

A GENERAL METHOD FOR ASSESSING THE ORIGIN OF INTERSTELLAR SMALL BODIES: THE CASE OF 1I/2017 U1 (‘Oumuamua)

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ABSTRACT

With the advent of more and deeper sky surveys, the discovery of interstellar small objects entering into the Solar System has been finally possible. In October 19, 2017, using observations of the PANSTARRS survey, a fast moving object, now officially named 1I/2017 U1 (‘Oumuamua), was discovered in a heliocentric unbound trajectory suggesting an interstellar origin. Assessing the provenance of interstellar small objects is key for understanding their distribution, spatial density and the processes responsible for their ejection from planetary systems. However, their peculiar trajectories place a limit on the number of observations available to determine a precise orbit. As a result, when its position is propagated $\sim 10^5 - 10^6$ years backward in time, small errors in orbital elements become large uncertainties in position in the interstellar space. In this paper we present a general method for assigning probabilities to nearby stars of being the parent system of an observed interstellar object. We describe the method in detail and apply it for assessing the origin of 1I/2017 U1. A preliminary list of potential progenitors and their corresponding probabilities is provided. In the future, when further information about the object and/or the nearby stars be refined, the probabilities computed with our method can be updated. We provide all the data and codes we developed for this purpose in the form of an open source C/C++/Python package, *iWander* which is publicly available at <http://github.com/seap-udea/iWander>.

Subject headings: Interstellar small body — asteroids: individual: 1I/2017 U1 — Methods: numerical

1. INTRODUCTION

The detection of interstellar small objects, wandering through the Solar System, has challenged the astronomers over the last century (see e.g. [Opik 1932](#); [McGlynn & Chapman 1989](#); [Sen & Rama 1993](#)). The detection, characterization and investigation of the origin of these objects could shed light on the processes of planetary formation, the architecture of their parent planetary systems, as well as on planetary ejection mechanisms (see e.g. [Raymond et al. 2017](#)). Moreover, interstellar visitors can also be the target for future exploration missions (the first ones traveling to an interstellar object; [Mamajek 2017](#)), become an indirect way to detect planetary systems of nearby stars and to infer some of their properties ([Trilling et al. 2017](#)) or help to test bold hypotheses about the origin and distribution of life in the Universe, such as lithopanspermia ([Adams & Spergel 2005](#); [Belbruno et al. 2012](#)).

Recently, [Engelhardt et al. 2017](#) calculated the number density of detectable interstellar objects, obtaining a discouraging value of $1.4 \times 10^{-4} \text{ au}^{-3}$ which seemed to restrict severely the chances of detecting one of these objects in the coming years, at least with the current available instrumentation. Nevertheless, on 19 October 2017 a small object with an uncommon orbit ($e = 1.1995 \pm 0.0002$ and $v_\infty = 26.33 \pm 0.03 \text{ km/s}$) was discovered using the PANSTARRS Survey ([Chambers et al. 2016](#)). The orbital properties determined at that time using a short orbital arc, while the object was still visible after their rapid passage through perihelion, suggested an interstellar origin. This result was supported by follow-up spectroscopic observations ([Bolin et al. 2018](#)) and other

theoretical considerations ([Ye et al. 2017](#); [Masiero 2017](#)). The interloper object has been now named “1I/2017 U1 (‘Oumuamua)” or simply ‘Oumuamua as we will call it consistently through this paper¹.

The first follow-up observations suggested that the object was of asteroidal origin, and its composition seemed to be similar to that of transneptunian objects (TNOs) ([Merlin et al. 2017](#)). More recently, [Jewitt et al. \(2017\)](#) measured the observed color and suggested a composition overlapping the mean colors of D-type Trojan asteroids and other inner solar system populations, but inconsistent with the ultra-red matter found in the Kuiper belt. [Ferrin & Zuluaga \(2017\)](#) compared the color of the object with other 21 active and extinct Solar System comets and suggest that ‘Oumuamua could actually be an inactive extrasolar comet. This result could be very important for assessing their dynamical origin. On the theoretical side, [Raymond et al. \(2017\)](#) suggested than from a dynamical standpoint it is more likely that ‘Oumuamua be cometary rather than asteroidal in origin.

Only a few days after the announcement of the discovery, several works attempting to pinpoint its interstellar origin were published in the form of research notes and short papers ([Mamajek 2017](#); [de la Fuente Marcos & de la Fuente Marcos 2017](#); [Gaidos et al. 2017](#); [Portegies Zwart et al. 2017](#); [Dybczyński & Królikowska 2017](#)). Most of these initial works were able to restrict the origin of the object to nearby stars and young planetary systems from which it could have escaped via planet-planet scattering. These early attempts, however, either rely on rough comparisons between the heliocentric entrance velocity

¹ IAU Minor Planet Center, 2017, U183

of the object and that of nearby stars (Mamajek 2017; Gaidos et al. 2017) and/or on the numerical propagation of the orbit of the object among many nearby stars, in the galactic potential (Portegies Zwart et al. 2017; Dybczyński & Królikowska 2017; Feng & Jones 2018). These latter efforts, however, originally lack of a rigorous consideration of the orbit uncertainties and the errors in the astrometric and radial velocities of the stars. A more rigorous kinematic treatment was recently presented by Feng & Jones (2018). However, their approach lack of a estimation of the probability that the object were originated in any of their potential progenitors. Several authors have even suggested that given the current orbital uncertainties and astrometric information about nearby stars, pinpointing the exact origin of ‘Oumuamua (and possibly other future interstellar objects) to a specific stellar system could be impossible (Zhang 2018).

The detection of ‘Oumuamua however, allowed some authors to update estimations of the number densities of interstellar objects and their detection probability. Thus, for instance, Trilling et al. 2017 recently determined that if during planet formation processes the ejected mass was about 20 Earth’s masses, the detection rate of such interstellar objects could be at least 0.2 per year with the current instrumentation. This result is consistent with the discovery of ‘Oumuamua. Moreover, when the Large Synoptic Survey Telescope (LSST, Ivezić et al. 2008) begins its wide, fast and deep all-sky survey, the rate could climb to 1 object per year. As a result, developing a general and kinematically rigorous strategy for assessing the origin of this and probably other objects detected in the future, is an important goal to pursue.

The problem of tracking small Earth’s impactors towards their progenitor objects in the Solar System has been extensively studied in the literature (see e.g. Strom et al. 2005; Zuluaga et al. 2013; Strom Robert et al. 2015; Zuluaga & Sucerquia 2018). However, the dynamic of the Solar System is well constrained. The timescales are relatively short and the the position of the perturbing objects are known to exquisite levels of precision. This is not the case when reconstructing the orbit of an interstellar object. Timescales are huge amplifying even small uncertainties in initial positions. The perturbing objects (stars) are very distant and small errors in their projected position in the sky correspond to large errors in their position in space. Moreover, the gravitational scattering from random encounters with nearby stars, may prevent a successful track-down of their origins. With the advent of new precise astrometric data such as that provided by Gaia, the situation is improving significantly.

Tracking the motion of objects in the interstellar space is not new. Several authors have studied the problem, aiming to determine the past and future close encounters of the Sun with nearby stars (See e.g. García-Sánchez et al. 2001; Bailer-Jones 2015; Berski & Dybczyński 2016). Of particular interest for this work is the recent paper by Bailer-Jones (2017) which use up-to-date astrometric and radial velocity catalogs to study this problem, while rigorously considering the uncertainties involved. The present paper is inspired and mostly based on the models, data and techniques developed in that work.

In this paper we present a general methodology and a computer tool designed for assessing the kinematic origin

of an interstellar object. Instead of determining which particular stellar system could be the source of a given object, the methodology presented here aims at computing “interstellar origin probabilities” (hereafter IOP) of many nearby stars. For that purpose our work takes into account rigorously the uncertainties in the object and stars kinematic properties. When more and better astrometric information become available, the values of the IOP computed with our methods and software can be improved.

This paper is organized as follows: in section 2 we outline the method. Sections 3-6 present the details of the implementation, while illustrating each technique in the particular case of ‘Oumuamua. Section 8 defines the concept of “Interstellar Origin Probability” and explains in detail how to compute it. The results of applying the methodology to the case of ‘Oumuamua are presented in section 9 including a list of the potential progenitors with their respective IOP. Section 10 is devoted at discussing the limitations of the method, but also its future potential as a general framework to study the orbit of newly discovered interstellar objects. Finally, in section 11 we present a summary of the paper and draw the main conclusions derived from it.

2. OUTLINE OF THE METHOD

Once a small-body is discovered in the Solar System, the astrometry and a reference orbit (computed from the observation weighting differences) is published by the Minor Planet Center (MPC). An up-to-date best-fit orbital solution of the astrometric data provided by the MPC is then computed and made available publicly in the JPL Small-Body Database Browser². The JPL orbit solution is provided in the form of a vector of “nominal orbital elements” $E_0 : (e_0, q_0, t_{p,0}, \Omega_0, \omega_0, i_0)$ (orbital eccentricity, perihelion distance, time of perihelion passage, longitude of the ascending node, argument of the perihelion and inclination, respectively) at a reference epoch t_0 . Along with this information, the JPL also provides the nominal mean orbital motion n_0 , and its standard errors σ_{n0} . The uncertainties in the orbital fit are characterized with an “orbit covariance matrix”, C_{jk} , defined as:

$$C_{jk} = \begin{cases} \sigma_j^2 & j = k \\ \rho_{jk}\sigma_j\sigma_k & j \neq k \end{cases} \quad (1)$$

where $j : e, q, t_p, \Omega, \omega, i$ and ρ_{jk} are the correlations among the orbital elements.

