

Learning to think recursively

Recursion, generally, is when a function calls itself.

The main idea behind this is that a problem can be solved with the same logic, and by splitting the problem into smaller bits.

Recursion is used a lot with searching and sorting algorithms.





Iterative

```
void DrawLine_Iterative( int amount, char symbol )
{
    for ( int i = 0; i < amount; i++ )
        {
            cout << symbol;
        }
}</pre>
```

Sometimes, we can implement something as a simple loop...

Recursive

```
void DrawLine_Recursive( int amount, char symbol )
{
   if ( amount == 0 ) return;
   cout << symbol;
   DrawLine_Recursive( amount-1, symbol );
}</pre>
```

...or as a recursive function, with relative ease.

However, sometimes a recursive function makes for the simplest implementation

Recursive

```
void DrawLine_Recursive( int amount, char symbol )
{
   if ( amount == 0 ) return;
   cout << symbol;
   DrawLine_Recursive( amount-1, symbol );
}</pre>
```

When creating a function that will call itself, we need to make sure to include a

Base case (aka stopping case)

so the function does not loop forever.

But if that base case is not hit, we will do the process over again, and call the function with new parameters.

Iterative

```
int Factorial_Iterative( int number )
{
    int value = number;
    for ( int i = number-1; i > 0; i-- )
    {
       value *= i;
    }
    return value;
}
```

Recursive

```
int Factorial_Recursive( int number )
{
   if ( number == 0 )
      return 1;

   return ( number * Factorial_Recursive( number - 1 ) );
}
```

A recursive function can be void, or it can return a value.

It can take some work to think in terms of "recursion" instead of "iteration".

Build your function a step at a time, and test after each addition.



Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
    if ( number == 0 )
        return 1;

    return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
```

Factorial Recursive(5);

Number isn't 0, so multiply 5 by the result of Factorial_Recursive(4)

Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
    if ( number == 0 )
        return 1;
    return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
Factorial Recursive( 5 );
```

```
Call #2:
Factorial Recursive( 4 );
```

```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive( 4 )
```

Number isn't 0, so multiply 4 by the result of ${\tt Factorial_Recursive(3)}$

int Factorial Recursive(int number)

Let's step through the execution of this function...

```
of this function...

if ( number == 0 )
return 1;

return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
Factorial_Recursive( 5 );
```

Call #2: Factorial_Recursive(4);

```
Call #3:
Factorial_Recursive( 3 );
```

```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive( 4 )
```

```
Number isn't 0, so multiply 4 by the result of {\tt Factorial\_Recursive(3)}
```

```
Number isn't 0, so multiply 3 by the result of Factorial_Recursive( ^2 )
```

Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
   if ( number == 0 )
      return 1;

   return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
Factorial_Recursive( 5 );

Call #2:
Factorial_Recursive( 4 );

Call #3:
Factorial_Recursive( 3 );
```

```
Call #4:
Factorial_Recursive( 2 );
```

```
Call #5:
Factorial_Recursive( 1 );
```

```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive( 4 )
```

Number isn't 0, so multiply 4 by the result of Factorial_Recursive(3)

Number isn't 0, so multiply 3 by the result of Factorial Recursive(2)

Number isn't 0, so multiply 2 by the result of Factorial_Recursive(1)

Number isn't 0, so multiply 1 by the result of Factorial_Recursive(0)

Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
   if ( number == 0 )
      return 1;

   return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
Factorial_Recursive( 5 );
```

Call #2: Factorial Recursive(4);

```
Call #3:
Factorial_Recursive( 3 );
```

```
Call #4:
Factorial_Recursive( 2 );
```

```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive( 4 )
```

```
Number isn't 0, so multiply 4 by the result of Factorial_Recursive( 3 )
```

Number isn't 0, so multiply 3 by the result of Factorial Recursive(2)

Number isn't 0, so multiply 2 by the result of Factorial_Recursive(1)

Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
    if ( number == 0 )
        return 1;
    return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
  Factorial_Recursive( 5 );

Call #2:
  Factorial_Recursive( 4 );
```

```
Call #3:
Factorial_Recursive( 3 );
```

```
Call #4:
Factorial_Recursive( 2 );
```

```
Call #5:
Factorial_Recursive( 1 );
```

```
Call #6:
Factorial_Recursive( 0 );
```

```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive( 4 )
```

```
Number isn't 0, so multiply 4 by the result of Factorial_Recursive( 3 )
```

```
Number isn't 0, so multiply 3 by the result of Factorial Recursive( 2 )
```

```
Number isn't 0, so multiply 2 by the result of Factorial_Recursive( 1 )
```

```
Number isn't 0, so multiply 1 by the result of Factorial_Recursive( 0 )
```

Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
    if ( number == 0 )
        return 1;

    return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
Factorial_Recursive( 5 );
```

