# **ASEN 3128 - Lab Deliverable 3**

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#### I. Problem 3 Question 1

Yes, the results found from problem 3 of the lab does make sense as the quad-rotor was to be modeled in steady equilibrium and that is what is seen in all of the linearized plots. For every plot with variables associated with steady equilibrium flight, those variables were found to be constant and don't vary with time. These variables that were found to be constant throughout time and need to be constant throughout time to ensure steady equilibrium flight include; Euler angles, angular velocity, and the control forces and moments. Thus, the behavior does make sense.

#### II. Problem 3 Question 2

Yes, steady hover is a stable flight condition, as the variables mentioned above (Euler angles, angular velocity, and the control forces and moments) are constant throughout time. While in a steady a quad-rotor is not changing its orientation at all and thus, its Euler angles are not changing. Additionally, it is not spinning about any of its axes and thus it has no angular velocity. Lastly, there is no no motion for the quad-rotor and thus the control forces and moments are constant. With all of the above knowledge it can be understood that the quad-rotor is in stable equilibrium flight while in a steady hover.

#### III. Problem 5 Question 1

The addition of the feedback control law to the non-linearized model, makes it so that the non-linearized model now acts the same as the linearized model in the sense that the results demonstrate steady equilibrium flight for the quad-rotor given the roll, pitch, and yaw rates. Without this control law in the non-linearized model the output would be such that the quad-rotor would not be in equilibrium flight as demonstrated in our figures comparing the uncontrolled non-linearized model and the linearized model.

