

# Online Knapsack Problem

Term Paper - Theoretical Computer Science

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2015-06-03

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## 1 Preamble

Online problems and algorithms are problems where the inputs for the algorithm are not known at the beginning, but appear one by one. This could be a job-scheduler in an operating system where you have to decide whether to do a job immediately after it appears or wait for other, maybe shorter jobs. It could also be the decision whether to buy new ski-gear at the beginning of the season or rent it every day, when you do not know, how the weather will be like during the season. Every day, it could snow, rain or be a perfect powder-day, but should you buy skis on one sunny day, when you do not know if there will be another nice day to go to the mountains?

It would be nice to have some information about the future, something like an omniscient oracle, that gives us a glimpse of whats coming next.

We introduce such an oracle for online problems and try to find out, how much information do we need from the oracle to get an optimal solution.

In this interactive paper, we deal with the so called online knapsack problem, where we have knapsack that we want to fill with a maximum amount of value but respect the maximum capacity of it.

### 1.1 About this paper

This paper is written as *literate CoffeeScript*-source-code<sup>1</sup> of a set of experiments with these online-problem and it is running on *Meteor*<sup>2</sup>.

It is compiled using *pandoc*<sup>3</sup>, which enables you to compile Markdown and many other formats to latex+pdf.

A live version of the experiments is available at: <http://online-knapsack.macrozone.ch>, the source-code is available on github: [https://github.com/macrozone/seminar\\_np](https://github.com/macrozone/seminar_np).

## 2 The knapsack-problem

Consider a knapsack with a certain capacity of weight (or volume) and a set of items, each with a value and a weight.

Which subset of these items would you put into the knapsack to get the maximum possible total value respecting the capacity of the knapsack?

This question is the so called knapsack-problem.

### 2.1 The simple-knapsack-problem

In this paper, we only consider the so called *simple-knapsack-problem* where the value of one item is the same as its weight and where the knapsack has always a capacity of 1.

We call the total value of all items in the knapsack as the *gain*.

Let's define such a knapsack:

```
1 Knapsack = class
2   constructor: ->
3     @size = 1
4     @dep = new Tracker.Dependency
5     @reset()
```

---

<sup>1</sup>See <http://coffeescript.org/#literate>

<sup>2</sup><https://www.meteor.com/>

<sup>3</sup><http://pandoc.org/>

```
6
7     fits: (item) ->
8         @gain() + item.value <= @size
9
10    addItem: (item) ->
11        if @fits item
12            @items.push item
13            @dep.changed()
14
15    gain: ->
16        roundValue _.reduce @getItems(), ((total, item) -> total+item.
17            value), 0
18
19    getItems: ->
20        @dep.depend()
21        @items
22
23    reset: ->
24        @items = []
25        @dep.changed()
```

### 3 The Online-Knapsack-Problem

In the former *offline*-knapsack-problem, we know all items that we want to put in the knapsack. In the *online*-version of this problem, we do not know every item, but get the items one by one. We therefore have to decide after every item, whether we put the item in the knapsack or not.

We create a base-algorithm for that:

```
1  Algorithm = class
2      constructor: ->
3          @act = new ReactiveVar
4          @_knapsack = new Knapsack
5      knapsack: -> @_knapsack
6
7      handle: (item) ->
8          if @decide item
9              @_knapsack.addItem item
10             return yes
11          else
12              return no
13      decide: (item) ->
14          # implement me and return yes or no
15
16      reset: ->
17          @_knapsack.reset()
18          @act.set null
19      doAct: (like) -> @act.set like
20      acts: (like) -> @act.get() is like
```

What maximum gain would can we achieve and how would an online-algorithm perform in comparison with an optimal offline-algorithm, which would know every item?

