

Input: $G = (V, E)$: graph to analyze

Input: n, m : order and size of G

Output: H : graph with n vertices where the neighbors of each vertex are those of distance one or two in G

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1 Algorithm: ExpandedNeighborhood
2  $H = \text{Graph}(n)$  //  $\Theta(n^2)$ 
3 for  $v \in V$  do
    //  $\Theta(\deg u)$  per iteration,  $\Theta(\deg v)$  iterations: total  $\Theta(\sum \deg u)$ 
4     for  $u \in N_G(v)$  do
5          $H.\text{AddEdge}(v, u)$  //  $\Theta(1)$ 
        //  $[\Theta(n) \text{ or } \Theta(\Delta)] \times \Theta(\deg w) = \Theta(n \deg v) \text{ or } \Theta(\Delta \deg v)$ 
6         for  $w \in N_G(u)$  do
7              $H.\text{AddEdge}(v, w)$  //  $\Theta(1)$ 
8         end
9     end
10 end
11 return  $H$  //  $\Theta(1)$ 

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$$\begin{aligned} &\sum (n \deg v) \text{ or } \sum (\Delta \deg v) \\ &n^2 + n \times m \text{ or } n^2 + \Delta \times m \end{aligned}$$