

COP 4020 Programming Languages

Fall 2015

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Assignment 1: Description of Syntax and Semantics

Due: Monday October 5, 2015 at 11:59pm via Blackboard

1. Given the following grammar, rewrite the BNF to give + precedence over * and force + to be right associative. Show your parse tree to demonstrate that your answer is correct.

```
<assign> → <id> = <expr>
<id> → A | B | C
<expr> → <expr> + <term>
        | <term>
<term> → <term> * <factor>
        | <factor>
<factor> → ( <expr> )
          | <id>
```

2. Using the grammar given in question 1, show a parse tree and a leftmost derivation for each of the following statements:

$A = (A + B) * C$

3. Given the grammar in question 1, modify the grammar to add a unary minus operator that has higher precedence than either + or *. (Assume the unary operator can precede any operand).

4. Describe, in English or in mathematic notation, the language defined by the following grammar:

```
<S> → <A> <B> <C>
<A> → a <A> | a
<B> → b <B> | b
<C> → c <C> | c
```

5. Please explain your answers.

Write a grammar for the language consisting of strings that have n copies of the letter a followed by the same number of copies of the letter b , where $n > 0$. For example, the strings ab , $aaaabbbb$ and in the language, but a , abb , ba , and $aaabb$ are not.

6. Compute the weakest precondition for each of the following assignment statements and post conditions

$$a = 2 * (b - 1) - 1 \{ a > 0 \}$$

$$b = (c + 10) / 3 \{ b > 6 \}$$

7. Compute the weakest precondition for each of the following sequences of assignments statements and their post-conditions

$$a = 2 * b + 1; \text{-----} S1$$

$$b = a - 3; \text{-----} S2$$

$$\{ b < 0 \}$$

8. Let $\Sigma = \{a, b\}$, For the following language, find a grammar that generates it.

$$L = \{a^n b^{n-3} : n \geq 3\}$$

9. [No grading] Practice derivations of the following English sentences from the grammar given below.

The following example of CFG describes a fragment of the English sentence

<SENTENCE> \rightarrow <NOUN-PHRASE><VERB-PHRASE>

<NOUN-PHRASE> \rightarrow <CMPLX-NOUN> | <CMPLX-NOUN><PREP-PHRASE>

<VERB-PHRASE> \rightarrow <CMPLX-VERB> | <CMPLX-VERB><PREP-PHRASE>

<PREP-PHRASE> \rightarrow <PREP><CMPLX-NOUN>

<CMPLX-MOUN> \rightarrow <ARTICLE><NOUN>

<CMPLX-VERB> \rightarrow <VERB> | <VERB> <NOUN-PHRASE>

<ARTICLE> \rightarrow a | the

<NOUN> \rightarrow boy | girl | flower

<VERB> \rightarrow touches | likes | sees

<PREP> \rightarrow with

This L(G) include the following three examples

a boy sees

the boy sees a flower

a girl with a flower likes the boy