Let's try out.

```
1  experiments = []
```

Lets start with the greedy aproach. Here, we just take every item we get, if it fits:

```
1 decideGreedy = (item) -> if @knapsack().fits item then yes else no
```

and we define an algorithm with it:

```
1 Greedy = class extends Algorithm
2   decide: decideGreedy
```

The gain of this algorithm is at least  $1 - \beta$ , where  $\beta$  is the size of the item with the highest value (weight). The proof is simple: if we get this item with value  $\beta$ , the gain is certainly higher than  $\beta$ . If this item does not fit anymore in the knapsack, we will have at least  $1 - \beta$  gain.

Lets do some experiments with it to verify this:

```
1 experiments.push
2   name: -> "Greedy G"
3   description: -> "G archieves at least 1-beta, where beta is here
4     #{@beta}"
5   beta: 0.5
6   Algorithm: Greedy
7
8 experiments.push
9   name: -> "Greedy G"
10  description: -> "G archieves at least 1-beta, where beta is here
11    #{@beta}"
12  beta: 0.2
13  Algorithm: Greedy
14
15 experiments.push
16   name: -> "Greedy G"
17   description: -> "G archieves at least 1-beta, where beta is here
18     #{@beta}"
19   beta: 0.8
20   Algorithm: Greedy
```

## 4 Online-Algorithm with advice

Imaging you had an oracle, that would know all items that will come. How many bits of information from this oracle would you need to get an optimal solution? And for a given amount of these advice bits, how good would your algorithm perform?

We define such an algorithm as *online algorithm with advice*.

Let  $I$  be an input of such an online algorithm  $A$  and  $\Phi$  an (infinite) sequence of bits (1 or 0), called \*advice bits. The online-algorithm can read a finit prefix of this sequence.

The gain of this Algorithm is  $gain(A^\Phi(I))$ .

If we have  $n$  items in a solution and have read  $s(n)$  advice-bits while computing this solution in the algorithm we call  $s(n)$  the *advice-complexity*.

If we compare the *gain* of this algorithm with the gain of an optimal offline algorithm  $OPT$ , we can define its *competitiveness*:

$$gain(A^\Phi(I)) \geq 1/c * gain(OPT(I)) - \alpha$$

where  $\alpha$  is a constant and we call this algorithm *c-competitive*. If  $\alpha = 0$ ,  $A$  is *strictly c-competitive*.

Let's implement a base class for such an algorithm:

```

1 AlgorithmWithAdvice = class extends Algorithm
2   constructor: ->
3     @adviceBits = new ReactiveVar
4     super
5   askOracle: (items) ->
6     if @oracle?
7       @adviceBits.set @oracle items
8   oracle: (items) ->
9     # implement me and return an array of advice-bits
10  readAdviceBit: (index) ->
11    @adviceBits.get()[index]
12  reset: ->
13    super
14    @adviceBits.set null

```

## 4.1 Optimal online algorithm with advice

Let's go back to the first question with the first question: how many advice bits do we have to read to get an optimal solution?

Consider an algorithm with an oracle, that would give us a bit for every item coming with

- value 1 if the item is part of the solution
- value 0 if the item does not belong to the solution

Obviously, we need  $n$  bits of advice for that, or  $n-1$ , because for the last item, we can assume that it is part of the optimal solution.

We now define an algorithm for that.

Note: The items are prepared in a way, that some are already marked as solution. That makes it easier to define the oracle here:

```

1 TotalInformation = class extends AlgorithmWithAdvice
2   oracle: (items) ->
3     bits = []
4     for item in items
5       bits[item.index] = if item.isPartOfSolution then 1 else 0
6     # we do not need the last bit
7     bits.pop()
8     return bits

```

The decision is now easy. If we have a bit (yes / no), we use it:

```

1   decide: (item) ->
2     adviceBit = @readAdviceBit item.index
3     if adviceBit? then adviceBit else yes

```

Lets do an experiment with it:

```

1 experimentsWithAdvice = []
2 experimentsWithAdvice.push
3   name: -> "Total Information"
4   beta: 0.4
5   Algorithm: TotalInformation

```

As (Böckenhauer et al.) states, any algorithm for the online simple knapsack problem needs at least  $n-1$  bits to be optimal.

