

Computational results for E2

INSTANCE	n	m	U	LPT	MF	COMB	LIST	PSMF	JOH	LB
1	2	10	100.800	2029.0	2039.0	2029.0	2029.0	2029.0	2027.0	2025.0
2	2	10	100.800	2200.0	2221.0	2200.0	2166.0	2163.0	2163.0	2160.0
3	2	10	100.800	2053.0	2098.0	2053.0	2029.0	2031.0	2029.0	2028.0
4	2	10	100.800	2243.0	2277.0	2243.0	2243.0	2243.0	2243.0	2241.0
5	2	10	100.800	2340.0	2321.0	2321.0	2317.0	2315.0	2315.0	2315.0
6	2	10	100.800	1983.0	2008.0	1983.0	1973.0	1973.0	1973.0	1971.0
7	2	10	100.800	2617.0	2652.0	2617.0	2611.0	2606.0	2590.0	2589.0
8	2	10	100.800	2733.0	2706.0	2706.0	2701.0	2693.0	2684.0	2680.0
9	2	10	100.800	1753.0	1706.0	1706.0	1701.0	1706.0	1706.0	1700.0
10	2	10	100.800	1884.0	1908.0	1884.0	1866.0	1877.0	1864.0	1864.0
11	2	10	100.800	1975.0	2071.0	1975.0	1975.0	1975.0	1971.0	1970.0
12	2	10	100.800	2343.0	2338.0	2338.0	2336.0	2321.0	2322.0	2321.0
13	2	10	100.800	2134.0	2132.0	2132.0	2132.0	2132.0	2132.0	2132.0
14	2	10	100.800	2604.0	2563.0	2563.0	2560.0	2562.0	2560.0	2558.0
15	2	10	100.800	2047.0	2019.0	2019.0	2006.0	2003.0	2002.0	2002.0
16	2	10	100.800	2435.0	2440.0	2435.0	2434.0	2425.0	2424.0	2423.0
17	2	10	100.800	1751.0	1753.0	1751.0	1738.0	1737.0	1737.0	1736.0
18	2	10	100.800	2267.0	2321.0	2267.0	2266.0	2267.0	2266.0	2266.0
19	2	10	100.800	2283.0	2355.0	2283.0	2283.0	2283.0	2282.0	2279.0
20	2	10	100.800	2284.0	2324.0	2284.0	2278.0	2279.0	2278.0	2270.0
21	2	10	100.800	2222.0	2179.0	2179.0	2179.0	2179.0	2179.0	2179.0
22	2	10	100.800	2659.0	2688.0	2659.0	2659.0	2654.0	2654.0	2653.0
23	2	10	100.800	2624.0	2633.0	2624.0	2600.0	2598.0	2598.0	2597.0
24	2	10	100.800	1992.0	1983.0	1983.0	1983.0	1967.0	1967.0	1962.0
25	2	10	100.800	2720.0	2742.0	2720.0	2716.0	2709.0	2709.0	2709.0
26	2	10	100.800	2172.0	2173.0	2172.0	2172.0	2172.0	2172.0	2172.0
27	2	10	100.800	2628.0	2622.0	2622.0	2622.0	2620.0	2615.0	2615.0
28	2	10	100.800	2111.0	2083.0	2083.0	2083.0	2075.0	2075.0	2074.0
29	2	10	100.800	2264.0	2271.0	2264.0	2251.0	2252.0	2251.0	2250.0
30	2	10	100.800	2049.0	2034.0	2034.0	2027.0	2030.0	2027.0	2026.0
31	2	10	100.800	2222.0	2214.0	2214.0	2195.0	2195.0	2195.0	2195.0
32	2	10	100.800	2345.0	2255.0	2255.0	2254.0	2249.0	2249.0	2248.0
33	2	10	100.800	1889.0	1918.0	1889.0	1870.0	1873.0	1870.0	1868.0
34	2	10	100.800	1999.0	1992.0	1992.0	1965.0	1979.0	1965.0	1963.0
35	2	10	100.800	2521.0	2506.0	2506.0	2467.0	2463.0	2463.0	2459.0
36	2	10	100.800	2248.0	2278.0	2248.0	2248.0	2248.0	2247.0	2246.0
