

Module 3 | Lesson 3

# GLOBAL NAVIGATION SATELLITE SYSTEMS

# Global Navigation Satellite Systems

By the end of this video, you will be able to...

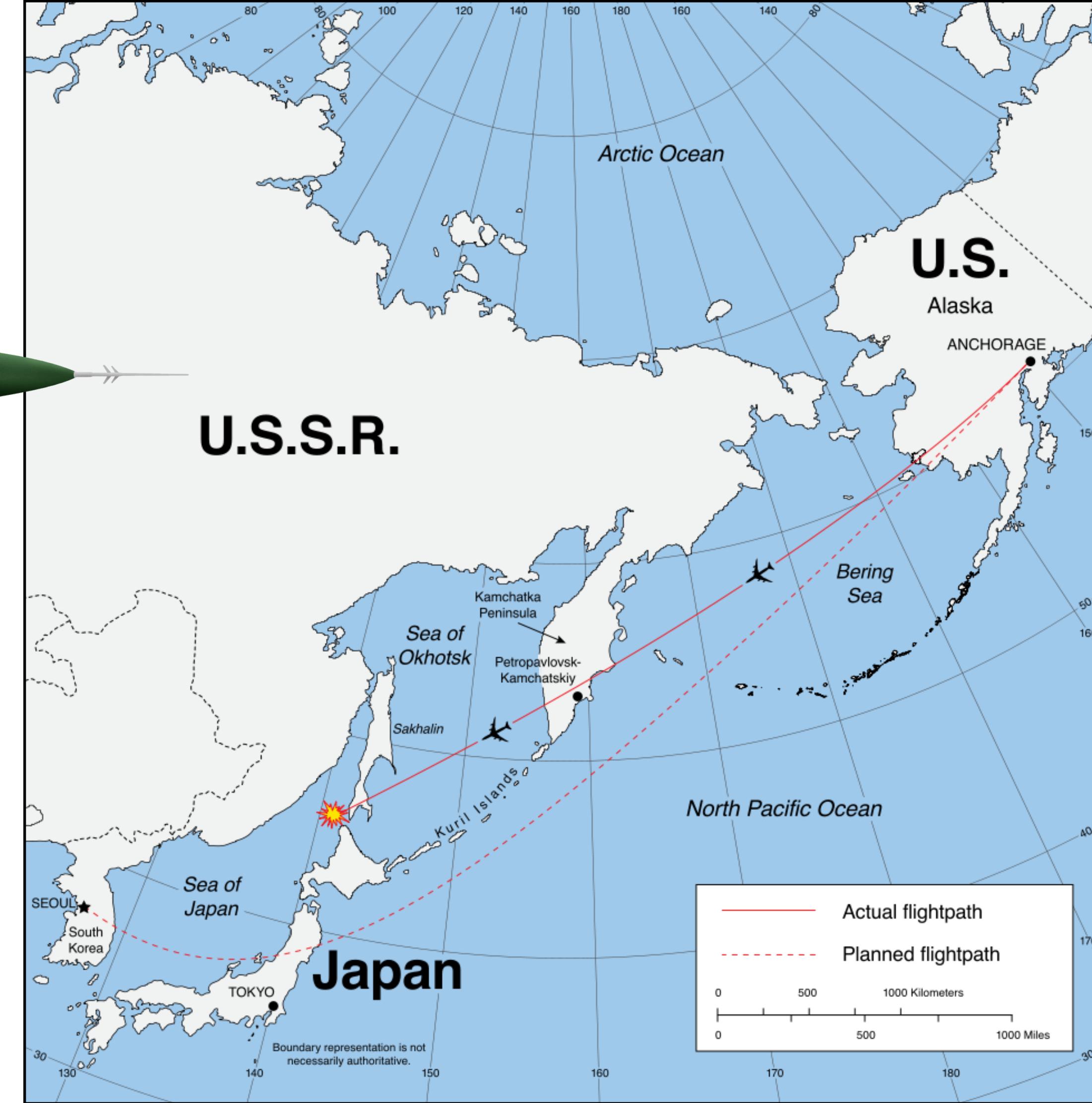
- Develop a model of GNSS positioning based on pseudoranging and trilateration.
- Become familiar with the sources of GNSS positioning error.
- Describe two ways to improve GNSS.