## IV. Figures

## A. Problem 3.a and 4.a

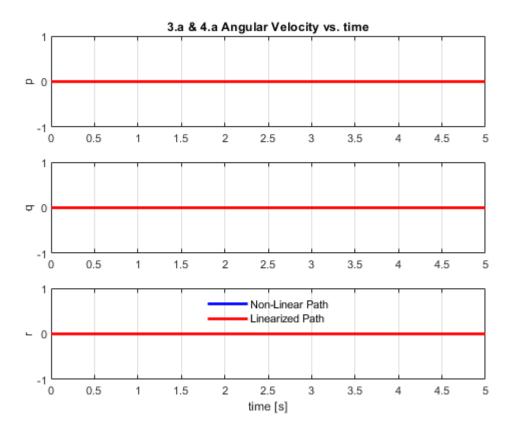


Fig. 1 Angular Velocity

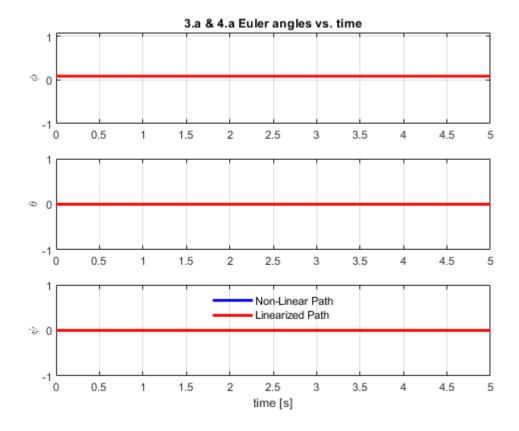


Fig. 2 Euler Angles

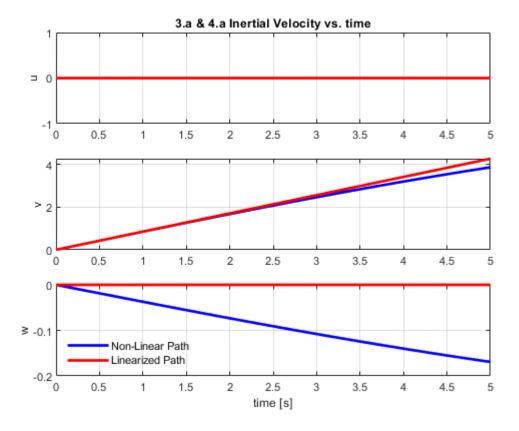


Fig. 3 Inertial Velocity

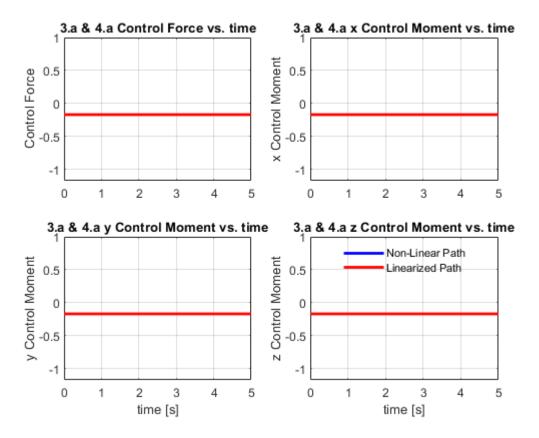


Fig. 4 Control Forces

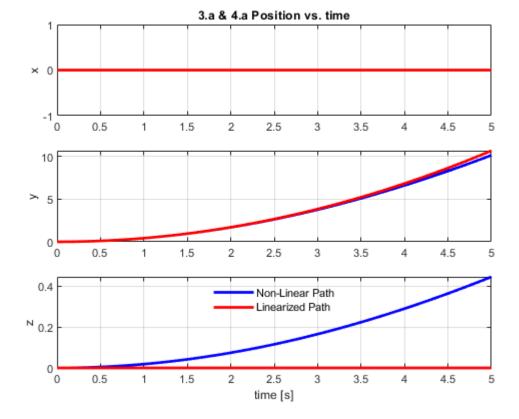


Fig. 5 Flight Path

## B. Problem 3.b and 4.b

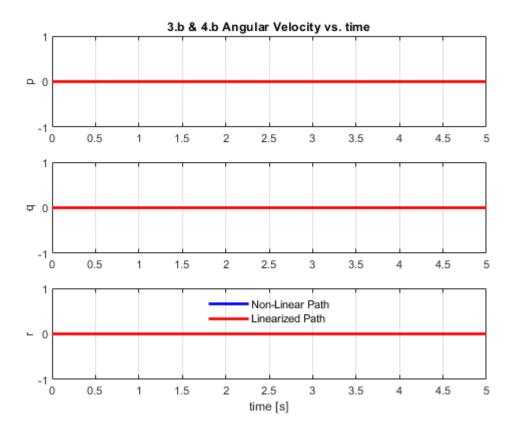


Fig. 6 Angular Velocity

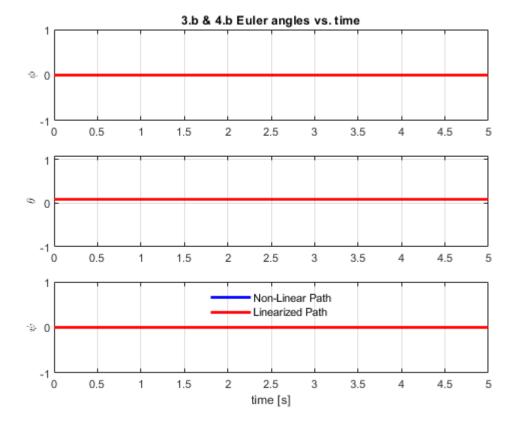


Fig. 7 Euler Angles

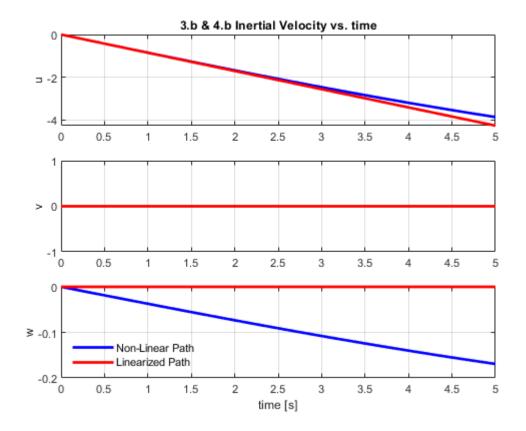


Fig. 8 Inertial Velocity

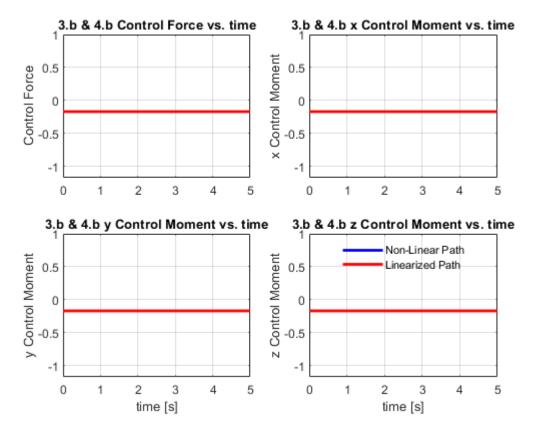


Fig. 9 Control Forces

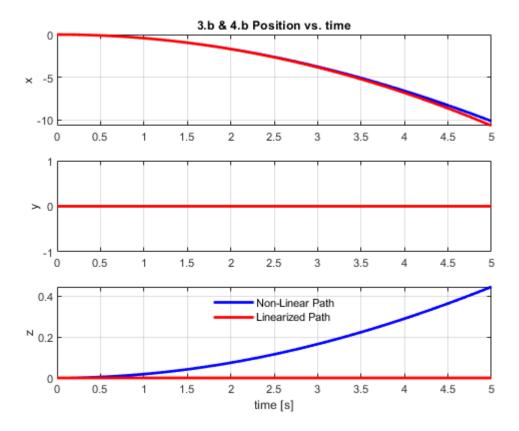


Fig. 10 Flight Path

## C. Problem 3.c and 4.c

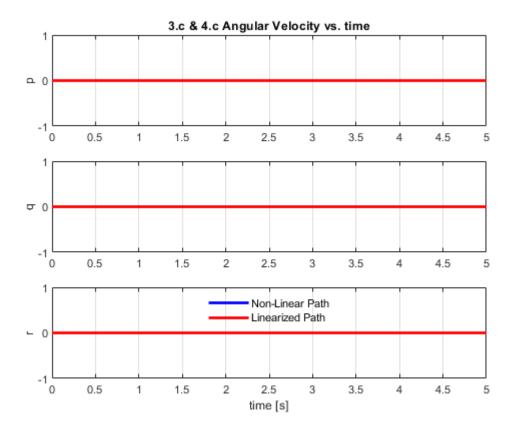


Fig. 11 Angular Velocity

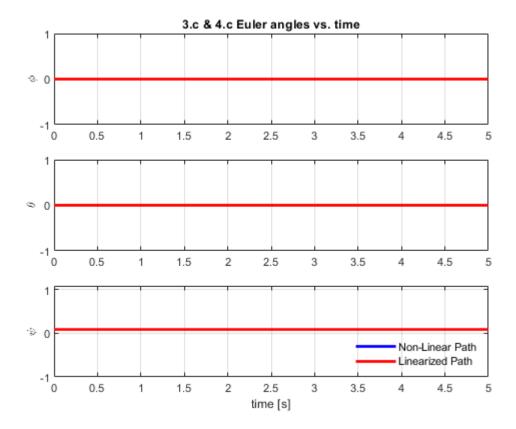


Fig. 12 Euler Angles

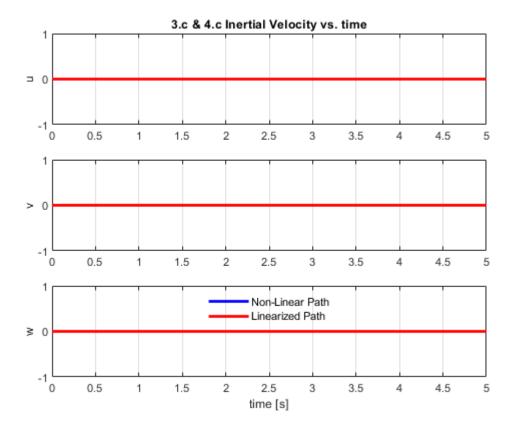


Fig. 13 Inertial Velocity

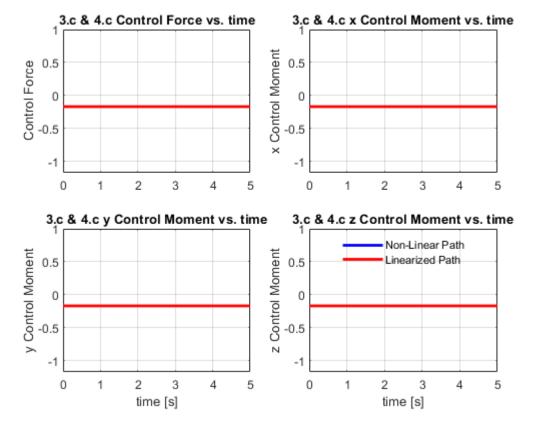


Fig. 14 Control Forces

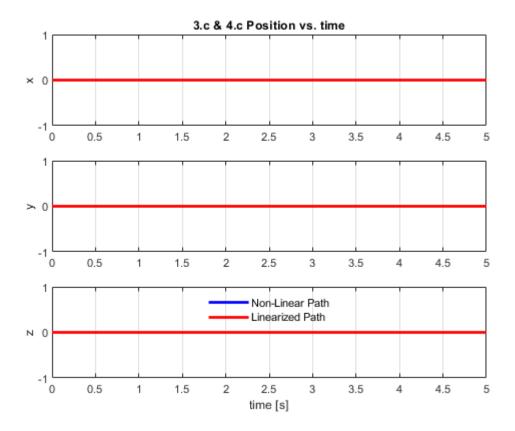


Fig. 15 Flight Path

## D. Problem 3.d and 4.d

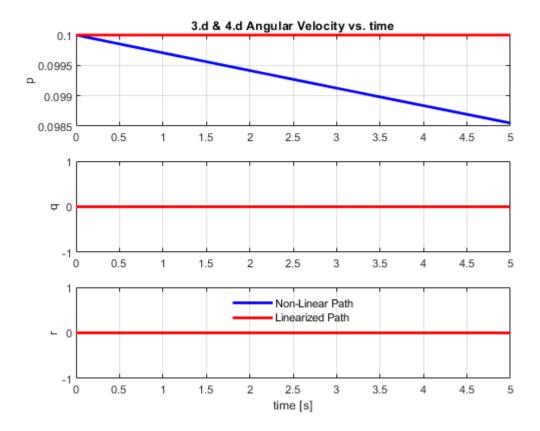


Fig. 16 Angular Velocity

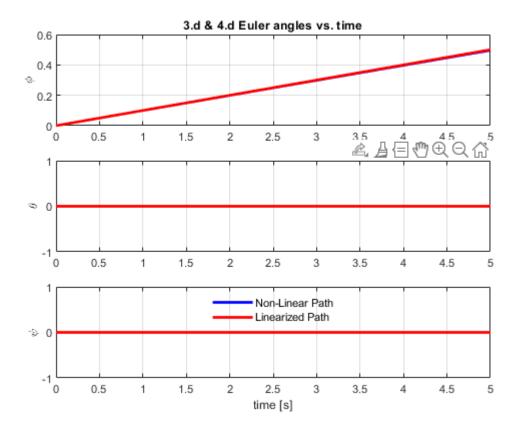


Fig. 17 Euler Angles

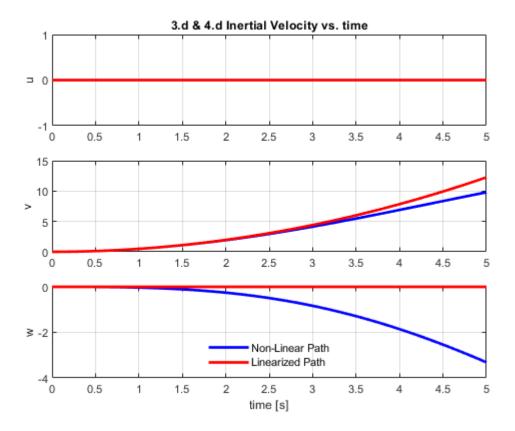


Fig. 18 Inertial Velocity

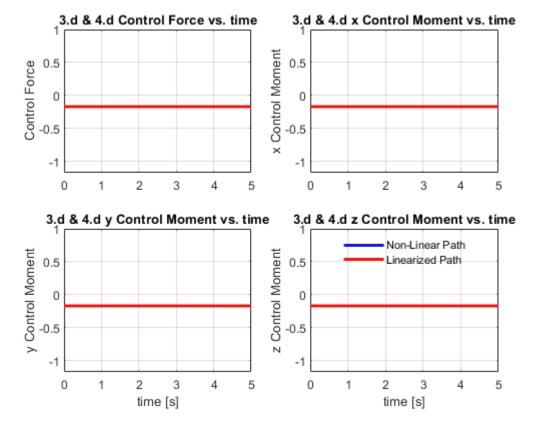


Fig. 19 Control Forces

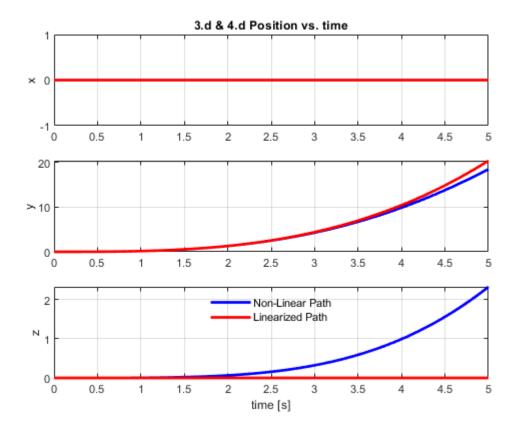


Fig. 20 Flight Path

## E. Problem 3.e and 4.e

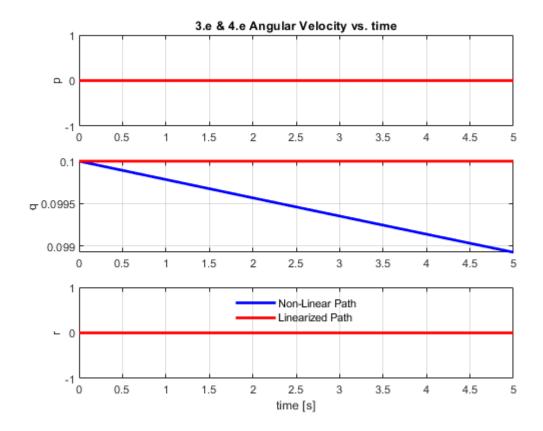


Fig. 21 Angular Velocity

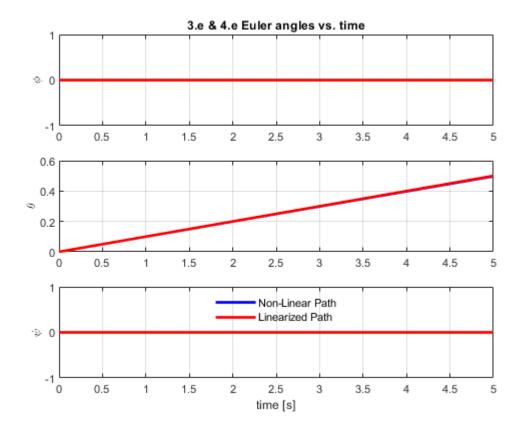


Fig. 22 Euler Angles

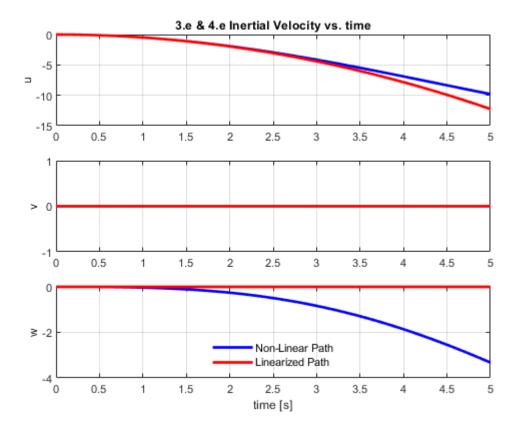


Fig. 23 Inertial Velocity

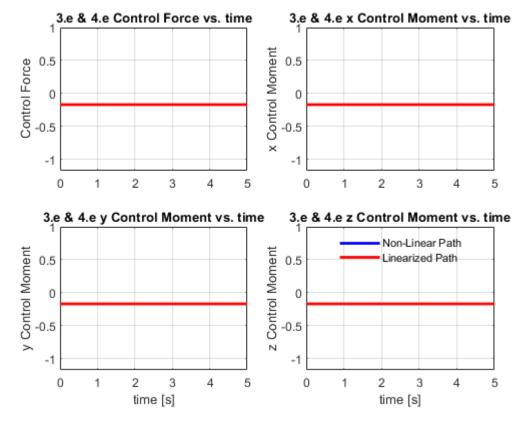


Fig. 24 Control Forces

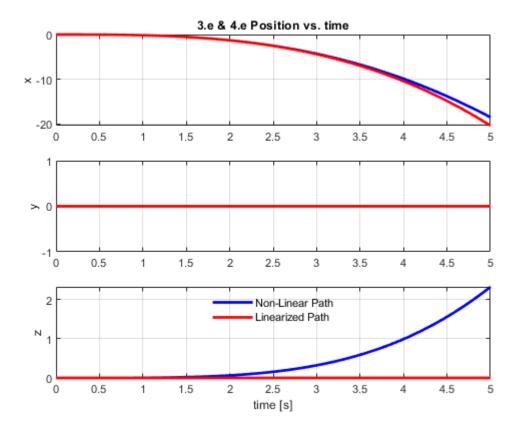


Fig. 25 Flight Path

## F. Problem 3.f and 4.f

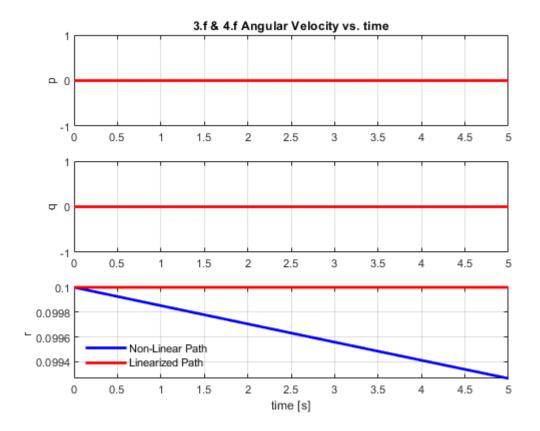


Fig. 26 Angular Velocity

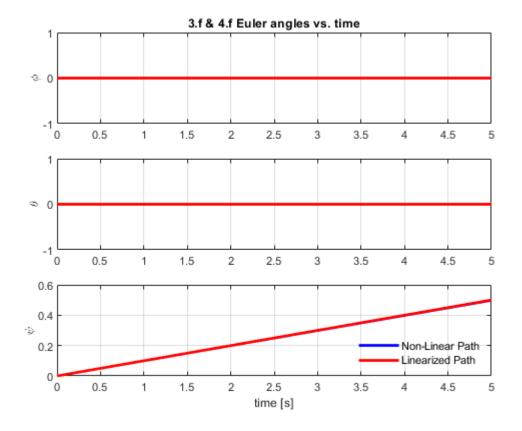


Fig. 27 Euler Angles

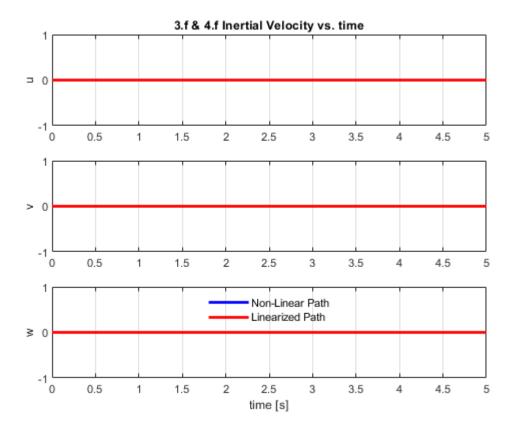


Fig. 28 Inertial Velocity

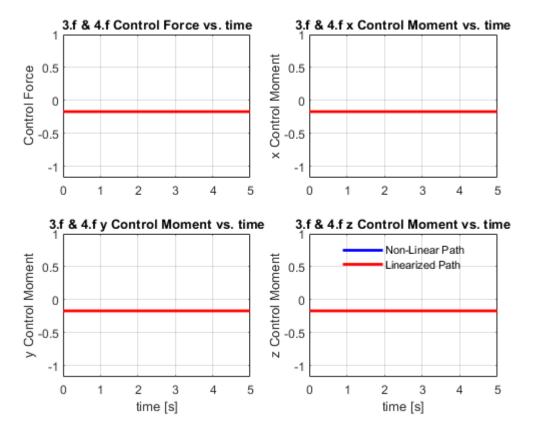


Fig. 29 Control Forces

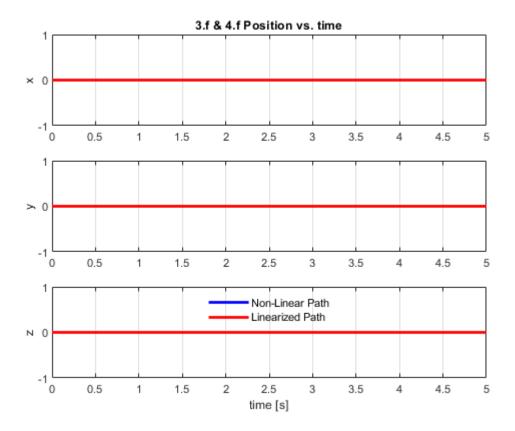


Fig. 30 Flight Path

#### G. Problem 5

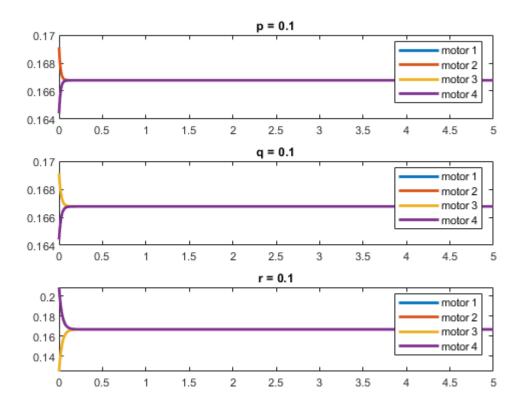


Fig. 31 Motor Forces with Feedback Control

## V. Appendix

### A. MATLAB Code

Main code