The question we seek to solve in this paper is if given this initial orbital information, in particular in the case of an unbound object ($e_0 > 1$), there exists an efficient method to compute the probability that a given star, whose position in the sky and velocity in space is known only approximately, be the progenitor of the small body.

In the following paragraphs we outline the method we devised to solve the origin probability problem of interstellar objects. The details of the method and the theory behind them are presented in the following sections. Of course, the method is not completely original and has its roots in preceding works, particularly on those of Zuluaga & Sucerquia (2018) and Bailer-Jones (2015, 2017).

² <https://ssd.jpl.nasa.gov/>

2.1. The method

To calculate the probability that a set of nearby stars be the progenitors of an interstellar object we follow this procedure:

1. Generate N_p clones of the orbital elements vector E of the interstellar object compatible with the latest orbital solution E_o and C_{jk} (see section 3). These clones describe the orbit of what we will call the “surrogate objects” (following the convention of Bailer-Jones 2017).
2. Integrate backwards the orbits of the surrogate objects, until a time when the object in the nominal orbit reaches a distance from the Sun where the galactic tides become relevant for the dynamic of the object (see section 4).
3. Using the “linear motion approximation” (LMA), identify the stars in an astrometric and radial velocity catalog, such that their minimum distance to the nominal object, $d_{\text{LMA},\text{min}}$, be less than or equal to a threshold distance. Stars identified with this procedure are called the “candidates” (see section 5).
4. For each candidate, compute a more precise encounter time t_{min} and minimum distance d_{min} by integrating the orbit of the star and the nominal object in the galactic potential (see section 6).
5. For each candidate star, generate N_s “surrogate stars” (hypothetical stars having astrometric properties compatible with the observed properties of the star and their errors). These new surrogates are used to calculate the “interstellar origin probability” (IOP) that the object comes from the selected star. IOP is roughly defined as the probability that the object had the same position as the surrogate star and a relative velocity of a magnitude compatible with reasonable ejection mechanisms. The probability is “corrected” by the present distance of the object to the surrogate star (see section 8).
6. Identify those candidates for which the more precisely computed minimum distances is below a tighter distance threshold and the IOP probability is the highest. We call these the “potential progenitors”.

All the potential progenitors identified with this procedure are tabulated in descending order of IOP probability (Table 4). The idea is not to select an individual star, but to assign a probability to each of them that can be improved with this method as the interstellar object and the stars itself are better known.

3. THE SURROGATE OBJECTS

Since the trajectory of the object is uncertain, and small errors inside the Solar System amplify when the orbit is integrated into the interstellar space, assessing its interstellar origin require than more than a single orbit (the nominal solution) be computed.

For this purpose we generate N_p vectors of orbital elements E compatible with the orbital solution described

with E_o and C_{jk} (see section 2). Random realizations of the orbital elements are computed using a multivariate gaussian random number generator³, having mean values equal to the nominal solution element vector E_o and covariance, equal to the orbit covariance published by JPL.

In Figure 1 we show the “ingress” position and velocity (see next section) of 1000 surrogate objects whose orbits were generated using this procedure. The strong correlation between the orbital parameters places the orbits of the surrogate objects in a very narrow ellipsoid which is projected in the sky at the time of ingress to the Solar System as a narrow line around the nominal radiant of the object (upper panel in Figure 1). The error in the present ‘Oumuamua’s orbital solution (JPL 15), propagates as an error in the position at the time of ingress (~ 2000 years before present) of ~ 7 AU (middle panel in Figure 1), and an error in its velocity of ~ 0.03 km/s (lower panel in Figure 1).

4. TRAJECTORY IN THE SOLAR SYSTEM

Once the orbital elements of the surrogate objects have been generated at the reference epoch, we proceed to calculate the trajectory of each object in the gravitational field created by the sun and the 8 planets⁴.

For that purpose we use a Gragg-Bulirsch-Stoer algorithm (Gragg 1965; Bulirsch & Stoer 1966) adapted from site⁵. Positions and velocities of the planets were not computed with the integrator itself, but using NASA NAIF SPICE software (Acton Jr 1996 and Jon D. Giorgini)⁶. For that purpose we use the latest DE431 planetary kernel. We verified that for the case of ‘Oumuamua our integrations were close to the precise solutions computed by the JPL Solar System Dynamics group and published in the on-line NASA Horizons system. A maximum error of 0.1% at back to 400 years before the reference epoch were obtained with our integrator.

Since the trajectory of the object is hyperbolic, and in the case of ‘Oumuamua, highly inclined with respect to the ecliptic ($i=122.6^\circ$), the object reached large distances to the Sun and the planets in relatively short times. Given the original uncertainty in the orbit, using the integrator to compute a very precise position of the surrogate objects within the Solar System is pointless. At some time in the past, the accumulated errors in the state vector (x, y, z, v_x, v_y, v_z) due only to the orbit uncertainty, will be much larger than the errors from assuming that the objects move in an ideal hyperbola.

Thus, for instance, in the case of ‘Oumuamua, we verified that at $t = -100$ years, the positions of the surrogate objects were spread inside an ellipsoid with a characteristic size of ~ 0.5 AU. On the other hand, the osculating elements of the object orbit at $t=-6$ years, when it was at ~ 40 AU from the Sun and above the ecliptic plane, allows us to predict the position at $t = -100$ years with

³ Most numerical libraries are provided with a multivariate random number generator. In the particular case of this work we use the generator and related routines provided by the GNU Scientific Library GSL (Galassi et al. 2002)

⁴ Although dwarf planets and major asteroids were not included in the integrations presented here, it is easy to add them in the iWander package provided with this work.

⁵ <http://www.mymathlib.com/>

⁶ <http://naif.jpl.nasa.gov/pub/naif>

an uncertainty of ~ 0.04 AU. We call the orbital elements at this point, the “asymptotic elements” and use them to compute the position of the object inside the Solar System in the far past. The value of the asymptotic elements for ‘Oumuamua along with other relevant information about its orbit in the Solar System are presented in Table 1.

Using the asymptotic orbital elements we calculate the position and velocity of the surrogate objects at arbitrary times in the past. However, when the object is at a distance comparable with the truncation tidal radius of the Solar System, $d_{T,\odot}$, the effects of the galactic potential in its motion cannot be neglected. We call this epoch the “time of ingress” t_{ing} . The interstellar orbit integration for the surrogate objects and stars, starts precisely at t_{ing} .

It is important to stress that the particular value assumed for $d_{T,\odot}$ does not modify considerably our final results and the conclusions of this work. In a numerical experiment we find that changing the value of $d_{T,\odot}$ from 10,000 AU to 100,000 AU introduces differences below 0.1% in the interstellar positions and velocities of the surrogate objects, an error which is much smaller than their intrinsic orbital uncertainties.

In Table 1 we present the time of ingress for ‘Oumuamua and its position and velocity in the ICRS galactic reference frame at that time. Our results are in agreement to those of Mamajek (2017).

In order to illustrate the effect that uncertainties in the orbit solution has in the predicted position of the object in the past, we show in Figure 1 the radiant in the sky of the surrogate objects at ingress time. We also plot the position in space of the objects in the ICRS galactic reference frame, their velocities in the same reference frame and their corresponding errors. The convention stands that (U, V, W) correspond to $(v_{\text{gal},x}, v_{\text{gal},y}, v_{\text{gal},z})$.

As commented before, even a small error in the orbital elements at the reference epoch are propagated as relatively large errors at the ingress time. While at $t = -100$ yrs the surrogate objects were contained in an ellipsoid with a characteristic size of 0.5 AU, at t_{ing} the surrogate objects have spread as a ~ 100 AU cloud (at this time the objects are by definition at a distance equivalent to the truncation radius, namely 50,000 AU). We have verified that this trend continues into the interstellar space, with a expansion velocity of ~ 0.05 km/s (the “size” of the cloud in the velocity UVW space, see bottom panel in Figure 1). At this rate, the cloud characteristic size will grow to ~ 2 pc (the typical distance between stars in the solar neighborhood) in ~ 40 Myr. Beyond this time, the cloud of surrogate objects will encounter at the same time more than one nearby star, and hence the reliability of our method will be compromised. We call this the “maximum retrospective time”, t_{ret} . In the case of ‘Oumuamua, $t_{\text{ret}} \sim 40$ Myr.

5. ASTROMETRIC AND RADIAL VELOCITY DATABASES

In order to compare the position of our interstellar object with the position of nearby stars in the far past, we need to know as precisely as possible the position and velocities of those stars at present time. For this purpose we have compiled up-to-date astrometric information (position, parallaxes, proper motion and radial velocities) of 285,114 stars (see Table 2).