# Korean Air Lines Flight 007



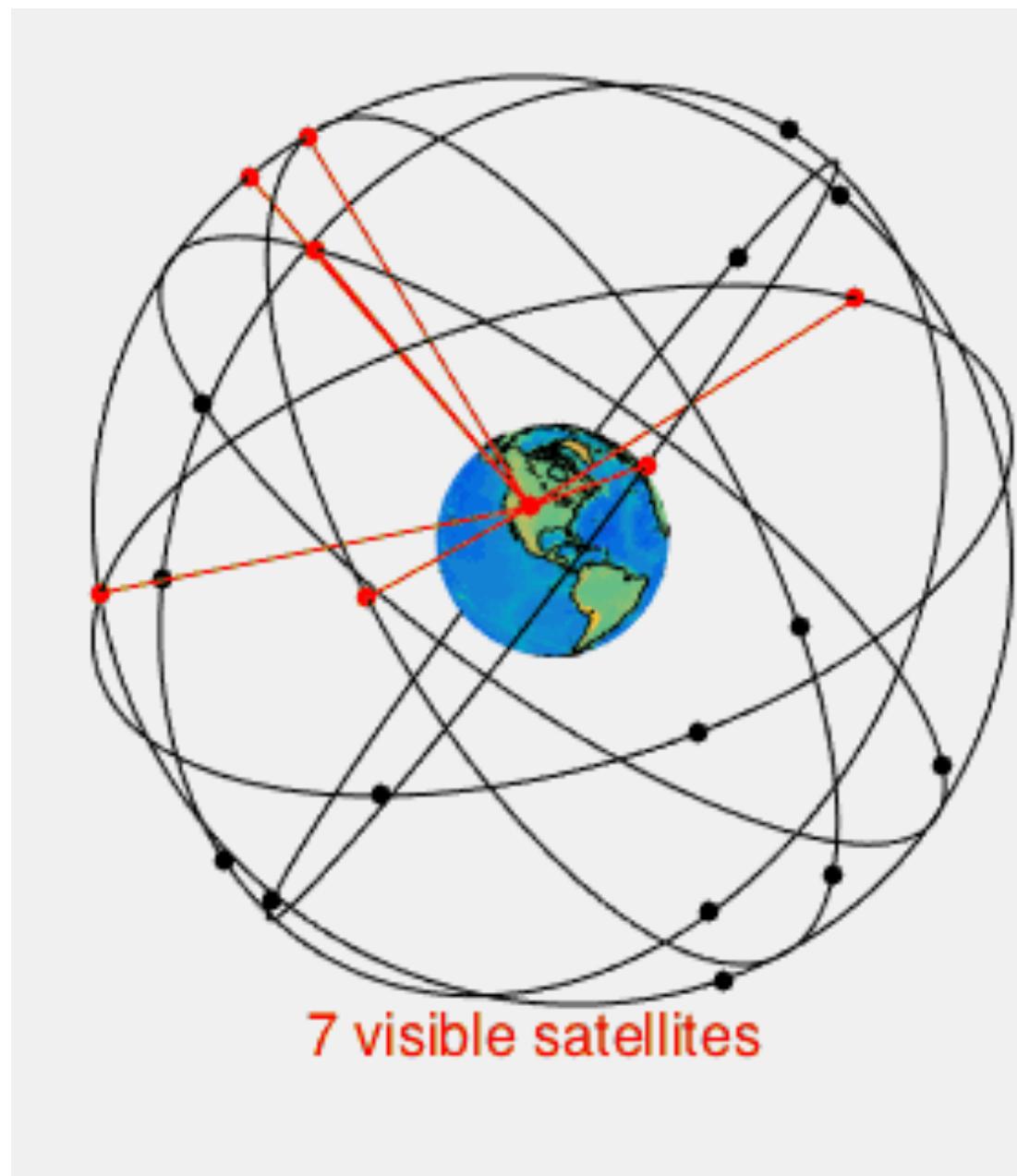
Korean Air Flight 007 was shot down in 1983 after deviating into Soviet airspace due to improper use of their Inertial Navigation System.

