**Decoding the coupled decision-making of epithelial-mesenchymal transition and metabolic reprogramming in cancer**

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**Abstract**

Abnormal metabolism and metastasis are two hallmarks of cancer. During metastasis, a developmental program, epithelial-mesenchymal transition (EMT) is often used by cancer cells to become motile. Aside from complete EMT, cancer cells can alternatively acquire a hybrid epithelial/mesenchymal (E/M) phenotype, combining the features of E and M, and in many cases serving as the primary instigator of metastasis. Cancer cells have been observed to largely use glycolysis, referred to as the Warburg effect. In addition to glycolysis, when leaving the primary tumor and entering blood circulation, cancer cells can increase oxidative phosphorylation without compromising glycolysis, thus acquiring a hybrid metabolic phenotype. The hybrid metabolic state has been associated with elevated metastatic potential. Clearly, both EMT and metabolism are actively involved in metastasis. Indeed, there are extensive cross-talk between EMT and metabolism. Understanding the mutual regulation between metabolism and EMT may contribute to better anti-metastasis strategies. Here, we coupled the decision-making molecular networks of metabolism and EMT and systematically elucidate how different phenotypes during EMT (E, M and hybrid E/M) are associated with different metabolic phenotypes (O, W and W/O). Specifically, we identified a feedback loop that leads to the coupling of the E/M state with the W/O state, thereby enabling a potentially highly aggressive E/M-W/O phenotype. Strikingly, we found that even if the individual molecular network of EMT or metabolism does not support a hybrid phenotype, the crosstalk can give rise to the E/M-W/O state. Moreover, in this case, there is an order of events in that the W/O state emerges first and is followed by the E/M state, suggesting that metabolic reprogramming can be a primary driver of EMT and the acquisition of highly metastatic hybrid E/M cells.

**Introduction**

Metastasis remains the leading cause of cancer-related deaths [1] and thus it is critical to understand the physiological properties of cells that migrate from the primary tumor and initiate metastatic lesions. Typically, these properties have been studied one at a time. For example, cell motility is assumed to be related to the epithelial-mesenchymal transition (EMT). During EMT, the cells progressively lose epithelial (E) features such as cell-cell adhesion and apical-basal polarity, and acquire mesenchymal (M) features such as migration, invasion, and resistance to immune response [2,3]. The EMT has consistently been implicated in cells acquiring metastatic potential [4,5], and also plays a role in therapeutic resistance [6]. Recently, the bimodal picture of EMT has been superseded by a more complex scenario involving the hybrid epithelial/mesenchymal (E/M) phenotype which exhibits combined traits of epithelial (cell-cell adhesion) and mesenchymal (invasion) at the single-cell level. The hybrid E/M cells migrate collectively as a cluster and may account for the majority of metastases [7–10]. The existence of a hybrid E/M state has since been experimentally verified both in vitro (in many cancer cell lines) and in vivo (e.g. using a genetic mouse model of squamous cell carcinoma) and has been shown to be associated with therapy resistance alongside with poor survival rates [11–14]. Most importantly, these states appear to the most capable of initiating metastatic growth [15,16]. Fully understanding the behavior of the hybrid E/M phenotype is still an active area of research.

Metabolic reprogramming, another hallmark of cancer, enables cancer cells to adjust their metabolic activity for biomass and energy supply to survive in hostile environments [1,17]. Normal cells typically utilize oxidative phosphorylation (OXPHOS, O) under normoxic conditions and glycolysis when there is a lack of oxygen. However, cancer cells often prefer glycolysis even when oxygen is available, referred to as the Warburg effect (W) or aerobic glycolysis [18,19]. During metastasis, cancer cells must be able to adjust their metabolic phenotype in order to survive in varying environments, resulting in these cells switching between different types of metabolism [20–23]. Metabolic reprogramming, specifically in the context of switching between the O state and W state, can enable cancer cells to combine different metabolic modes, leading to the acquisition of a hybrid W/O phenotype and metabolic low-low phenotype (L/L). The W/O cells, often associated with enhanced metabolic potentials, actively use both glycolysis and OXPHOS [24,25]. The L/L cells are metabolically inactive, exhibiting both low glycolysis and low OXPHOS, and are associated with therapy resistance in melanoma [26]. The highly metastatic murine breast cancer 4T1 cells exhibit both higher glycolytic and OXPHOS activity relative to the isogenic and less metastatic 67NR cells [27]. Furthermore, when the circulating tumor cells (CTCs) formed by 4T-1 cells exhibited enhanced OXPHOS relative to both the primary tumor and lung metastasis formed by 4T1 [28]. The high metastatic potential enabled by the hybrid metabolic phenotype has been confirmed in a number of additional experimental studies [27,29]. Together, these experiments suggest a tight connection between metabolic plasticity and cancer metastasis, specifically the hybrid W/O state with high metastatic potential.

As already mentioned, many studies focused on either EMT or metabolism[7–10,20–23]. However, it has become increasingly clear that there exists extensive crosstalk between EMT and metabolism [29]. For example, there is bi-directional regulation between hypoxia-inducible factor 1 (HIF-1) and miR-200 [30]. The repression of miR-200 by HIF-1 induces EMT [31] and HIF-1 is able to repress the expression of HIF-1 [32]. Understanding the crosstalk between EMT and metabolic reprogramming is important for an increased comprehension of metastasis and tumor proliferation [29,33–35]. Recent studies show that metabolic reprogramming can increase metastatic potential and drive EMT, or conversely that induction of EMT can drive metabolic reprogramming [36–39]. The underlying mechanisms of interaction between EMT and metabolic reprogramming remain poorly understood, with several competing hypotheses as discussed below. Kang et. al. suggested cancer cells typically undergo metabolic reprogramming first and then trigger EMT [40,41]; this coupling, presumably, is a consequence of changes in the tumor microenvironment fostering metabolic reprogramming which drives EMT [42–44]. Another hypothesis is that the mutual activation between EMT and metabolic reprogramming can contribute to flexible coupling of various EMT states (E, M, and E/M) with different metabolic states (W, O, W/O) and possibly the two hybrid phenotypes (E/M and W/O) become coupled under certain crosstalk, leading to a greatly increased metastatic potential [29]. Evidence supporting this connection has recently been noticed in CTCs, where the CTCs exhibit enhanced OXPHOS with no compromise in glycolysis [28] and have also been shown to mainly consist of hybrid E/M cells, especially at high levels of NRF2, an antioxidation regulator [45]. Consistent coupling of E/M and W/O has been seen in breast cancer stem cells (BCSCs). Specifically, the hybrid E/M-like BCSCs (E/M-BCSCs) exhibit higher levels of both OXPHOS and glycolysis as compared to the mesenchymal-like BCSCs (M-BCSCs) [46,47]. While there have been preliminary indications of the coupling of EMT states and metabolic states, a systematic analysis of how different EMT and metabolism states are coupled remains to be explored.

To decode the coupled decision-making of EMT and metabolism, we developed a mathematical model which couples the core gene regulatory circuit of EMT – /SNAIL//ZEB [7] with that of metabolism – AMPK/HIF-1/ROS [48]. Regarding the EMT circuit, the miRNAs, and promote the E state while the transcription factors (TFs) SNAIL and ZEB promote the M state. In the metabolism circuit, AMPK promotes the O state while HIF-1 promotes the W state, and the reactive oxygen species (ROS) may be associated with the W/O state. By analyzing the coupled circuit, we found that mtROS is a key promoter of “double-hybrid” state, namely the hybrid E/M state coupled with the hybrid metabolic phenotype, referred to as the E/M-W/O state. Additionally, as we will show later, HIF-1 may play a more central role in metabolic reprogramming driving EMT than AMPK. Strikingly, we found that when the crosstalk is bi-directional there are parameter space regions for which the E/M-W/O state is the only accessible state, and the biological significance of these parameters will depend on details of the microenvironment. Interestingly, even if the individual circuit cannot give rise to the hybrid phenotype (i.e., neither the E/M or W/O states are initially accessible), upon including crosstalk, the hybrid states (E/M or W/O) emerge. Indeed, a single crosstalk is sufficient for the metabolism circuit or EMT circuit to gain tristability. We also show that previously identified phenotypic stability factors (PSFs) of the E/M state - GRHL2 and OVOL2 [14,49], not only stabilize the E/M state but also stabilized the E/M-W/O state. Our results therefore suggest that a highly aggressive plastic phenotype along both the EMT and metabolic axes (E/M-W/O) is a likely choice for a subset of cancer cells and, speculatively, may be critical for metastasis.