```
%% ASEN 3128 - LAb 3 - Main
  % Script to compare the linearized and non-linearized models of a quadrotor
  % in steady equilibrium flight. Additionally, control moments and forces
  % are to be added to model how a quadrotor remains in steady hover flight
  % Author: Cole MacPherson
  % Collaborators: S. Packard, D. Wolfe, D. Zhao
  % Date: 5th Mar 2021
  %% Housekeeping
  clc;
  clear;
  close all;
  tic
  %% declare constants
  m = 0.068; % mass of the quadrotor [kg]
  R = 0.06; % radial distance from CG to propeller [m]
  k_m = 0.0024; % control moment coefficient [N*m/N]
  I_x = 6.8e-5; % x-axis moment of inertia [kg*m^2]
I_y = 9.2e-5; % y-axis moment of inertia [kg*m^2]
```

```
|\mathbf{I}_{z}| |\mathbf{I}_{z}| = 1.35e-4; % z-axis moment of inertia [kg*m^2]
    nu = 1e-3; % aerodynamic force coefficient [N/(m/s)^2]
    mu = 2e-6; % aerodynamic moment coefficient [N*m/(rad/s)^2]
    g = 9.81; % graviational constant [m/s^2]
    Z_c = -m*g; % control force
    L_c = 0; % x control moment
    M_c = 0; % y contorl moment
    N_c = 0; % z control moment
    tspan = [0 5]; % time to integrate over
    %% initialize figure information
    col = 'b';
    fig_a = [1,2,3,4,5,6]; % figure a number vector
     fig_b = [1,2,3,4,5,6] + 6; \% figure b number vector
    fig_c = [1,2,3,4,5,6] + 2*6; % figure c number vector
    fig_d = [1,2,3,4,5,6] + 3*6; \% figure d number vector
    fig_e = [1,2,3,4,5,6] + 4*6; % figure e number vector
    fig_f = [1,2,3,4,5,6] + 5*6; \% figure f number vector
    %% 3a
    state_vec_0 = [0 0 0 deg2rad(5) 0 0 0 0 0 0 0]';
    ,L_c,M_c,N_c),tspan,state_vec_0);
    PlotAircraftSim(t_a, state_vec_a, ones(length(t_a), 4)*Z_c/4, fig_a, col, '3.a')
    %% 3b
    state_vec_0 = [0 \ 0 \ 0 \ deg2rad(5) \ 0 \ 0 \ 0 \ 0 \ 0]';
    ,L_c,M_c,N_c),tspan,state_vec_0);
    PlotAircraftSim(t_b, state_vec_b, ones(length(t_b), 4)*Z_c/4, fig_b, col, '3.b')
    %% 3c
    state_{vec_0} = [0 \ 0 \ 0 \ 0 \ deg2rad(5) \ 0 \ 0 \ 0 \ 0]';
    ,L_c,M_c,N_c),tspan,state_vec_0);
    PlotAircraftSim(t_c,state_vec_c,ones(length(t_c),4)*Z_c/4,fig_c,col,'3.c')
    %% 3d
    [p,q,r] = rollrate2pqr(0,0,0,0.1,0,0);
     state_vec_0 = [0 0 0 0 0 0 0 0 0 p q r]';
