

```

Constants =
  SCALE: 300
  KNAPSACK_SIZE: 1

roundValue = (value) -> Math.round(value*100)/100

```

Knapsack

The Knapsack will contain the objects and can return its yield (= the total of items' value)

```

Knapsack = class
  constructor: ->
    @size = Constants.KNAPSACK_SIZE
    @dep = new Tracker.Dependency
    @reset()

  reset: ->

    @items = []
    @dep.changed()

  fits: (item) -> @yield() + item.value <= Constants.KNAPSACK_SIZE

  addItem: (item) ->
    if @fits item
      @items.push item
      @dep.changed()

  yield: ->
    roundValue _.reduce @getItems(), ((total, item) -> total+item.value), 0

  getItems: ->
    @dep.depend()
    @items

if Meteor.isClient
  experiments = []

  Algorithm = class
    constructor: ->
      @adviceBits = new ReactiveVar
      @act = new ReactiveVar
      @_knapsack = new Knapsack

```

```

knapsack: -> @_knapsack
askOracle: (items) ->
  if @oracle?
    @adviceBits.set @oracle items
    delete item.isPartOfSolution for item in items
readAdviceBit: (index) ->
  @adviceBits.get()[index]
reset: ->
  @_knapsack.reset()
  @adviceBits.set null
  @act.set null
handle: (item) ->
  if @decide item
    @_knapsack.addItem item
    yes
  else
    no
doAct: (like) -> @act.set like
acts: (like) -> @act.get() is like

```

Lets start with the greedy approach. Here, we just take every item we get, if it fits:

```
decideGreedy = (item) -> if @_knapsack.fits item then yes else no
```

and we define an algorithm with it:

```

Greedy = class extends Algorithm
  decide: decideGreedy

```

The yield of this algorithm is at least $1-\beta$, where β is the size of the item with the highest value (weight). Lets do some experiments with it:

```

experiments.push
  name: -> "Greedy G"
  description: -> "G achieves at least 1-beta, where beta is here #{@beta}"
  beta: 0.5
  Algorithm: Greedy

experiments.push
  name: -> "Greedy G"
  description: -> "G achieves at least 1-beta, where beta is here #{@beta}"
  beta: 0.2
  Algorithm: Greedy

```

```

experiments.push
  name: -> "Greedy G"
  description: -> "G achieves at least 1-beta, where beta is here #{@beta}"
  beta: 0.8
  Algorithm: Greedy

```

Advice bits

Imagine you had an oracle, that would know all items that will come. How many bits of information from this oracle would you need to get an optimal solution? And for a given amount of these advice bits, how good would your algorithm perform?

Let's start with the first question.

Consider an algorithm with an oracle, that would give us a bit for every item coming with

- value 1 if the item is part of the solution
- value 0 if the item does not belong to the solution

We now define an algorithm for that.

Note: The items are prepared in a way, that some are already marked as solution. That makes it easier to define the oracle here:

```

TotalInformation = class extends Algorithm
  oracle: (items) ->
    bits = []
    for item in items
      bits[item.index] = if item.isPartOfSolution then 1 else 0
    # we do not need the last (n-1)
    bits.pop()
    return bits

```

The decision is now easy. If we have a bit (yes / no), we use it:

```

decide: (item) ->
  adviceBit = @readAdviceBit item.index
  if adviceBit? then adviceBit else yes

```

Let's do an experiment with it:

```

experiments.push
  name: -> "Total Information"
  beta: 0.4
  Algorithm: TotalInformation

```

1 Advice bit

What's the best yield if we had only 1 advice bit?

Let's do an experiment where we have an oracle that gives us one bit:

```
AONE = class extends Algorithm
  oracle: (allItems) -> [ _.some allItems, (item) -> item.value > 0.5 ] # array with c
```

The bit tells us:

- 1: There exists an item with a size > 0.5
- 0: There is no such item

If the bit is 0, the algorithm acts greedy (like before). If the bit is 1, the algorithm waits until the item with size > 0.5 appears and will start acting greedily:

```
decide: (item)->
  adviceBit = @readAdviceBit item.index
  if adviceBit? # existence
    if adviceBit is false then @doAct "greedy" else @doAct "wait"
  if @acts "greedy" then decideGreedy.call @, item else @wait item

wait: (item) ->
  if item?.value > 0.5
    @doAct "greedy"
    decideGreedy.call @, item
  else
    no
```

We do an experiment with a max size of one item of 0.55:

```
experiments.push
  name: "AONE - with one advice bit"
  description: "AONE is 2-competitive"
  beta: 0.55
  Algorithm: AONE
```