## 4.2 1 Advice bit

What's the best gain if we had only 1 advice bit?

Let's do an experiment where we have an oracle that gives us one bit:

```
1 AONE = class extends AlgorithmWithAdvice
2   oracle: (allItems) -> [ _.some allItems, (item) -> item.value >
      0.5 ] # array with one bit
```

The bit tells us:

- 1: There exists an item with a size  $> 0.5$
- 0: There is no such item

If the bit is 0, the algorithm acts greedy (like before). If the bit is 1, the algorithm waits until the item with size  $> 0.5$  appears and will start acting greedily:

```
1   decide: (item)->
2     adviceBit = @readAdviceBit item.index
3     if adviceBit? # existence
4       if adviceBit is false then @doAct "greedy" else @doAct "
        wait"
5     if @acts "greedy" then decideGreedy.call @, item else @wait
        item
6
7   wait: (item) ->
8     if item?.value > 0.5
9       @doAct "greedy"
10      decideGreedy.call @, item
11    else
12      no
```

This algorithm is 2-competitive:

- If there is no item with weight  $> 1/2$ , the gain is at least  $1/2$  as we have already seen in the greedy approach.
- On the other hand if such an item exists, the algorithm will wait for it and put it in, so it will get a gain of at least  $1/2$

We do an experiment with a max size of one item of 0.55 to verify this:

```
1 experimentsWithAdvice.push
2   name: "AONE - with one advice bit"
3   description: "AONE is 2-competitive"
4   beta: 0.55
5   Algorithm: AONE
```

This one single bit gives us an competitive-ratio of 2, but what happens if we increase the amount of bits? Can we achieve a better ratio?

Unfortunately, more advice bits does not give us a better competitive-ratio, at least for a sub-logarithmic amount  $s(n)$  of advice bits. Figure 1 shows the number of bits compared with the achieved competitive-ratio.

There is a second jump at  $SLOG$ -bits, where competitiveness is  $1 + \varepsilon$ . The proof for these intervals is found in the source (Böckenhauer et al.).

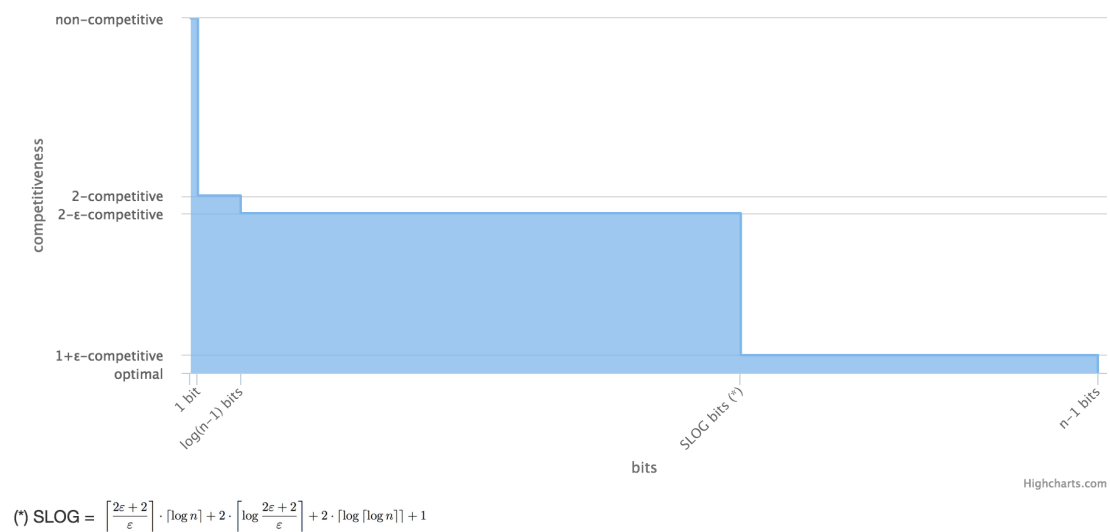


Figure 1: Number of bits VS competitiveness

## 5 Randomized online-algorithms

Obviously in real online-problems, we do not have an omniscient oracle. But we can use the idea of the oracle and just guess the advice bits *randomly*.