    [\texttt{t\_d}, \texttt{state\_vec\_d}] = \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d}) \quad \texttt{quadrotorODE}(\texttt{t\_d}, \texttt{state\_vec\_d}, \texttt{m}, \texttt{I\_x}, \texttt{I\_y}, \texttt{I\_z}, \texttt{nu}, \texttt{mu}, \texttt{Z\_c}) \\ = \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d}) \quad \texttt{quadrotorODE}(\texttt{t\_d}, \texttt{state\_vec\_d}, \texttt{m}, \texttt{I\_x}, \texttt{I\_y}, \texttt{I\_z}, \texttt{nu}, \texttt{mu}, \texttt{Z\_c}) \\ = \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d})) \quad \texttt{quadrotorODE}(\texttt{t\_d}, \texttt{state\_vec\_d}, \texttt{m}, \texttt{I\_x}, \texttt{I\_y}, \texttt{I\_z}, \texttt{nu}, \texttt{mu}, \texttt{Z\_c}) \\ = \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d})) \quad \texttt{quadrotorODE}(\texttt{t\_d}, \texttt{state\_vec\_d}, \texttt{m}, \texttt{I\_x}, \texttt{I\_y}, \texttt{I\_z}, \texttt{nu}, \texttt{mu}, \texttt{Z\_c}) \\ = \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d})) \quad \texttt{quadrotorODE}(\texttt{t\_d}, \texttt{state\_vec\_d}, \texttt{m}, \texttt{I\_x}, \texttt{I\_y}, \texttt{I\_z}, \texttt{nu}, \texttt{mu}, \texttt{Z\_c}) \\ = \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d})) \quad \texttt{quadrotorODE}(\texttt{t\_d}, \texttt{state\_vec\_d}, \texttt{m}, \texttt{I\_x}, \texttt{I\_y}, \texttt{I\_z}, \texttt{nu}, \texttt{mu}, \texttt{Mu}, \texttt{I\_z}) \\ = \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d})) \quad \texttt{quadrotorODE}(\texttt{t\_d}, \texttt{state\_vec\_d}, \texttt{m}, \texttt{I\_x}, \texttt{I\_y}, \texttt{I\_x}, \texttt{I\_y}, \texttt{I\_y}, \texttt{I\_z}) \\ = \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d})) \quad \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d})) \quad \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d})) \\ = \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d})) \\ = \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d})) \quad \texttt{ode45}(@(\texttt{t\_d}, \texttt{state\_vec\_d})) \\ = \texttt{od
               ,L_c,M_c,N_c),tspan,state_vec_0);
    PlotAircraftSim(t_d, state_vec_d, ones(length(t_d), 4)*Z_c/4, fig_d, col, '3.d')
    %% 3e
    [p,q,r] = rollrate2pqr(0,0,0,0,0.1,0);
    state_vec_0 = [0 0 0 0 0 0 0 0 0 p q r]';
    [t_e,state_vec_e] = ode45(@(t_e,state_vec_e) quadrotorODE(t_e,state_vec_e,m,I_x,I_y,I_z,nu,mu,Z_c
               ,L_c,M_c,N_c),tspan,state_vec_0);
