Novel Code

Streamflow affects life history in a headwater salamander. Ecology

Cochrane, M. M., Addis, B. A., Swartz, L. K., and W. H. Lowe

Simulating Growth Data

To start simulating fake growth data we included 50 initial body sizes drawn from a random uniform distribution with a minimum of 35 mm and a maximum of 115 mm. We then randomly assigned between 5 and 400 days between all initial sizes and five subsequent capture events for each individual. To estimate growth over time we used the Von Bertalanffy (VB) growth function for one individual with at least two captures (Fabens 1965, Eaton and Link 2011):

$$S_t = S_{t-1} + (a - S_{t-1})(1 - e^{-k\Delta t})$$

Where S = size at capture, t = time step, a = asymptotic size, and k = growth rate.

We set a = 120 and k = 0.20 in order to simulate fake growth data over time for each individual. This allowed us to compare estimated model parameter values to the given ones above to ensure our model was correct.

We also simulated random watershed areas for all individuals with mean = 1.5 and SD = 1, in order to estimate the effect of watershed area on k.

```
# generate 50 initial sizes with min = 35, max = 115
S1 \leftarrow runif(n=50, min=35, max=117)
# generate random time steps (between 5-400 days) for all 50 individuals across 5 captures
t1 <- sample(5:400, 50, replace=FALSE)
t2<-sample(5:400, 50, replace=FALSE)
t3 <- sample(5:400, 50, replace=FALSE)
t4<-sample(5:400, 50, replace=FALSE)
t5 <- sample(5:400, 50, replace=FALSE)
# turn vectors for initial size and time steps into a dataframe
growth_data<-data.frame(t1,t2,t3,t4,t5,S1)</pre>
# set asymptotic size and growth rate parameter to simulate subsequent capture sizes
a = 120
k = 0.20
# generate size at capture for five additional capture occasions for all 50 individuals
growth_data <- growth_data %>%
 mutate(S2 = (S1 + (a-S1)*(1-exp(-k*(t1/365))))) %>%
  mutate(S3 = (S2 + (a-S2)*(1-exp(-k*(t2/365)))))) \%
  mutate(S4 = (S3 + (a-S3)*(1-exp(-k*(t3/365)))))) %>%
  mutate(S5 = (S4 + (a-S4)*(1-exp(-k*(t4/365)))))) \%
```

```
mutate(S6 = (S5 + (a-S5)*(1-exp(-k*(t5/365)))))
# simulating fake watershed areas for all individuals
area.km2 < -abs(rnorm(n=50, mean=1.5, sd=1))
# scale and center area
area <- as.vector(scale(area.km2))</pre>
# add watershed area to growth dataframe
growth data$area.km2 <- area.km2</pre>
growth_data$area <- area</pre>
# view fake growth data and time steps
head(growth_data)
                                          S2
##
      t1 t2 t3 t4 t5
                                S1
                                                    S3
                                                              S4
                                                                        S5
## 1 134 383 243 310 313 74.61680 77.82965 85.81270 90.07472 94.74964
## 2 221 363 345   25 196 113.66037 114.38341 115.39648 116.18943 116.24127
## 3 101 343 26 72 308 99.84838 100.93332 104.20020 104.42370 105.02625
## 4 124 87 158 27 80 72.54379 75.66111 77.72521 81.23120 81.80055
## 5 26 253 319 12 60 52.52411 53.47860 62.08980 71.37688 71.69555
## 6 65 20 211 62 190 74.80359 76.38499 76.86035 81.57048 82.85410
##
            S6
                area.km2
                                 area
## 1 98.72923 1.21721681 -0.53277163
## 2 116.62403 0.03914875 -1.79668915
## 3 107.35159 1.26361102 -0.48299653
## 4 83.43887 3.02630448 1.40814985
## 5 73.25782 1.99598856 0.30275161
## 6 86.52684 1.78387196 0.07517743
# separate out encounter history
y <- as.matrix(growth_data[,6:11])
# separate out days since last capture
dslc <- as.matrix(growth_data[,1:5])</pre>
# set number of individuals
NIND <- nrow(growth_data)</pre>
```