We can then estimate the competitiveness of this *randomized online-algorithm*.

### 5.1 RONE - AONE with random advice bit

Let's start with AONE from the previous experiment, but guess the adviceBit randomly:

```
1 RONE = class extends AONE
2   oracle: ->
3     [Math.random() < 0.5]
```

If we guess wrong, we might get a lower gain than 0.5 or even 0, if the adviceBit is 1 and we have no item with size > 0.5.

So while we have a 2-competitiveness in AONE, we have here a 4-competitiveness in expectation (in 50% of the cases, we are wrong).

```
1 randomExperiments = []
2 randomExperiments.push
3   name: "RONE - one random bit"
4   description: "Is 4-competitive in expectation"
5   beta: 0.55
6   Algorithm: RONE
```

The experiment does not show this directly, because the items are prepared in a way, that not all possible cases are evenly distributed. We expected that in 50% of the cases, the algorithm would guess wrongly and we would gain nothing, but in the experiment this probability is lower.



## 5.2 2-competitiveness with 1 advice bit

The competitive-ratio of 4 is somewhat obvious, but surprisingly, we can also achieve a ratio of 2 with only 1 advice bit.

Consider an algorithm that chooses randomly between two algorithms A1 and A2. A1 is the greedy approach we already know:

```
1 A1 = Greedy
```

A2 internally simulates A1 at the beginning:

```
1 A2 = class extends Algorithm
2   reset: ->
3     super
4     @a1 = new A1
5     @doAct "simulateA1"
```

To decide whether it will use the item or not, it first offers it to the simulated A1-Algorithm. As soon as A1 won't take the item anymore (A1's knapsack is full), A2 starts to act greedily:

```
1   decide: (item) ->
2     if @acts "simulateA1"
3       if @a1.handle item
4         return no
5       else
6         @doAct "greedy"
7         return @decide item
8     else if @acts "greedy"
9       return decideGreedy.call @, item
```

We now compose an algorithm "RONE2", that chooses randomly between A1 and A2:

```
1 RONE2 = class extends AlgorithmWithAdvice
2   constructor: ->
3     @a1 = new A1
4     @a2 = new A2
5     super
6   oracle: -> [Math.random() < 0.5]
7   reset: ->
8     super
9     @a1.reset()
10    @a2.reset()
11   knapsack: -> @algorithm().knapsack()
12   # handle decides and put the item in the knapsack
13   handle: (item) ->
14     adviceBit = @readAdviceBit item.index
15     if adviceBit? # existence of the first bit
16       if adviceBit then @doAct "A1" else @doAct "A2"
17     @algorithm().handle item
18   algorithm: ->
19     if @acts "A1" then @a1 else @a2
```

We do now an experiment with it:

```
1 randomExperiments.push
2   name: "RONE2 - one random bit"
3   description: "Is 2-competitive in expectation"
4   beta: 0.55
5   Algorithm: RONE2
```

To show that this algorithm is 2-competitive in expectation, we consider two cases:

- If the sum of all items is less than the knapsack's capacity, A1 is optimal, while A2 gains 0. Because we chose randomly between the two algorithm, we have a 50% chance to get an optimal gain (or to get 0).
- If the sum is greater, the total gain of A1 and A2 is at least 1. Because we chose randomly between the two, we get a 0.5 gain in expectation.

Considering both cases, we get a gain of 0.5 in expectation, so the algorithm is 2-competitive.

### 5.3 The limit

While we can achieve different levels of competitiveness by increasing the number of bits in online algorithms with advice, this is not the case in randomized-online-algorithms.

As (Böckenhauer et al.) states, there is no algorithm that performs better than 2-competitive in expectation. So 2-competitiveness with 1 bit is the best we can achieve.