    PlotAircraftSim(t_e, state_vec_e, ones(length(t_e), 4)*Z_c/4, fig_e, col, '3.e')
     [p,q,r] = rollrate2pqr(0,0,0,0,0,0.1);
    state_vec_0 = [0 0 0 0 0 0 0 0 0 p q r]';
     ,L_c,M_c,N_c),tspan,state_vec_0);
    PlotAircraftSim(t\_f, state\_vec\_f, ones(length(t\_f), 4)*Z\_c/4, fig\_f, col, '3.f')
    %% Redefine figure line color for problem 4
83 col = 'r';
```

```
%% 4a
  t_final = 5;
  state_{vec_0} = [0 \ 0 \ 0 \ deg2rad(5) \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]';
  [state_vec_a,t_a] = linearizedEOM(state_vec_0,t_final);
  PlotAircraftSim(t_a, state_vec_a, ones(length(t_a), 4)*Z_c/4, fig_a, col, '3.a & 4.a')
  %% 4b
  state_vec_0 = [0 0 0 0 deg2rad(5) 0 0 0 0 0 0]';
  [state_vec_b,t_b] = linearizedEOM(state_vec_0,t_final);
  PlotAircraftSim(t_b, state_vec_b, ones(length(t_b), 4)*Z_c/4, fig_b, col, '3.b & 4.b')
  state_{vec_0} = [0 \ 0 \ 0 \ 0 \ deg2rad(5) \ 0 \ 0 \ 0 \ 0]';
  [state_vec_c,t_c] = linearizedEOM(state_vec_0,t_final);
  PlotAircraftSim(t_c, state_vec_c, ones(length(t_c), 4)*Z_c/4, fig_c, col, '3.c & 4.c')
  [p,q,r] = rollrate2pqr(0,0,0,0.1,0,0);
  state_vec_0 = [0 0 0 0 0 0 0 0 0 p q r]';
  [state_vec_d,t_d] = linearizedEOM(state_vec_0,t_final);
  PlotAircraftSim(t_d,state_vec_d,ones(length(t_d),4)*Z_c/4,fig_d,col,'3.d & 4.d')
  %% 4e
  [p,q,r] = rollrate2pqr(0,0,0,0,0.1,0);
  state_vec_0 = [0 0 0 0 0 0 0 0 0 p q r]';
  [state_vec_e,t_e] = linearizedEOM(state_vec_0,t_final);
  PlotAircraftSim(t_e, state_vec_e, ones(length(t_e), 4)*Z_c/4, fig_e, col, '3.e & 4.e')
  [p,q,r] = rollrate2pqr(0,0,0,0,0,0.1);
  state_vec_0 = [0 0 0 0 0 0 0 0 0 p q r]';
  [state_vec_f,t_f] = linearizedEOM(state_vec_0,t_final);
  PlotAircraftSim(t_f, state_vec_f, ones(length(t_f), 4)*Z_c/4, fig_f, col, '3.f & 4.f')
  %% 5d
  [p,q,r] = rollrate2pqr(0,0,0,0.1,0,0);
  state_vec_0 = [0 0 0 0 0 0 0 0 0 0 0 p q r Z_c -0.004*p -0.004*q -0.004*r]';
  [t_d,state_vec_d] = ode45(@(t_d,state_vec_d) quadrotorODE_controlled(t_d,state_vec_d,m,I_x,I_y,
       I_z, nu, mu, Z_c, L_c, M_c, N_c), tspan, state_vec_0);
  % compute forces
  F_5d = ComputeMotorForces(state\_vec\_d(:,13), state\_vec\_d(:,14), state\_vec\_d(:,15), state\_vec\_d(:,16)
       ,R,k_m);
% plot force
  figure
  subplot(3,1,1)
  plot(t_d, F_5d(1,:), 'linewidth', 2); hold on;
  plot(t_d,F_5d(2,:),'linewidth',2); hold on;