**Model: Coupling the regulatory networks of EMT and metabolism**

While the mechanisms of EMT and cancer metabolism have been investigated individually, the crosstalk between the two circuits and how the phenotypes are correlated is still largely unknown. To decode the crosstalk between EMT and metabolism, we couple our previously published regulatory networks of EMT [7] and metabolism [48] by including the mutual regulatory links between these two circuits; see Figure 1A for the coupled network and see SI for details for each of the crosstalks (Table S5). The crosstalk between the EMT circuit and the metabolism circuit can be direct (e.g., HIF-1 upregulating SNAIL) or indirect (e.g., upregulating mtROS), the latter arising because our formulation focuses only on a few core components and effective interactions between them that can occur via intermediate reactants. We initially focus on the core networks and investigate the role of crosstalk on the coupling of different EMT and metabolism states. Then we ask an interesting question whether the crosstalks contributed to the emergence of the hybrid states. Lastly, we evaluate the role of the PSFs of E/M, OVOL and GRHL2,on the stability of the E/M-W/O state.

The core EMT network is comprised of the EMT-inducing transcription factors (EMT-TFs), ZEB and SNAIL, and the microRNA families, μ200 and μ34. It is modeled as a transcription-translation chimeric circuit [7]. For a two-component chimeric circuit consisting of one microRNA (u) and one TF (RNA m, protein B), the binding/unbinding dynamics are given by

(1)

(2)

(3)

where the three functions, , and which represent respectively the active miRNA degradation rate, active mRNA degradation rate, and translation rate (details in SI section 1.1, Fig. S1-S3). The transcriptional activation and inhibition by SNAIL and ZEB are mathematically represented as a shifted Hill function [50] which is defined shown below,

(4)

The fold change () represents the magnitude of the activation ( >1) or inhibition (0=< <1), and the sensitivity to the changes in X is represented by the Hill coefficient n (Fig. S3). For readability of the figures, we define the parameter Λ=1-λ such that maximal inhibition occurs when Λ=1 (λ=0) and no inhibition occurs when Λ=1 (λ=1). Previous investigation of the core EMT network by Lu and collaborators showed that the /ZEB module was responsible for the EMT tristability – epithelial (E) with high /low ZEB, mesenchymal (M) with low /low ZEB, and E/M with intermediate /intermediate ZEB, whereas the /SNAIL module mainly acted as a noise buffer [7](see Fig. 1B, and section S2.1 for nullcline analysis).

In a separate line of investigation, a proposed generic regulatory circuit of metabolism AMPK/HIF-1/ROS, provided insight into cancer metabolism plasticity and switching between different metabolism phenotypes. Through this reduced circuit, Yu and collaborators show that cancer cells can acquire at least three different metabolic phenotypes – an “O” state (high AMPK/low HIF-1), a ‘W’ state (low AMPK/high HIF-1), and a hybrid ‘W/O’ state (intermediate AMPK/HIF-1) [48](see Fig. 1C).

To couple the regulatory circuits of EMT and metabolism, we did extensive literature search and identified main crosstalks between these two circuits (see Fig. 1A). The crosstalk is obviously bi-directional. For example, regarding EMT regulating metabolism, ROS levels are increased by  via downregulating the NRF2-dependent antioxidant capability [51–53], downregulating SOD2 [54], or upregulating the p53 pathway [55,56]. This increase in ROS levels by is potentially more pronounced for mitochondrial ROS (mtROS) versus NADPH oxidase mediated ROS (noxROS), and we will explain in more detail later[51,57]. Next, family members can either upregulate or downregulate Hif1 expression [30]. While miR-429 upregulates HIF-1, both miR-200b [31] and miR-200c [58] downregulate HIF-1 expression. We focus on the negative feedback loop which seems to be present in a larger portion of the miR-200 family members [30,59]. Regarding metabolism regulating EMT, HIF-1 inhibits miR-200b through upregulation of the HIF-1 downstream target ASCL2 [31]. Therefore, there is a mutual inhibitory feedback loop between and HIF-1. Additionally, HIF-1 can directly upregulate SNAIL [60], while AMPK represses the production of SNAIL [61] by activating FOXO3. Similarly, AMPK suppresses ZEB2 by activating FOXO1 [62,63]. Additionally, CREB, after being activated by AMPK via phosphorylation, can transcribe resulting in the upregulation of [64–68]. Please refer to supplementary Table S5 for a detailed description of all crosstalks that have been included in our modeling framework.

The new model we propose here is built by including these crosstalk links so as to couple the circuits of EMT and metabolism respectively. We modify the metabolic circuit such that the mathematical model includes the miRNA regulation of HIF-1 by and confirm that the nullclines and expression of AMPK/HIF-1/ROS for the modified metabolic network model is consistent with results from the model detailed in Ref. [48] (Fig. S4). The full equations for the dynamics of all components of the circuit are given in SI Section 1.3 and the parameters along with a brief explanation are given in SI Section 1.4.

We started with parameters such that both the EMT and metabolic networks are tristable. This means when the crosstalk are inactive, there are at maximum nine possible combinations of the EMT and metabolic phenotypes: E-W, E-O, E-W/O, M-W, M-O, M-W/O, E/M-W, E/M-O, and E/M-W/O (Fig. 1D, details of numerical integration using the Euler method are given in section S2.2). By including active crosstalks, we can identify crosstalk affects the coupling between EMT states and metabolism states.

While the W state is characterized by high HIF-1/low AMPK and the E state is characterized by high /low ZEB expression, including the crosstalk will quantitatively alter the expression profiles for the various steady states. This means that the use of fixed thresholds to determine the state of the cell is no longer appropriate. Therefore, we use a distance metric normalized by the expression of the decoupled network to classify the generated expression profiles as indicative of one of the nine coupled states (see Section S2.3 for details). With our baseline decoupled network parameters, we show that 1000 initial conditions are large enough to generate consistent percentages of different states (Fig. S5-S7) - with the hybrid states being most populous (W/O and E/M) followed by the W and M phenotypes, followed by the O and E states. This result is just for one set of parameters and others will lead to a different fraction of initial conditions leading to these disparate states.



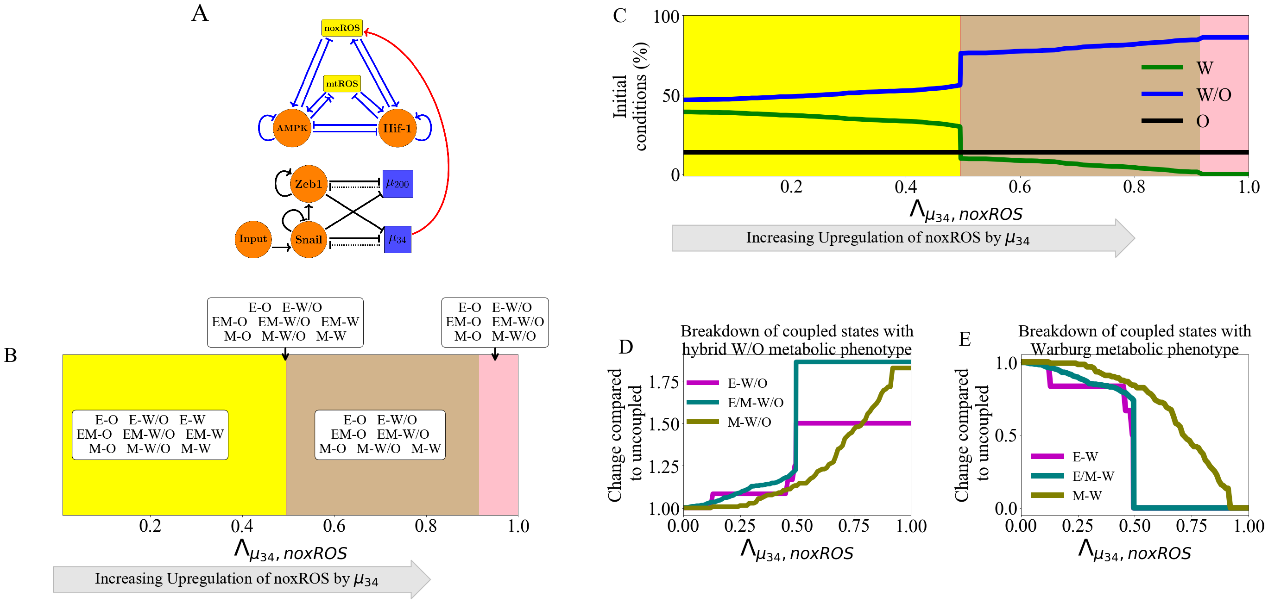
**Figure 1**. **The coupled EMT/MR circuit results in 9 possible steady states.** With inactive crosstalks all combinations of the steady states of the core EMT and metabolic networks are accessible. **(A)** The network showing the core EMT module (bottom) with regulatory links designated by black, the core metabolic circuit (top) with regulatory links designated by blue, and the crosstalks noted in red. The dashed lines denote miRNA-based regulation. The solid lines denote transcriptional regulation. Regulatory links ending in bars represent inhibition while the arrows represent activation. **(B)** The nullclines of the EMT network. The system is tristable and the three stables states (high /low Zeb, low /high ZEB, and intermediate /ZEB) represent the three states (E, M, E/M) respectively. **(C)** The nullclines of the metabolic network. The system is tristable with three stable states (high AMPK/low HIF-1, low AMPK/high HIF-1, and intermediate AMPK/HIF-1) represent the three to metabolic states (O, W, W/O) respectively. **(D)** The 9 possible phenotypic states when all crosstalks are inactive. The blue, purple, and black markers represent the M, E/M, and E states, respectively. The circle, cross, and square represent the W, W/O, and O states, respectively. Therefore, the coupled E/M-W/O state is represented as a purple cross.