*This prompted the U.S. to open GPS for worldwide use.*

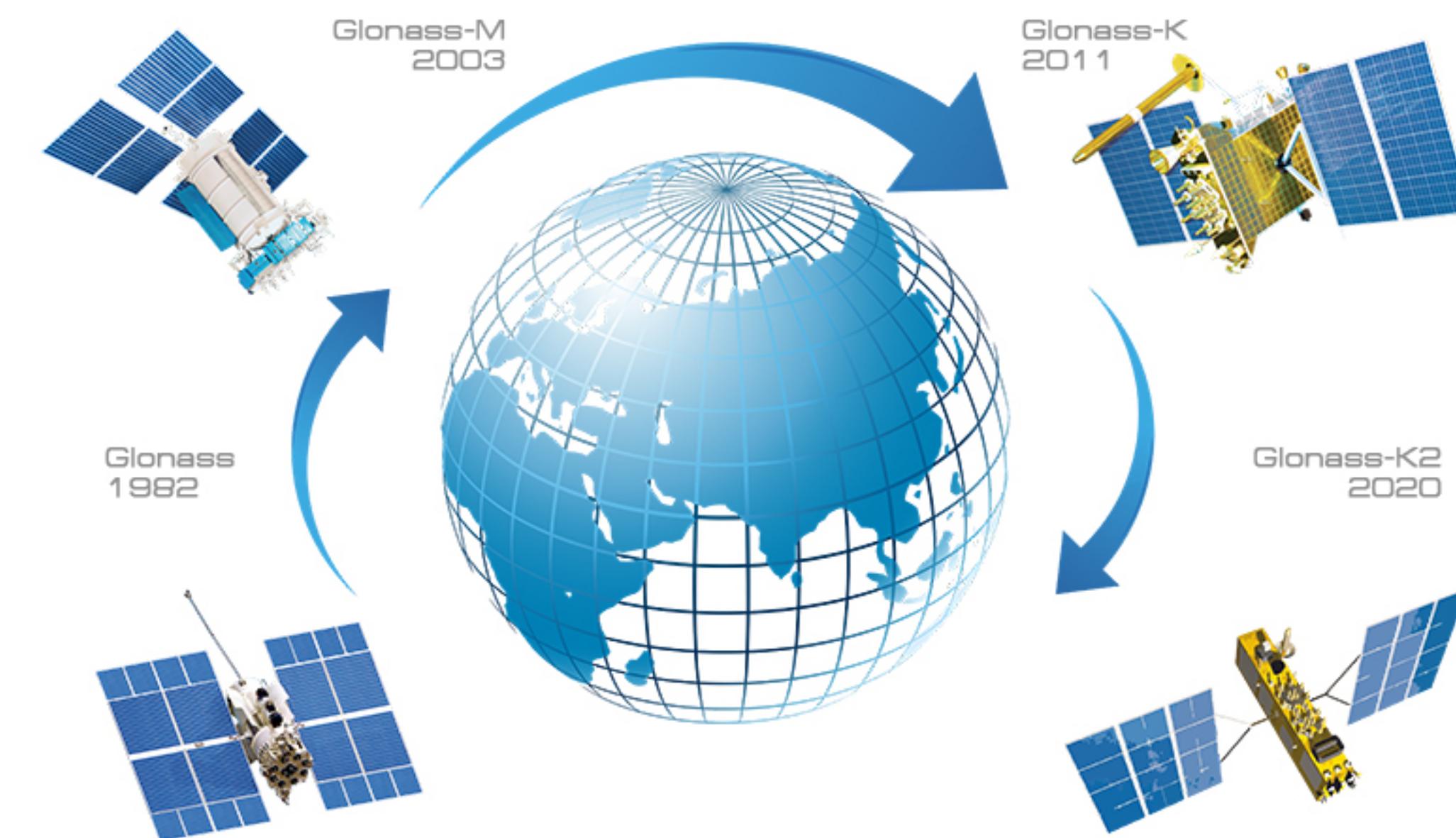


# GNSS | Accurate Global Positioning

- **Global Navigation Satellite System (GNSS)** is a