  plot(t_d,F_5d(3,:),'linewidth',2); hold on;
  plot(t_d, F_5d(4,:), 'linewidth', 2); hold on;
  title(['p = ' num2str(p)]);
  legend('motor 1', 'motor 2', 'motor 3', 'motor 4');
142 hold on;
  %% 5e
  [p,q,r] = rollrate2pqr(0,0,0,0,0.1,0);
  state_vec_0 = [0 0 0 0 0 0 0 0 0 0 p q r Z_c -0.004*p -0.004*q -0.004*r]';
  [t_e,state_vec_e] = ode45(@(t_e,state_vec_e) quadrotorODE_controlled(t_e,state_vec_e,m,I_x,I_y,
       I_z, nu, mu, Z_c, L_c, M_c, N_c), tspan, state_vec_0);
```

```
% compute forces
F_5e = ComputeMotorForces(state_vec_e(:,13), state_vec_e(:,14), state_vec_e(:,15), state_vec_e(:,16)
     R,k_m);
% plot force
subplot(3,1,2)
plot(t_e,F_5e(1,:),'linewidth',2); hold on;
plot(t_e,F_5e(2,:),'linewidth',2); hold on;
plot(t_e,F_5e(3,:),'linewidth',2); hold on;
plot(t_e,F_5e(4,:),'linewidth',2); hold on;
title(['q = ' num2str(q)]);
legend('motor 1', 'motor 2', 'motor 3', 'motor 4');
hold on;
%% 5f
[p,q,r] = rollrate2pqr(0,0,0,0,0,0.1);
state_vec_0 = [0 0 0 0 0 0 0 0 0 p q r Z_c -0.004*p -0.004*q -0.004*r]';
[t_f,state_vec_f] = ode45(@(t_f,state_vec_f) quadrotorODE_controlled(t_f,state_vec_f,m,I_x,I_y,
     I_z, nu, mu, Z_c, L_c, M_c, N_c), tspan, state_vec_0);
% compute forces
F\_5f = ComputeMotorForces(state\_vec\_f(:,13), state\_vec\_f(:,14), state\_vec\_f(:,15), state\_vec\_f(:,16)
     ,R,k_m);
% plot force
subplot(3,1,3)
plot(t_f,F_5f(1,:),'linewidth',2); hold on;
plot(t_f,F_5f(2,:),'linewidth',2); hold on;
plot(t_f,F_5f(3,:),'linewidth',2); hold on;
plot(t_f,F_5f(4,:),'linewidth',2); hold on;
title(['r = ' num2str(r)]);
legend('motor 1', 'motor 2', 'motor 3', 'motor 4');
hold on;
%% Plot Housekeeping
% make legends for each plot
for N = 1:6
     figure(6*N-5)
     legend('Non-Linear Path','Linearized Path','location','best');
     legend('boxoff');
     figure(6*N-4)
     legend('Non-Linear Path','Linearized Path','location','best');
     legend('boxoff');
     figure (6*N-3)
     legend('Non-Linear Path','Linearized Path','location','best');
     legend('boxoff');
     figure(6*N-2)
     legend('Non-Linear Path','Linearized Path','location','best');
     legend('boxoff');
     figure (6*N-1)
     legend('Non-Linear Path','Linearized Path','location','best');
     legend('boxoff');
     figure (6*N)
     legend('Non-Linear Path','Start','End','Linearized Path');
end
%% End Housekeeping
toc
```