**Results**

**Individual crosstalk can push the downstream circuit towards a single state:** Let us start by making just one cross-link active, caused by e.g. an EMT-related microRNA. Now, in our model there is a clearly an unaffected upstream subnetwork (EMT, from where the link originates) and a regulated downstream one. (Note that the model ignores any possible dilution of the microRNA due to its action on ROS; see below).

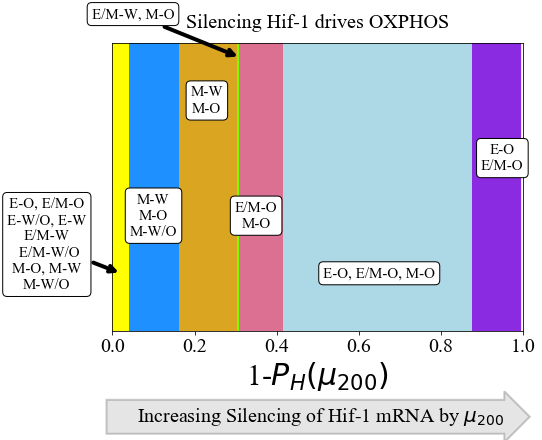
When noxROS is upregulated by (Fig. 2A), as there is no feedback to the EMT network, the percentages of initial conditions leading to the E, E/M, and M states are unchanged; increasing noxROS enhances the W/O state and consequently the coupled E/M-W/O states are upregulated. In other words, the E/M state becomes more likely to be associated with the W/O state (Fig. 2D). As the level of noxROS increases, the possible coupled states reduce from nine to six, losing first the E-W state, then the E/M-W, and finally the M-W state (Fig. 2B, section S2.4). Further we show that increasing noxROS pushing the W-associated states towards the W/O-associated states, with little change occurring for the O-associated states (Fig. 2C).

Analyzing the states coupled with the W state we found that the M-W state exists for a larger parameter space, compared to the other W-associated states, as the coupling is increased (Fig. 2E). This is as expected since the W state has the lowest level of the metabolism states (Fig. 2E). Similar changes have been observed via the upregulation of mtROS (Fig. S8); the E-W and E/M-W states are also the first suppressed states. Consistent with the effect of upregulating noxROS, upregulating mtROS is also correlated with an increase of the E/M-W/O state. Further, activation of mtROS results in a downregulation of the O state alongside downregulation of the W state, thus stabilizing the W/O state. Together, these results suggest both mtROS and noxROS may be critical factors in regulating the coupling of two hybrid states – E/M-W/O, and mtROS exhibited a greater increase in the E/M-W/O state than noxROS.



**Figure 2. noxROS upregulated by stabilizes the W/O state and enhances the E/M-W/O coupled state.** As noxROS is upregulated by , the number of initial conditions leading to the O state is minimally changed, the W state is reduced, and the W/O state is increased. The EMT network is unchanged, as there is no feedback, but the coupling of metabolic states with the EMT states changes, and the E/M-W/O state is upregulated. **(A)** A diagram of the core EMT circuit (left) and the core metabolic circuit (right) connected by the crosstalk upregulating noxROS (red link representing transcriptional regulation). **(B)** Of the nine possible coupled states, as noxROS is upregulated by , there are 4 distinct groupings. All possible couplings of the EMT states (E, M, and E/M) with both the O and W/O states persist for all levels of noxROS upregulation. The coupled states associated with the W state, (E-W, E/M-W, and M-W), are lost as the level of noxROS increases, as shown in the red, tan, and pink regions, respectively. **(C)** The W/O state (blue) is upregulated, W (green) state is downregulated, and O (black) is unchanged. The lines represent the total number of initial conditions leading to the W, O, or W/O states as a function of increasing regulation of noxROS by . (The background colors correspond to the colors representing the possible steady states of (B).**) (D)** Showing the breakdown of the coupled states associated with the W/O state (i.e., E-W/O, M-W/O, and E/M-W/O) compared to the inactive system (). The E/M-W/O coupled state is greatly upregulated once , the M-W/O coupled state is slowly upregulated, and E-W/O is also upregulated. **(E)** Same as (D) but for the coupled states associated with the W state. Once , both the E-W and M-W states are fully suppressed. The E/M-W coupled state continues to be downregulated until it is fully suppressed near .

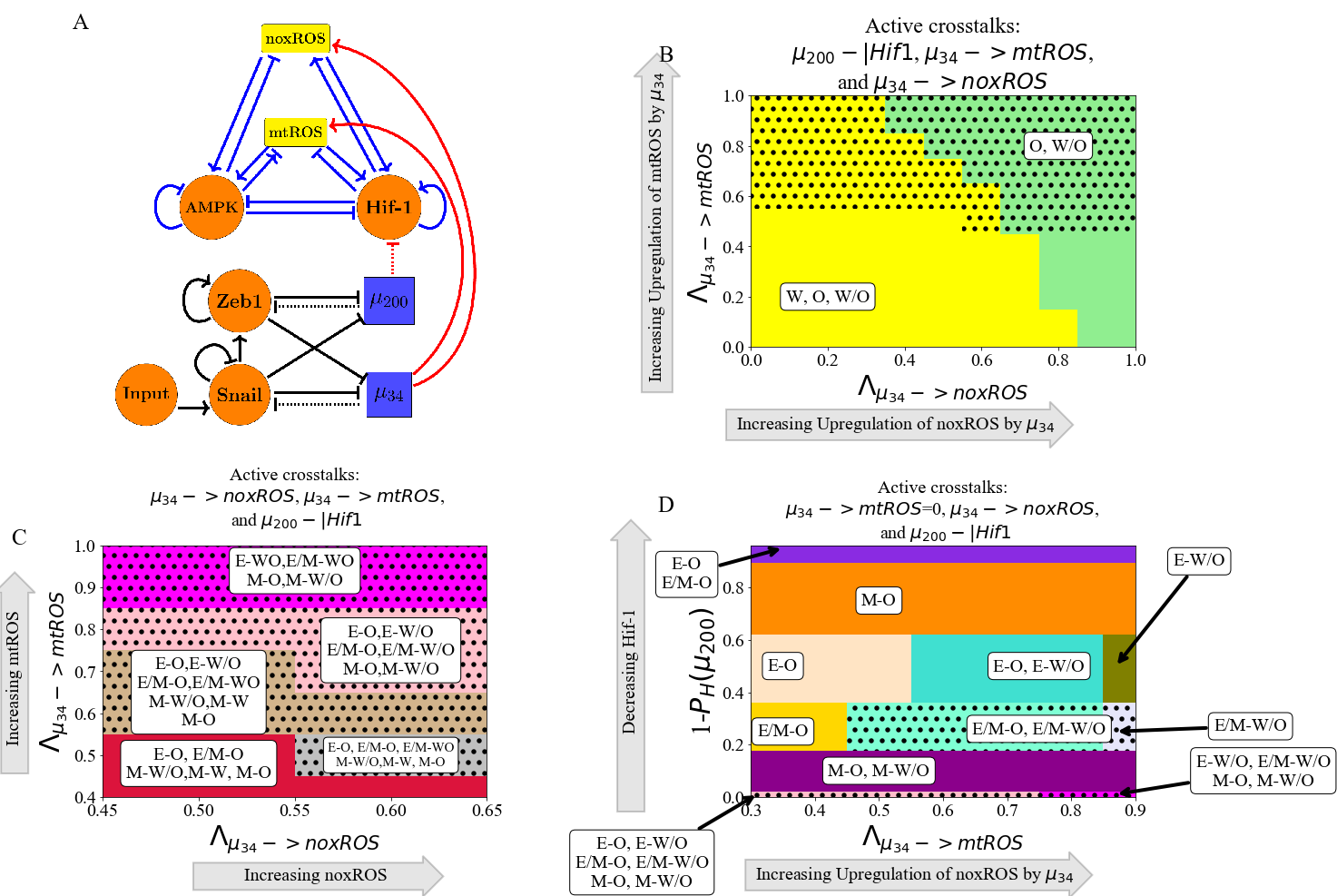
**Regulation of HIF-1 affects both subcircuits:** While the previous link only affected the downstream network, the miRNA regulation of HIF-1 by can affect both networks. This arises because of the reduction in the microRNA level caused by this coupling. In our model, mediates both the transcription and translation of HIF-1 mRNA, and as a result, can be recycled or degraded. Therefore, while the downstream metabolic network is modulated, the upstream EMT network is also affected via change of We have defined a function to stimulate the above-mentioned effect of on HIF-1 (details of silencing function in section S2.5). Note that as we include increased silencing, the first thing which occurs is the restriction of the EMT state; close to the only EMT state allowed is M. When we enter this region, all the metabolic phenotypes are allowed. As the mediated regulation of HIF-1 increases, the W/O and W states are suppressed sequentially and the O state is promoted. As the HIF-1 is suppressed by , the degradation of due to binding binding to HIF-1 RNA is reduced and as a results and the W state gradually disappears. When HIF-1 mRNA is fully silenced, only the E-O and E/M-O coupled states remain (Fig. 3). Since the E/M state does not reappear until after the metabolic system has fully transitioned to O, the coupled E/M-W/O state is not observed for all values of silencing HIF-1 mRNA. These results suggest overexpression could promote the O-associated states (O-E and O-E/M) and destabilized the coupled E/M-W/O.

