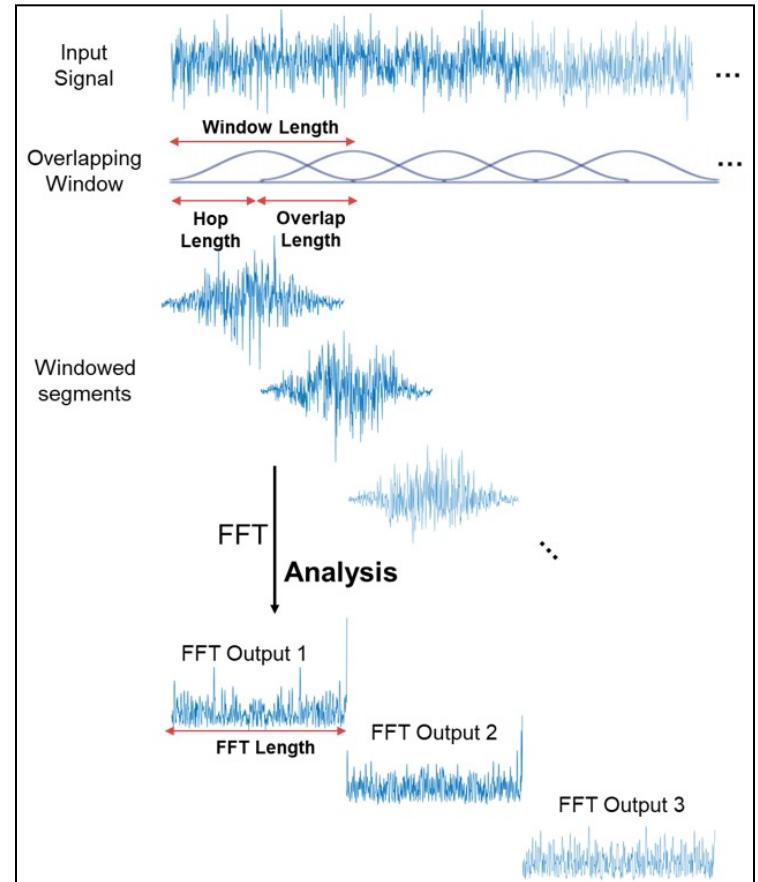


Fig. 9.5

---

# Audio Representations

## Short-term Fourier Transform (STFT)

---

- Discrete Short-Term Fourier Transform (STFT)

$$X(m, k) = \sum_{n=0}^{N-1} x(n + mH)w(n)e^{-2\pi i kn/N}$$

- Windowed local signal frames (with overlap)
- Time-frequency decomposition

# Audio Representations

## Short-term Fourier Transform (STFT)

- Discrete Short-Term Fourier Transform (STFT)

$$X(m, k) = \sum_{n=0}^{N-1} x(n + mH)w(n)e^{-2\pi i kn/N}$$

- Windowed local signal frames (with overlap)
- Time-frequency decomposition
- Linearly-spaced frequency axis
- Trade-off between
  - Frequency resolution
  - Time resolution

# Audio Representations

## Short-term Fourier Transform (STFT)

- Example: Sinusoid signal, two frequencies

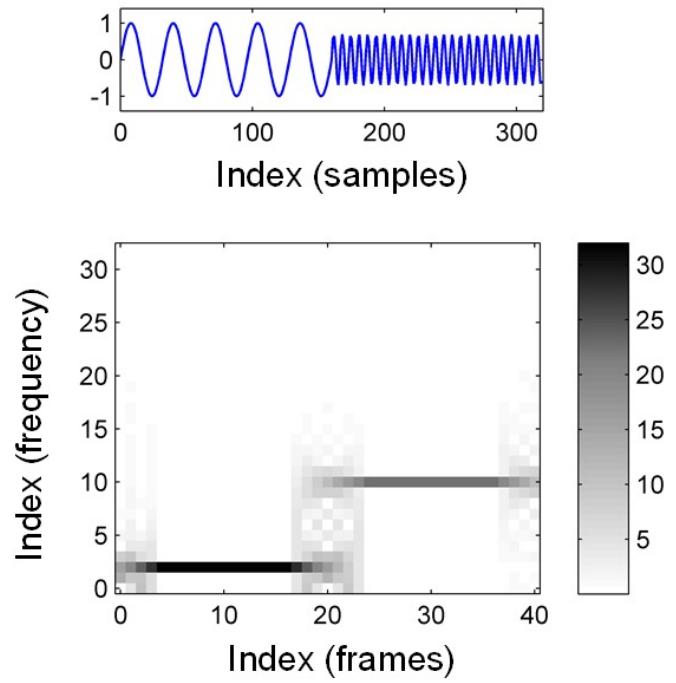


Fig. 10

# Audio Representations

## Short-term Fourier Transform (STFT)

- Example: C major scale, fundamental frequencies ( $f_0$ ) & overtones

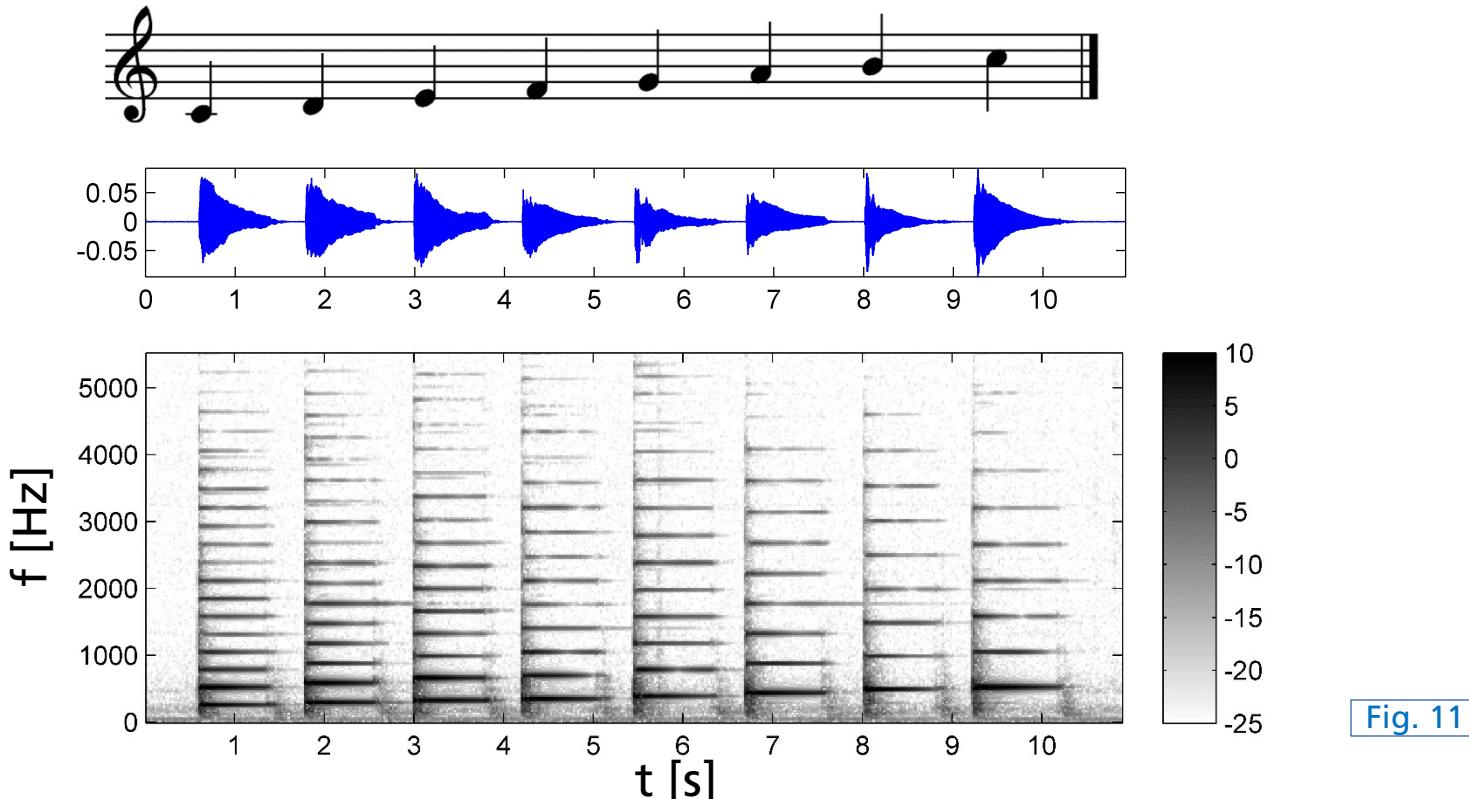


Fig. 11

---

# Audio Representations

## Constant-Q Transform (CQT)

---

- Bank of filters with geometrically spaced center frequencies

$$f_k = f_0 \cdot 2^{k/b}$$

$k$  - Filter index

$b$  - Number of filters per octave

# Audio Representations

## Constant-Q Transform (CQT)

---

- Bank of filters with geometrically spaced center frequencies

$$f_k = f_0 \cdot 2^{k/b}$$

$k$  - Filter index

$b$  - Number of filters per octave

- Filter bandwidth (for adjacent filters)

$$\Delta_k = f_{k+1} - f_k = f_k \left( 2^{\frac{1}{b}} - 1 \right)$$

- Increasing time resolution towards higher frequencies
- Resembles human auditory perception