Organizing Data to Run Model in JAGS

We fit a Bayesian VB growth model using Markov chain Monte Carlo (MCMC) methods in JAGS (Plummer 2003).

```
# format data for jags

# NIND = number of individuals
# y = SVL (size) measurements
# f = first capture occasion
# l = last capture occasion

### functions for data manipulation
# determine the occasion of the first capture of each individual
```

```
get.first <- function(x){</pre>
  # a function to identify the time period of the first capture from an encounter history matrix
  return( min(which( x != 0 ) ) )
# get last occasion of capture for each individual
get.last <- function(x){</pre>
  # a function to identify the time period of the first capture from an encounter history matrix
 return( max(which( x != 0 ) ) )
fall <- apply( y, 1, get.first )</pre>
f <- fall # vector of first cap time step
lall <- apply(y, 1 ,get.last)</pre>
1 <- lall # vector for which time period has last capture
### get ready to run JAGS
# Define a list of data to be passed to JAGS
growth.data <- list( y = y, NIND = NIND, f= f, 1 = 1, dslc = dslc, area=area)
# set parameters (measurement error, asymptotic size,
# transformed growth rate parameter, effect of area on k) to track in JAGS
growth.parms <- c("tau.eps", "a", "mean.k", "area.k")</pre>
# set initial values for parameters
sal.inits <- function(){</pre>
  list(
    tau.eps = runif(1, 0, 1),
   mean.k = runif(1, -5, 5),
    a = runif(1, 80, 130),
    area.k = runif(1, -5, 5)
  )
}
# set up for MCMC run
ni <- 5000 # number of iterations
nt <- 5 # thinning number, e.g. only keeping out of 5 values
nb <- 3000 # burn in
nc <- 3 # number of chains</pre>
# total iterations kept = (ni/nb)/nt*nc
```

JAGS Model Script

To run our Bayesian VB growth model we set priors and defined the likelihood below. This initial (simplified) model includes the linear effect of watershed area on k. For this initial model, k is calculated across the entire year equally. We also estimate a parameter, tau.eps, that accounts for measurement error.

```
model {
    # Prior Specification (Growth Model)
```

```
a ~ dunif(80,130) # uniform prior for asymptotic size with minimum of 80 and maximum of 130
tau.eps ~ dgamma(0.001, 0.001) # gamma prior for measurement error with shape = 0.001, rate = 0.001
sd.eps <- 1/sqrt(tau.eps) # measurement error sd</pre>
mean.k ~ dnorm(0,0.01) # normal prior for log of the growth rate parameter
# assums mean of 1 with a wide variance
area.k ~ dnorm(0,0.01) # normal prior for the effect of area on mean k
# Likelihood
for (i in 1:NIND){ # Loop through individuals
  for (t in f[i]:f[i]){ # First survey
    y[i,t] ~ dnorm(H[i,t],tau.eps) # Measured size is the true size +/- measurement error
    H[i,t] ~ dunif(35,115) # Prior: Expected size at first capture (between 30 and 120)
  }
  for (t in (f[i]+1):l[i]){ # Loop through surveys
    # (1st capture to last survey date for each individual)
    y[i,t] ~ dnorm(H[i,t],tau.eps) # measured size is a fact of
    # true size plus measurement error
    # Expected size at time t = H.m
    H[i,t] \leftarrow H[i,t-1]+(a-H[i,t-1])*
      (1-\exp(-k[i,t]*(dslc[i,t-1]/365)))
    log(k[i,t]) <- mean.k + area.k*area[i]</pre>
    # log-link function to allow active k to vary in relation to area
  }
}
```

Run Model and View Results

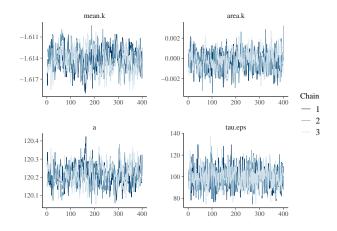
We used the package R2jags (Su and Yajima 2021) to run our JAGS model, and the package bayesplot (Gabry and Mahr 2022) to check for model convergence and view posterior estimates, all in RStudio (Version 1.4.1716; R Development Core Team 2021).

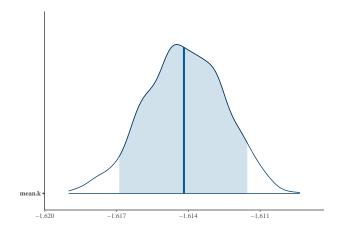
Posterior estimates for a should be around 120 and estimates for k should be around 0.20 if model is set up correctly.

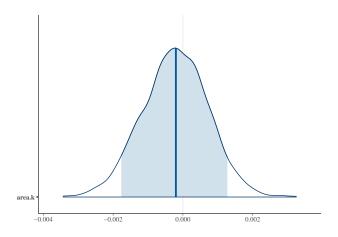
```
setwd("C:/Users/maddy/Box Sync/HB/Data/growth/")
# run model in R2jags
```