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**Figure 3.** **The coupled phenotypes associated with increased silencing of the HIF-1 mRNA by .** Both the EMT and metabolic networks are affected by the mediated regulation of HIF-1, and the E/M-W/O state is suppressed if any fraction of silencing occurs. At minimal silencing (PH( near 1) only the coupled states with M are accessible (M-W, M-O, and M-W/O). Then as -mediated inhibition of HIF-1 increases, the W/O state is suppressed, then the M-W state undergoes partial EMT and becomes the E/M-W state, and after that only the O-associated states are accessible. At complete silencing of the HIF-1 mRNA only the E-O and E/M-O states are accessible.

**Inclusion of multiple miRNAs of the EMT network can stabilize the W/O metabolic phenotype**: We next wish to determine how including links emanating from both and can synergistically drive metabolic reprogramming, and specifically enhance the chances of being in the coupled E/M-W/O state. As mentioned previously, upregulated ROS leads to an increased W/O state (Fig. S8). If both noxROS and mtROS are upregulated by the E/M-W/O state is further upregulated (Fig. S15). While upregulation of ROS causes an increase in the E/M-W/O state, we showed above that silencing HIF-1 mRNA suppresses the E/M-W/O state; therefore, we may expect some suppression of the E/M-W/O state when including both  and . Interestingly, the hybrid E/M-W/O state can be fully suppressed when downregulates HIF-1 and upregulates noxROS, but only partially suppressed when downregulates HIF-1 and upregulates mtROS (Fig. S16). These results suggest the type of ROS present can have different affects on the E/M-W/O state.

The coupled hybrid E/M-W/O state is stabilized if mtROS is upregulated, but noxROS upregulation has minimal effect on the E/M-W/O state. Strikingly, if all three miRNA crosstalk are active ( silencing HIF-1 mRNA and upregulating noxROS and mtROS, Fig. 4A) the E/M-W/O coupled state can be suppressed even if the W/O state is present (Fig. 4B). Further, the E/M-W/O state is present for all values of noxROS upregulation but is only present at high values of mtROS upregulation (Fig. 4B). Analyzing the coupled state phases shows the E/M-W/O state is suppressed when mtROS is only slightly upregulated (Fig. 4C). Further, the E and E/M states are associated with the O state when mtROS levels are slightly upregulated. Interestingly, the M state is coupled with O and W/O states while the E and E/M states are only coupled to the W/O state when mtROS is fully upregulated (Fig. 4C). Additionally, depending on the initial conditions, if noxROS is maximally upregulated (λu34,noxROS=0), mtROS is upregulated, and HIF-1 is partially silenced by the system can access the hybrid E/M-W/O state (Fig 4D). Also, while mtROS must be upregulated for the system to access the coupled E/M-W/O state, the E/M-W/O state is accessible for all levels of noxROS upregulation (SI Fig S17). There also seems to be a synergistic effect between the three crosstalks resulting in an increased parameter space leading to the E/M-W/O state than what is expected from the individual crosstalks. Further, the difference in the effect of noxROS and mtROS seems to result from the frustrated regulation of mtROS by HIF-1 and . Therefore, feedback loops between mtROS, HIF-1, , and together control the appearance of the E/M-W/O state.



**Figure 4.**  **and can upregulate the W/O phenotype.** When all three crosstalks from the EMT network (-|HIF-1, -> mtROS, and ->noxROS) are active the E/M-W/O state can be upregulated. The E/M-W/O state is accessible when mtROS is high and at intermediate silencing of HIF-1. The level of noxROS seems to have minimal effect. This suggests the //HIF-1/mtROS axis plays a significant role in stabilizing the hybrid E/M-W/O state. **(A)** Schematic illustration of the coupled metabolic (top) and EMT (bottom) regulatory network with all EMT driven regulatory links active ( upregulating mtROS, upregulating noxROS, and silencing HIF-1). **(B)** The phase plane corresponding to all EMT driven regulatory links (network pictured in A). The regulation of HIF-1 by in this phase plane corresponds to the rightmost, blue region of Fig. 3 where all metabolic phenotypes are possible. As noxROS is upregulated (right to left), the W state is suppressed. However, as the level of mtROS increases (top to bottom), the black dotted region appears showing the existence of the E/M-W/O coupled state, suggesting mtROS may have a stronger effect on the E/M-W/O state than noxROS. **(C)** The coupled states of (B) when only EMT driven crosstalks are active ( downregulating HIF-1 and upregulating mtROS and noxROS). The E/M-W/O state exists when mtROS is upregulated. This is zoomed in on the middle region of (C). **(D)** At maximum upregulation of noxROS (=0), as mtROS increases (x-axis) and HIF-1 is moderately silenced (y-axis) there are regions where the E/M-W/O state is possible (black dotted regions).

**Metabolic reprogramming can drive EMT:** We next turn to a consideration of information flowing in the other direction, from metabolism to EMT. To elucidate the way in which metabolic reprogramming can drive EMT, we determined the effect of each metabolism-driven crosstalk on the coupled states. First, we analyzed the links in which HIF-1 upregulates SNAIL (Fig. 5A and S9) or inhibits (Fig. S10). As expected, both HIF-1 mediated links push the system towards the M state. Further, both the E and hybrid E/M states are most associated with the O state (when the HIF-1 level is relatively low) while the M state is initially associated with the W state. The correlation between the E-O and M-W states is assumed in much of the literature [29]. Similarly, modulating the EMT-inducing signals such as TGF-β that can activate SNAIL can alter the stability of the E/M state and therefore the coupled states(see Fig. S11). Opposite to the HIF-1 results, AMPK upregulating  pushes the EMT network to adopt an E state and suppresses the E/M state followed by the suppression of the M state (Fig. 5B and S12). Similarly, AMPK mediated downregulation of ZEB and/or SNAIL has an analogous effect to AMPK upregulating on the expression of the E/M state and the system saturates near fully epithelial (Fig. S13 and S14). Additionally, when AMPK regulates the EMT circuit alone, the E and M states are still most associated with the O and W states, respectively. However, the E/M state for AMPK driven crosstalk is associated with the W state. This is in direct contract to HIF-1 driven crosstalk in which the E/M state is coupled with O state. The results suggest that neither OXPHOS nor Warburg metabolism is automatically associated with the E/M state and that this state has metabolic plasticity to mix and match different metabolic phenotypes.

