

# Homework 6

Due 09/13/16

September 8, 2016

1. Analyze the *worst-case* time complexity of the algorithm below. Please show all work. The  $\lfloor \cdot \rfloor$  symbols represent the *floor* (“round down”) function. You may assume that this function takes  $\Theta(1)$  time for any input. You may also assume it takes a constant amount of time to determine whether an integer is odd.

Note that figuring out what problem this algorithm solves is *irrelevant* to analyzing its complexity.

```
Input:  $n$ : nonnegative integer
1 Algorithm: LoopMystery
2  $sum = 0$ 
3  $t = 1$ 
4  $d = 1$ 
5  $k = n$ 
6 while  $k > 1$  do
7   for  $i = 1$  to  $k$  do
8      $t = t + d$ 
9      $sum = sum + t$ 
10  end
11  if  $k$  is odd then
12     $d = -d$ 
13  end
14   $k = \lfloor k/2 \rfloor$ 
15 end
16 return  $sum$ 
```