37	2	10	100.800	2308.0	2310.0	2308.0	2308.0	2308.0	2308.0	2306.0
38	2	10	100.800	2028.0	2026.0	2026.0	2026.0	2024.0	2022.0	2022.0
39	2	10	100.800	2306.0	2343.0	2306.0	2294.0	2289.0	2289.0	2288.0
40	2	10	100.800	2303.0	2351.0	2303.0	2303.0	2303.0	2303.0	2302.0
41	2	10	100.800	2634.0	2619.0	2619.0	2598.0	2611.0	2598.0	2595.0
42	2	10	100.800	1864.0	1842.0	1842.0	1842.0	1842.0	1842.0	1841.0
43	2	10	100.800	2172.0	2212.0	2172.0	2169.0	2168.0	2168.0	2168.0
44	2	10	100.800	2888.0	2809.0	2809.0	2782.0	2809.0	2777.0	2771.0
45	2	10	100.800	2171.0	2167.0	2167.0	2147.0	2146.0	2141.0	2139.0
46	2	10	100.800	2464.0	2447.0	2447.0	2414.0	2408.0	2408.0	2405.0
47	2	10	100.800	2483.0	2487.0	2483.0	2461.0	2451.0	2448.0	2448.0
48	2	10	100.800	2050.0	2050.0	2050.0	2036.0	2040.0	2028.0	2024.0
49	2	10	100.800	2503.0	2502.0	2502.0	2502.0	2488.0	2488.0	2487.0
50	2	10	100.800	2212.0	2215.0	2212.0	2190.0	2189.0	2189.0	2189.0
51	2	10	100.800	2695.0	2643.0	2643.0	2643.0	2633.0	2632.0	2630.0
52	2	10	100.800	2480.0	2478.0	2478.0	2412.0	2426.0	2412.0	2411.0
53	2	10	100.800	2434.0	2438.0	2434.0	2414.0	2418.0	2414.0	2413.0
54	2	10	100.800	2074.0	2099.0	2074.0	2073.0	2069.0	2069.0	2068.0
55	2	10	100.800	2089.0	2079.0	2079.0	2078.0	2079.0	2073.0	2073.0
56	2	10	100.800	2542.0	2586.0	2542.0	2542.0	2539.0	2539.0	2539.0
57	2	10	100.800	1446.0	1435.0	1435.0	1427.0	1425.0	1425.0	1425.0
58	2	10	100.800	1812.0	1863.0	1812.0	1812.0	1820.0	1811.0	1810.0
59	2	10	100.800	2484.0	2469.0	2469.0	2456.0	2451.0	2451.0	2448.0
60	2	10	100.800	2206.0	2210.0	2206.0	2205.0	2206.0	2204.0	2200.0
61	2	10	100.800	2225.0	2250.0	2225.0	2225.0	2218.0	2218.0	2217.0
62	2	10	100.800	1833.0	1855.0	1833.0	1832.0	1833.0	1833.0	1829.0
63	2	10	100.800	2135.0	2136.0	2135.0	2135.0	2135.0	2135.0	2132.0
64	2	10	100.800	2354.0	2356.0	2354.0	2345.0	2354.0	2345.0	2345.0
65	2	10	100.800	2700.0	2622.0	2622.0	2617.0	2612.0	2612.0	2611.0
66	2	10	100.800	2138.0	2142.0	2138.0	2135.0	2138.0	2135.0	2135.0
67	2	10	100.800	2931.0	2889.0	2889.0	2861.0	2872.0	2859.0	2859.0
68	2	10	100.800	2328.0	2325.0	2325.0	2308.0	2311.0	2304.0	2303.0
69	2	10	100.800	2233.0	2228.0	2228.0	2221.0	2222.0	2221.0	2213.0
70	2	10	100.800	2804.0	2696.0	2696.0	2684.0	2686.0	2684.0	2682.0
71	2	10	100.800	2370.0	2390.0	2370.0	2370.0	2389.0	2370.0	2370.0
72	2	10	100.800	1867.0	1866.0	1866.0	1866.0	1866.0	1866.0	1866.0
73	2	10	100.800	2120.0	2126.0	2120.0	2076.0	2068.0	2068.0	2067.0