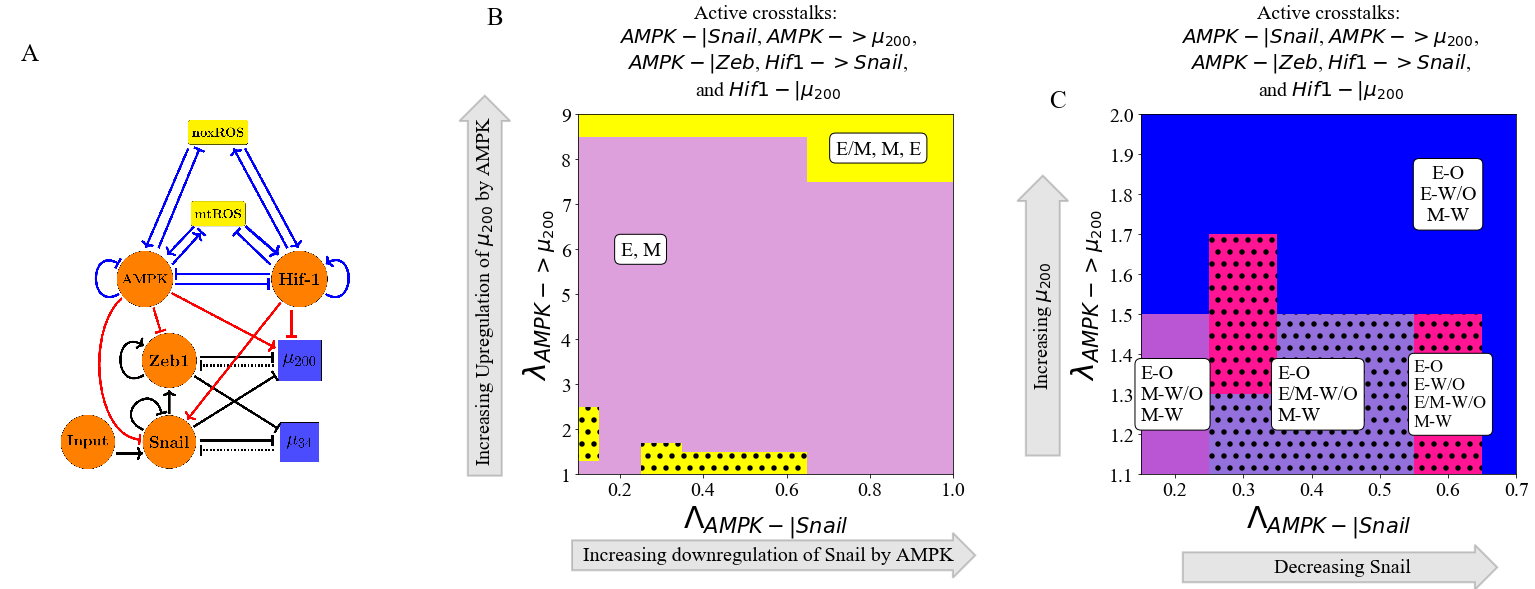
The crosstalk between the EMT network and metabolism network play various roles in mediating the coupled states. The mediated upregulation of mtROS or noxROS exhibit consistent upregulation of the E/M-W/O state and suppression of the E-W and E/M-W coupled states. The phases of the coupled states are also very similar when HIF-1 inhibits or upregulates Snail, first suppressing the E-W, E-W/O, and E/M-W states and stabilizing near fully mesenchymal. However, the E/M-W/O state does exist for a larger portion of the parameter space when HIF-1 inhibits (Fig. S9 and S10). Lastly, the AMPK driven crosstalks (inhibiting ZEB or SNAIL or upregulating ) are initially very similar, suppressing first the E/M-O and E/M-W/O states. In fact, the phases are nearly identical when AMPK inhibits ZEB or SNAIL (Fig. S13 and S14). However, AMPK upregulating has slightly different effect on the coupled states before saturating at epithelial (Fig. S12). These similarities between the effect of different crosstalk suggests a degree of consistency in how EMT drives metabolic reprogramming, and vice versa.

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**Figure 5. The role of metabolism in driving EMT.** HIF-1 mediated crosstalks drive the EMT circuit towards the M state, while AMPK mediated crosstalks drive the EMT network towards the E state. Neither type of crosstalk alone can stabilize the E/M state, but the E/M state persists longer for HIF-1 controlled crosstalks. **(A)** The number of initial conditions leading to an E/M, M, or E state as HIF-1 upregulates SNAIL. The hybrid E/M state is suppressed quickly as the system is driven towards the M state. **(B)** The number of initial conditions leading to an E/M, M, or E state as AMPK upregulates and drives the system towards epithelial. The E/M state exists for larger portions of the parameter spaces for HIF-1 regulation than for AMPK-mediated crosstalks.

**TFs of the metabolic network can stabilize the E/M metabolic phenotype**: There are two distinct events at play when the metabolic network regulates the EMT circuit. AMPK regulation quickly suppresses the E/M state and pushes the system towards the E state whereas HIF-1 regulation can allow the system to maintain the E/M state for a range of strengths while ultimately pushing the system towards the M state (Fig. 5A and 5B). As AMPK and HIF-1 push the system towards opposite states, having active links emanating from both should push the circuit towards a hybrid state. That is exactly what happens when at least one of the three AMPK crosstalks and at least one of the two HIF-1 crosstalks, although the exact values of where the E/M-W/O state exists depends in detail on the type of regulation (Fig. S18). Additionally, if AMPK and HIF-1 target different EMT TFs, the E/M-W/O state may exist in larger parameter spaces than if they target the same EMT TF (Fig. S18), suggesting multiple crosstalks should be active and multiple gene regulators should be targeted to stabilize the E/M-W/O state. If all crosstalks involving AMPK and HIF-1 regulating the EMT circuit are active (Fig. 6A) then there are significant regions in which the E/M state exists (Fig. 6B). However, when analyzing the system for the existence of the E/M-W/O state, it only exists in a small region where is minimally upregulated. Moreover, HIF-1 driven crosstalks are able to maintain the E/M state longer than AMPK driven crosstalks suggesting, the reduced regions of E/M-W/O existence is likely due to the suppression of the E/M state by AMPK regulated crosstalks, as mentioned above (see Fig. S12-S14). This suggests HIF-1 driven crosstalk is more strongly correlated with the E/M state than AMPK driven crosstalk, in agreement with a recent study based on publicly available expression data [69].

To stabilize the E/M state, both AMPK and HIF-1 crosstalk are necessary, and if all EMT regulating crosstalks are active then there are regions where the E/M-W/O state exists. Additionally, the E state is typically coupled to the O state (E-O), the M state is associated with the W state (M-W), and when the E/M state is present it is typically associated with the hybrid W/O state (Fig. 6C). In fact, for any system, if there are only three coupled states available and each has a distinct phenotype of the EMT and metabolic networks, then the only possible set of states is E-O, M-W, and E/M-W/O. This behavior represents the full coordination of EMT and metabolism and suggests clusters of migrating cells utilize a combination of aerobic glycolysis and OXPHOS. Given tumors are metabolically heterogeneous, this result suggests the topology and parameters of the system may only represent certain microenvironments and is a limitation of our study.



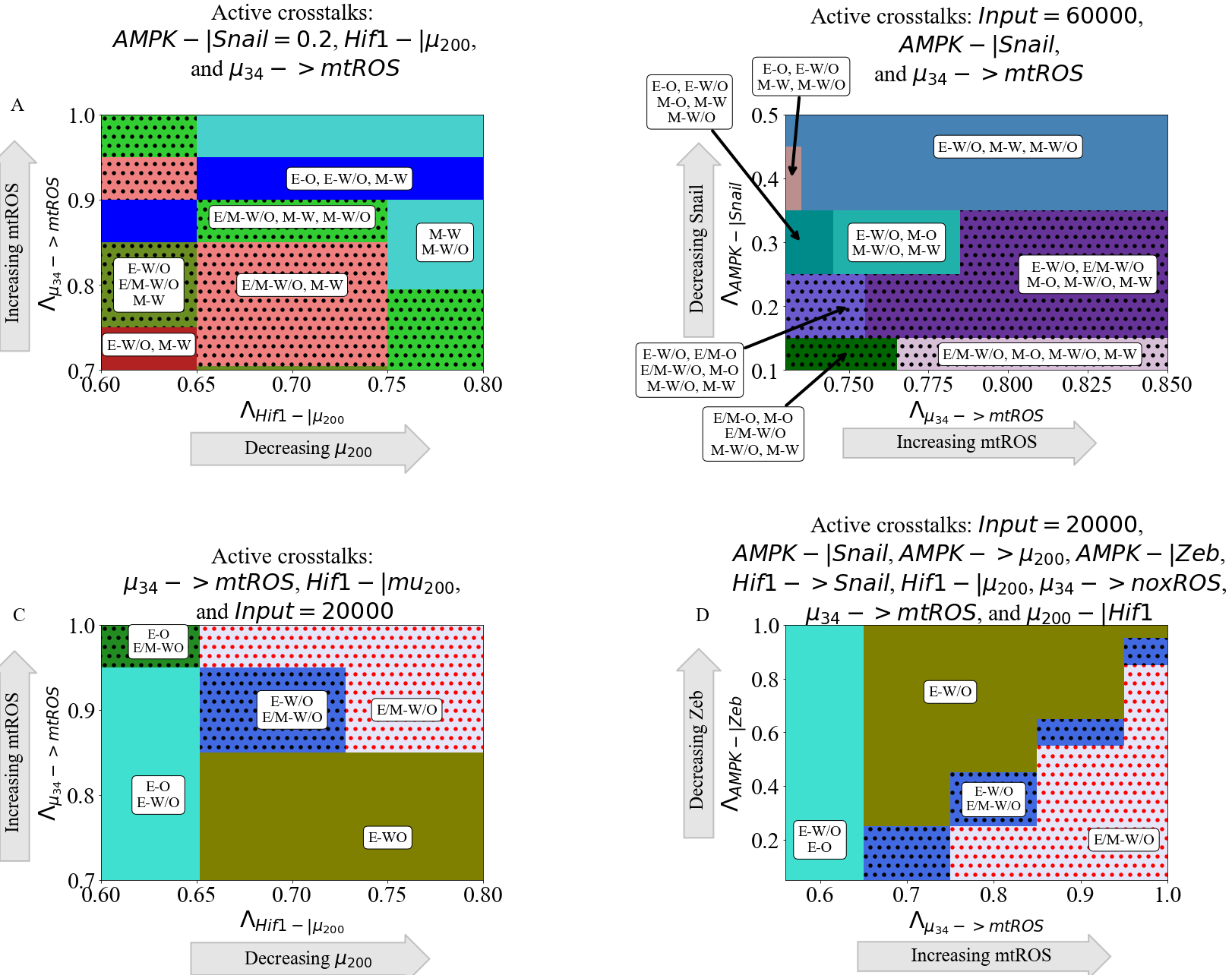
**Figure 6. AMPK and HIF-1 cooperate to upregulate the hybrid E/M state.** When all HIF-1 and AMPK controlled crosstalks are active (HIF1->Snail, HIF1-|, AMPK-|Snail, AMPK-|Zeb, AMPK-> ) the E/M-W/O state can be stabilized. HIF-1 driving the network to mesenchymal and AMPK driving the system towards the E state results in HIF-1 and AMPK cooperatively stabilizing the E/M state. Once stabilized, the E/M state is coupled with the W/O state (i.e., stabilizing the coupled E/M-W/O state). **(A)** Schematical illustration of the network showing how metabolism drives EMT. ZEB is inhibited by AMPK, SNAIL is upregulated by HIF-1 while being downregulated by AMPK, and is upregulated by AMPK while being inhibited by HIF-1. **(B)** The phases plane of potential EMT states when all metabolic driven crosstalks are active. The E/M state is only accessible when λAMPK-| μ200 is near 1 or very high (i.e., at the extremes of regulation). **(C)** The coupled states when the EMT circuit is regulated by the metabolic circuit (AMPK-|SNAIL, AMPK-|ZEB, AMPK->, HIF-1 -|, HIF-1 -> SNAIL). The results suggest a direct correlation between the E, E/M, and M states to the O, W/O, and W states, respectively.