---

# Audio Representations

## Constant-Q Transform (CQT)

---

- Constant frequency-to-resolution ratio

$$Q = \frac{f_k}{\Delta_k} = \frac{1}{2^{\frac{1}{b}-1}}$$

# Audio Representations

## Constant-Q Transform (CQT)

---

- Constant frequency-to-resolution ratio

$$Q = \frac{f_k}{\Delta_k} = \frac{1}{2^{\frac{1}{b}-1}}$$

- Correspondence to musical note frequencies

$$f_m[\text{Hz}] = 440 \cdot 2^{\frac{m-69}{12}}$$

*m*: MIDI pitch

440 Hz = "A4" (reference pitch)

---

# Audio Representations

## Constant-Q Transform (CQT)

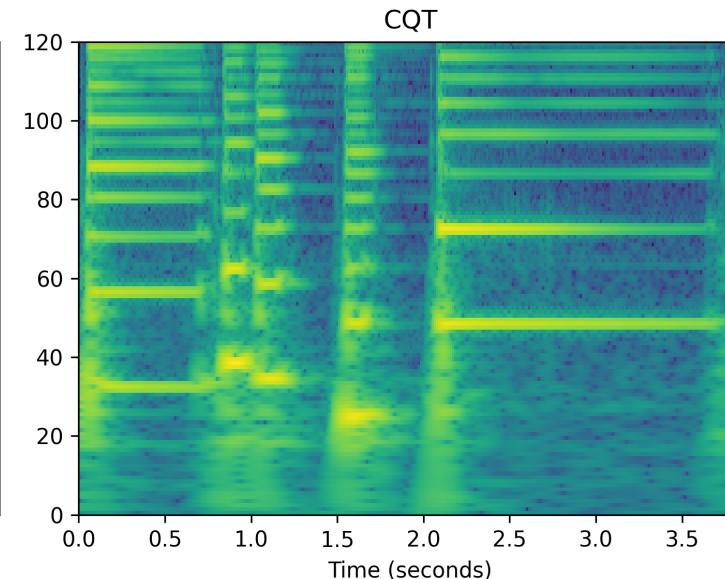
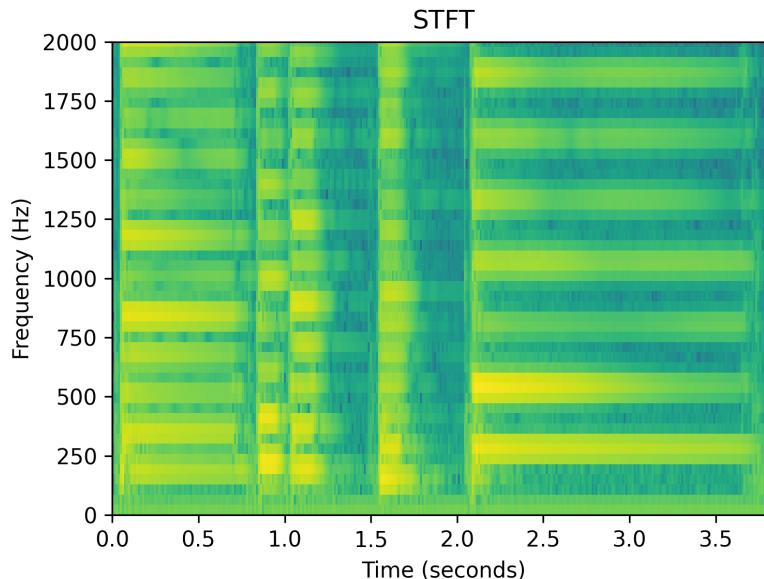
---

- STFT (linearly-spaced frequencies)
- CQT (logarithmically-spaced, closer to human auditory perception)
  - Fixed number of frequency bins per octave
  - Increasing time resolution towards higher frequencies

# Audio Representations

## Constant-Q Transform (CQT)

- STFT (linearly-spaced frequencies)
- CQT (logarithmically-spaced, closer to human auditory perception)
  - Fixed number of frequency bins per octave
  - Increasing time resolution towards higher frequencies

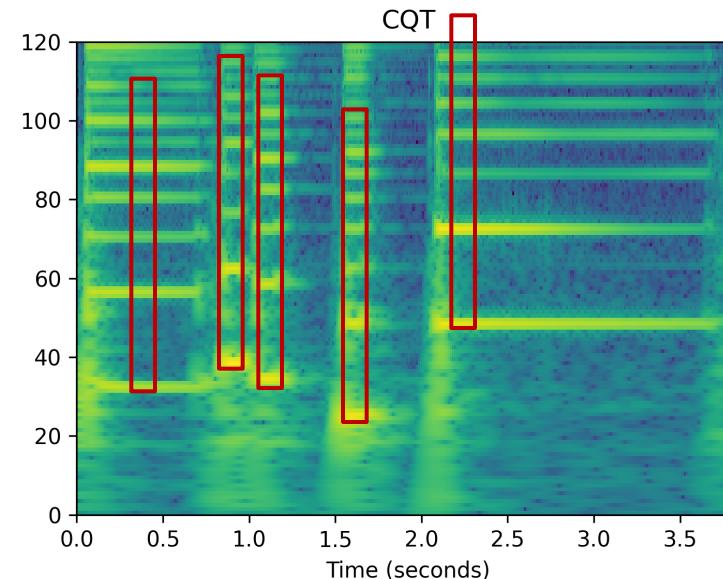
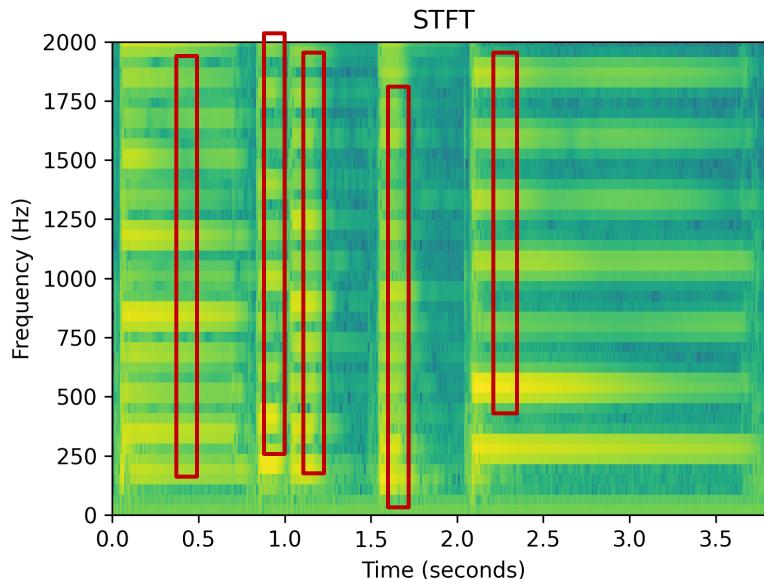


Audio 1

# Audio Representations

## Constant-Q Transform (CQT)

- Suitable for music transcription
- Partials have a constant frequency pattern
  - Vertically shifted
  - Pitch-independent

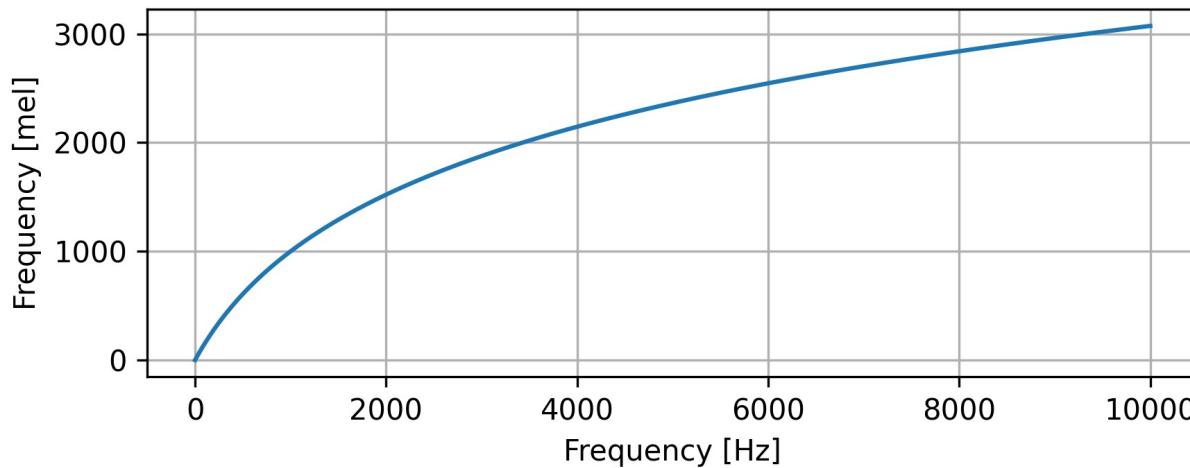


Audio 1

# Audio Representations

## Mel Spectrogram

- Logarithmic frequency mapping (human pitch perception)
- $f[\text{mel}] = 2595 \cdot \log_{10} \left( 1 + \frac{f[\text{Hz}]}{700} \right)$



