

A Principled Approach to Developing Chlorophyll Models for Remote Sensing

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1 Abstract

2 Introduction

2.1 Background

- Necessity for estimating chlorophyll
- Opportunities afforded by chlorophyll estimation through remote sensing
- State of current chlorophyll algorithms for remote sensing
 - OC4 for SeaWiFS→there is a dichotomy in remote sensing between empirical models and quasi-analytical models. Empirical models are so-called because their structure is dictated by their ability to fit the training data, often without any inter-model comparison, or post-training model skill assessment exercise. As a result, these are high order polynomials that are eminently uninterpretable with regards to the predictor data used. Moreover because of the training method used, they are overfitting the training data used and are therefor rarely generalizable to the variety of regions sampled remotely. Quasi analytical models (QAA), on the other hand claim an origin in first principles but end up resorting to some degree of empiricism as described above, where first principles fall short. In short, empirical models are frowned upon because they are inscrutable and don't work well for anything but the open ocean; QAAs are frowned upon because they don't work well. The contention of the present paper is that such a dichotomy is unnecessary.
 - Hu & Franz 2012
 - Gholizadeh et al (2015?)
- Basic empirical form

$$\log_{10}(\text{chlor}_a) = a_0 + \sum_{i=1}^j a_i \log_{10} \left(\frac{\max(Rrs(\lambda_{blue}))}{Rrs(\lambda_{green})} \right) \quad (1)$$

- Problems with current algorithms:
 - collinearity of inputs
 - poor performance in coastal
 - maximum likelihood estimation approach → risk of overfitting (lack of in-situ data availability compared to satellite data makes it worse)

2.2 Proposed framework

Here, I use Bayesian regression models to predict chlorophyll concentration from apparent optical properties. There are a number of advantages for adopting this approach. The first of these is a problem agnostic set of steps detailed in the methods section. A second advantage is that model construction is transparent and assumptions are laid bare. This makes any model developed with this framework easily, and constructively, criticizable. A positive spillover of this is that the process requires that the model code be made available for model criticism to occur; i.e. the study in question must be reproducible to be effective. Another attractive feature of the Bayesian framework is that rather than point predictions, the output of the Bayesian model is the posterior distribution. The posterior distribution is a rich construct that can be used to develop insight in the process of interest, uncertainties around predictions, and a means to rank model performance. Finally, Bayesian regression models are inherently regularized through the stipulated priors. This has a 'calming' effect on the model, which is less likely to overfit an inappropriately scant data set; a common problem in bio-optical model development for marine remote sensing.

Succintly, this approach ensures:

- transparent construction of models with explicit formulation of assumptions,
- assumptions/background information codified as priors that are easy to criticize and modify;

- verifiable prior feasibility before data collection via prior predictive checks
- built-in regularization, which lessens the risk of overfitting;
- built-in structure for selecting relevant features;
- posterior distribution as rich information structure from which to estimate parameter uncertainty, output prediction uncertainty, and likelihood of model performance on out-of-sample data;
- assessment of predictive ability via posterior predictive checks;
- multiple model development, which avoids overemphasis on any particular formulation;
- evaluation/comparison between models using information theory.

For the sake of reproducibility of the models and their results, the code for both data preparation, model construction and fitting and result assessment are available from the github repository [\[here\]](#). In addition, the data in their various stages of processing (raw, standardized, split, transformed), are available from the Open Science Framework (OSF) page associated with this project, [\[here\]](#).

3 Methods

3.1 Model Development

Four models are developed here

3.1.1 Bayesian Linear Regression

- Order 1 regression for interpretable coefficients
- no interaction terms
- regularized horseshoe prior for feature selection

3.1.2 Bayesian Linear Regression with Interaction Terms

- generation of 1st order interaction terms
- allowing for both strong and weak heredity

3.1.3 Bayesian Neural Network

- Specific hierarchical structure for ARD
- HL1 4 NN with elu activation

3.1.4 Bayesian OC4 version as Baseline

3.2 Prior Predictive Checks

3.3 Data Acquisition/Exploration/Transformation

3.3.1 Data exploration and transformation

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3.3.2 Basis reduction via PCA

- PCA of Rrs to reduce overlap of information between predictor variables

3.4 Model Fitting

3.5 Marginal Posterior of Coefficients \rightarrow Feature Relevance Determination

3.6 Posterior Predictive Checks

3.7 Model Comparison Through Posterior Predictive Checks

4 Results