**The Hybrid E/M-W/O phenotype:** Recently, it has been suggested that the most metastatic cancer phenotype is characterized by the hybrid E/M state and hybrid W/O state[29]. Therefore, it is now useful to focus our discussion onto how the crosstalk between EMT and metabolism regulatory networks specifically affects the E/M-W/O state and the possibility that it could be the only possible coupled state for certain parameter spaces. From our analysis of activating individual crosstalks, we deduce that two competing metabolic driven crosstalk and one competing EMT driven crosstalks would be minimally necessary to fully stabilize the E/M-W/O state and suppress all other coupled states.

In detail, the hybrid E/M-W/O state can be stabilized when AMPK downregulates SNAIL, HIF-1 downregulates , and upregulates mtROS. The E/M-W/O state exists in much of the space and is increased in prevalence when SNAIL is significantly repressed by AMPK (λAMPK-| SNAIL=0.2), mtROS is upregulated, and levels have been moderately downregulated (Fig 7A and S19A). Further, instead of HIF-1 downregulating , increasing SNAIL levels can promote the E/M-W/O state to become even more prevalent (Fig. 7B and S19B). While, the E/M-W/O state was stabilized in both cases (Fig. 7A and B), neither was able to fully stabilize the E/M-W/O state and suppress all other states.

It is possible to suppress all states except the coupled E/M-W/O state with just three regulatory links; HIF-1 inhibiting , upregulating mtROS, and modulating the EMT-inducing signal (Fig. 7C and S19C). In fact, no other combination consisting of only three regulatory links seems to enable only the E/M-W/O state(Fig. S?). Additionally, this region which only includes the E/M-W/O state persists even if all remaining crosstalks are activated (Fig. 7D and S19D).

Looking at the proximal phases next to the one with just E/M-W/O suggests that stabilization of the E/M-W/O state requires mutual activation between metabolic reprogramming and EMT. When the E/M-W/O state can be the only available state (Fig. 7C and 7D), the surrounding phases are the same whether only three crosstalks or all crosstalks are active (E-O and E-W/O), suggesting there may be a sequential path to generate the E/M-W/O state. Further, if the E/M-W/O state is not the only allowed state (Fig. 7A and 7B), the surrounding phases include M-coupled states (M-O, M-W/O, and M-W) as well as E-coupled (E-O and E-W/O). Together the results suggest that to reach the E/M-W/O state for epithelial cancer, first metabolic reprogramming should occur and the E-W/O state should be acquired, followed by a partial EMT (E/M-W/O). Additionally, the persistence of the E/M-W/O state suggests there might be other combinations of crosstalks that generate phases where only the E/M-W/O state is possible, although it is outside the scope of this manuscript to find all possible combinations of crosstalks that can enable only the hybrid E/M-W/O coupled state. However, based on these results, we would expect HIF-1 suppressing and upregulating mtROS to be prominent among all such combinations.



**Figure 7. The coupling of the EMT and metabolic regulatory networks can enable a coupled hybrid E/M-W/O state.** Minimally, three links (one effecting the metabolic network and two controlling the EMT network) are necessary to suppress all coupled states except the E/M-W/O state. Many combinations of crosstalk can upregulate the E/M-W/O state, but to enable the E/M-W/O state to be the only stable state, three crosstalk are necessary – upregulating mtROS, HIF-1 inhibiting , and EMT-inducing signaling that regulate SNAIL. **(A)** Phase diagrams of the coupled states when considering three crosstalk; the Input=60000 molecules, AMPK downregulates SNAIL, and upregulates mtROS. The E/M-W/O state is upregulated when mtROS levels are increased. **(B)** The phase diagram of the coupled states when considering the inhibition of SNAIL by AMPK (λAMPK-| SNAIL=0.2), HIF-1 inhibiting μ200, and upregulating mtROS. The E/M-W/O state is upregulated for some regions. **(C)** When considering the bi-directional regulation between EMT and metabolism by the three minimally necessary regulatory links, there are parameter regions in which the only possible coupled state is the E/M-W/O state. **(D)** When all crosstalks are active there are regions where only the E/M-W/O state exists. Similar sets of coupled states in (C) and (D) suggest a preferential pathway to drive the system towards the hybrid E/M-W/O coupled state.

**Hybrid phenotypes are enabled by crosstalk in cells initially without the E/M or W/O state:** We have showed that the E/M and W/O states are often connected, the population in the E/M-W/O state can be expanded depending on the relative strength of various links, and there are parameter sets with only the hybrid E/M-W/O state available and all other coupled states suppressed. Next, to investigate whether the crosstalk between EMT and metabolism enables cancer plasticity e.g., by acquiring the hybrid states. We simulate scenarios where the individual EMT and metabolism networks cannot acquire a hybrid state, corresponding to normal physiological conditions where we expect most cells will be restricted to a binary choice of E versus M and W versus O [70]. Then we systematically analyze whether any crosstalk can enable the hybrid state to emerge.

First, we confirmed both the EMT network and metabolic network are independently bistable when the crossstalk is inactive( Fig. S20), and ensured the solutions from the initial conditions were evenly divided between the steady states (Fig. S21-S22). We can then proceed to determine the consequences if EMT and metabolism mutually regulate each other.