Property	Value
Reference Epoch	2458059.5 TDB = 2017-Nov-02.0
Nominal elements (JPL 15)	$q = 0.255343194$ AU $e = 1.199512420$ $i = 122.687205$ deg $\Omega = 24.599211$ deg $\omega = 241.702983$ deg $M = 36.425313$ deg $\mu = 1.327124400 \times 10^{11}$ km ³ /s ²
Epoch of Asymptotic elements	2455736.51 TDB = JUN 24.01 2011
Asymptotic elements	$q = 0.252440118$ AU $e = 1.197253807$ $i = 122.735691$ deg $\Omega = 24.252921$ deg $\omega = 241.680101$ deg $M = -1544.878492$ deg $\mu = 1.327124400 \times 10^{11}$ km ³ /s ²
Asymptotic covariance $\times 10^{-6}$	Eccentricity $C_{ee} = 0.028$ $C_{eq} = 0.010$ $C_{et} = 7.558$ $C_{e\Omega} = -0.047$ $C_{ew} = 1.905$ $C_{ei} = 1.002$ Perihelion distance $C_{qq} = 0.004$ $C_{et} = 2.831$ $C_{q\Omega} = -0.018$ $C_{q\omega} = 0.714$ $C_{qi} = 0.375$ Periapsis time $C_{tt} = 4847.133$ $C_{t\Omega} = -14.358$ $C_{t\omega} = 514.030$ $C_{ti} = 271.891$ Long. ascending node $C_{\Omega\Omega} = 0.080$ $C_{\Omega\omega} = -3.205$ $C_{\Omega i} = -1.686$ Argument of periapsis $C_{\omega\omega} = 130.021$ $C_{\omega i} = 68.363$ Inclination $C_{ii} = 35.963$
Truncation radius	50000.0 AU
Time of ingress	8994.0 years
Radiant at ingress	$RA = 279.80 \pm 0.03$ deg $DEC = 33.99 \pm 0.01$ deg $l = 62.90 \pm 0.02$ deg $b = 17.11 \pm 0.02$ deg
Velocity at ingress	$U = -11.463 \pm 0.011$ km/s $V = -22.401 \pm 0.001$ km/s $W = -7.748 \pm 0.010$ km/s

TABLE 1
PROPERTIES OF THE ‘OUMUAMUA’S ORBIT IN THE SOLAR SYSTEM.

Compiling precise astrometric and radial velocity measurements for a significant number of nearby stars, is tricky. On one hand, precise astrometric databases such as Hipparcos (Perryman et al. 1997) and Tycho-2 (Høg et al. 2000) does not include radial velocities measurements. The Gaia mission have the potential to provide this information, but it will only be available since Data Release 2 (DR2) in April 2018⁷.

On the other hand, there are several public catalogs that provide precise radial velocities (see Table 2). However, not all the objects in those catalogs are included in the astrometric catalogs, and in some cases they

⁷ <https://www.cosmos.esa.int/web/gaia/release>

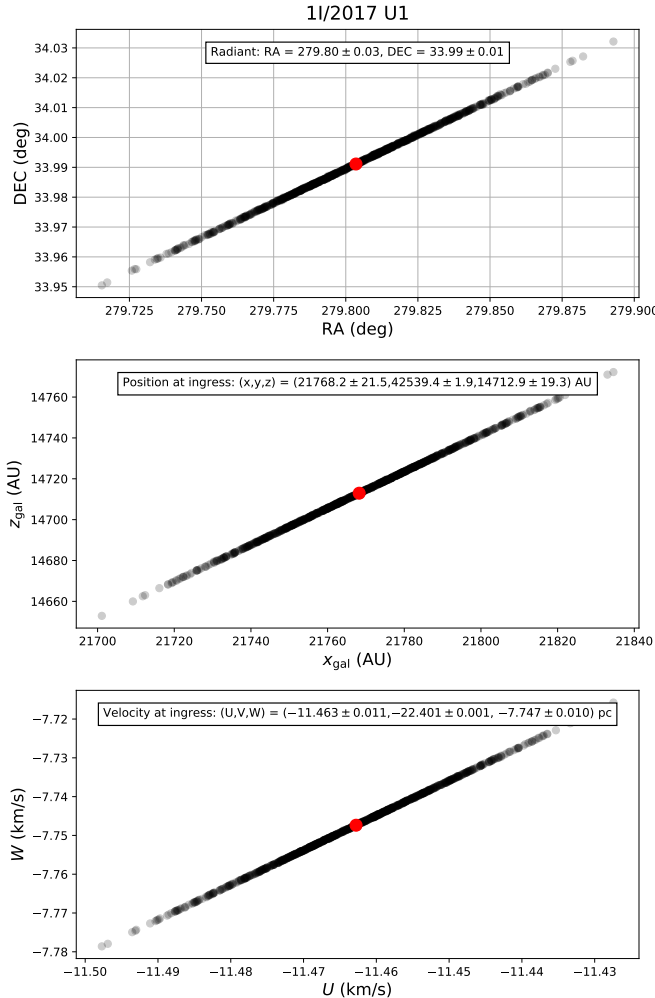


FIG. 1.— Dispersion in the position of the surrogate objects at the time of ingress into the Solar System. Right ascension, RA and declinations, DEC are referred to the Solar System Barycenter and the J2000 equinox. Galactic cartesian coordinates ($x_{\text{gal}}, y_{\text{gal}}, z_{\text{gal}}$) and velocities (U, V, W) are referred to the ICRS galactic system of reference.

have unique identifications without any reference to the Hipparcos/Tycho-2 ids, which are to the date of writing this paper, the identification for objects having precise astrometric measurements (either from the Hipparcos or the Gaia mission).

We compile the information required for this work following the detailed directions recently published by Bailer-Jones 2017. Additionally, and in order to include nearby bright stars (which were not included in the Gaia catalog) we search for other information about the Hipparcos stars in the *Simbad* information system⁸.

The importance of having this information in a properly-structured table, led us to create the so-called *AstroRV* catalog (astrometric and radial velocities catalog). The catalog is provided with the *iWander* package developed for this work.

For the sake of completeness and reproducibility we outline below the procedure required to compile the *AstroRV* catalog:

⁸ <http://simbad.u-strasbg.fr/simbad/>

1. Get available astrometric and radial velocities catalogs. In Table 2 we summarize the information of the catalogs we use for this work. The most important one is the Gaia DR1 catalog containing over 1 billion objects (Brown et al. 2016). Among those objects, however, only 2,026,210 were previously included in Hipparcos and Tycho-2 catalogs and a full astrometric solution (with a positive parallax) was obtained (Gaia TGAS catalogue). Among them, 93,398 are in the Hipparcos catalog and 1,932,812 belongs to the Tycho-2 catalog.
2. Obtain the general information available in *Simbad* for all the stars having an Hipparcos ID. The information includes other designations for the stars (Henry Draper catalog id and proper names for the bright stars) and radial velocities for some of those stars.
3. Find all the objects in the Hipparcos and Tycho Catalogues (ESA 1997) and in the *Simbad* table compiled before, that are not included in the GAIA TGAS catalog. Append the resulting objects to the latest catalog to create a final table with all the available astrometric information.
4. Create a table including all objects in the radial velocities catalogs that have Hipparcos and/or Tycho-2 ids. For those objects not having any of those ids, find the Hipparcos/Tycho-2 objects matching the coordinates within a 50 arcsec radius (we use for this purpose the X-match tool of *Simbad*). For detailed instructions about how to compile the available radial velocity catalogs please refer to Bailer-Jones (2017).
5. Merge the astrometric and radial velocity tables according to the Hipparcos/Tycho-2 ids.

The catalog compiles with this procedure contains 285,114 stars including the nearest and brightest ones. We provide with the *iWander* package the required scripts for creating the catalog as described before. Those scripts can be modified to include future radial velocity and astrometric catalogs, or to update the information in older versions. An up-to-date version of the *AstroRV* catalog will be available at the *iWander* GitHub repository⁹.

6. TRAJECTORIES IN INTERSTELLAR SPACE

Having the position and velocity of both, the surrogate objects and the nearby stars, we now may integrate their orbits backward in time to identify any close approach. Since we need to perform a comparison between the position of at least $\sim 1,000$ surrogate objects with $\mathcal{O}(10^5)$ stars, computing times may become prohibitively large. In a first step we perform a selection of “candidate stars” using the so-called “linear motion approximation” (LMA).

6.1. The LMA approximation

Under this approximation, all particles, the surrogate objects and the stars, move in straight lines:

⁹ <http://github.com/seap-udea/iwander.git>

Catalog name	Number of objects	Hipparcos ID	Tycho-2 ID	Contribution	CDS Code	Reference
Astrometric						
Gaia TGAS	2026210	93398	1932812	2026210	I/337/tgas	(1)
Hipparcos	117955	117955	–	24557	I/239/hip_main	(2)
Tycho	579054	–	579054	164550	I/259/tyc2	(2)
Simbad	118004	118004	–	67	--	(3)
Totals	2841223	329357	2511866	2215384	This work	
Radial velocities						
WEB1995	1167	494	673	252	III/213	(5)
GCS	14139	12977	–	7091	J/A+A/530/A138	(6)
RAVE-DR5	520701	121	309596	217257	III/279/rave_dr5	(7)
PULKOVO	35493	35493	–	23412	III/252/table8	(8)
FAMAIEY2005	6028	6028	–	5544	J/A+A/430/165/tablea1	(9)
BB2000	673	–	673	503	III/213	(10)
MALARODA	2032	–	2032	416	III/249/catalog	(11)
GALAH	10680	–	10680	7837	J/MNRAS/465/3203	(12)
MALDONADO	473	473	–	301	J/A+A/521/A12/table1	(13)
APOGEE2	29173	–	29173	22501	--	(14)
AstroRV	620559	55586	352827	285114	This work	