---

# Audio Representations

## Mel Spectrogram

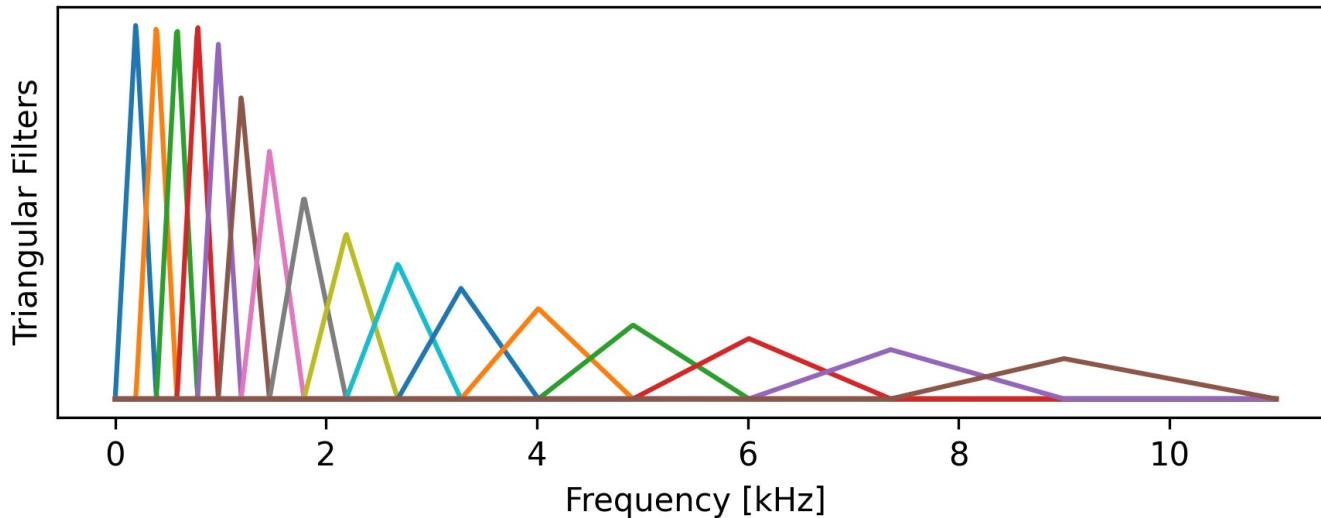
---

- Mapping from STFT magnitude spectrogram to Mel spectrogram
- Triangular filterbank + Matrix multiplication

# Audio Representations

## Mel Spectrogram

- Mapping from STFT magnitude spectrogram to Mel spectrogram
  - Triangular filterbank + Matrix multiplication
- Example: 16 mel bands,  $f_s = 22.05$  kHz



---

# Audio Representations

## Mel Spectrogram

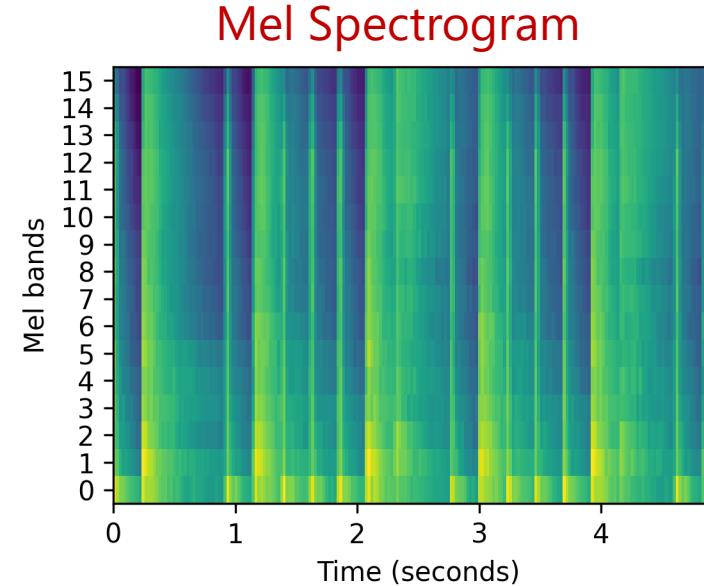
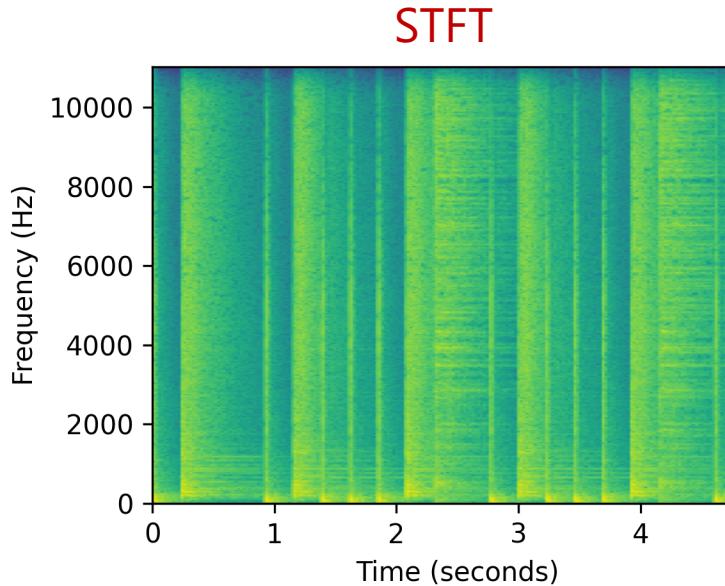
---

- More efficient representation (fewer frequency bands)
- Still captures perceptually relevant information

# Audio Representations

## Mel Spectrogram

- More efficient representation (fewer frequency bands)
- Still captures perceptually relevant information

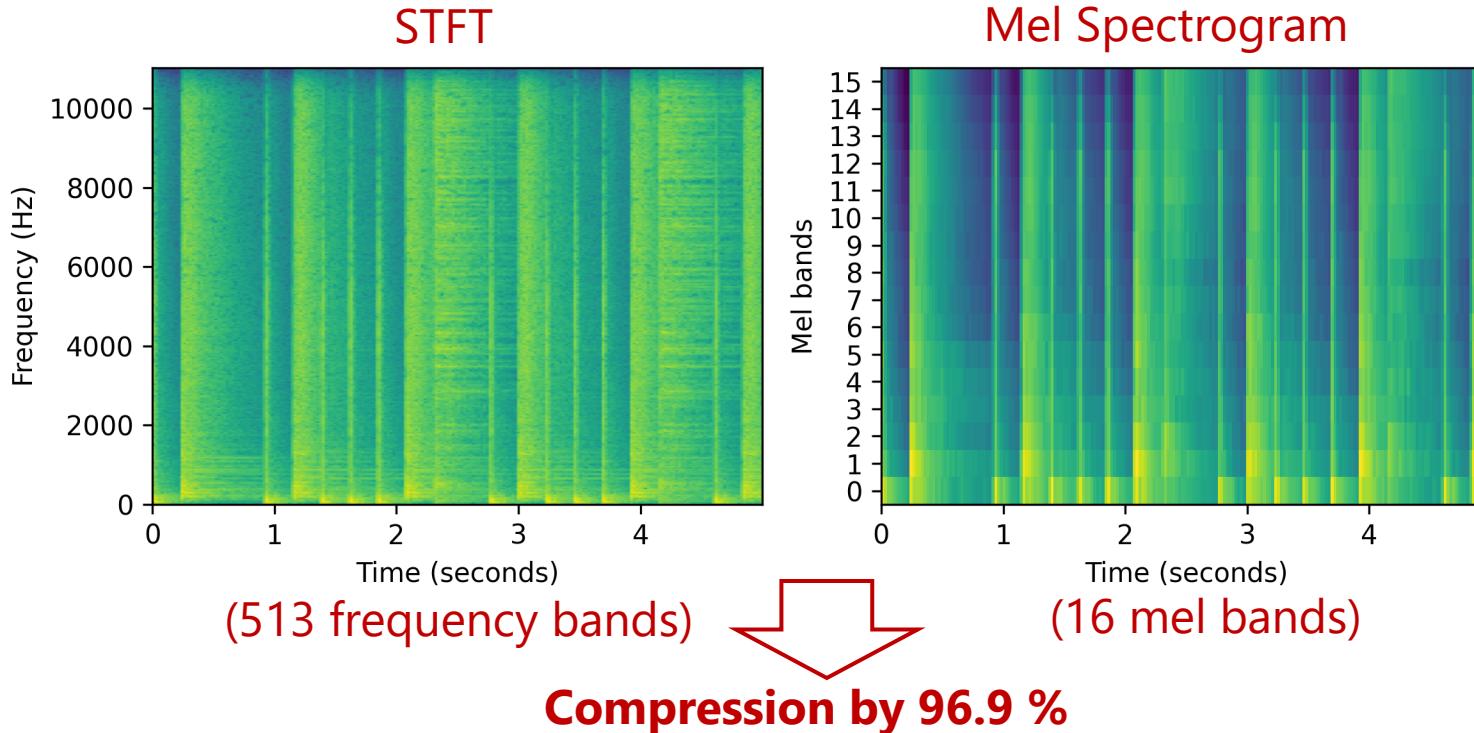


Audio 3

# Audio Representations

## Mel Spectrogram

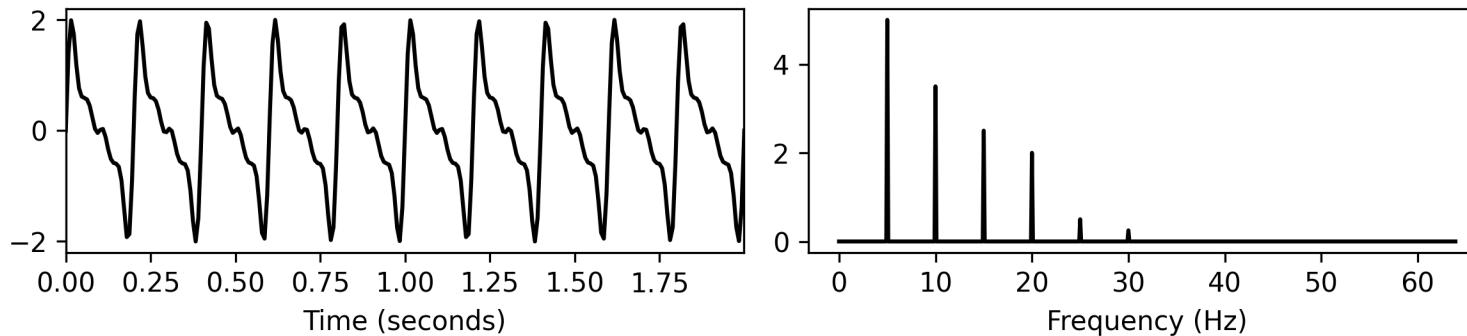
- More efficient representation (fewer frequency bands)
- Still captures perceptually relevant information