## 6 Setup

The following code sets the experiments up. First, define some constants and helpers:

```
1 Constants =  
2     SCALE: 300  
3  
4 roundValue = (value) -> Math.round(value*100)/100
```

### 6.1 Create items

The creation of items is done here. The items are prepared in a way, so that we now which elements are part of the solution (for experiment "Total information").

```
1 createItems = ({beta, maxSize}) ->  
2     items = []  
3     beta ?= 0.5  
4     maxSize ?= 1  
5     totalSize = 0  
6  
7     loop  
8         randomValue = -> roundValue Math.random()*beta  
9         value = randomValue()  
10        if totalSize+value < maxSize  
11            totalSize += value  
12            items.push {value, isPartOfSolution: yes}  
13        else  
14            # add one that fits exactly  
15            items.push  
16                value: roundValue maxSize - totalSize  
17                isPartOfSolution: yes  
18            # add the one that does not fit  
19            items.push {value}  
20            break  
21  
22        items = _.shuffle items  
23        for item, index in items  
24            item.index = index  
25        # we later pop the elements out (from the end) because it is  
26        # faster. So we reverse here:  
27        return items.reverse()
```

### 6.2 Experiment templates

Add the experiments to the template:

```
1 Template.experiments.helpers  
2     experiments: -> experiments  
3     experimentsWithAdvice: -> experimentsWithAdvice  
4     randomExperiments: -> randomExperiments
```

Initialize it. We use some ReactiveVars to store the state of the experiment on the template instance.

```
1 Template.Experiment.onCreated ->  
2     @items = []  
3     @currentItem = new ReactiveVar  
4     @numberOfItems = new ReactiveVar  
5     @algorithm = new @data.Algorithm
```

Lets define a history, where we can read some stats about the experiments from:

```

1  @gainHistory =
2    history: []
3    dep: new Tracker.Dependency
4    add: (gainValue) ->
5      if gainValue > 0
6        @worstGain = Math.min @worstGain ? gainValue,
          gainValue
7        @bestGain = Math.max @bestGain ? gainValue, gainValue
8        @history.push gainValue
9        @dep.changed()
10   size: ->
11     @dep.depend()
12     @history.length
13   worst: ->
14     @dep.depend()
15     @worstGain
16   best: ->
17     @dep.depend()
18     @bestGain
19   competitiveCount: ->
20     @dep.depend()
21     _.countBy @history, (value) ->
22       if value is 1
23         "1-competitive"
24       else if 0.5 <= value < 1
25         "2-competitive"
26       else if 0.25 <= value < 0.5
27         "4-competitive"
28       else
29         "non-competitive"
30
31   competitivePercentage: (cGroup)->
32     @dep.depend()
33     if @history.length > 0
34       roundValue 100 * @competitiveCount()[cGroup] /
          @history.length
35   avg: ->
36     @dep.depend()
37     if @history.length > 0
38       roundValue (_.reduce @history, (total, value) -> total
          +value)/@history.length
39   reset: ->
40     @history = []
41     @bestGain = null
42     @worstGain = null
43     @dep.changed()

```

### 6.3 Initialize and reset experiment

```

1  resetExperiment = =>
2    @items = createItems beta: @data.beta
3    @algorithm.reset?()
4    @algorithm.askOracle? @items
5    @numberOfItems.set @items.length
6    @currentItem.set @items.pop()
7
8  do reset = =>

```

```

9      @gainHistory.reset()
10     resetExperiment()

```

## 6.4 Running the experiment

The Ticker is a package, that can run a callback in a loop. We can run it step-by-step or fast.

```

1      @ticker = new Ticker
2      reset: => reset()
3      turn: =>
4          item = @currentItem.get()
5          if item?
6              @algorithm.handle item
7              @currentItem.set @items.pop()
8          else
9              # no more items
10             @gainHistory.add @algorithm.knapsack().gain()
11             resetExperiment()