TABLE 2

CATALOGS USED TO COMPILE THE **AstroRV** CATALOG FOR THIS WORK. REFERENCES: (1) [BROWN ET AL. 2016](#), (2) [ESA 1997](#) (3) [WENGER ET AL. 2000](#), (5) [BARBIER-BROSSAT & FIGON 2000A](#), (6) [CASAGRANDE ET AL. 2011](#), (7) [KUNDER ET AL. 2017](#), (8) [GONTCHAROV 2006](#), (9) [FAMAIEY ET AL. 2005](#), (10) [BARBIER-BROSSAT & FIGON 2000B](#), (11) [MALARODA ET AL. 2000](#), (12) [MARTELL ET AL. 2016](#), (13) [MALDONADO ET AL. 2010](#), (14) [BAILER-JONES 2017](#).

$$\vec{r}_i(t) = \vec{r}_{i,0} + \vec{v}_{i,0}t$$

Here, \vec{r}_i ($\vec{r}_{i,0}$) and \vec{v}_i are the position and velocity of the i -th particle. The instantaneous distance between particles j and k (surrogate objects and stars), is given by:

$$|\Delta\vec{r}_{jk}(t)|^2 = |\Delta\vec{r}_{jk,0} + \Delta\vec{v}_{jk,0}t|^2 = |\Delta\vec{r}_{jk,0}|^2 + 2\Delta\vec{r}_{jk,0} \cdot \Delta\vec{v}_{jk,0}t + |\Delta\vec{v}_{jk,0}|^2t^2$$

where $\Delta\vec{r}_{jk,0} = \vec{r}_{j,0} - \vec{r}_{k,0}$ and $\Delta\vec{v}_{jk,0} = \vec{v}_{j,0} - \vec{v}_{k,0}$. This function has a minimum when $d|\Delta\vec{r}_{jk}(t)|^2/dt = 0$, ie. at the time $t_{jk,\min}$ when the distance between the objects is $d_{jk,\min}$:

$$t_{jk,\min} = -\frac{\Delta\vec{r}_{jk,0} \cdot \Delta\vec{v}_{jk,0}}{|\Delta\vec{v}_{jk,0}|^2} \quad (2)$$

$$d_{jk,\min} = |\Delta\vec{r}_{jk}(t_{\min})|$$

We compute $t_{jk,\min}$ and $d_{jk,\min}$ for the nominal object and all the stars in our **AstroRV** in order to select the “candidate stars”, namely those stars that could actually have close encounters with the object. After numerically testing several criteria, we found that the most cost-effective (in terms of computational resources in the succeeding steps), albeit simple condition is:

$$d_{jk,\min} < \sup \left\{ d_{\max}, \frac{1}{5}d_0 \right\} \quad (3)$$

where d_{\max} is an arbitrary distance threshold, d_0 is the present distance of the star and the $1/5$ is an adjustable numerical factor. For our present analysis we assume $d_{\max} = 10$ pc.

It should be stressed that with an arbitrary amount of computational resources all the stars in the **AstroRV** catalog could be integrated in the galactic potential (see next section) and no heuristic selection criterion (such as that in [Equation 3](#)) need to be used. This criterion is only intended to save computational resources.

In the case of ‘Oumuamua we have found that after applying the criterion in [Equation 3](#), only 2560 among the 285114 stars in the input catalog, were selected as candidates (see red circles in [Figure 2](#)). We verified with full simulation (including only the nominal object and stars) that only a handful of suitable candidates (blue triangles in [Figure 2](#)) were excluded from the probability calculations.

For each “candidate star” selected with the preceding criterion, we should convert their observed properties (RA, DEC, $\varpi, \mu_\alpha, \mu_\delta, v_r$) (right ascension, declination, parallax, projected proper motion in RA, proper motion in declination and radial velocity, respectively) into its spatial cartesian coordinates in the galactic system, $(x_{\text{gal}}, y_{\text{gal}}, z_{\text{gal}}, U, V, W)$ (and more importantly their corresponding uncertainties). We use for this purpose the prescription [Johnson & Soderblom 1987](#).

6.2. Motion in the galactic potential

As mentioned before, the minimum LMA distances are useful at selecting the candidates but are a very crude approximation of the actual encounter conditions. The integrated effect of the galactic potential may modify substantially the position of the objects and the stars, especially after a long time of wandering in the interstellar space.

In order to obtain a “second order” estimation of the minimum distances, we need to integrate the trajectory of the surrogate objects and the stellar candidates in the galactic potential. Given the axisymmetric nature of the potential, we need to transform the cartesian coordinates of the objects with respect to the Sun $(x_{\text{gal}}, y_{\text{gal}}, z_{\text{gal}}, U, V, W)$ to cylindrical coordinates referred to the galactocentric reference system (see [Figure 3](#)). This coordinate transformation is achieved in three steps:

1. Convert the position and velocities referred to the local standard of rest (LSR) into position and velocities relative to the galactic center:

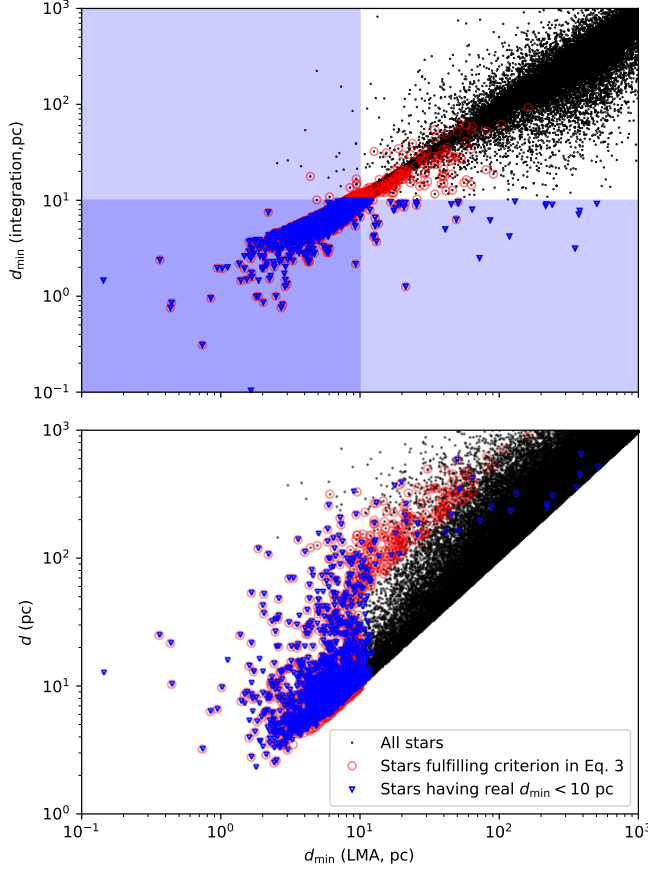


FIG. 2.— Minimum encounter distances for the nominal orbit of ‘Oumuamua and all the stars in the *AstroRV* catalog (black dots), calculated with the LMA approximation (horizontal axis) and with a precise galactic potential integration (vertical axis of the upper panel). Blue triangles represent the potential progenitors selected from their precise minimum distance, ie. $d_{\min} < 10$ pc; red circles mark the position of the stars fulfilling the heuristic selection criteria in Equation 3. The lower panel is intended to illustrate the way as this criterion was especially devised to minimize the number of actual potential progenitors that are missed when using only the LMA approximation (blue triangles without a corresponding red circle).

$$\vec{v}_{\text{GC}} = \vec{v}_{\text{gal}} + \vec{v}_{\odot} + v_{\text{circ}} \hat{y}_{\text{gal}}$$

$$\vec{r}_{\text{GC}} = \vec{r}_{\text{gal}} - R_{\odot} \hat{x}$$

where $\vec{v}_{\text{gal}} : (U, V, W)$ is the velocity of the star with respect to the Sun in galactic coordinates, $\vec{v}_{\odot} : (U_{\odot}, V_{\odot}, W_{\odot})$ is the velocity of the Sun with respect to the local standard of rest (LSR) and v_{circ} is the local circular galactic velocity. In Table 3 we show the values adopted in this work for these quantities.

2. \vec{v}_{GC} and \vec{r}_{GC} are referred to a system pointing to the galactic center (the unprimed $x_{\text{gal}}, y_{\text{gal}}, z_{\text{gal}}$ in Figure 3). This system is rotated at an angle $\alpha = \sin^{-1}(z_{\odot}/R_{\odot})$ with respect to the plane of the Galaxy. Thus, the actual physical galactocentric coordinates on which we must perform the orbital integration are obtained after the rotation:

Property	Value	Reference
U_{\odot}	11.1 km/s	(1)
V_{\odot}	12.24 km/s	(1)
W_{\odot}	7.25 km/s	(1)
v_{circ}	220.0 km/s	(2)
z_{\odot}	17 pc	(3)
R_0	8.2 kpc	(3)
M_d, a_d, b_d	$7.91 \times 10^{10} M_{\odot}, 3500 \text{ pc}, 250 \text{ pc}$	(4)
M_b, a_b, b_b	$1.40 \times 10^{10} M_{\odot}, 0, 350 \text{ pc}$	(4)
M_h, a_h, b_h	$6.98 \times 10^{11} M_{\odot}, 0, 24000 \text{ pc}$	(4)

TABLE 3
PROPERTIES OF THE GALAXY. REFERENCES: (1) SCHÖNRICH ET AL. 2010, (2) BOVY 2015, (3) KARIM & MAMAJEK 2016, (4) BAILER-JONES 2015.

$$\vec{r}'_{\text{GC}} = R_{\alpha} \vec{r}_{\text{GC}}$$

$$\vec{v}'_{\text{GC}} = R_{\alpha} \vec{v}_{\text{GC}}$$

with

$$R_{\alpha} = \begin{pmatrix} \cos \alpha & 0 & \sin \alpha \\ 0 & 1 & 0 \\ -\sin \alpha & 0 & \cos \alpha \end{pmatrix}$$

3. Finally, we need to express the resulting galactocentric position and velocity in cylindrical coordinates, ie. $\vec{r}'_{\text{GC}} : (R, \theta, z)$, $\vec{v}'_{\text{GC}} : (\dot{R}, R\dot{\theta}, \dot{z})$.