# Audio Signal Decomposition

## Periodic Signals

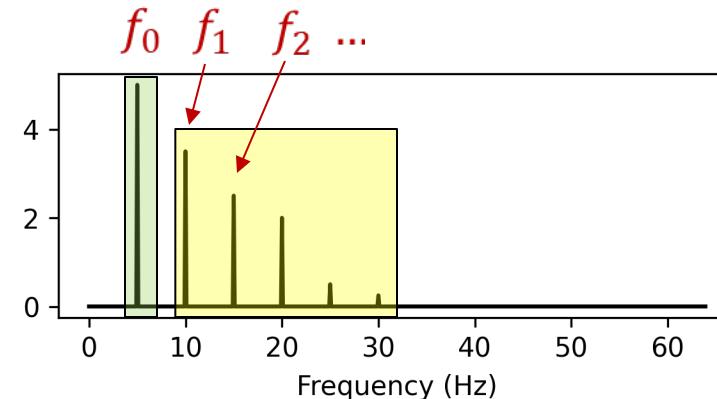
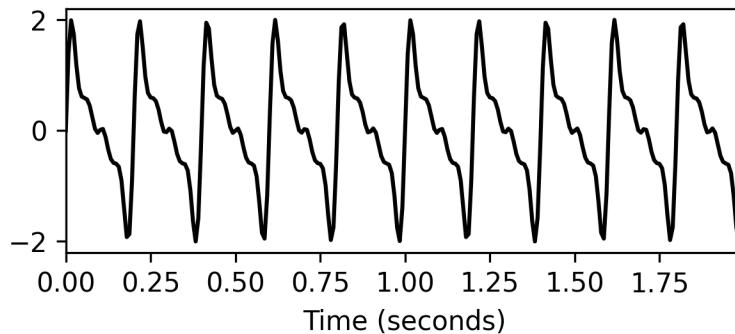
- Periodic signals:
  - Sum of pure tones (partials)
    - Fundamental frequency  $f_0$
    - Harmonics  $f_k$  (approx. integer multiples of  $f_0$ ):
      - $f_k \approx (k + 1) \cdot f_0$



# Audio Signal Decomposition

## Periodic Signals

- Periodic signals:
  - Sum of pure tones (partials)
    - Fundamental frequency  $f_0$
    - Harmonics  $f_k$  (approx. integer multiples of  $f_0$ ):
      - $f_k \approx (k + 1) \cdot f_0$



# Audio Signal Decomposition

## Pitch

- Perceptual property (sort sounds from low to high pitch)
- Closely related to frequency

$$■ f = 440 \cdot 2^{\frac{p-69}{12}} [\text{Hz}]$$

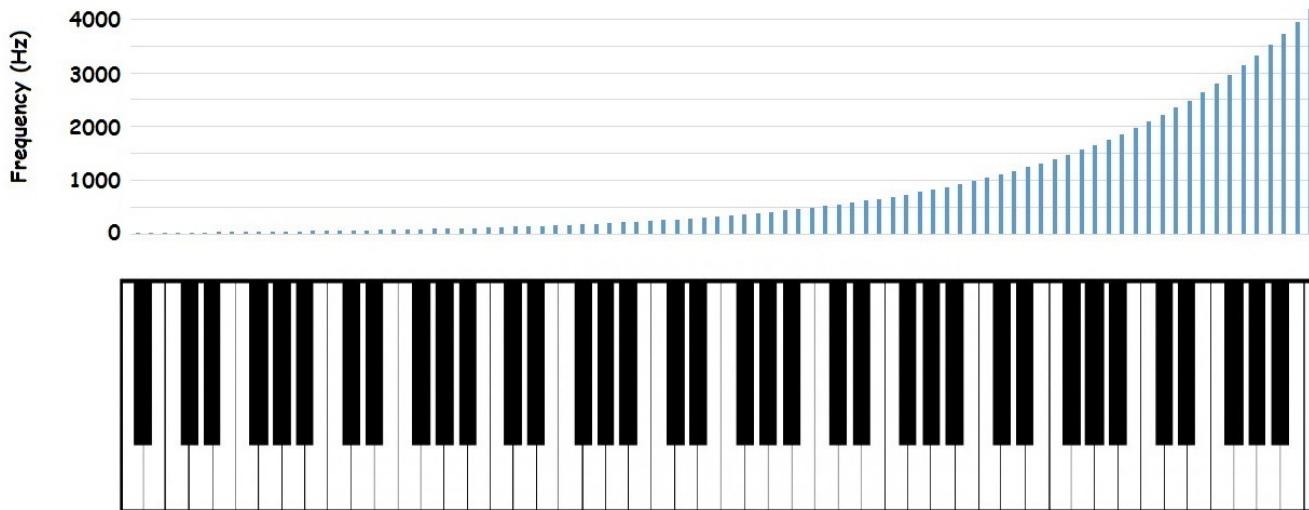
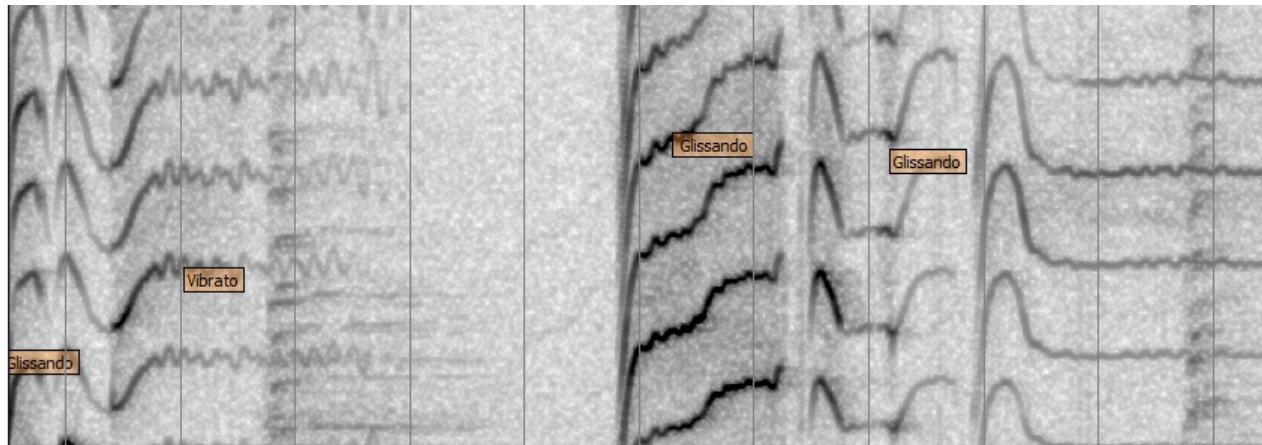


Fig. 2.5

# Audio Signal Decomposition

## Frequency Modulation

- Techniques
  - Glissando – continuous transition between note pitches
  - Vibrato – periodic frequency modulation



Spectrogram example (frequency x time)

Fig. 2.6

---

# Audio Signal Decomposition

## Transients

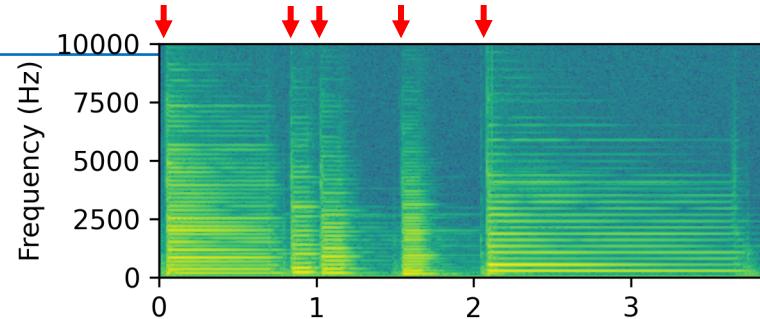
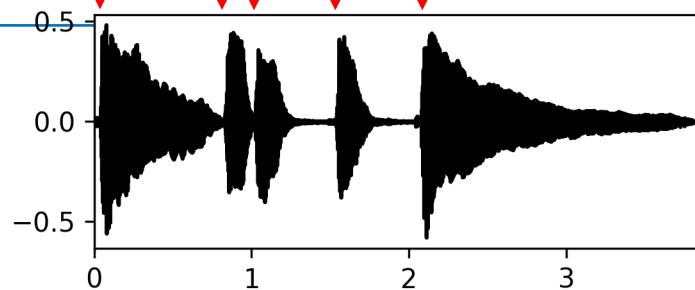
---

- Sound characteristics
  - High amplitude
  - Short duration
  - Wide-band signal

# Audio Signal Decomposition

## Transients (Examples)

- String instruments
-  [Audio 1](#)