catch-all term for a satellite system(s) that can be used to pinpoint a receiver's position anywhere in the world



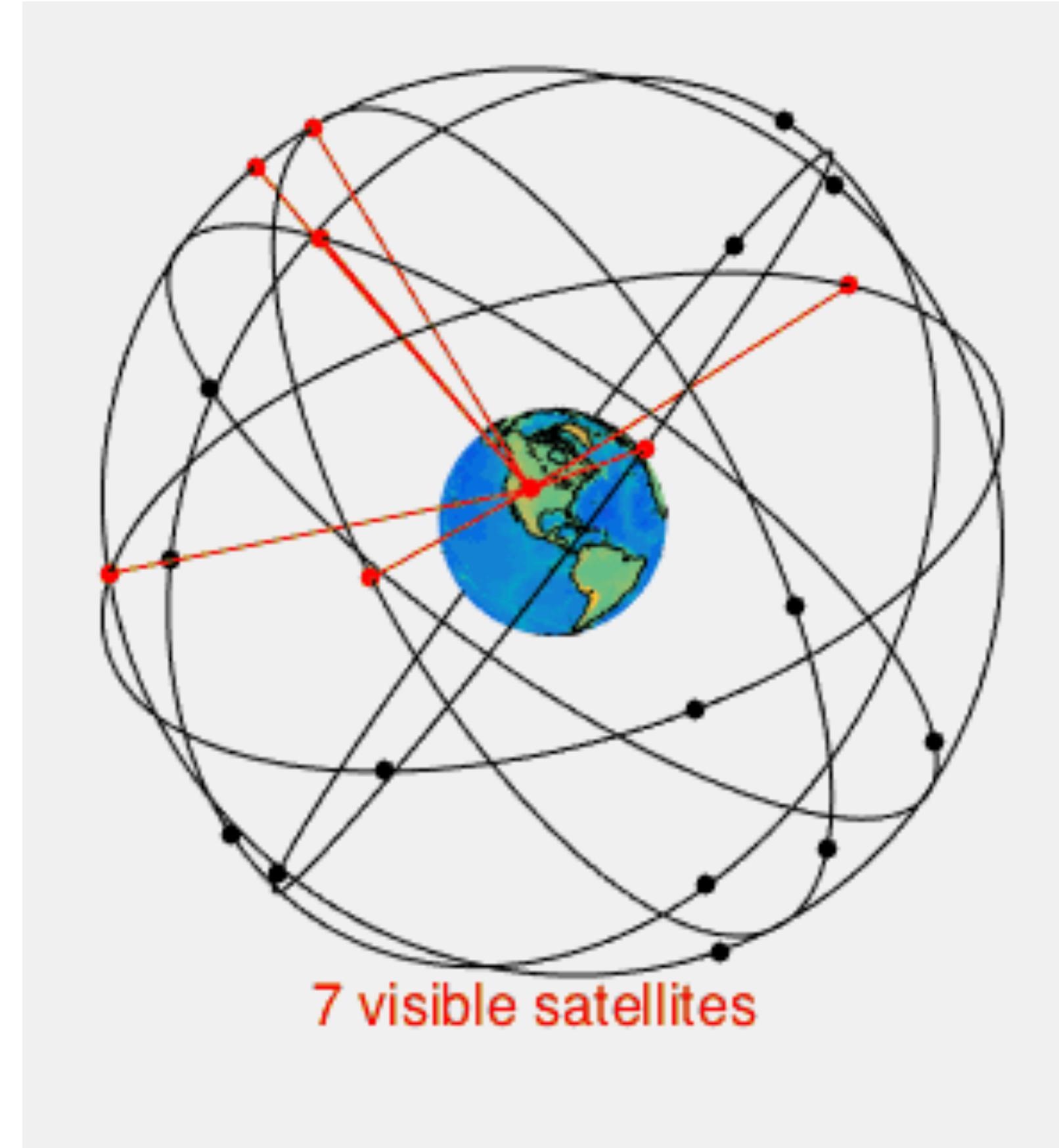
Global Positioning System (GPS)