In this coordinate system, the equations of motion of an object moving in the potential of the galaxy $\Phi(R, \theta, z)$ are given by (see eg. García-Sánchez et al. 2001):

$$\begin{aligned} \ddot{R} &= -\frac{\partial \Phi}{\partial R} + R\dot{\theta}^2 \\ \ddot{\theta} &= -\frac{\partial \Phi}{\partial \theta} - 2\frac{\dot{R}\dot{\theta}}{R} \\ \ddot{z} &= -\frac{\partial \Phi}{\partial z} \end{aligned} \quad (4)$$

Here we assume for simplicity an axisymmetric Kuzmin-like potential for the three galactic subsystems (Kuzmin 1956; Miyamoto & Nagai 1975), disk (d), bulge (b) and halo (h):

$$\Phi(R, \theta, z) = - \sum_{i=d,b,h} \frac{GM_i}{\sqrt{R^2 + (a_i + \sqrt{z^2 + b_i^2})^2}} \quad (5)$$

The value of the potential parameters M_i, a_i, b_i assumed for each component are summarized in Table 3

Once the trajectory of the objects in the potential of the Galaxy are integrated, we proceed at finding the encounter distance and time of the nominal object to each stellar candidate. This is a refined estimation of d_{\min} and t_{\min} .

7. THE SURROGATE STARS

In the same way as we generate N_p surrogate objects to take into account the uncertainties in the orbit solution of the interstellar interloper, we need to generate, for each stellar candidate, N_s “surrogate stars” with

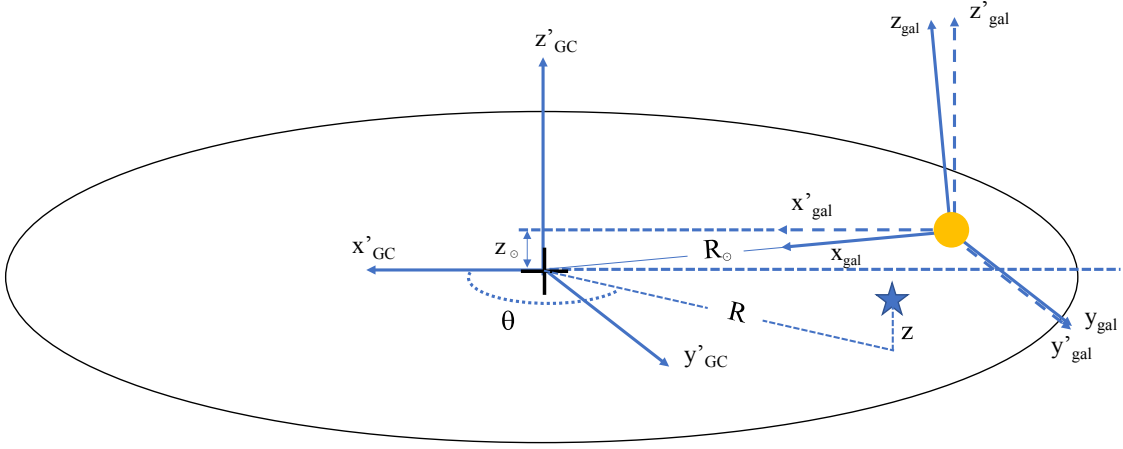


FIG. 3.— Galactic Reference Systems.

observed properties compatible with the nominal astrometric observables, namely $(\alpha_0, \delta_0, \varpi_0, \mu_{\alpha,0}, \mu_{\delta,0})$. For this purpose we build a covariance matrix (see Equation 1) using the errors reported for each astrometric variable and their related correlations¹⁰.

Summarizing the previous sections, studying the coincidence in time and space of an interstellar object with a nearby star, implies dealing properly with the kinematics of N_p surrogate objects and N_s surrogate stars. It is quite evident that assessing the probability of a close encounter, using just the nominal solutions for the object and the stars is certainly unrealistic.

8. INTERSTELLAR ORIGIN PROBABILITY

The question that originally motivates this work was how to compute the probability that a star with present astrometric properties $(\alpha, \delta, \varpi, v_r)$ has ejected in the past, a body that entered into the solar system with heliocentric orbital elements $(q, e, i, \Omega, \omega, t_p)$ at a given reference epoch t_0 .

If both, the astrometric position of a star and the orbital elements of the interstellar object were known with no uncertainties, the question could be answered by integrating backward the orbits of the object and the star, as described in the preceding sections, and verifying if they coincide in space at some point in the past. However, with uncertain initial conditions, assessing the probability is non-trivial. Even if the nominal trajectories of the object and the star do not coincide, there is a non-zero probability that they were actually related.

Let's assume first that the orbit of the interstellar object is known with zero uncertainty. If we propagate all the surrogate stars until the time of minimum distance between the object and the nominal star, t_{\min}^{nom} , the object will be surrounded by a cloud of points (see Figure 4), each one representing the position of one surrogate star at that time. In the continuous limit, even if none of the N_s surrogate stars coincide in position with the object, a probability different than zero exists that they

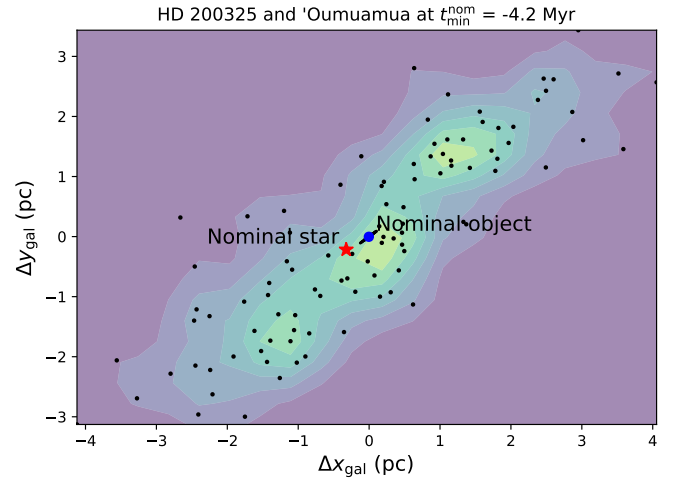


FIG. 4.— Scattering plot of the position of the surrogate stars corresponding to HD 200325 (red star marks its nominal position) at the time of minimum distance with the nominal object (blue dot). Contours show the number density of stars around the object estimated with the methods in this work.

were related. Our central assumption here is that the probability that such a relationship actually existed will be proportional to the density of surrogate stars at the position of the object.

Computing the number density from a discrete set of positions of the surrogate stars, is challenging. Several numerical techniques have been devised and applied in other areas such as cosmology and hydrodynamics (see eg. Price 2012), to assess similar problems. More recently, Zuluaga & Sucerquia 2018 applied the approach used in Smooth Particle Hydrodynamics in the context of impact probabilities in the the Solar System. According to this approach, the number density of stars around an object with position \vec{r}_p can be computed as:

$$n(\vec{r}_p) = \sum_i^{N_s} W(|\vec{r}_p - \vec{r}_{*i}|, h) \quad (6)$$

where $|\vec{r}_p - \vec{r}_{*i}|$ is the distance between the object and the i th surrogate star, h is a distance-scale for the distri-

¹⁰ In the Hipparcos and Gaia databases, correlations are reported in the form of fields such as RA_DEC_CORR, RA_PARALLAX_CORR, etc.

bution, and $W(d, h)$ is called a *smoothing kernel*. In this work we use for h , the characteristic size of the solar-mass truncation radius, namely $h \approx 0.5$ pc. Other prescriptions can be used, but for the purpose of testing our method we will restrict to this simple ansatz.

Different kernel function can be used for calculating n as precisely as possible. Although it is common in SPH to use a *B-spline kernel* (see eg. Zuluaga & Sucerquia 2018), for the purposes pursued here, the best suited function is one that provide a non-zero, although still very low value of $n(\vec{r}_p)$ for large values of $|\vec{r}_p - \vec{r}_{*i}|$. The kernel function used in this work will be a gaussian one (Price 2012):

$$W(d, h) = \sigma \exp(-d^2/h^2) \quad (7)$$

where $\sigma = (\int W dV)^{-1}$ is a normalization constant.

We assume that the probability that the candidate star be at t_{\min}^{nom} inside a small volume dV around the object position will be given by:

$$p(\vec{r}_p)dV = \frac{n(\vec{r}_p)dV}{N_s} \quad (8)$$

Since the number density in Equation 6 has by definition the property $\int n dV = N_s$, the probability density function in Equation 8 is properly normalized.