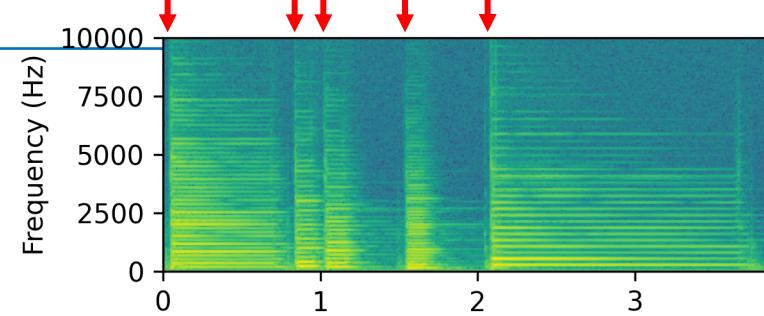
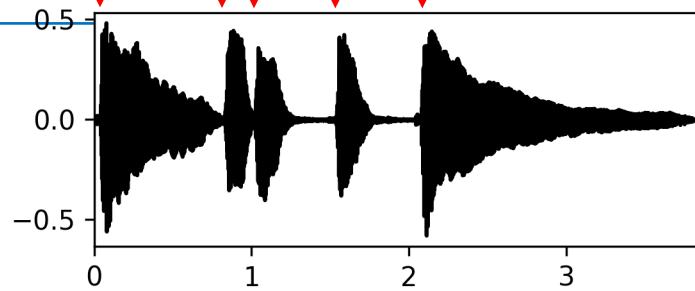
# Audio Signal Decomposition

## Transients (Examples)

- String instruments



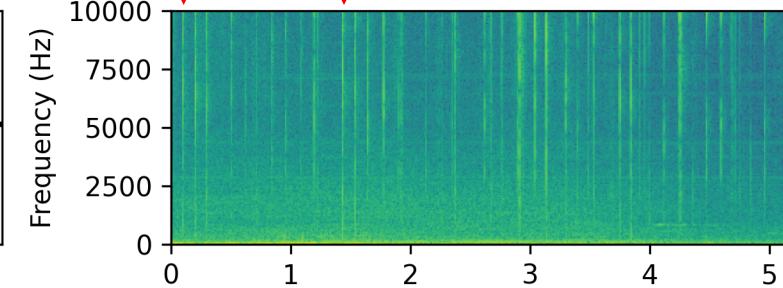
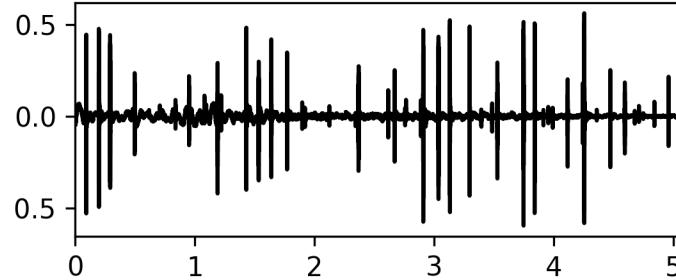
Audio 1



- Bat vocalizations



Audio 2

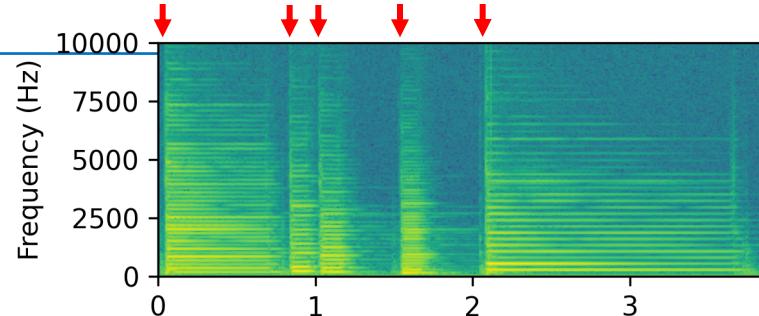
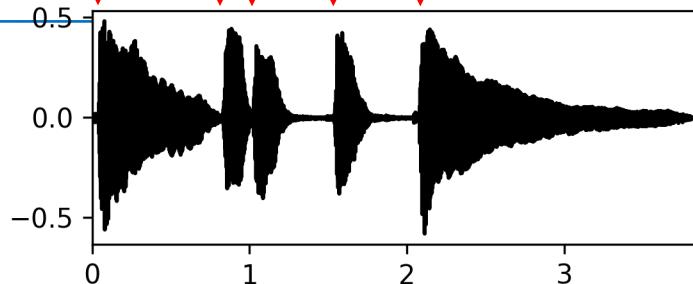


# Audio Signal Decomposition

## Transients (Examples)

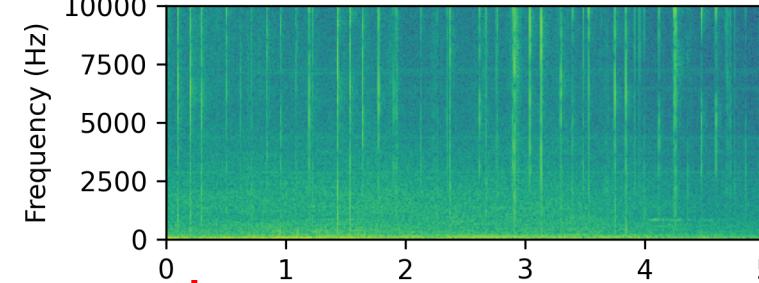
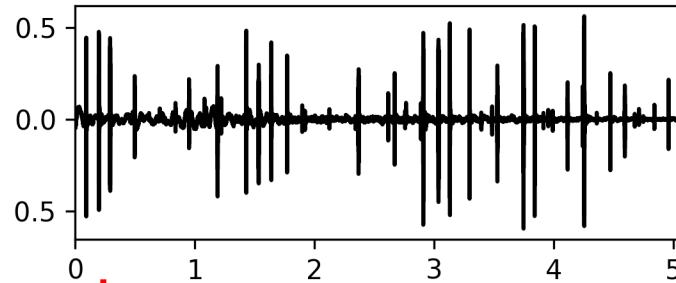
- String instruments

🔊 [Audio 1](#)



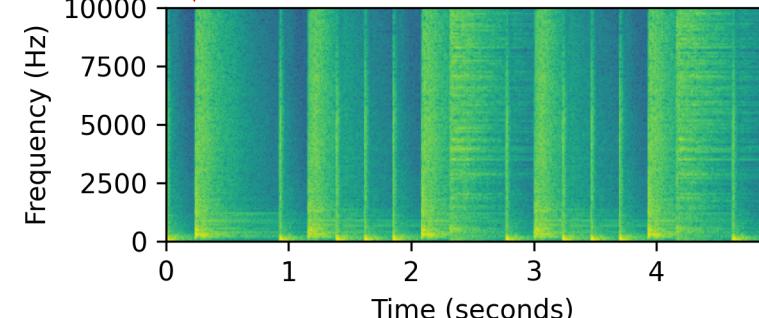
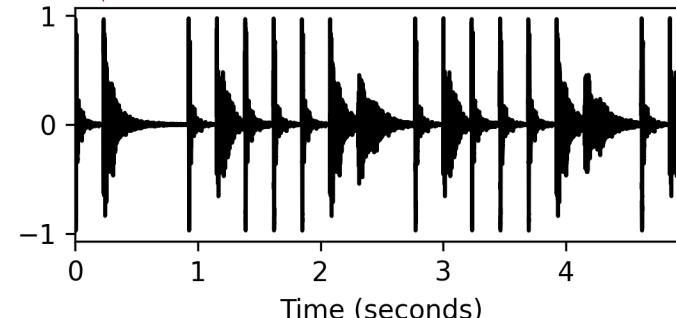
- Bat vocalizations

🔊 [Audio 2](#)



- Drum instruments

🔊 [Audio 3](#)



---

# Audio Signal Decomposition

## Noise

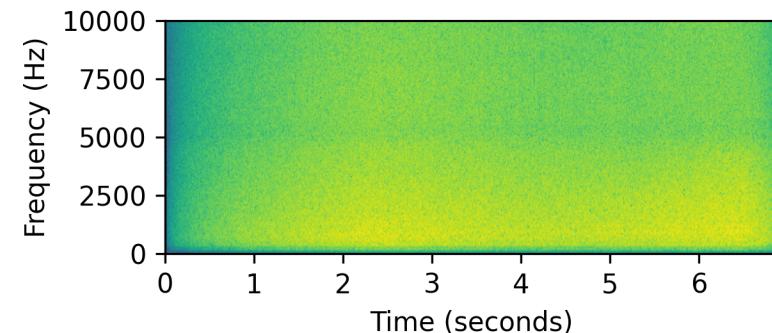
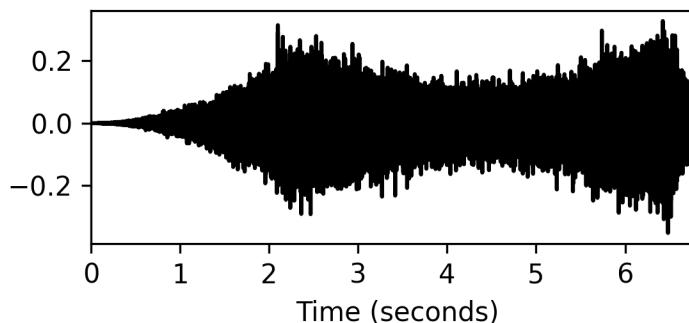
---

- Sound characteristics
  - Non-periodic, texture-like
  - Random fluctuations of air pressure

# Audio Signal Decomposition

## Noise

- Sound characteristics
  - Non-periodic, texture-like
  - Random fluctuations of air pressure
- Examples
  - Consonants (speech)
  - Wind (random aerodynamic turbulences)
  - Waves (ocean)  [Audio 4](#)