74	2	10	100.800	1978.0	1972.0	1972.0	1972.0	1970.0	1970.0	1969.0
75	2	10	100.800	1774.0	1791.0	1774.0	1768.0	1775.0	1767.0	1767.0
76	2	10	100.800	2055.0	2016.0	2016.0	2010.0	2005.0	2005.0	2003.0
77	2	10	100.800	1879.0	1882.0	1879.0	1846.0	1846.0	1846.0	1844.0
78	2	10	100.800	1952.0	1963.0	1952.0	1952.0	1942.0	1942.0	1941.0
79	2	10	100.800	2015.0	2015.0	2015.0	2015.0	2008.0	2008.0	2008.0
80	2	10	100.800	2056.0	2071.0	2056.0	2050.0	2054.0	2050.0	2049.0
81	2	10	100.800	1982.0	2004.0	1982.0	1965.0	1958.0	1956.0	1950.0
82	2	10	100.800	2054.0	2087.0	2054.0	2047.0	2041.0	2041.0	2041.0
83	2	10	100.800	2544.0	2543.0	2543.0	2531.0	2531.0	2524.0	2511.0
84	2	10	100.800	1815.0	1846.0	1815.0	1815.0	1815.0	1815.0	1813.0
85	2	10	100.800	2154.0	2136.0	2136.0	2125.0	2125.0	2125.0	2124.0
86	2	10	100.800	2746.0	2752.0	2746.0	2717.0	2725.0	2709.0	2704.0
87	2	10	100.800	2241.0	2202.0	2202.0	2197.0	2198.0	2197.0	2195.0
88	2	10	100.800	1951.0	1983.0	1951.0	1931.0	1932.0	1923.0	1921.0
89	2	10	100.800	2959.0	2873.0	2873.0	2838.0	2851.0	2838.0	2837.0
90	2	10	100.800	1903.0	1893.0	1893.0	1865.0	1859.0	1859.0	1859.0
91	2	10	100.800	2701.0	2645.0	2645.0	2645.0	2645.0	2645.0	2645.0
92	2	10	100.800	2107.0	2073.0	2073.0	2073.0	2072.0	2072.0	2071.0
93	2	10	100.800	1791.0	1839.0	1791.0	1791.0	1791.0	1791.0	1790.0
94	2	10	100.800	2302.0	2291.0	2291.0	2286.0	2291.0	2285.0	2284.0
95	2	10	100.800	2876.0	2882.0	2876.0	2856.0	2853.0	2853.0	2849.0
96	2	10	100.800	2120.0	2096.0	2096.0	2079.0	2082.0	2079.0	2079.0
97	2	10	100.800	2351.0	2378.0	2351.0	2327.0	2327.0	2326.0	2326.0
98	2	10	100.800	2933.0	2853.0	2853.0	2853.0	2853.0	2851.0	2851.0
99	2	10	100.800	2367.0	2368.0	2367.0	2357.0	2355.0	2353.0	2352.0
100	2	10	100.800	1902.0	1922.0	1902.0	1895.0	1893.0	1886.0	1885.0
1	2	30	100.800	6220.0	6199.0	6199.0	6197.0	6197.0	6197.0	6197.0
2	2	30	100.800	6375.0	6408.0	6375.0	6364.0	6363.0	6363.0	6363.0
3	2	30	100.800	6761.0	6782.0	6761.0	6756.0	6755.0	6755.0	6755.0
4	2	30	100.800	6657.0	6638.0	6638.0	6630.0	6629.0	6629.0	6629.0
5	2	30	100.800	6176.0	6152.0	6152.0	6149.0	6149.0	6149.0	6149.0
6	2	30	100.800	7607.0	7589.0	7589.0	7581.0	7581.0	7581.0	7581.0
7	2	30	100.800	7395.0	7400.0	7395.0	7388.0	7387.0	7387.0	7387.0
8	2	30	100.800	7398.0	7387.0	7387.0	7387.0	7387.0	7387.0	7387.0
9	2	30	100.800	6801.0	6807.0	6801.0	6781.0	6781.0	6781.0	6781.0
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