```

Expose the state to the template:

```

1  Template.Experiment.helpers
2      adviceBits: -> Template.instance().algorithm.adviceBits?.get()
3      act: -> Template.instance().algorithm.act.get()
4      knapsack: -> Template.instance().algorithm.knapsack()
5      ticker: -> Template.instance().ticker
6      currentItem: -> Template.instance().currentItem?.get()
7      gainHistory: -> Template.instance().gainHistory
8      numberOfItems: -> Template.instance().numberOfItems.get()
9      willMatch: ->
10         ctx = Template.instance()
11         ctx.currentItem?.get()?.value + ctx.algorithm.knapsack().gain
12         () <= ctx.algorithm.knapsack().size
13
14 Template.Knapsack.helpers
15     totalWidth: ->
16         @size * Constants.SCALE + 2
17     items: ->
18         @getItems()
19
20 Template.KnapsackItem.helpers
21     width: ->
22         @value * Constants.SCALE
23     color: ->
24         hue = @value*360
25         "hsl({hue}, 73%, 69%)"

```

## 6.5 Chart

The chart from 1 is created by this code:

```

1  Template.competitivenessChart.helpers
2      chartObject: ->
3          legend: enabled: false
4          title: text: ""
5          yAxis:
6              title: text: "competitiveness"
7              tickPositioner: -> [1,1.1,1.9,2,3]

```

```

8         labels:
9             formatter: ->
10                 switch @value
11                     when 1 then "optimal"
12                     when 1.1 then "1+eps-competitive"
13                     when 1.9 then "2-eps-competitive"
14                     when 2 then "2-competitive"
15                     when 3 then "non-competitive"
16
17     xAxis:
18         title: text: "bits"
19         tickPositioner: -> [0,1,7,77,127]
20         labels:
21             rotation: -45
22             formatter: ->
23                 switch @value
24                     #when 0 then "0 bits"
25                     when 1 then "1 bit"
26                     when 7 then "log(n-1) bits"
27                     when 77 then "SLOG bits (*)"
28                     when 127 then "n-1 bits"
29
30     series: [
31         type: "area"
32         step: "left"
33         data: [
34             (x: 0, y: 3, name: "non-competitive")
35             (x: 1, y: 2, name: "2-competitive")
36             (x: 7, y: 1.9, name: "2-eps-competitive")
37             (x: 77, y: 1.1, name: "1+eps-competitive")
38             (x: 127, y: 1, name: "optimal")
39         ]
40     ]

```

## 6.6 GUI for the Ticker

```

1 Template.TickerGui.helpers
2     counter: -> @ticker.getCounter()
3
4 Template.TickerGui.events
5     'click .btn-step': -> @ticker.step()
6     'click .btn-play': ->
7         @ticker.setTimeout 100
8         @ticker.play()
9     'click .btn-play-fast': ->
10         @ticker.setTimeout 0
11         @ticker.play()
12     'click .btn-stop': -> @ticker.stop()
13     'click .btn-reset': -> @ticker.reset()