#### Plotting (Problem 1)

```
function PlotAircraftSim(t,state,control,fig,col,num)
```

```
%% Plot position vs time
figure(fig(1))
subplot(3,1,1)
plot(t,state(:,1),col,'linewidth',2); hold on;
ylabel('x');
title([num ' Position vs. time']);
subplot(3,1,2)
plot(t,state(:,2),col,'linewidth',2); hold on;
grid on
ylabel('y');
subplot(3,1,3)
plot(t,state(:,3),col,'linewidth',2); hold on;
ylabel('z');
xlabel('time [s]');
%% Plot Euler andgles vs time
figure(fig(2))
subplot(3,1,1)
plot(t,state(:,4),col,'linewidth',2); hold on;
grid on
ylabel('\phi');
title([num ' Euler angles vs. time']);
subplot(3,1,2)
plot(t,state(:,5),col,'linewidth',2); hold on;
grid on
ylabel('\theta');
subplot(3,1,3)
plot(t,state(:,6),col,'linewidth',2); hold on;
grid on
ylabel('\psi');
xlabel('time [s]');
%% Plot velocity vs time
figure(fig(3))
subplot(3,1,1)
plot(t,state(:,7),col,'linewidth',2); hold on;
grid on
ylabel('u');
title([num ' Inertial Velocity vs. time']);
subplot(3,1,2)
plot(t,state(:,8),col,'linewidth',2); hold on;
grid on
ylabel('v');
subplot(3,1,3)
plot(t,state(:,9),col,'linewidth',2); hold on;
grid on
ylabel('w');
xlabel('time [s]');
%% Plot angular velocity vs time
figure(fig(4))
subplot(3,1,1)
plot(t,state(:,10),col,'linewidth',2); hold on;
grid on
ylabel('p');
title([num ' Angular Velocity vs. time']);
subplot(3,1,2)
plot(t,state(:,11),col,'linewidth',2); hold on;
grid on
ylabel('q');
subplot(3,1,3)
plot(t,state(:,12),col,'linewidth',2); hold on;
grid on
ylabel('r');
xlabel('time [s]');
```

```
%% Plot control forces and moments vs time
    figure(fig(5))
    subplot(2,2,1)
    plot(t,control(:,1),col,'linewidth',2); hold on;
    title([num ' Control Force vs. time']);
    ylabel('Control Force');
    xlim([t(1) t(end)]);
    subplot(2,2,2)
    plot(t,control(:,2),col,'linewidth',2); hold on;
    grid on
    title([num ' x Control Moment vs. time']);
    ylabel('x Control Moment');
    xlim([t(1) t(end)]);
    subplot(2,2,3)
    plot(t,control(:,3),col,'linewidth',2); hold on;
    grid on
    title([num ' y Control Moment vs. time']);
    ylabel('y Control Moment');
    xlabel('time [s]');
    xlim([t(1) t(end)]);
    subplot(2,2,4)
    plot(t,control(:,4),col,'linewidth',2); hold on;
    grid on
    title([num ' z Control Moment vs. time']);
    xlabel('time [s]');
    ylabel('z Control Moment');
    xlim([t(1) t(end)]);
    %% Plot flight path of the simulated quadrotor
    figure(fig(6))
    plot3(state(:,1),state(:,2),state(:,3),col,'linewidth',2); hold on;
    plot3(state(1,1), state(1,2), state(1,3), 'g.', 'markersize',20); hold on;
    plot3(state(end,1),state(end,2),state(end,3),'r.','markersize',20); hold on;
    set(gca, 'YDir','reverse')
set(gca, 'ZDir','reverse')
    grid on
    title([num ' Flight Path']);
    xlabel('x');
    ylabel('y');
    zlabel('z');
end
```