In the discrete case, if we take ΔV as the volume of the surrogate objects cloud at t_{\min} , the probability of a coincidence in position (hereafter “position probability”), P_{pos} between star and the interstellar object at that specific time, can be estimated as:

$$P_{\text{pos}} \approx \frac{n(\vec{r}_p)\Delta V}{N_s} \quad (9)$$

The position probability will depend on the particular values assumed for t_{\min} and d_{\min} . In Figure 4, for instance, we show the configuration resulting in the case of the nominal encounter parameters, t_{\min}^{nom} and d_{\min}^{nom} . However, if the actual star would not have the nominal astrometric parameters, the encounter would occur at a different set of conditions; it could, for instance, occur at the time $t_{\min,i}$ and minimum distance $d_{\min,i}$ corresponding to the i th surrogate star. If we calculate the value of $P_{\text{pos},i}$ for the encounter conditions of each surrogate star, the probability of a coincidence in position between the interstellar object and the star can be estimated as:

$$P_{\text{pos}} \approx \frac{1}{N_s} \sum_i P_{\text{pos},i} \quad (10)$$

The fact that the position of the object and the star coincide in space does not guarantee that the object be ejected from an hypothetical planetary system around it. Thus, for instance, if ‘Oumuamua reaches another stellar system in the future, their inhabitants may think that the Solar System is the progenitor of the object.

There are actually two additional factors constraining the origin probability: the relative velocity and the stellar distance.

8.1. Relative velocity

Only a few processes may lead to the ejection of a small body from an almost-isolated planetary system

(Melosh 2003; Napier 2004). In the low density solar neighborhood the more feasible ejection mechanisms are the particle-particle gravitational scattering, where small bodies receive a gravitational slingshot effect after encountering a planet or even a star in a multiple stellar system, at the right conditions (Raymond et al. 2017; Čuk 2018; Wiegert 2014). We estimate the distribution of excess velocities, v_{∞} , that small bodies (asteroids and comets) receive from their encounters with a giant planet around a solar mass star, using a semi analytical approach inspired in the works by Wiegert (2011, 2014).

For this purpose, we first set up a planetary system having a single planet of mass M_p located in a circular orbit with semimajor axis a_p . We randomly generate orbital elements for small bodies such that they intersect the orbit of the planet. For simplicity the small-body semimajor axis, eccentricity and orbital inclinations were uniformly generated in the whole range of possible values, eg. $a \in (0.5a_p - 1.5a_p)$, $e \in (0, 1)$, $i \in (0, 90)$ deg. Longitude of ascending node and argument of periapsis were calculated imposing the condition that the small body and the planet collide.

For each planet-small body orbit configuration we compute the relative velocity with which they encounter and the direction with respect to the planet reference frame from which the small body approaches. From here we follow the prescription of Wiegert (2011) to compute the outbound velocity of the object after interacting with the planet. A random position (x_p, y_p) over the tangent plane to the Hill sphere is generated (see Figure 1 in Wiegert 2014). From there we compute the impact parameter, scattering angle, planetocentric orbital eccentricity and periapsis distance. Finally we rotate the planetocentric inbound velocity to compute the outbound velocity of the small-body at the Hill radius with respect to the planet and then with respect to the star.

Once the synthetic small bodies in our simulation are scattered by the planet, we evaluate if their outbound velocity v with respect to the star is larger than the escape velocity v_{esc} at the position of the planet. If this is the case, we compute the excess velocity, $v_{\text{inf}}^2 = v^2 - v_{\text{esc}}^2$.

In Figure 5 we show the distribution of excess velocities resulting from the interactions of small bodies with planets of different mass M_p located in a circular orbit $a_p = 5$ AU around a solar mass-star. The results are given in canonic units for which we have set $G = 1$, $u_L = 1$ AU and $u_M = 1 M_{\odot}$. In these units, $u_T = \sqrt{u_L^3/(Gu_M)}$, and $u_L/u_T = 30$ km/s.

An interesting advantage of expressing the results in canonic units is that they can be used to predict ejection velocities distribution from planetary systems around stars of arbitrary mass. Thus, for instance, the average ejection velocity for a planet with the mass of Jupiter around a solar mass star, $u_M = 1 M_{\odot}$, $M_p = 0.001 u_M$ is $\bar{v}_{\infty} = 0.2 u_L/u_T$, or 6 km/s (see the leftmost curve in Figure 5). If we consider now an early M-dwarf with mass $M_{\star} = 0.5 M_{\odot}$, the same results in Figure 5 will apply, but now for the case of a planet with half the mass of Jupiter. The value of \bar{v}_{∞} in km/s, will depend on what value is assumed for u_L . If we take $u_L = 1$ AU (as in the case of the solar-mass star), then $u_L/u_T = 20$ km/s for the early M-dwarf, and the average ejection velocity will be 4 km/s.

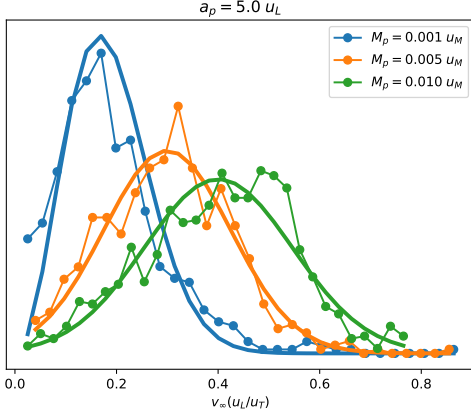


FIG. 5.— Ejection velocity distribution for a planet in a circular orbit at $a_p = 5.0 u_L$ and different planetary masses. Continuous thick lines are Maxwell-Boltzmann distributions with the same mean as the numerical results.

In Figure 6 we show contours of \bar{v}_∞ in the $a_p - M_p$ plane. We discover that for masses below $10^{-3} u_M$ ejection velocities are only a function of planetary orbital distance and are very insensitive to planetary mass.

Another interesting result from our semi analytical experiments is that the ratio of the standard deviation σ_{v_∞} to the mean value of the ejection velocity \bar{v}_∞ , is almost independent of planetary orbital distance. For its dependency on planetary mass, in the lower panel of Figure 6 we show a plot of the value of $\sigma_{v_\infty}/\bar{v}_\infty$ for different planetary masses. It is interesting to notice that in the case of a Maxwell-Boltzmann distribution (MBD) the ratio σ/μ (with μ the mean) is constant and equal to 0.42 which is of the order of $\sigma_{v_\infty}/\bar{v}_\infty$ in our own experiments. This seems to suggest that the ejection velocities can be fitted by a MBD with a mean that depends on M_p and a_p . This is precisely the fitting functions we have used in Figure 5.

Using the average ejection velocities and the dispersion-to-mean ratio in Figure 6, we can estimate the velocity distribution of small-bodies being ejected from a planetary system around a star of a given mass. Since ejection velocities depend on the unknown mass M_p and semimajor axis a_p of the largest planet in the system, we estimate the “posterior” ejection velocity probabilities, assuming for simplicity uniform “priors” for these quantities. The resulting posterior distribution $p_{v_\infty}(v)$ for the case of a solar-mass star is shown in Figure 7.

Returning back to our original problem, we may now ask, which is the probability that an object be ejected from a star with velocity around $\vec{v}_{\text{rel}} = \vec{v}_p - \vec{v}_*$? Assuming that the ejection from the stellar system is isotropic (as suggested in the Solar System from the geometry of the Oort cloud, see e.g. [Emel'Yanenko et al. 2007](#) and references therein), the desired probability will be given by:

$$p(\vec{v}_{\text{rel}})d\vec{v}_{\text{rel}} = v_{\text{rel}}^2 p_{v_\infty}(v_{\text{rel}}) dv_{\text{rel}} d\Omega_v \quad (11)$$

where $d\Omega_v$ is a differential solid angle in the velocity space.

In the discrete limit:

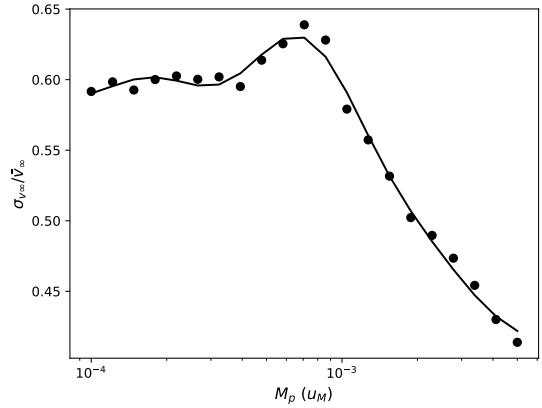
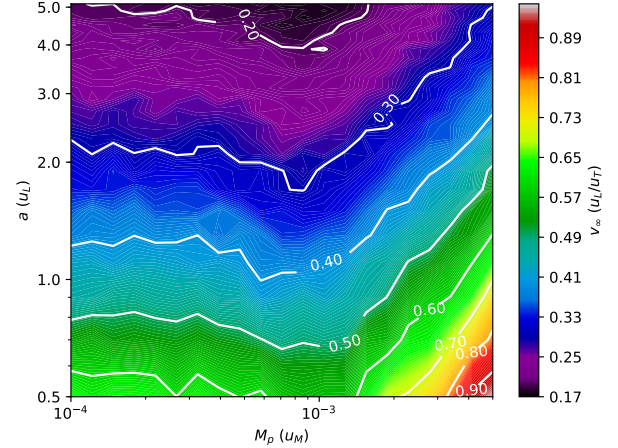


FIG. 6.— Upper panel: ejection mean velocity for different planetary masses and orbital sizes. Lower panel: ratio of the average to the standard deviation of the ejection velocities for different planetary masses. Properties are given in canonic units. If $u_L = 1 \text{ AU}$ and $u_M = 1 M_\odot$, $u_v = u_L/u_T = 30 \text{ km/s}$.