Random Online-Algorithm:

```
RONE = class extends AONE
  oracle: ->
    [Math.random() < 0.5]
```

```

experiments.push
  name: "RONE - one random bit"
  description: "Is 4-competitive in expectation"
  beta: 0.55
  Algorithm: RONE

A1 = Greedy
A2 = class extends Algorithm
  reset: ->
    super
    @a1 = new A1
    @doAct "simulateA1"

  decide: (item) ->
    if @acts "simulateA1"
      if @a1.handle item
        no
      else
        @doAct "greedy"
        @decide item
    else if @acts "greedy"
      decideGreedy.call @, item

RONE2 = class extends Algorithm
  constructor: ->
    @a1 = new A1
    @a2 = new A2
    super
  oracle: -> [Math.random() < 0.5]
  reset: ->
    super
    @a1.reset()
    @a2.reset()
  knapsack: -> @algorithm().knapsack()
  handle: (item) ->
    adviceBit = @readAdviceBit item.index
    if adviceBit? # existence
      if adviceBit then @doAct "A1" else @doAct "A2"
    @algorithm().handle item

```

```

algorithm: ->
  if @acts "A1" then @a1 else @a2

experiments.push
  name: "RONE2 - one random bit"
  description: "Is 2-competitive in expectation"
  beta: 0.55
  Algorithm: RONE2

createItems = ({beta, maxSize}) ->

  items = []
  beta ?= 0.5
  maxSize ?= 1
  totalSize = 0

  loop
    randomValue = -> roundValue Math.random()*beta
    value = randomValue()
    if totalSize+value < maxSize
      totalSize += value
      items.push {value, isPartOfSolution: yes}
    else
      # add one that fits exactly
      items.push
        value: roundValue maxSize - totalSize
        isPartOfSolution: yes
      # add the one that does not fit
      items.push {value}

  break

  items = _.shuffle items
  for item, index in items
    item.index = index
  return items.reverse() # we later pop the elements out (from the end) because it is

```

```
Template.experiments.helpers
  experiments: -> experiments
```

```
Template.Experiment.onCreated ->
```

```
  @items = []

  @currentItem = new ReactiveVar
  @numberOfItems = new ReactiveVar
  @algorithm = new @data.Algorithm
  @yieldHistory =
    history: []
    dep: new Tracker.Dependency
    add: (yieldValue) ->
      if yieldValue > 0
        @worstYield = Math.min @worstYield ? yieldValue, yieldValue
        @bestYield = Math.max @bestYield ? yieldValue, yieldValue
        @history.push yieldValue
        @dep.changed()
    size: ->
      @dep.depend()
      @history.length
    worst: ->
      @dep.depend()
      @worstYield
    best: ->
      @dep.depend()
      @bestYield
    competitiveCount: ->
      @dep.depend()
      _.countBy @history, (value) ->

        if value is 1
          "competitive"
        else if value is 0
          "nonCompetitive"
        else
          "neither"
    nonCompetitive: ->
      @dep.depend()
      if @history.length > 0
        roundValue @competitiveCount().nonCompetitive / @history.length
    competitive: ->
```

```

        @dep.depend()
        if @history.length > 0
            roundValue @competitiveCount().competitive / @history.length
    avg: ->
        @dep.depend()
        if @history.length > 0
            roundValue (_.reduce @history, (total, value) -> total+value)/@history.length
    reset: ->
        @history = []
        @bestYield = null
        @worstYield = null
        @dep.changed()
    resetExperiment = =>

    @items = createItems beta: @data.beta
    @algorithm.reset?()
    @algorithm.askOracle? @items
    @numberOfItems.set @items.length
    @currentItem.set @items.pop()

    do reset = =>
        @yieldHistory.reset()
        resetExperiment()

    @ticker = new Ticker
    reset: =>
        reset()

    turn: =>
        # 1. step: fetch new item
        # 2. step: put it in knapsack

        item = @currentItem.get()
        if item?
            @algorithm.handle item
            @currentItem.set @items.pop()
        else
            # no more items

            @yieldHistory.add @algorithm.knapsack().yield()
            resetExperiment()

```

```

Template.Experiment.helpers
  adviceBits: -> Template.instance().algorithm.adviceBits.get()

```



```

act: -> Template.instance().algorithm.act.get()
knapsack: -> Template.instance().algorithm.knapsack()
ticker: -> Template.instance().ticker
currentItem: ->Template.instance().currentItem?.get()
yieldHistory: -> Template.instance().yieldHistory
numberOfItems: -> Template.instance().numberOfItems.get()
willMatch: ->
    ctx = Template.instance()
    ctx.currentItem?.get()?.value + ctx.algorithm.knapsack().yield() <= ctx.algorithm.knapsack().capacity

Template.Knapsack.helpers
totalWidth: ->
    @size * Constants.SCALE+2 #2 is for rounding issues
items: ->
    @getItem()
Template.KnapsackItem.helpers
width: ->
    @value * Constants.SCALE
color: ->
    hue = @value*360
    "hsl({hue}, 73%, 69%)"

Template.TickerGui.helpers
counter: -> @ticker.getCounter()
Template.TickerGui.events
'click .btn-step': -> @ticker.step()
'click .btn-play': ->
    @ticker.setTimeout 100
    @ticker.play()
'click .btn-play-fast': ->
    @ticker.setTimeout 0
    @ticker.play()

'click .btn-stop': -> @ticker.stop()
'click .btn-reset': -> @ticker.reset()

```