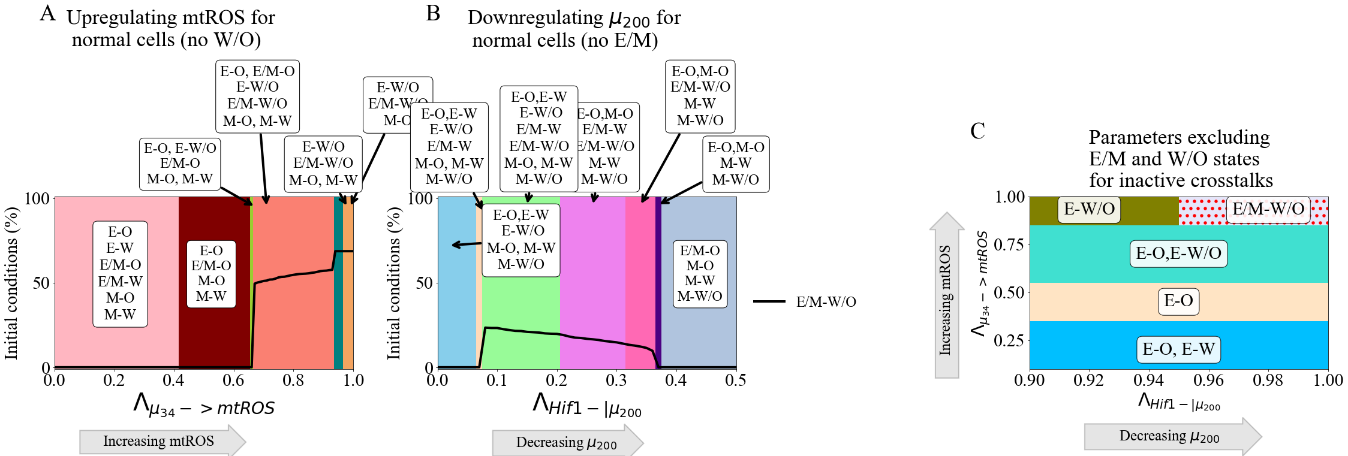
As already mentioned, the EMT network can drive metabolic reprogramming via microRNA-mediated links. We first kept the metabolic circuit as a bistable system where only W and O are the available stable states, i.e., no hybrid W/O state when the cross-talk is inactive. Then we analyzed the coupled states considering links - upregulating mtROS, downregulating HIF-1, or upregulating noxROS. We found that the metabolic circuit becomes tristable, i.e., the hybrid W/O state emerges, when mtROS is upregulated by (Fig. 8A) but doesn’t appear if only noxROS is upregulated or μ200 is downregulated (Fig. S23). Additionally, the upregulation of mtROS by can further stabilize the coupled E/M-W/O state so that all E/M states become coupled with the W/O states. Furthermore, the upregulation of noxROS in the bistable circuit causes an increase in the frequency of the O state, in contrast to an increase of the frequency of the hybrid W/O state in the tristable circuit (Fig. S23 compared to Fig. 2). This suggests, noxROS may play a context-dependent role on the coupled state, while mtROS often stabilizes the E/M-W/O state.

Next to see whether metabolic reprogramming can enable the emergence of the hybrid E/M state, we kept the metabolic circuit as a tristable circuit and set the EMT network to be bistable (i.e., unable to acquire a hybrid E/M state alone). Then we investigated the effects of the following cross-talk, HIF-1 inhibiting , and HIF-1 upregulating SNAIL. When analyzing the inhibition of by HIF-1, we found that the coupled EMT-metabolism network is able to quickly generate the E/M-W/O state before it is once again suppressed (Fig. 8B). However, the E/M state persists but is coupled to the O state (E/M-O). Additionally, when analyzing the effect of HIF-1 upregulating SNAIL, we found that the E/M-W/O state is only generated when SNAIL is moderately upregualted (Fig. S24). Furthermore, both HIF-1 inhibiting and HIF-1 upregulating SNAIL can stabilize the system in the phase - (E/M-O, M-W, M-O, M-W/O), where the hybrid E/M state can be stably maintained. This suggests the master regulator of glycolysis, HIF-1, can drive cells towards the hybrid E/M state. Conversely, an individual AMPK-mediated crosstalk is unable to generate the hybrid E/M state and saturates in the epithelial phase (Fig. S24), as seen in the tristable circuit. Additionally, as with the tristable networks, the coupled hybrid E/M-W/O state can be stabilized by two competing crosstalk, such as AMPK upregulating SNAIL and HIF-1 downregulating (Fig. S25). These results suggest HIF-1 can strongly affect and drive EMT into a hybrid E/M state while AMPK can only help stabilize the E/M-W/O state if it is already present.

When both the EMT and metabolism networks are in the parameter regime where hybrid E/M or hybrid metabolism state is not available, the cross-talk can enable the emergence of these hybrid states. Recall that for the coupled tristable circuits, the simplest set of crosstalk with a parameter region that suppressed all coupled states except the E/M-W/O state consisted of three regulatory links: (1) HIF-1 inhibiting , (2) upregulating mtROS, and (3) EMT-inducing signaling acting on SNAIL. When these same links are active for the bistable EMT and metabolism circuits, the results are qualitatively very similar to the tristable circuit results (Fig. 8C and S26 compared to Fig. 7C). The E/M state is only possible near full inhibition of and the W/O state is possible when mtROS is greatly upregulated. Further, the system must be near maximum regulation (i.e., and must be close to zero) to generate the region where only the coupled hybrid E/M-W/O state is available. Additionally, the nearby phases surrounding the phase containing only the E/M-W/O state (E-O and E-W/O) is similar relative to those of the tristable circuit, further supporting a progression that must be followed to reach the E/M-W/O state.

Overall, we showed that if the metabolic network is bistable (W or O states) and the EMT network is tristable (E, E/M, or M states), upregulating mtROS can generate the W/O state and upregulate the E/M-W/O state. Conversely, if the EMT network is bistable (E or M) and the metabolic network is tristable (W, O, or W/O), a HIF-1 controlled crosstalk can briefly generate the E/M state and stabilize the E/M-W/O state. If both networks are bistable, the same three links as the tristable case (-> mtROS, HIF1-| and reducing the EMT-inducing signal) generates the E/M-W/O state and suppresses all other coupled states.

We also identified a sequential event to reach the coupled hybrid E/M-W/O state. starting from an E state, which typically associated with an O state, then transitioning from E-O to E-W/O, and finally transitioning to the coupled hybrid E/M-W/O state. In other words, cells may first reprogram their metabolism from O to the hybrid W/O state, followed by the initiation of EMT and a transition to the hybrid E/M state, thus exhibiting the E/M-W/O state.