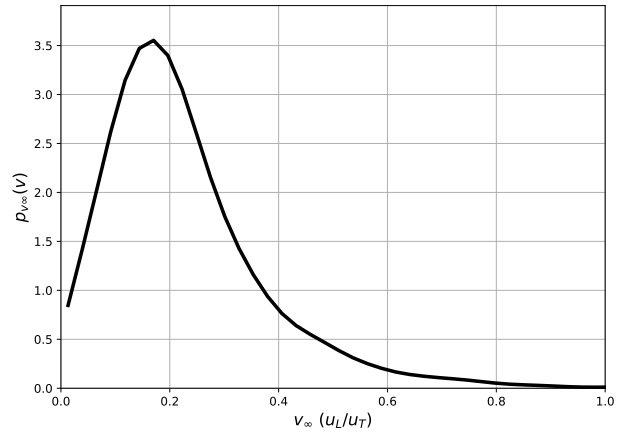


FIG. 7.— Ejection velocity posterior distribution as estimated in this work.

$$P_{\text{vel}}(\vec{v}_{\text{rel}}) \approx v_{\text{rel}}^2 p_{v\infty}(v_{\text{rel}}) \Delta|\vec{v}_{\text{rel}}| \Delta\Omega_v \quad (12)$$

where $\Delta|\vec{v}_{\text{rel}}|$ is dispersion of the magnitude of relative velocities for the cloud of surrogate objects with respect to the nominal star, $\Delta\Omega_v$ is the solid angle enclosing those relative velocities and $p_{v\infty}(v)$ is the posterior distribution of ejection speeds in Figure 7.

The joint probability $P_{\text{vel,pos},i}$ that the interstellar object has relative velocity \vec{v}_{rel} with respect to the i th surrogate star, and that their position coincide, is given by the conditional probability formula:¹¹

$$P_{\text{vel,pos},i} = P_{\text{vel}}(\vec{v}_{\text{rel},i})P_{\text{pos},i} \quad (13)$$

Integrating over the whole set of surrogate stars results in:

$$P_{\text{vel,pos}} \approx \frac{1}{N_s} \sum_i P_{\text{vel}}(\vec{v}_{\text{rel},i})P_{\text{pos},i} \quad (14)$$

8.2. Stellar distance

If we assume again that objects are ejected isotropically from the planetary system, the probability that an ejected object crosses the Solar truncation radius $R_{\text{T},\odot}$ while the star is at a distance d_* will be simply given by $(R_{\text{T},\odot}/d_*)^2$.

Moreover, if we consider that the object entered into the Solar System inside a solid angle $\Delta\Omega_{\text{ing}}$, the probability of an object be “transferred” from the stellar system, towards the Solar System will be given by,

$$P_{\text{dis}} \approx \frac{\Delta\Omega_{\text{ing}}}{4\pi} \left(\frac{R_{\text{T},\odot}}{d_*} \right)^2 \quad (15)$$

With all these elements at hand the interstellar origin probability of a given object will be:

$$P_{\text{IOP}} \approx P_{\text{vel,pos}}P_{\text{dis}} \quad (16)$$

9. RESULTS

As an illustrative example (not necessarily the best one, but the only to date), we apply our methodology to assess the interstellar origin of ‘Oumuamua. In Table 4 we present a list of the potential progenitors satisfying the conditions $t_{\text{min}}^{\text{nom}} < t_{\text{Ret}} \approx 40$ Myr and $d_{\text{min}}^{\text{nom}} < 2$ pc. For each progenitor we present several statistics of the encounter conditions, namely, encounter time t_{min} , minimum encounter distance d_{min} , and relative velocity v_{rel} . Along with the nominal value of these quantities (first row of each entry) we provide the value of the 10%, 50% (median) and 90% percentiles. In the last column of the table the value of the IOP is reported. For reference, we also provide the value of the separate probability contributions, namely, position P_{pos} (Equation 9), velocity P_{vel} (Equation 12), join velocity-position $P_{\text{vel,pos}}$ (Equation 14) and distance probability contribution P_{dis} (Equation 15). For clarity, in all cases we report the logarithm of the probabilities and their contributions.

For reference, the present distance d_* to each progenitor is also provided. To give an idea of the astrometric uncertainties involved in the calculation of the origin probability, we have tabulated for each potential progenitor, an “astrometric quality index” q , defined as the minimum ratio between the value of each astrometric key property (parallax, proper motion and radial velocity) and its standard error. Thus, a quality factor of 1 implies that one of these quantities has an error of the same order than its magnitude (relatively poor astrometry). On the other hand, a large q -value are indicative of the availability of very precise astrometric properties (including radial velocity).

With the available information, we have identified only 16 potential progenitors for ‘Oumuamua fulfilling all the selection criteria. Most of the potential progenitors have moderately large q -values and are located at distances beyond 5 pc. As expected the IOP probability has achieved at selecting candidates with moderate relative velocities and encounter distances between 0.2 and 5 pc (with a few exceptions, eg. TYC 7582-1449-1 that has a poor astrometry).

Although the value of the IOP probability for all potential progenitors is very small $\mathcal{O}(10^{-30})$, it should be taken into account that for having a properly normalized probability, several small factors are involved in the IOP calculation. Thus, for instance, the ingress solid angle (Equation 15) is of the order of $\Delta\Omega_{\text{ing}} \sim 5 \times 10^{-8}$ while the velocity solid angle in Equation 12 is typically $\Delta\Omega_v \sim 10^{-6}$. The dispersion in relative speeds in the same equation is $|\Delta\vec{v}_{\text{rel}}| \sim 10^{-3}$ km/s, while the volume occupied by the cloud of surrogate objects (Equation 9) varies from $\Delta V \sim 10^{-8}$ pc³ for encounters happening at recent times and $\Delta V \sim 10^{-7}$ pc³ for those at earlier epochs (it should be recalled that although the cloud of objects expand from several AU at the time of ingress into the solar System to ~ 2 pc at ~ 40 Myr, it preserve an elongated and thin shape at all times). This result stresses the fact that the IOP is useful only at sorting the potential progenitors, rather than at conclusively demonstrating the origin of an interstellar object in a particular stellar system. More interestingly, if the origin of an object is probed with an independent method the way as the IOP is defined could actually provide a way to estimate the total number of ejected particles from that particular system which will be roughly $\sim 1/\text{IOP}$.

The method presented here does not necessarily intend to identify a single object as the actual progenitor of ‘Oumuamua. Finding the origin would require follow-up observations of the interstellar object (while reachable), and improving the astrometric properties of the potential progenitors. When more and better information be available about these and other stars, the list could be extended or reduced, and more importantly the IOP probability could be modified.

Still, it is interesting to notice the properties of several of these progenitor candidates. The most interesting case is of course that of HD 200325 (HIP 103749), the first object in the list. The star is probably a double or multiple system (Cvetković 2011). It is located at the present at a distance of 53.8 pc from the Sun and their physical properties are well constrained (see eg. Cvetković 2011; Holmberg et al. 2007). Its radial velocity has been mea-

¹¹ $P(\text{velocity} \wedge \text{position}) = P(\text{velocity}|\text{position})P(\text{position})$.

Basic properties				Encounter conditions			log P				
#	Name	d_* (pc)	q	t_{\min} (Myr)	d_{\min} (pc)	v_{rel} (km/s)	P_{pos}	P_{vel}	$P_{\text{pos,vel}}$	P_{dist}	IOP
1	HIP 103749 (HD 200325)	53.8	1	-4.22	1.75	12.0	-8.1	-9.2	-17.2	-13.1	-30.3
2	TYC 7069-1289-1	8.3	1	[-4.41, -4.22, -4.05] -0.39	[0.37, 1.52, 4.98] 0.99	[11.4, 12.0, 12.5] 24.6	-11.3	-10.3	-21.4	-11.4	-32.8
3	TYC 3144-2040-1	4.5	2	[-0.41, -0.38, -0.26] -0.12	[0.61, 1.53, 5.25] 1.00	[23.3, 25.1, 30.6] 17.9	-12.8	-9.5	-22.2	-10.9	-33.1
4	HIP 3821 (* eta Cas)	6.0	85	[-0.12, -0.11, -0.11] -0.17	[0.88, 0.99, 1.14] 1.26	[17.3, 18.0, 18.5] 23.5	-13.3	-9.9	-23.3	-11.1	-34.4
5	TYC 7582-1449-1	192.2	1	[-0.17, -0.17, -0.17] -8.96	[1.23, 1.25, 1.27] 1.26	[23.3, 23.5, 23.6] 22.1	-10.1	-10.3	-20.4	-14.2	-34.6
6	TYC 3663-2669-1	6.1	34	[-9.20, -8.83, -8.59] -0.17	[2.59, 10.24, 25.59] 1.34	[21.8, 22.4, 23.3] 23.9	-13.5	-10.1	-23.6	-11.2	-34.7
7	HIP 18453 (* 43 Per)	37.4	30	[-0.17, -0.17, -0.16] -0.86	[1.20, 1.32, 1.46] 0.86	[23.1, 23.8, 24.3] 41.0	-10.3	-12.6	-22.9	-12.7	-35.6
8	TYC 6573-3979-1	6.5	2	[-0.87, -0.86, -0.85] -0.18	[0.80, 1.00, 1.42] 0.95	[40.6, 41.1, 41.5] 44.6	-11.3	-13.6	-24.8	-11.2	-36.1
9	HIP 63797 (HD 113376)	118.1	11	[-0.18, -0.18, -0.17] -2.90	[0.27, 0.95, 1.81] 1.00	[44.1, 44.7, 45.8] 40.2	-9.5	-12.4	-22.5	-13.7	-36.3
10	TYC 7142-1661-1	21.7	1	[-3.33, -2.83, -2.49] -0.62	[0.67, 1.55, 3.28] 0.75	[35.0, 41.2, 46.8] 36.9	-11.8	-12.7	-24.2	-12.3	-36.4
11	HIP 91768 (HD 173739)	3.5	11	[-0.62, -0.59, -0.54] -0.03	[1.43, 3.08, 14.50] 0.82	[36.8, 37.9, 47.4] 36.8	-13.7	-12.1	-25.8	-10.7	-36.5
12	HIP 91772 (HD 173740)	3.5	10	[-0.03, -0.03, -0.03] -0.03	[0.81, 0.82, 0.82] 0.76	[36.7, 36.8, 36.9] 39.3	-13.6	-12.4	-26.0	-10.7	-36.7
13	TYC 7093-310-1	6.7	1	[-0.03, -0.03, -0.03] -0.19	[0.75, 0.76, 0.76] 1.96	[39.1, 39.3, 39.4] 40.3	-14.0	-12.5	-26.4	-11.2	-37.6
14	HIP 101180 (LHS 3558)	8.1	52	[-0.21, -0.20, -0.19] -0.17	[1.56, 1.97, 2.50] 1.58	[38.6, 40.2, 41.7] 32.6	-15.0	-12.1	-27.0	-11.4	-38.5
15	HIP 1475 (V* GX And)	3.6	106	[-0.17, -0.17, -0.16] -0.03	[1.58, 1.58, 1.60] 1.47	[32.4, 32.6, 32.7] 38.7	-16.3	-12.2	-28.5	-10.7	-39.2
16	HIP 21553 (HD 232979)	9.9	171	[-0.03, -0.03, -0.03] -0.24	[1.47, 1.47, 1.47] 1.94	[38.6, 38.7, 38.8] 34.8	-16.7	-11.7	-28.4	-11.6	-40.0
				[-0.25, -0.24, -0.24] -0.24	[1.91, 1.94, 1.96] 1.96	[34.6, 34.8, 34.9] 34.9					