#### Coord frame conversions

#### Non feedback control ODE for problem 3

```
function xdot = quadrotorODE(t,state_vec,m,I_x,I_y,I_z,n,mu,Z_c,L_c,M_c,N_c)

phi = state_vec(4); % roll angle
    theta = state_vec(5); % pitch angle
    psi = state_vec(6); % yaw angle
```

```
u = state_vec(7); % x velocity
    v = state_vec(8); % y velocity
    w = state_vec(9); % z velocity
   p = state_vec(10); % roll velocity
    q = state_vec(11); % pitch velocity
    r = state_vec(12); % yaw velocity
    q = 9.81; %Gravity m/s^2
    M = -mu*norm([p;q;r])*[p;q;r]; % aerodynamic moment
    V = norm([u;v;w]); % velocity
   F = -n*V*[u;v;w]; % aerodynamic force
    MomCntl = [L_c; M_c; N_c]; % control moment
   % transformation matrix
    R = [\cos(\text{theta}) * \cos(\text{psi}) \sin(\text{phi}) * \sin(\text{theta}) * \cos(\text{psi}) - \cos(\text{phi}) * \sin(\text{psi}) \cos(\text{phi}) * \sin(\text{theta}) *
    cos(psi)+sin(phi)*sin(psi);..
        cos(theta)*sin(psi) sin(phi)*sin(theta)*sin(psi)+cos(phi)*cos(psi) cos(phi)*sin(theta)*
    sin(psi)-sin(phi)*cos(psi);..
        -sin(theta) sin(phi)*cos(theta) cos(phi)*cos(theta)];
    % equations of motion
    v_inertial = R * [u;v;w];
    euler_dot = [1 sin(phi)*tan(theta) cos(phi)*tan(theta);...
        0 cos(phi) -sin(phi);...
        0 sin(phi)*(1/cos(theta)) cos(phi)*(1/cos(theta))]...
        * [p;q;r];
    a_{inertial} = [r*v-q*w; p*w-r*u; q*u-p*v]...
        + g*[-sin(theta);cos(theta)*sin(phi);cos(theta)*cos(phi)]...
        + (1/m)*F + (1/m)*[0;0;Z_c];
    + [(1/I_x)*M(1); (1/I_y)*M(2); (1/I_z)*M(3)]...
        + [(1/I_x)*MomCntl(1); (1/I_y)*MomCntl(2); (1/I_z)*MomCntl(3)];
    xdot = [v_inertial; euler_dot; a_inertial; a_angular]; % vecotr output for the integrals
end
```

#### Motor Forces (Problem 2)

#### Linearization for problem 4

```
function [x,t] = linearizedEOM(x0,t_f)

g = 9.81; %acceleration due to gravity

%% Defien state space matrix
A = zeros(12,12);
A(1,7) = 1;
A(2,8) = 1;
A(3,9) = 1;
A(4,10) = 1;
```

```
A(5,11) = 1;

A(6,12) = 1;

A(7,5) = -g;

A(8,4) = g;

%% Define state space system

sys = ss(A,zeros(12,1),eye(12),0);

%% Simulate state space system

[x,t] = initial(sys,x0,t_f);

end
```

#### Feedback control ODE for problem 5

```
function xdot = quadrotorODE_controlled(t,state_vec,m,I_x,I_y,I_z,n,mu,Z_c,L_c,M_c,N_c)
              %% Define variables
             phi = state_vec(4); % roll angle
              theta = state_vec(5); % pitch angle
             psi = state_vec(6); % yaw angle
             u = state_vec(7); % x velocity
             v = state_vec(8); % y velocity
             w = state_vec(9); % z velocity
             p = state_vec(10); % roll velocity
             q = state_vec(11); % pitch velocity
             r = state_vec(12); % yaw velocity
             g = 9.81; %Gravity m/s^2
             M = -mu*norm([p;q;r])*[p;q;r]; % aerodynamic moment
             V = norm([u;v;w]); % velocity
             F = -n*V*[u;v;w]; % aerodynamic force
             MCntl = -0.004*[p;q;r]; \% control moment
             %% Transformation matrix
             R = [\cos(\theta)^*\cos(\phi)] \sin(\phi)^*\sin(\theta)^*\cos(\phi) - \cos(\phi)^*\sin(\phi) \cos(\phi)^*\sin(\theta)^*\sin(\theta)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\cos(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\cos(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\sin(\phi)^*\cos(\phi)^*\cos(\phi)^*\sin(\phi)^*\sin(\phi)^*\cos(\phi)^*\cos(\phi)^*\sin(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^*\cos(\phi)^
               cos(psi)+sin(phi)*sin(psi);...
                            cos(theta)*sin(psi) sin(phi)*sin(theta)*sin(psi)+cos(phi)*cos(psi) cos(phi)*sin(theta)*
               sin(psi)-sin(phi)*cos(psi);..
                             -sin(theta) sin(phi)*cos(theta) cos(phi)*cos(theta)];
             %% Equations of motion
              v_inertial = R*[u;v;w];
               euler_dot = [1 sin(phi)*tan(theta) cos(phi)*tan(theta);...
                            0 cos(phi) -sin(phi);...
                             0 sin(phi)*(1/cos(theta)) cos(phi)*(1/cos(theta))]...
                             * [p;q;r];
               a_{inertial} = [r*v-q*w; p*w-r*u; q*u-p*v]...
                             + g*[-sin(theta);cos(theta)*sin(phi);cos(theta)*cos(phi)]...
                             + (1/m)*F + (1/m)*[0;0;Z_c];
               + [(1/I_x)*M(1); (1/I_y)*M(2); (1/I_z)*M(3)]...
                             + [(1/I_x)*MCntl(1); (1/I_y)*MCntl(2); (1/I_z)*MCntl(3)];
             deltaF = [0; -0.004*a_angular];
               xdot = [v_inertial; euler_dot; a_inertial; a_angular; deltaF]; % vecotr output for the
               integrals
end
```

# VI. Team Participation Table

Name	Plan	Model	Experiment	Results	Report	Code	Ack
Cole MacPherson	1	2	X	2	1	2	CM
Donny Wolfe	1	1	X	1	2	1	DW
Samuel Packard	1	1	X	1	2	1	SP
Dawei Zhao	2	1	X	1	1	1	DZ