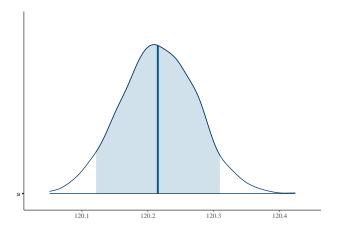
```
vbgm.result.area <- R2jags::jags(data=growth.data,</pre>
                                inits = sal.inits,
                                parameters.to.save=growth.parms,
                                model.file="vbgm/jags/areamodel.txt",
                                n.chains=nc,
                                n.iter=ni,
                                n.burnin=nb,
                                n.thin=nt)
## module glm loaded
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
## Graph information:
##
      Observed stochastic nodes: 300
      Unobserved stochastic nodes: 54
##
##
      Total graph size: 2646
## Initializing model
# view summary table
vbgm.result.area$BUGSoutput$summary
##
                                                2.5%
                                                                25%
                                                                              50%
                                    sd
             1.202162e+02 5.691320e-02 1.201073e+02 1.201775e+02 1.202152e+02
## a
           -2.202140e-04 9.371773e-04 -2.053666e-03 -8.143061e-04 -2.021087e-04
## deviance -5.288744e+02 1.187045e+01 -5.497751e+02 -5.370469e+02 -5.296584e+02
## mean.k -1.614168e+00 1.632252e-03 -1.617450e+00 -1.615283e+00 -1.614185e+00
## tau.eps 9.986246e+01 9.399761e+00 8.235380e+01 9.354695e+01 9.972551e+01
                                  97.5%
##
                      75%
                                            Rhat n.eff
            1.202549e+02 1.203281e+02 1.012106
## a
## area.k
            4.043527e-04 1.573009e-03 1.007409
                                                   340
## deviance -5.217269e+02 -5.034167e+02 1.001550 1200
## mean.k -1.612973e+00 -1.611129e+00 1.020885
                                                  100
           1.061819e+02 1.184373e+02 1.000903 1200
## tau.eps
# a parameter estimate should be ~ 120
# area.k parameter estimate should be ~ 0
# we want all Rhat values < 1.05
# get an un-transformed estimate of k (should be ~ 0.20 if model worked)
mean.k<-exp(vbgm.result.area$BUGSoutput$sims.list$mean.k)</pre>
quantile(mean.k, 0.50) # mean k
##
         50%
## 0.1990528
# standard deviation of measurement error
tau.eps<-exp(vbgm.result.area$BUGSoutput$sims.list$tau.eps)</pre>
mean(1/sqrt(tau.eps)) # should be pretty close to 0
```

```
# view traceplots to see if chains converged
posterior <- as.array(vbgm.result.area$BUGSoutput$sims.array)
bayesplot::mcmc_trace(posterior, pars = c("mean.k", "area.k", "a", "tau.eps"))</pre>
```









Model Validation

We calculated a Bayesian p-value to make sure our observed data matched our model output.

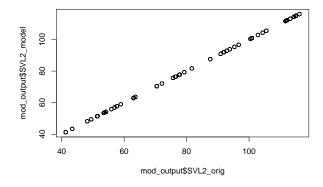
```
#### posterior predictive check ####
# comparing observed data to posterior predictive distribution
# bayesian p -value = probability that the replicated data could be
# more extreme than the observed data

# posterior distributions
a_output <- vbgm.result.area$BUGSoutput$sims.list$a
area_k_output <- vbgm.result.area$BUGSoutput$sims.list$area.k
mean_k_output <- vbgm.result.area$BUGSoutput$sims.list$mean.k

# create data frame with posterior distributions for all parameters
mod_output <- data.frame(a_output, area_k_output, mean_k_output)

# add in first time step SVL and time to next capture, in addition to discharge co-variates on k
mod_output$original_SVL <- growth_data$S1</pre>
```

```
mod_output$days <- growth_data$t1</pre>
mod_output$area <- growth_data$area</pre>
# calculate size at next time step based on posterior iterations
mod_output <- mod_output %>%
  mutate(k = exp(mean_k_output + area_k_output*area )) %>%
  mutate(SVL2_model = original_SVL + (a_output - original_SVL)*(1-exp((-k*(days/365)))))
# add in original size at next time step to df
mod_output$SVL2_orig <- growth_data$S2</pre>
head(mod_output)
     a_output area_k_output mean_k_output original_SVL days
                                                                                 k
## 1 120.2381 0.0008556311
                                -1.615668
                                              74.61680 134 -0.53277163 0.1986673
## 2 120.1902 0.0003170814
                                -1.614186
                                             113.66037 221 -1.79668915 0.1989392
## 3 120.2690 0.0009938708
                                -1.614702
                                              99.84838 101 -0.48299653 0.1988545
## 4 120.1098 -0.0008403239
                                -1.612596
                                              72.54379 124 1.40814985 0.1991336
## 5 120.2238 -0.0006037631
                                -1.614945
                                              52.52411
                                                         26 0.30275161 0.1988652
## 6 120.1871 -0.0003476542
                                -1.614050
                                              74.80359
                                                         65 0.07517743 0.1990745
     SVL2_model SVL2_orig
##
## 1
       77.82576 77.82965
## 2 114.40138 114.38341
## 3 100.94168 100.93332
      75.65524 75.66111
## 4
       53.47637 53.47860
## 5
## 6
       76.38432 76.38499
# calculate the proportion of simulated values that are equal to or greater than the original dataset
mod_output <- mod_output %>%
  mutate(greater_than = if_else(SVL2_model >= SVL2_orig, 1,0))
# plot original size compared to modeled size
# want all points on or near 1:1 line
plot(mod_output$SVL2_orig, mod_output$SVL2_model)
```