# Audio Features

## Motivation

---

- Compact representation of audio signal for machine learning applications
- Capture different properties at different semantic levels
  - Timbre – perceived sound, instrumentation
  - Rhythm – tempo, meter
  - Melody/Tonality – pitches, harmonies
  - Structure – repetitions, novelty, homogeneous segments

---

# Audio Features

## Timbre

---

- Timbre

- Timbre distinguishes musical sounds that have the same pitch (fundamental frequency) and loudness

# Audio Features

## Timbre

- Timbre
  - Timbre distinguishes musical sounds that have the same pitch (fundamental frequency) and loudness
  - Affected by different acoustic phenomena such as
    - Spectral structure / envelope of overtones
    - Noise-like components

# Audio Features

## Timbre

### ■ Timbre

- Timbre distinguishes musical sounds that have the same pitch (fundamental frequency) and loudness
- Affected by different acoustic phenomena such as
  - Spectral structure / envelope of overtones
  - Noise-like components
  - Formants (speech)
  - Inharmonicity (non-integer relationship between partials)
  - Variations over time: frequency (vibrato) or loudness (tremolo)



FMP Notebooks

---

# Audio Features

## Timbre

---

- Timbre
  - When looking at musical instruments, we need to consider
    - Instrument's construction

# Audio Features

## Timbre

---

- Timbre
  - When looking at musical instruments, we need to consider
    - Instrument's construction
    - Sound production principles
      - Membranophones, chordophones, aerophones, electrophones

---

# Audio Features

## Timbre

---

- Timbre
  - When looking at musical instruments, we need to consider
    - Instrument's construction
    - Sound production principles
      - Membranophones, chordophones, aerophones, electrophones
    - Human performance
      - Playing techniques, expressivity, dynamics, style

# Audio Features

## Temporal Envelope

- Smooth curve outlining the signal extreme points
- ADSR envelope model (also used for audio synthesis)
  - Attack, Decay, Sustain, Release

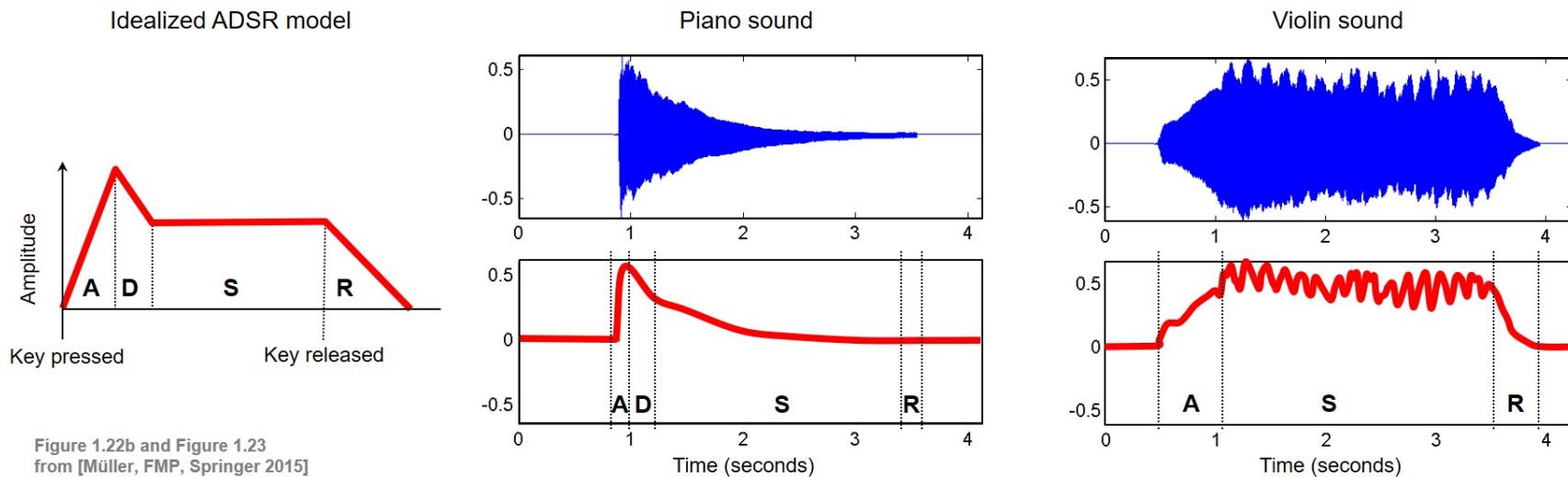


Fig. 2.7

# Audio Features

## Temporal Envelope

- Tremolo
  - Periodic amplitude modulation
  - Often coincides with frequency modulation (vibrato)
  - Examples: instrument sounds



FMP Notebooks

Fig. 2.7

# Audio Features Categorization

	<b>Timbre</b>	<b>Rhythm</b>	<b>Tonality</b>
<b>Low-Level</b> (Q~10 ms)	<ul style="list-style-type: none"><li>- Zero Crossing Rate (ZCR)</li><li>- Linear Predictive Coding (LPC)</li><li>- Spectral Centroid / Spectral Flatness</li></ul>		
<b>Mid-Level</b> (Q ~ 2.5s)	<ul style="list-style-type: none"><li>- Mel-Frequency Cepstral Coefficients (MFCC)</li><li>- Octave-Based Spectral Contrast (OSC)</li><li>- Loudness</li></ul>	<ul style="list-style-type: none"><li>- Tempogram</li><li>- Log-Lag Autocorrelation (ACF)</li></ul>	<ul style="list-style-type: none"><li>- Chromagram</li><li>- Enhanced Pitch Class Profiles (EPCP)</li></ul>
<b>High-Level</b>	<ul style="list-style-type: none"><li>- Instrumentation</li></ul>	<ul style="list-style-type: none"><li>- Tempo</li><li>- Time Signature</li><li>- Rhythm Patterns</li></ul>	<ul style="list-style-type: none"><li>- Key</li><li>- Scales</li><li>- Chords</li></ul>

# Audio Features Categorization

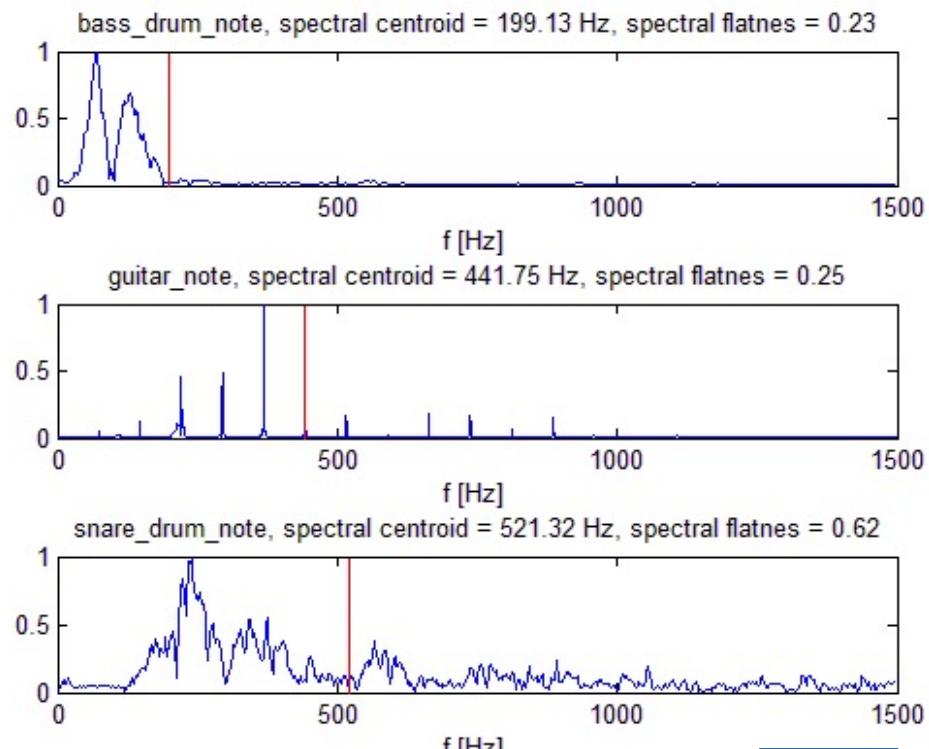
	<b>Timbre</b>	<b>Rhythm</b>	<b>Tonality</b>
Low-Level (Q~10 ms)	<ul style="list-style-type: none"><li>- Zero Crossing Rate (ZCR)</li><li>- Linear Predictive Coding (LPC)</li><li>- Spectral Centroid / Spectral Flatness</li></ul>		
Mid-Level (Q ~ 2.5s)	<ul style="list-style-type: none"><li>- Mel-Frequency Cepstral Coefficients (MFCC)</li><li>- Octave-Based Spectral Contrast (OSC)</li><li>- Loudness</li></ul>	<ul style="list-style-type: none"><li>- Tempogram</li><li>- Log-Lag Autocorrelation (ACF)</li></ul>	<ul style="list-style-type: none"><li>- Chromagram</li><li>- Enhanced Pitch Class Profiles (EPCP)</li></ul>
High-Level	<ul style="list-style-type: none"><li>- Instrumentation</li></ul>	<ul style="list-style-type: none"><li>- Tempo</li><li>- Time Signature</li><li>- Rhythm Patterns</li></ul>	<ul style="list-style-type: none"><li>- Key</li><li>- Scales</li><li>- Chords</li></ul>

# Audio Features

## Timbre Low-level Audio Features

- Spectral Centroid (SC):

- Center of mass in the magnitude spectrogram
- Low-pitched vs. high-pitched sounds