Globalnaya navigatsionnaya  
sputnikovaya sistema (GLONASS)

# GPS | Global Positioning System

- Composed of 24 to 32 satellites in 6 orbital planes
  - *Altitude of ~20,200 km (12,550 miles)*
  - *Orbital period of ~12 hours*
- Each satellite broadcasts on two frequencies:
  - *L1 (1575.42 MHz, civilian + military)*
  - *L2 (1227.6 MHz, military)*



4 satellites  
are visible  
at any  
surface point  
on earth  
at all time

# GPS I Computing Position

- Each GPS satellite transmits a signal that encodes
  1. its *position*  
(via accurate ephemeris information)
  2. time of signal transmission  
(via onboard atomic clock)
- To compute a GPS position fix in the Earth-centred frame, the receiver uses the **speed of light** to compute distances to each satellite based on time of signal arrival



At least **four** satellites are required to solve for 3D position, three if only 2D is required (e.g., if altitude is known)

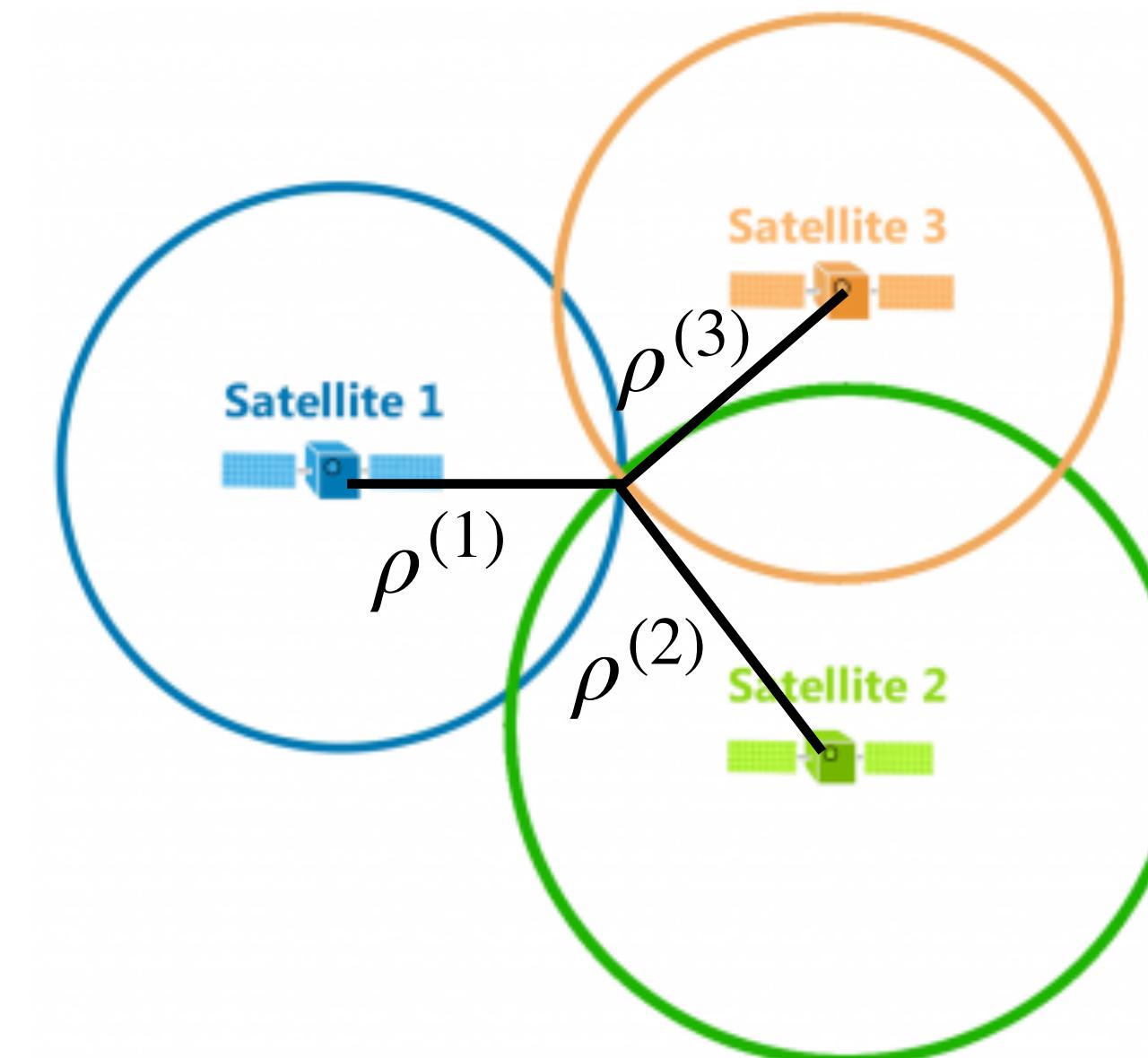
# Trilateration

Corrupted by errors & noises

- For each satellite, we measure the **pseudorange** as follows:

$$\rho^{(i)} = c(t_r - t_s) = \sqrt{(\mathbf{p}^{(i)} - \mathbf{r})^T (\mathbf{p}^{(i)} - \mathbf{r})} + c\Delta t_r + c\Delta t_a^{(i)} + \eta^{(i)}$$

$\mathbf{r}$	receiver (3D) position
$\mathbf{p}^{(i)}$	position of satellite $i$
$\Delta t_r$	receiver clock error
$\Delta t_a^{(i)}$	atmospheric propagation delay
$\eta$	measurement noise
$c$	speed of light
$t_s, t_r$	time sent, time received



Trilateration in 2D

# Trilateration

- By using at least 4 satellites, we can solve for:

$\mathbf{r}$  receiver (3D) position

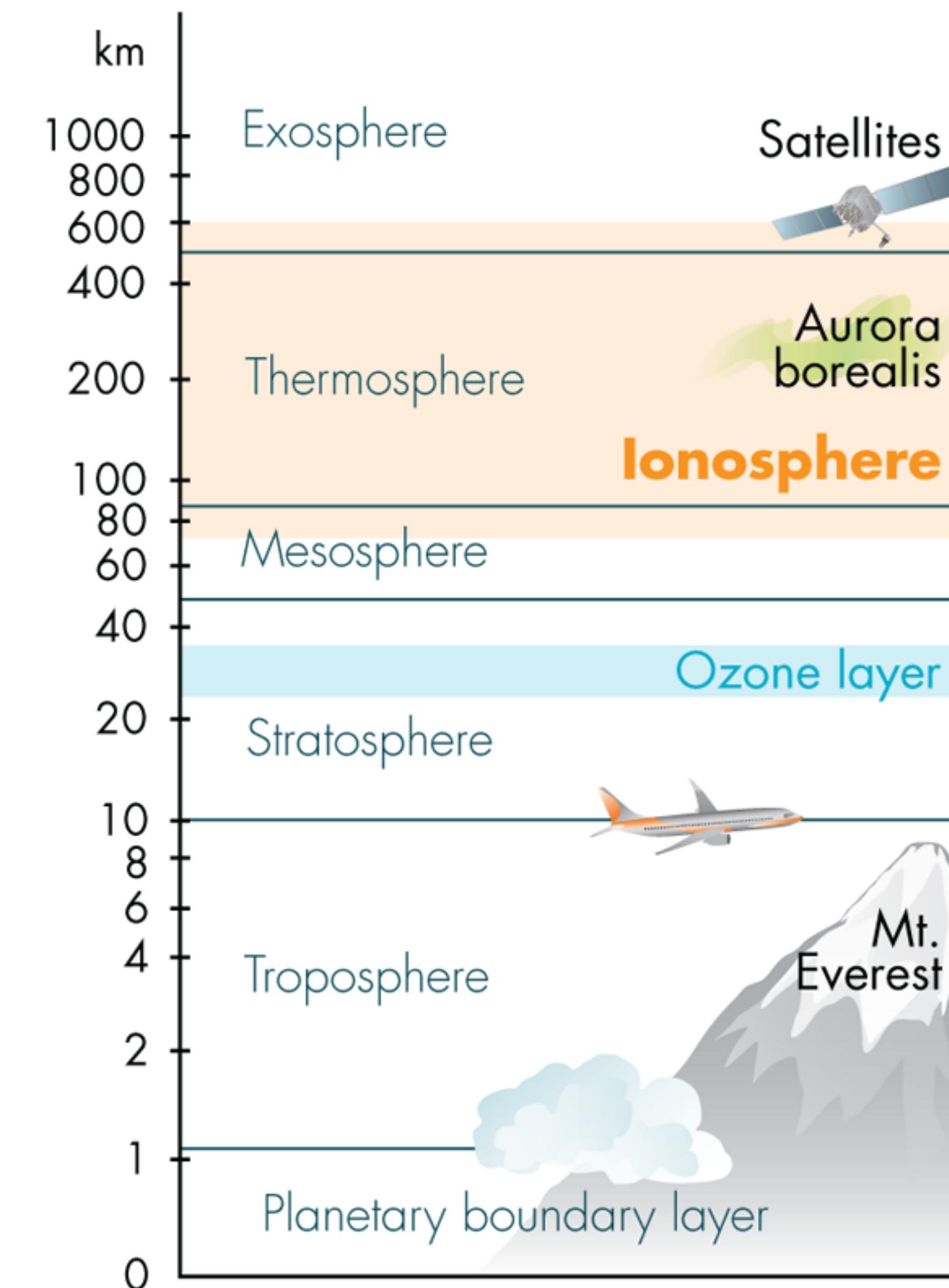
$\Delta t_r$  receiver clock error



*Multilateration in 3D*

# GPS | Error Sources (I)

- **Ionospheric delay**
  - Charged ions in the atmosphere affect signal propagation
- **Multipath effects**
  - Surrounding terrain, buildings can cause unwanted reflections



# GPS | Error Sources (II)

- Ephemeris & clock errors
  - A clock error of  $1 \times 10^{-6}$  s gives a 300 m position error!
- Geometric Dilution of Precision (GDOP)
  - The configuration of the visible satellites affects position precision.



Poor config - high GDOP



Good config - low GDOP

# GPS | Improvements

Basic GPS	Differential GPS (DGPS)	Real-Time Kinematic (RTK) GPS
mobile receiver	mobile receiver + fixed base station(s)	mobile receiver + fixed base station
no error correction	estimate error caused by atmospheric effects	estimate relative position using phase of carrier signal
~10 m accuracy	~10 cm accuracy	~2 cm accuracy

*Costly to implement*

# Summary | The Global Navigation Satellite System

- A GNSS works through trilateration via pseudoranging from at least 4 satellites (for a 3D position fix).
- GNSS error can be caused by ionospheric delays, multipath effects, and precision is also affected by GDOP.
- For GPS, differential GPS and RTK GPS are potential methods to substantially improve performance.