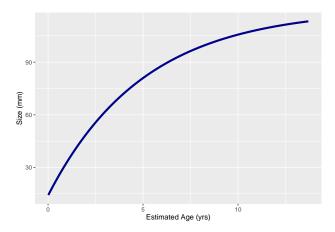
Plot Growth Trajectory from Parameter Estimates

In order to plot growth over time based on posterior parameter estimates we also had to define the initial size of animals as 14 mm based on historic observations. In order to do this we used a different organization of the VB growth function to plot growth over time:

$$S_t = a(1 - be^{-kt})$$

Where S_t = size at age t, a = asymptotic size estimated from model, hatchling size = a(1-b), and k = growth rate parameter estimated from model.

```
# set initial size at time 0
init.size <- 14
\# get parameter estimates from model for a and k
mean.a<-vbgm.result.area$BUGSoutput$mean$a
mean.k <-vbgm.result.area$BUGSoutput$mean$mean.k</pre>
# create a dataframe with a column for days since hatching
days_vec \leftarrow seq(5,5000,by=1)
growth_traj <- data.frame(days_vec)</pre>
# project growth across each time step given parameter estimates
growth_traj <- growth_traj%>%
  mutate(k =exp(mean.k))%>%
 mutate(a = mean.a)%>%
 mutate(init.size = init.size)%>%
 mutate(size = init.size + (a-init.size)*(1-exp(-k*(days_vec/365))))
\# plot size on y axis and age on x axis
ggplot(data = growth_traj, aes(x=days_vec/365, y=size)) +
  # set x axis to yrs instead of days
  geom_line(size=1.5, color="darkblue")+
  labs(y="Size (mm)", x = "Estimated Age (yrs)")
```



Final JAGS Model Script

Below is the script for our final VB growth model, which includes added complexity (compared to the model described above) when estimating parameters to describe the effect of covariates on k. For example, this model includes both a linear and quadratic relationship between k and watershed area. This model also includes the effect of fish presence on k, and separates out active season verse inactive season growth rates.

```
model {
  # Prior Specification
  a ~ dunif(80,130) # uniform prior on asymptotic size, min = 80, max = 130
  tau.eps ~ dgamma(0.001, 0.001) # gamma prior on measurement error with
  # shape = 0.001, rate = 0.001
  sd.eps <- 1/sqrt(tau.eps) # measurement error sd</pre>
  mean.k.active ~ dnorm(0,0.01) # normal prior on log of the active growth rate # parameter, assumes m
  area.k.active ~ dnorm(0,0.01) # normal prior on linear effect of area on mean k during summer
  area2.k.active ~ dnorm(0,0.01) # normal prior quadratic effect of area on mean k during summer
  fish.k.active ~ dnorm(0,0.01) # normal prior on the effect of fish on k
  mean.k.inactive ~ dnorm(0,0.01) # normal prior on the log of inactive growth rate
  # Likelihood
  for (i in 1:NIND){ # Loop through individuals
   for (t in f[i]:f[i]){ # First survey
     y[i,t] ~ dnorm(H[i,t],tau.eps) # Measured size is the true size +/- measurement error
     H[i,t] ~ dunif(30,120) # Prior: Expected size at first capture
   for (t in (f[i]+1):1[i]){ # Loop through surveys (1st capture to last
      # survey date for each individual)
```

Literature Cited

Eaton, M. J., and W. A. Link. 2011. Estimating age from recapture data: Integrating incremental growth measures with ancillary data to infer age-at-length. Ecological Applications 21:2487–2497.

Fabens, A. J. 1965. Properties and fitting of the von Bertalanfy growth curve. Growth 29:265–289.

Gabry J, and T. Mahr. 2022. "bayesplot: Plotting for Bayesian Models." R package version 1.9.0.

Plummer, M. 2003. JAGS: A program for analysis of Bayesian graphical models using Gibbs sampling. Proceedings of the 3rd international workshop on distributed statistical computing 125:1–10.

Su, Y. S., and Yajima, M. 2021. R Package "R2jags: A Package for Running jags from R".