Own

# Audio Features

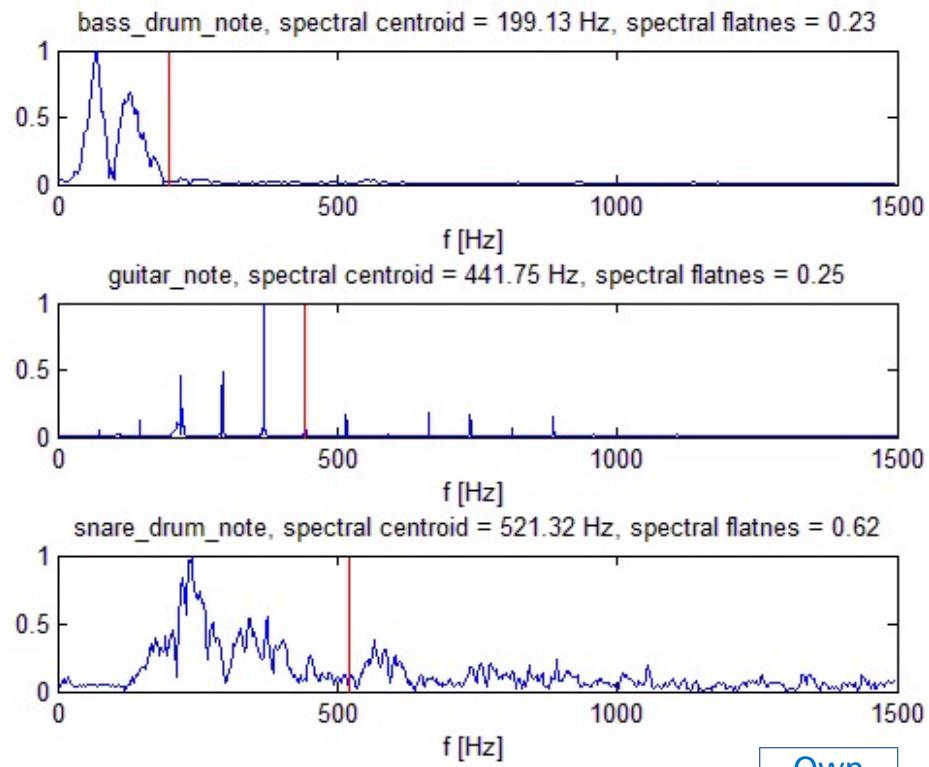
## Timbre Low-level Audio Features

- Spectral Centroid (SC):

- Center of mass in the magnitude spectrogram
- Low-pitched vs. high-pitched sounds

- Spectral Flatness Measure (SFM)

- Harmonic sounds (sparse energy distribution)
- Percussive sounds (wideband energy distribution)



# Audio Features

## Mel-Frequency Cepstral Coefficients (MFCC)

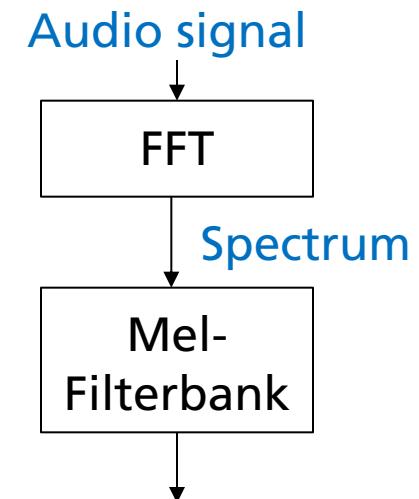
- Convulsive **excitation \* filter** model Audio signal
- Excitation: vibration of vocal folds
- Filter: resonance of the vocal tract

Own

# Audio Features

## Mel-Frequency Cepstral Coefficients (MFCC)

- Convulsive **excitation \* filter** model
  - Excitation: vibration of vocal folds
  - Filter: resonance of the vocal tract
- FFT magnitude spectrum
  - Multiplicative **excitation · filter** model

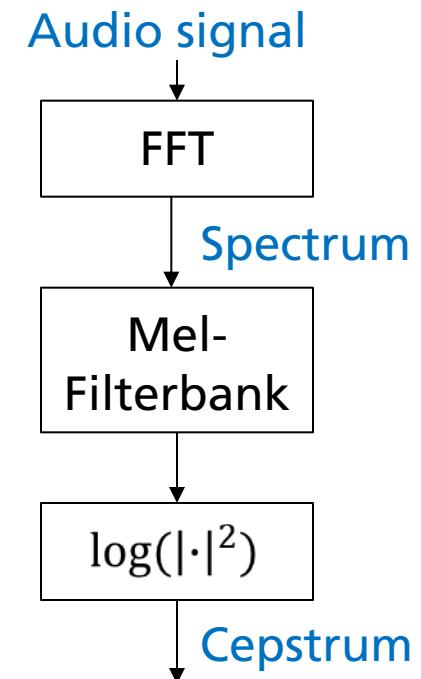


Own

# Audio Features

## Mel-Frequency Cepstral Coefficients (MFCC)

- Convulsive **excitation \* filter** model
  - Excitation: vibration of vocal folds
  - Filter: resonance of the vocal tract
- FFT magnitude spectrum
  - Multiplicative **excitation · filter** model
- Logarithm of magnitude spectrum
  - Additive **excitation + filter** model

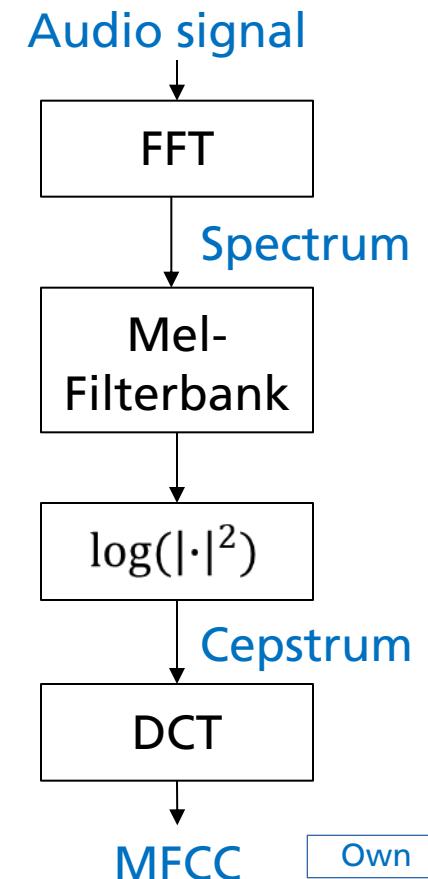


Own

# Audio Features

## Mel-Frequency Cepstral Coefficients (MFCC)

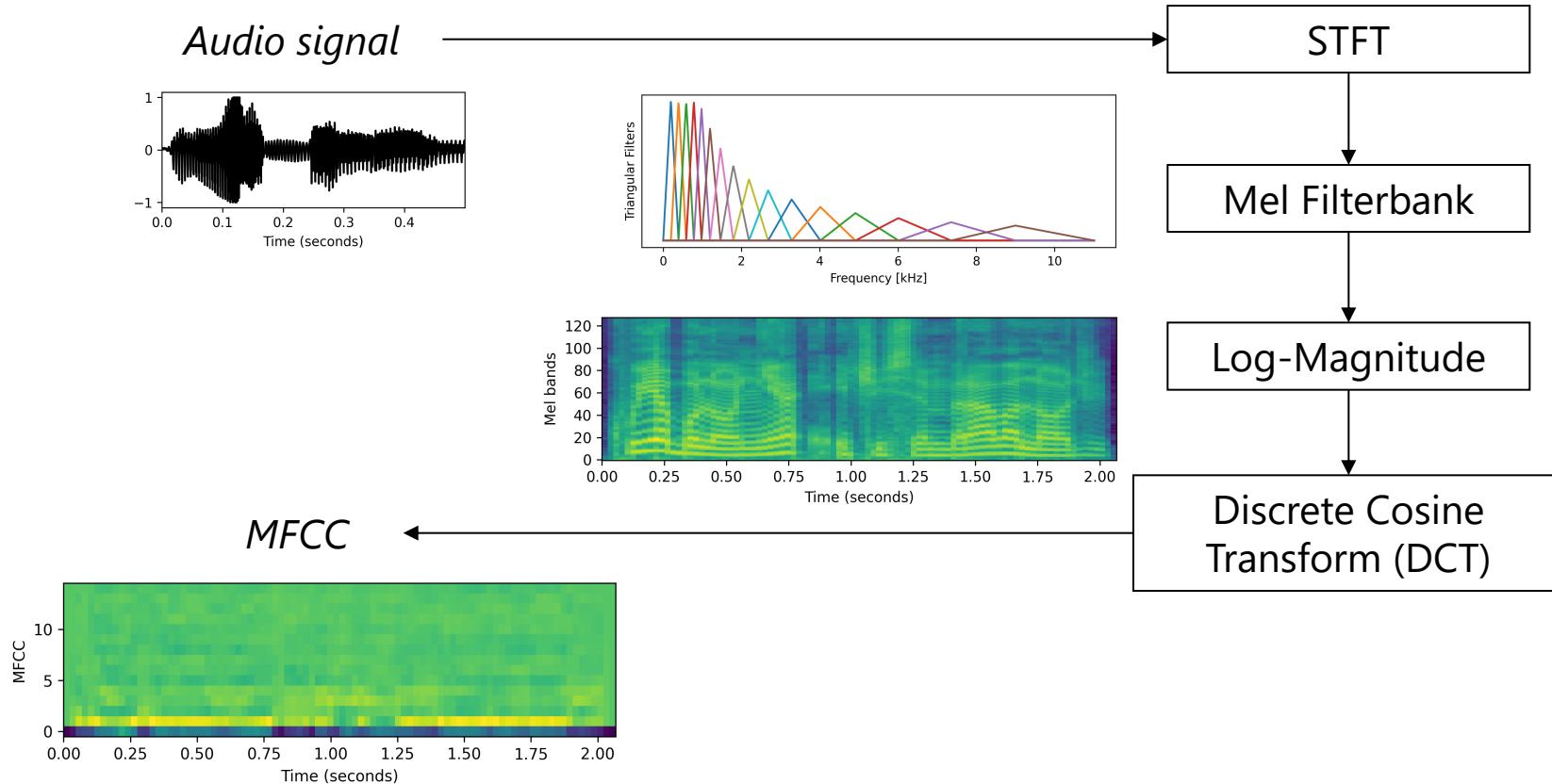
- Convulsive **excitation \* filter** model
  - Excitation: vibration of vocal folds
  - Filter: resonance of the vocal tract
- FFT magnitude spectrum
  - Multiplicative **excitation · filter** model
- Logarithm of magnitude spectrum
  - Additive **excitation + filter** model
- Discrete Cosine Transform (DCT)
  - First coefficients allow for a compact description of the spectral envelope shape