TABLE 4
INTERSTELLAR ORIGIN PROBABILITY (IOP) FOR A SELECTED GROUP OF NEARBY STARS.

sured very precisely ($v_r = -11.10 \pm 0.4$ km/s) and their astrometric properties are relatively well known (the object is in the Hipparcos catalog but not in the GAIA TGAS set). Its most uncertain astrometric property is the declination proper motion $\mu_{\text{dec}} = 0.90 \pm 0.60$ mas, which is responsible for its low q -value. We expect that the object be present in the next Gaia Data Release. The uncertain proper motion is the reason why the minimum encounter distance has a large uncertainty, ie. 0.5-5 pc. The mass of the main component of the HD 200325 system is $1.19 \pm 0.1 M_{\odot}$, and its age is around 3.2 Gyr. The companion seems to be a low mass K-dwarf (Cvetković 2011) located at ~ 25 AU from the primary. Although no planet has been discovered yet around the primary star, and its binary nature may prevent the formation of giant planets (Thebault 2011), the stars are far apart and their masses are very dissimilar. Interestingly there is a known binary system with similar characteristics, HD 41004 (a solar mass evolved primary with a low-mass companion at 20 AU) around which a jupiter-mass planet has been discovered at ~ 1 AU from the primary (Zucker et al. 2004). The existence of this “doppelgänger”, together with recent theoretical evidence that shows that formation of planets around this kind of binaries could not be as improbable as thought (Higuchi & Ida 2017), lead us to speculate that HD200325 may harbor a planetary system and probably be the source of ejected small bodies. The possibility that ‘Oumuamua be an ejecta of a binary system has been already considered by other authors (Čuk 2018; Raymond et al. 2017) which give some

theoretical support to our speculation.

It is, however, too early to conclude that ‘Oumuamua comes actually from our best potential progenitor. It was not either our aim proposing it. However, We expect that improved astrometric information about this and other stellar systems included in our *AstroRV* catalogue, be available with the Gaia Data Release 2 and help us to improve the IOP for our best candidates or to find even better ones.

10. DISCUSSION

When dealing with very uncertain processes such as those involved in this problem, it is important to ask if the identified close encounters could be just the product of chance. Further numerical experiments should be performed to test this idea and will be presented in a future work.

At least three groups, that of Portegies Zwart et al. (2017), Dybczyński & Królikowska (2017) and Feng & Jones (2018) published their own list of candidates. Some of their objects are among the candidates in the list in Table 4, but others are not there. We searched for the “missing” objects among our *AstroRV* catalog and find that either some of their candidates were not included in our input catalog or have properties (relative velocities, time for minimum approach) too large for our particular selection criteria. This fact put in evidence a limitation of any approach to asses the origin of an interstellar object: the completeness of the database.

The approach presented here to estimate ejection velocities of small bodies from planetary system, is only

our first attempt to model what could be a more complex problem. Although a lot of interest have been paid in to model the flux of planetesimals coming out from young planetary systems, predicting the direction and velocities of these ejected objects has received less attention. The case of interstellar objects and the investigation of their origin could encourage more investigation in this field. Thus, for instance, improved semi-analytical models and detailed numerical n-body simulations may be required to better constraint the kinematical properties of ejected small bodies from already formed planetary systems around single and multiple stellar systems. We have already performed several basic n-body simulations to investigate the problem that confirm some of our semi analytical results but seem to predict lower ejection velocities in some regions of the parameter space. These results match well with the works by Čuk (2018) and Raymond et al. (2017), that predict a non-catastrophic origin of ‘Oumuamua in the neighborhood of a binary stellar system.

Although trillions of interstellar small objects are wandering around the Solar System and most of them could be there for hundreds of millions if not billions of years, the effort for tracing back the origin of some of those that enter for chance into the inner Solar System, is not irrelevant. Although many stars may have contributed in the history of Galaxy to populate this graveyard, of course nearby stellar system could be an important source of many of these objects.

Assessing the origin of interstellar objects require that the small uncertainties in the initial kinematic parameters do not propagate into large errors in the resulting dynamical properties due to factors related with the simulation process. Some sources of errors include but are not restricted to galactic coordinate transformation, uncertainties in the galactic parameters and of course errors in coding and processing the data.

In the same way as the trajectory can be propagated backward, it could also be propagated forward in time to predict the fate of these interstellar interlopers. At studying their fate we can also learn interesting things that could shade some light on their own origin.

11. SUMMARY AND CONCLUSIONS

In this paper we presented a general method for calculating the probability that nearby stars be the source of an interstellar small object detected inside the Solar System. The method relies on the availability of a precisely determined orbit for the object and precise astrometric information about a large enough number of nearby stars. For illustrating the method we applied it for assessing the origin of ‘Oumuamua, the first identified interstellar

interloper.

The application of our method to the case of ‘Oumuamua, allowed us to identify a handful of stars whose kinematical and physical properties are compatible with the ejection of a small object in the latest couple of Myrs. Of particular interest, at least with the available information, is the binary(multiple) system HD200325. The system is dominated by a primary star $1.2 M_{\odot}$ with a K-dwarf companion at ~ 25 AU. Although no planetary system have been discovered yet around the primary or the secondary star, several similar multiple systems have been discovered in the past with planets; this fact, together with multiple recent theoretical evidences, suggest that the case for HD200325 as ‘Oumuamua progenitor is not as unlikely as previously thought.

Our method is not intended to identify a single object. Even with small uncertainties in the initial orbit and in the astrometric position of the stars, there will be always large enough uncertainties in the resulting kinematical properties that constrained our capability to pinpoint a single source. Our aim is to identify stars whose properties could be studied in more detail to reduce the uncertainties and increase/decrease the probability that they can be the sources of these objects.

One of the most interesting features of our method is the fact that IOP probabilities can be published and updated permanently when new and better information be obtained. A catalog of potential progenitors for this and other future discovered interstellar objects can also be compiled and published with a global ranking of IOP probabilities. The authors believe that it could be a time in the future when this and other efforts could allows us to pinpoint precisely the provenance of an interstellar object. Those will be the times when instead of going to other planetary systems we will be able to study them using natural probes flying through our Solar System.

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APPENDIX

We have provided with this work an open source package, *iWander*, that implements the general methodology described here. Providing a fully fledged computational tool is not only an effort to make these results reproducible, but also to allow the methodology to be applied by any researcher once future interstellar objects be discovered. The package can also serve as a basis or an inspiration to develop better computational tools for this and other related problems.

Here we provide some basic information about the package that can be useful for users and developers:

- The package is available at GitHub: <http://github.com/seap-udea/iWander>.
- The required NASA NAIF SPICE kernels as well as the libraries required to compile them, are provided with the

package while complying the corresponding licenses, in order to ease its compilation and use.

- The core modules of the package were written in C/C++ to guarantee computing efficiency. As a result they should be compiled before usage. Other post processing modules were written in Python and are provided as core python scripts as well as iPython notebooks.
- One of the key components of the methodology and the package are the astrometric and radial velocities catalogs. Although all of them are publicly available, we also provide them with the package. This is to allow future developers to attempt different merging and filtering strategies when compiling the input *AstroRV* catalog.
- The version of the *AstroRV* catalog used in this work is also provided with the package. As a result, the full size of the local copy is almost 3 GB in size. A smaller size version of the package with a size of only 450 MB is available at <http://github.com/seap-udea/iWander>.
- Any contribution to the development of the package is welcomed. We can provide full access to the developing branch to any researcher or developer interested in to contribute with this project.
- The package, as well as the related databases will be updated as future and best astrometric and radial velocity information be published.

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