Call #2: Factorial Recursive(4);

```
Call #3:
Factorial_Recursive( 3 );
```

```
Call #4:
Factorial_Recursive( 2 );
```

```
Call #5:
Factorial_Recursive( 1 );
```

```
Call #6:
Factorial_Recursive( 0 );
```

```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive( 4 )
```

```
Number isn't 0, so multiply 4 by the result of Factorial_Recursive( 3 )
```

```
Number isn't 0, so multiply 3 by the result of Factorial_Recursive( 2 )
```

```
Number isn't 0, so multiply 2 by the result of Factorial_Recursive( 1 )
```

```
Number isn't 0, so multiply 1 by the result of Factorial_Recursive( 0 )
```

Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
    if ( number == 0 )
        return 1;

    return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
Factorial_Recursive( 5 );
```

Call #2: Factorial Recursive(4);

Call #3: Factorial_Recursive(3);

```
Call #4:
Factorial_Recursive( 2 );
```

```
Call #5:
Factorial_Recursive( 1 );
```

```
Call #6:
Factorial_Recursive( 0 );
```

```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive( 4 )
```

```
Number isn't 0, so multiply 4 by the result of Factorial_Recursive( 3 )
```

```
Number isn't 0, so multiply 3 by the result of Factorial_Recursive( 2 )
```

```
Number isn't 0, so multiply 2 by the result of Factorial_Recursive( 1 )
```

```
Number isn't 0, so multiply 1 by the result of Factorial_Recursive( 0 )
```

Number is 0, so return 1

1 *

<u>+</u>

1

Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
    if ( number == 0 )
        return 1;

    return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
Factorial_Recursive( 5 );
```

```
Call #2:
Factorial_Recursive( 4 );
```

```
Call #3:
Factorial_Recursive( 3 );
```

```
Call #4:
Factorial_Recursive( 2 );
```

```
Call #5:
Factorial_Recursive( 1 );
```

```
Call #6:
Factorial_Recursive( 0 );
```

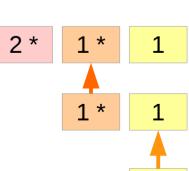
```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive( 4 )
```

```
Number isn't 0, so multiply 4 by the result of Factorial_Recursive( 3 )
```

```
Number isn't 0, so multiply 3 by the result of Factorial Recursive( 2 )
```

```
Number isn't 0, so multiply 2 by the result of Factorial_Recursive( 1 )
```

```
Number isn't 0, so multiply 1 by the result of Factorial_Recursive( 0 )
```



Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
    if ( number == 0 )
        return 1;

    return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
Factorial_Recursive( 5 );
```

Call #2: Factorial Recursive(4);

Call #3: Factorial_Recursive(3);

Call #4: Factorial_Recursive(2);

```
Call #5:
Factorial_Recursive( 1 );
```

```
Call #6:
Factorial_Recursive( 0 );
```

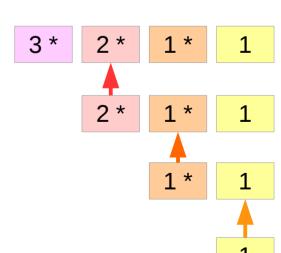
```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive( 4 )
```

```
Number isn't 0, so multiply 4 by the result of {\tt Factorial\_Recursive(3)}
```

```
Number isn't 0, so multiply 3 by the result of Factorial_Recursive( ^2 )
```

```
Number isn't 0, so multiply 2 by the result of Factorial_Recursive( 1 )
```

Number isn't 0, so multiply 1 by the result of Factorial_Recursive(0)



Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
    if ( number == 0 )
        return 1;

    return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
Factorial_Recursive( 5 );
```

Call #2: Factorial Recursive(4);

```
Call #3:
Factorial_Recursive( 3 );
```

```
Call #4:
Factorial_Recursive( 2 );
```

```
Call #5:
Factorial_Recursive( 1 );
```

```
Call #6:
Factorial_Recursive( 0 );
```

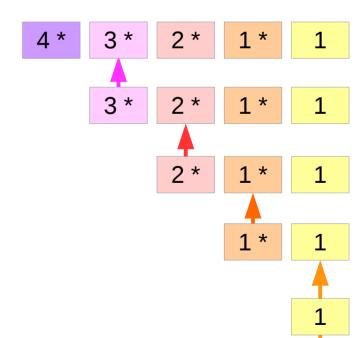
```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive( 4 )
```

```
Number isn't 0, so multiply 4 by the result of Factorial_Recursive( 3 )
```

Number isn't 0, so multiply 3 by the result of Factorial_Recursive(2)

Number isn't 0, so multiply 2 by the result of Factorial_Recursive(1)

Number isn't 0, so multiply 1 by the result of Factorial_Recursive(0)



Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
    if ( number == 0 )
        return 1;

    return ( number * Factorial_Recursive( number - 1 ) );
}
```

```
Initial call:
Factorial_Recursive( 5 );
```

Call #2: Factorial Recursive(4);

Call #3: Factorial_Recursive(3);

```
Call #4:
Factorial_Recursive( 2 );
```

```
Call #5:
Factorial_Recursive( 1 );
```

```
Call #6:
Factorial_Recursive( 0 );
```

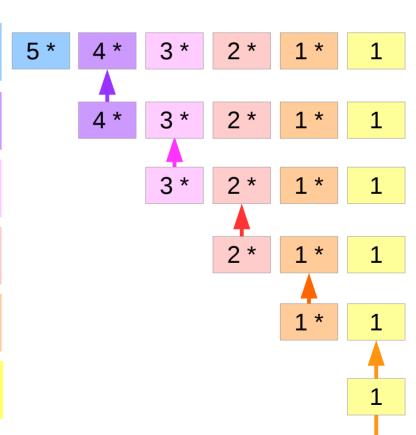
```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive(4)

Number isn't 0, so multiply 4 by the result of Factorial_Recursive(3)
```

Number isn't 0, so multiply 3 by the result of Factorial_Recursive(2)

Number isn't 0, so multiply 2 by the result of Factorial_Recursive(1)

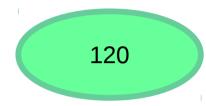
Number isn't 0, so multiply 1 by the result of Factorial_Recursive(0)



Let's step through the execution of this function...

```
int Factorial_Recursive( int number )
{
    if ( number == 0 )
        return 1;

    return ( number * Factorial_Recursive( number - 1 ) );
}
```



```
Initial call:
Factorial Recursive( 5 );
```

Call #2: Factorial Recursive(4);

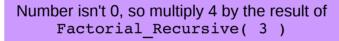
Call #3: Factorial_Recursive(3);

Call #4: Factorial_Recursive(2);

Call #5: Factorial_Recursive(1);

Call #6: Factorial_Recursive(0);

```
Number isn't 0, so multiply 5 by the result of Factorial_Recursive( 4 )
```



Number isn't 0, so multiply 3 by the result of Factorial_Recursive(2)

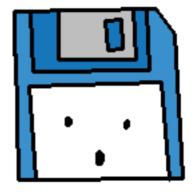
Number isn't 0, so multiply 2 by the result of Factorial_Recursive(1)

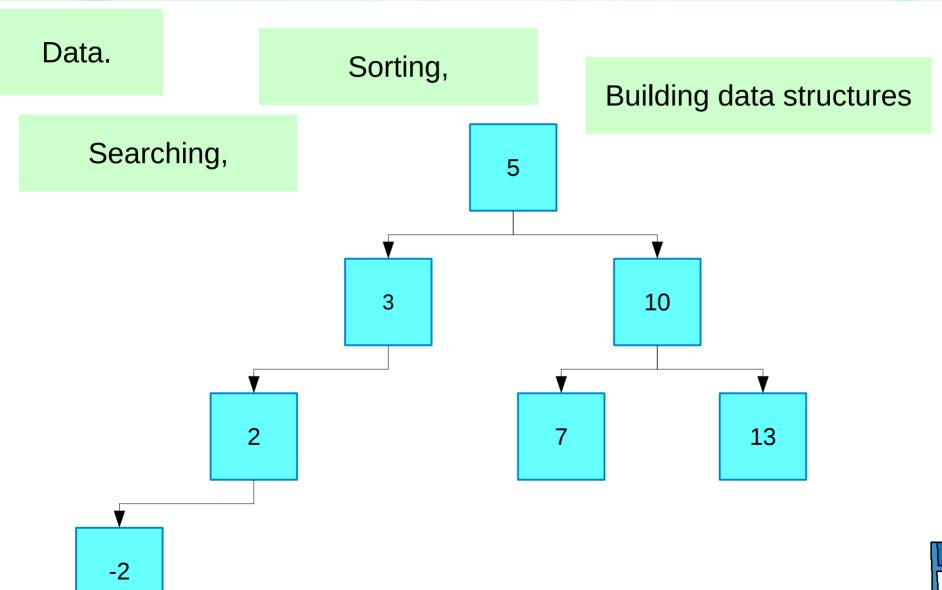
Number isn't 0, so multiply 1 by the result of Factorial_Recursive(0)



That was a simple example, but as functions that use recursion get more complex, it might still help to step through and write down variable values at each step.

Where does recursion really come in handy?







Here are some practice problems to work on...

Practice

- Write a recursive function that can be used to generate a Fibonacci sequence, up to some length specified by the user.
- Write a recursive function that can be used to compute the value of X^n , by multiplying X by itself n amount of times.
 - Write a recursive function that will reverse a string, so the first letter is last and vice versa, through the entire string.