```

## A Additional source files

### A.1 client/app.jade (template)

```
1 body
2   .container
3
4     .page-header
5       h1 Advice Complexity of the Online-Knapsack-Problem
6
7     +experiments
8
9   head
10    title Advice Complexity of the Online-Knapsack-Problem
11  template(name="experiments")
12    each experiments
13      +Experiment
14    h2 Online algorithms with advice
15    each experimentsWithAdvice
16      +Experiment
17    +competitivenessChart
18    h2 Randomized online algorithm
19    each randomExperiments
20      +Experiment
21
22
23
24
25  template(name="Experiment")
26    .panel.panel-default
27      .panel-heading
28        h2.panel-title {{name}}
29      .panel-body
30        {{description}}
31      .row
32        .col-xs-12.col-sm-5
33          table.table
34            tr
35              th Number of experiments:
36              td {{gainHistory.size}}
37            tr
38              th Average gain:
39              td {{gainHistory.avg}}
40            tr
41              th Best gain:
42              td {{gainHistory.best}}
43            tr
44              th Worst gain:
45              td {{gainHistory.worst}}
46            tr
47              th 1-competitive:
48              td {{gainHistory.competitivePercentage "1-competitive"}} %
49            tr
50              th 2-competitive:
51              td {{gainHistory.competitivePercentage "2-competitive"}} %
52            tr
53              th 4-competitive:
```

```

54         td {{gainHistory.competitivePercentage "4-
           competitive"}} %
55     tr
56         th non-competitive:
57         td {{gainHistory.competitivePercentage "
           non-competitive"}} %
58     .row
59         .col-xs-12
60         +TickerGui ticker=ticker
61     .row
62         .col-xs-12.col-sm-5
63         table.table
64             tr
65                 th acts:
66                 td {{act}}
67             tr
68                 th adviceBits:
69                 td.adviceBits=adviceBits
70             tr
71                 th Number of items:
72                 td {{numberOfItems}}
73
74     .row
75         .currentItemContainer.col-xs-6
76         h4 Current item:
77
78         if currentItem
79             p value: {{currentItem.value}}
80
81             +KnapsackItem(currentItem)
82             if willMatch
83                 .matches.yes
84                 .glyphicon.glyphicon-arrow-right
85             else
86                 .matches.no
87                 .glyphicon.glyphicon-remove
88
89         .knapsackContainer.col-xs-6
90         +Knapsack knapsack
91
92
93 template(name="Knapsack")
94     .knapsack(style="width: {{totalWidth}}px")
95         h4 knapsack
96         p items: {{items.length}}, gain: {{gain}}
97         .items
98
99         each items
100             +KnapsackItem
101
102
103 template(name="KnapsackItem")
104     .knapsack-item(style="width: {{width}}px; background-color: {{
        color}}")
105
106 template(name="competitivenessChart")
107
108
109     .panel.panel-default
110         .panel-heading
111         h2.panel-title Bits VS competitiveness

```



```
112     .panel-body
113       +highchartsHelper chartId="competitivenessChart"
114         chartWidth="100%" chartHeight="400px" chartObject=
115         chartObject
116       p (*) SLOG =
117         img(src="slog.png" height="40px")
118
119 template(name="TickerGui")
120   .ticker
121     .btn-group
122       button.btn.btn-step.btn-primary
123         .glyphicon.glyphicon-step-forward
124         | Step
125       button.btn.btn-play.btn-default
126         .glyphicon.glyphicon-play
127         | Play
128       button.btn.btn-play-fast.btn-default
129         .glyphicon.glyphicon-fast-forward
130         | Play Fast
131       button.btn.btn-stop.btn-warning
132         .glyphicon.glyphicon-stop
133         | Stop
134       button.btn.btn-reset.btn-danger
135         .glyphicon.glyphicon-fast-backward
136         | Reset
```

**A.2 client/app.styl (stylesheet)**

```
1
2 body
3     background-image: url("bg.png")
4
5 .knapsack
6     border: 2px solid blue
7     box-sizing: content-box
8     border-radius: 10px
9     overflow: hidden
10    text-align: center
11    .items
12        background-color: #eee
13        height: 75px
14        .knapsack-item
15            float: right;
16            border-right: none
17 .knapsack-item
18     border: 1px dashed black
19     height: 75px
20     box-sizing: border-box
21
22 .currentItemContainer
23     position: relative
24     .matches
25         position: absolute
26         right: 60px
27         bottom: 16px
28         border-radius: 10px
29         font-size: 32px
30         &.yes
31             color: green
32         &.no
33             color: red
34
35 .adviceBits
36     font-family: monospace
37
38 .table
39     td
40         text-align: right
41     th
42         text-align: left
43
44 .panel
45     margin-bottom: 200px
```

## References

Böckenhauer, Hans-Joachim, Dennis Komm, Richard Kralovic, and Peter Rossmanith. “The Online Knapsack Problem: Advice and Randomization.”