# Audio Features

## Mel-Frequency Cepstral Coefficients (MFCC)

- Compact representation of spectral envelope



---

# **Audio Processing**

## **Chroma Features**

---

- Human pitch perception is periodic
- 2 pitches one octave apart are perceived as similar

# Audio Processing

## Chroma Features

- Human pitch perception is periodic
- 2 pitches one octave apart are perceived as similar
- Pitch = chroma + tone height
  - Chroma: C, C#, D, D#, ..., B (12)
  - Tone height: Octave number

Figure 3.3a from [Müller, FMP, Springer 2015]

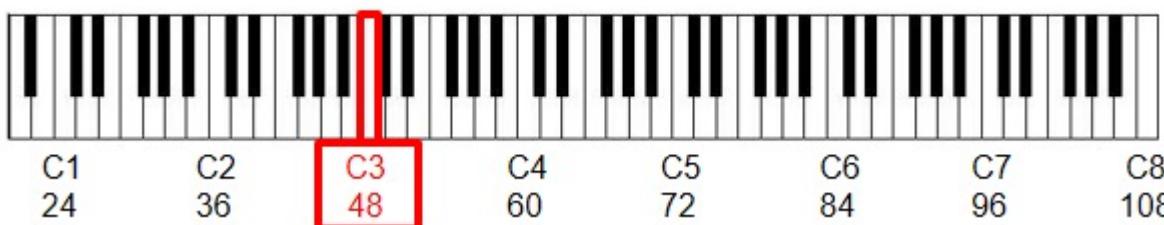
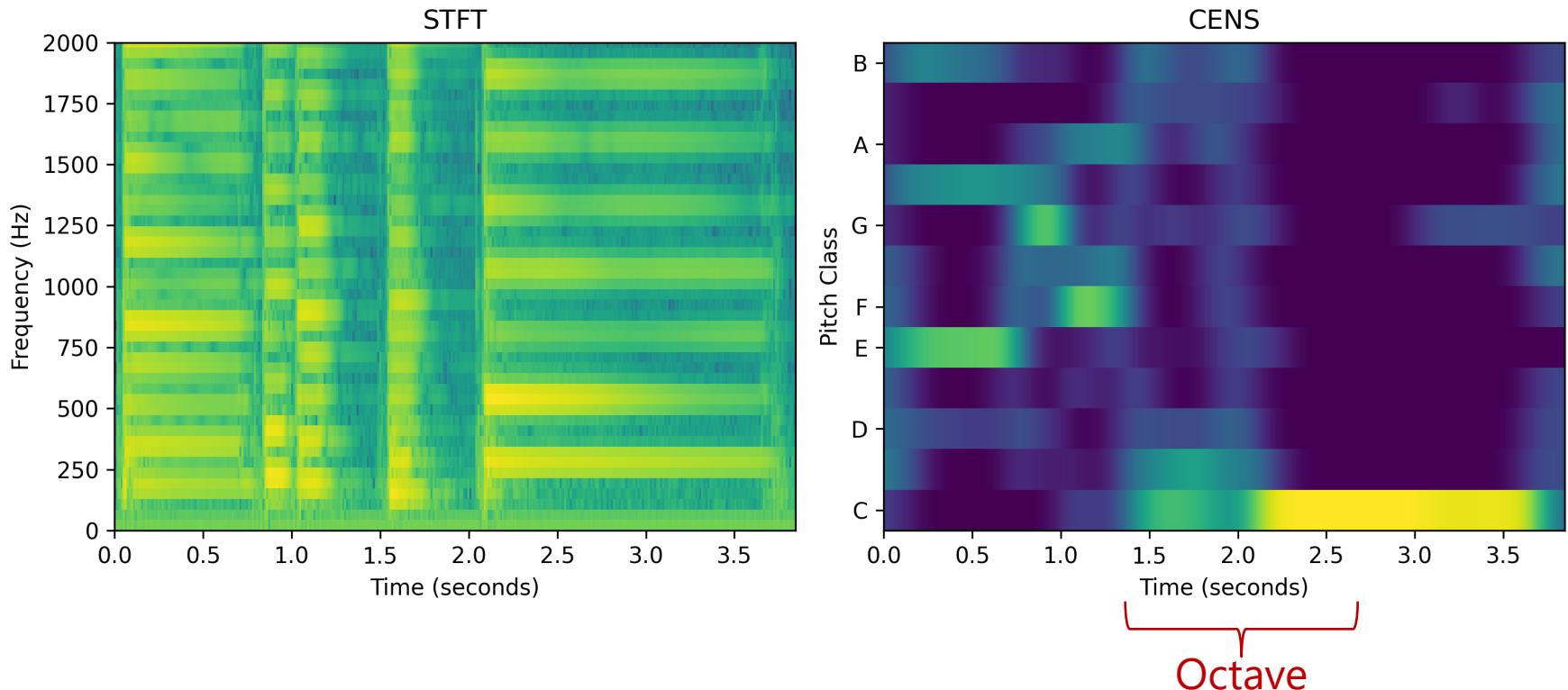


Fig. 2.8

# Audio Processing

## Chroma Features

- Example
- 🔊
- Audio 1



---

# Summary

---

- Sound categories
  - Music representations
  - Audio representations
  - Audio signal decomposition
  - Audio features
-

---

# References

---

- Müller, M. (2021). *Fundamentals of Music Processing - Using Python and Jupyter Notebooks* (2nd ed.). Springer.
- Shi, Z., Lin, H., Liu, L., Liu, R., & Han, J. (2019). Is CQT More Suitable for Monaural Speech Separation than STFT? An Empirical Study. *ArXiv Preprint ArXiv:1902.00631*.

---

# Images

---

Fig. 1: <https://ccsearch-dev.creativecommons.org/photos/39451123-ee45-4ec3-ad8d-b42d856bca06>

Fig. 2: <https://ccsearch-dev.creativecommons.org/photos/c69d3b07-76bd-43e2-a44e-8742edc8447a>

Fig. 2.8: [Müller, 2015]: Fundamentals of Music Processing (FMP), Springer, 2015, Fig. 3.3a

Fig. 3: <https://ccsearch-dev.creativecommons.org/photos/ab3062ab-fe0f-420d-b93d-7451db166b4e>

Fig. 4: <https://ccsearch-dev.creativecommons.org/photos/a27a7541-45f5-4176-91a4-e2cb70eea266>

Fig. 5: <https://ccsearch-dev.creativecommons.org/photos/79d466c1-cfa6-417e-9832-34438678bf5d>

Fig. 6: <https://ccsearch-dev.creativecommons.org/photos/269394a4-5803-47fd-abaa-57ef92735e24>

Fig. 7: [Müller, 2021], p. 2, Fig. 1.1

Fig. 8: [Müller, 2021], p. 14, Fig. 1.13

Fig. 9: [Müller, 2021], p. 17, Fig. 1.15

Fig. 9.5: [https://www.mathworks.com/help/dsp/ref/stft\\_output.png](https://www.mathworks.com/help/dsp/ref/stft_output.png)

Fig. 10: [Müller, 2021], p. 56, Fig. 2.9

Fig. 11: [Müller, 2021], p. 57, Fig. 2.10

Fig. 13: <https://newt.phys.unsw.edu.au/jw/graphics/notes.GIF>

---

---

# Sounds

---

**AUD-1:** Medley: <https://freesound.org/people/InspectorJ/sounds/416529>,  
<https://freesound.org/people/prometheus888/sounds/458461>,  
<https://freesound.org/people/MrAuralization/sounds/317361>

**AUD-2:** Medley: <https://freesound.org/people/whatsanickname4u/sounds/127337>,  
<https://freesound.org/people/jcveliz/sounds/92002>, <https://freesound.org/people/klankbeeld/sounds/192691>

[Audio 1] <https://freesound.org/people/xserra/sounds/196765/>

[Audio 2] <https://freesound.org/people/IliasFlou/sounds/498058/> (~0:00 – 0:05)

[Audio 3] <https://freesound.org/people/danlucaz/sounds/517860/> (~0:00 – 0:05)

[Audio 4] <https://freesound.org/people/IENBA/sounds/489398/> (~0:00 – 0:07)

# Thank you!

---

- 
- Any questions?

Dr.-Ing. Jakob Abeßer  
Fraunhofer IDMT

[Jakob.abesser@idmt.fraunhofer.de](mailto:Jakob.abesser@idmt.fraunhofer.de)

[\*\*https://www.machinelistingen.de\*\*](https://www.machinelistingen.de)

---