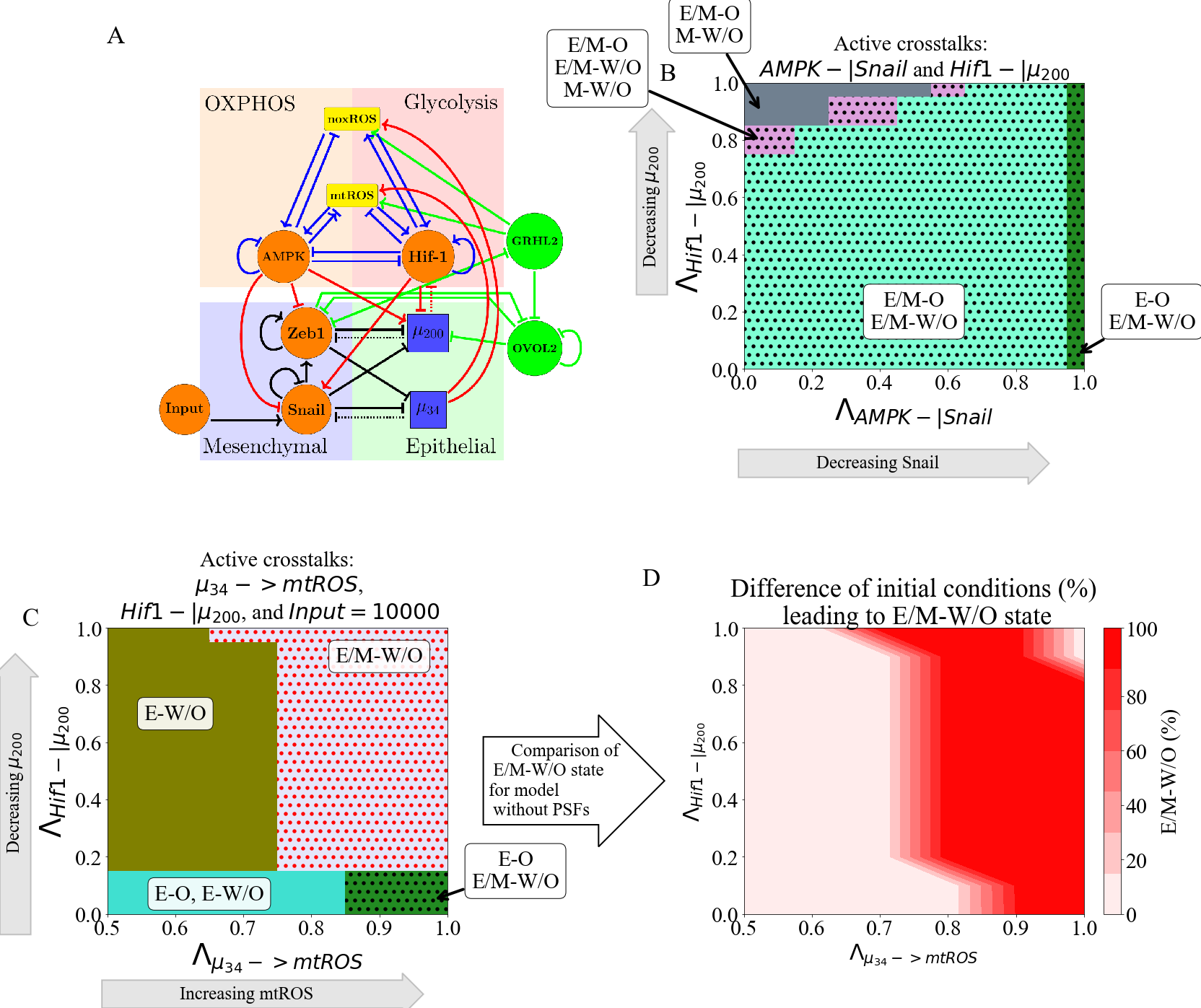


**Figure 8. Crosstalk can generate the hybrid states.** The activation of a single crosstalk (-> mtROS, HIF1 -> SNAIL, or HIF1 -|) can generate the hybrid state of the downstream network (W/O, E/M, or E/M), respectively. **(A)** The phase diagram showing coupled states where W/O is not available initially when the crosstalk is inactive (). Initially, only the O and W states can be accessed with an increase in the frequency of the O state and decrease of the W state. Once , there is a sharp change with the hybrid W/O state becoming the most often occupied state. **(B)** The phase diagram of coupled states when the hybrid E/M state is not available initially when the crosstalk is inactive. As the inhibition increases ( goes towards zero), the system goes from only the E and M states available to regions in which the E/M state is accessible. **(C)** Combining the models from (A) and (B), we generate a model which only has 4 possible coupled states if the crosstalk is inactive (E-O, E-W, M-O, and M-W). At maximum upregulation of mtROS and downregulation of , the E/M-W/O state is the only one accessible, similar to Fig. 7C.

**GRHL2 and OVOL can stabilize the coupled E/M-W/O state:** Previously, we have reported there are transcription factors, such as OVOL and GRHL2 that can stabilize the hybrid E/M state [14,49], referred to as phenotypic stability factors (PSFs) of the hybrid E/M state. We are curious whether these PSFs of the hybrid E/M state may also have a role in stabilizing the coupling of the hybrid E/M state with the hybrid W/O state. Since GRHL2 upregulates ROS in a manner similar to [71], GRHL2 may also stabilize the W/O state. Therefore, we extended the original coupled EMT-metabolism network to include these PSFs (Fig. 9A, parameters and modified equations of the PSF stabilized network are in Section S1.6). When the crosstalks are inactive, we find the PSF stabilized network can either be in the E/M-W/O or E/M-O state, and more than 90% of initial conditions lead to the hybrid E/M-W/O state (Fig. S27).

When a single crosstalk is active in the PSF coupled network, the behavior is as expected, with the E/M-W/O state persisting for larger parameter spaces relative to the coupled network without the PSFs. For instance, the hybrid E/M-W/O state exists for the entire parameter space when only one of the following crosstalk is active - AMPK downregulating SNAIL, AMPK upregulating , upregulating mtROS, or upregulating noxROS (see Fig. S28). Additionally, we can assume any EMT-mediated upregulation of mtROS or noxROS will have a similar effect by stabilizing the W/O state (and also the E/M-W/O state). The parameter space enabling the phases where the E/M-W/O state exists is also increased when these PSFs are present when the following crosstalk is active- HIF-1 downregulating or HIF-1 upregulating SNAIL (Fig. S28).

Next, we studied the effect of the PSFs on the E/M-W/O state when multiple crosstalks are active. If two competing crosstalks acting on the EMT circuit are active (e.g., one HIF-1 and one AMPK driven regulation active), then the E/M-W/O state is available for most of the parameter space (Fig. 9B). By comparing how the phases change as the foldchange increases, the regulatory crosstalks controlled by HIF-1 seem to have a stronger affect than the AMPK crosstalks and can push the system towards the M state, as shown by the presence of the M-W/O state as is inhibited by HIF-1. This corresponds with results from the tristable and bistable coupled networks where AMPK upregulating seems to have a weaker effect, specifically on the stability of the E/M-W/O state, than HIF-1 downregulating . Lastly, we activate all three crosstalks that were shown in the tristable and bistable networks to suppress all states except the E/M-W/O state (i.e., upregulating mtROS, HIF-1 downregulating , and including the EMT-inducing signaling acting on Snail). Once again, there is a phase where only the E/M-W/O state can exist (Fig. 9C). Furthermore, this phase exists in a far larger region in the presence of the PSFs (Fig. 9C and S29) relative to the absence of the PSFs (the light red region at the top right corner of Fig. 9D is the location of the E/M-W/O when no PSFs are present). The large red region on the right side of Fig. 9D is the additional parameter space where the E/M-W/O state is stabilized when the PSFs are coupled with the network. Further, the coupled states in the phases surrounding the region of E/M-W/O are the same as those in the bistable networks (E-W/O and E-O), and also appear in the analysis of the tristable network. These results confirm the PSFs can stabilize not only the E/M state but also stabilize the coupling of the hybrid E/M state with the hybrid W/O state, i.e., the E/M-W/O state.



**Figure 9. PSFs stabilizing the E/M state can stabilize the association of the E/M state with the W/O state.** Including the PSFs GRHL2 and OVOL2 further stabilizes the E/M-W/O state. Once again, the three links (-> mtROS, HIF1-|, and reducing the EMT-inducing signal) suppresses all states except the E/M-W/O state and increases the parameter regime of the phase. **(A)** The coupled EMT-metabolism network including GRHL2 and OVOL2. **(B)** The phase diagram of the coupled states when the PSFs are present. E/M-W/O state is present in a larger parameter space due to the PSFs stabilizing the E/M state even when AMPK downregulates SNAIL and HIF-1downregulates . **(C)** The phase diagram of the coupling states when the crosstalks – EMT-inducing signal acting on SNAIL is set to 10K, upregulating mtROS, and HIF-1 downregulating – are present together. The phase where the E/M-W/O state is the only possible coupled state is significantly enlarged compared to the coupled network without PSFs. **(D)** The difference in the frequency of the E/M-W/O state between (C, PSFs present) and the original model (Fig. S29B, PSFs are not present). The dark red region shows the phases in which only the PSF stabilized model can enable the E/M-W/O state. The light red in the bottom left corner near (0,0.1) is the only region in which the E/M-W/O state is the only stable state irrespective of the presence of PSFs. The light red on the right side is where neither model, PSFs present or not, can generate the E/M-W/O state.

**Discussion**

Cancer malignancy relies on the orchestration of multiple hallmarks, driven by different functional modules, such as metabolism, metastasis and stemness (cite Hallmarks of Cancer 2021 paper). It has become clear that different hallmarks of cancer are not independent and indeed are extensively coupled. Therefore, deciphering how these different modules affect each other can be critical to better understand cancer malignancy.

In this work, we focused on how reprogrammed cancer metabolism is coordinated with cancer metastasis. As EMT is often employed by cancer to as part of the metastasic process, we analyzed the mutual regulation between metabolism and EMT, through coupling their corresponding gene regulatory circuits – AMPK/HIF-1/ROS and miR-34/SNAIL/miR-200/ZEB. As both circuits potentially exhibit tri-stability, coupling of these two circuits in principle can give rise to nine coupled states (W-E, W-E/M and W-M, W/O-E, W/O-E/M and W/O-M, O-E, O-E/M and O-M). We systematically analyzed the effect of (1) each individual cross-talk between these two circuits, and (2) multiple cross-talks being active simultaneously, on each of the nine coupled states. We found that varying strengths of each cross-talk can destabilize or stabilize different coupled states and multiple cross-talks may exhibit synergistic or antagonistic effects on the coupled states. To incorporate the effect of the microenvironment, we further consider the role of external signals, e.g., the EMT-inducing signal TGF-beta, that can directly regulate EMT and subsequentially regulate metabolism. Our model helps reconcile the paradoxical observations regarding the coupling of EMT states with metabolism states, e.g., the fact that E/M states can be associated with both high glycolysis/low OXPHOS (the W state) and high glycolysis/high OXPHOS (the W/O state) [69].

In addition to a general analysis of the coupling between different metabolism and EMT, we specifically focus on the coupling of two hybrid states – hybrid E/M and hybrid W/O. These two hybrid states have both been reported to be associated with elevated metastatic potentials, which leads to the conjecture if these two hybrid states are coupled, cancer cells acquire flexibility in both EMT and metabolism and can thereby maximize their overall aggressiveness. If this conjecture holds, deciphering the cross-talk that stabilizes the coupled hybrid-hybrid state can indicate critical targets for anti-metastasis therapies. We found that (1) a single cross-talk mediated by miR-34 or miR-200 is enough to stablize the E/M-W/O state; (2) the PSFs (OVOL, GRHL2) that have been shown to stabilize the hybrid E/M state also stabilize the coupled E/M-W/O state. feature we identified a scenario wherein can ingthen ning and finally singinitial significantly possibleTogether, the results highlight the important role of the EMT-metabolism cross-talk in mediating cancer metastasis.

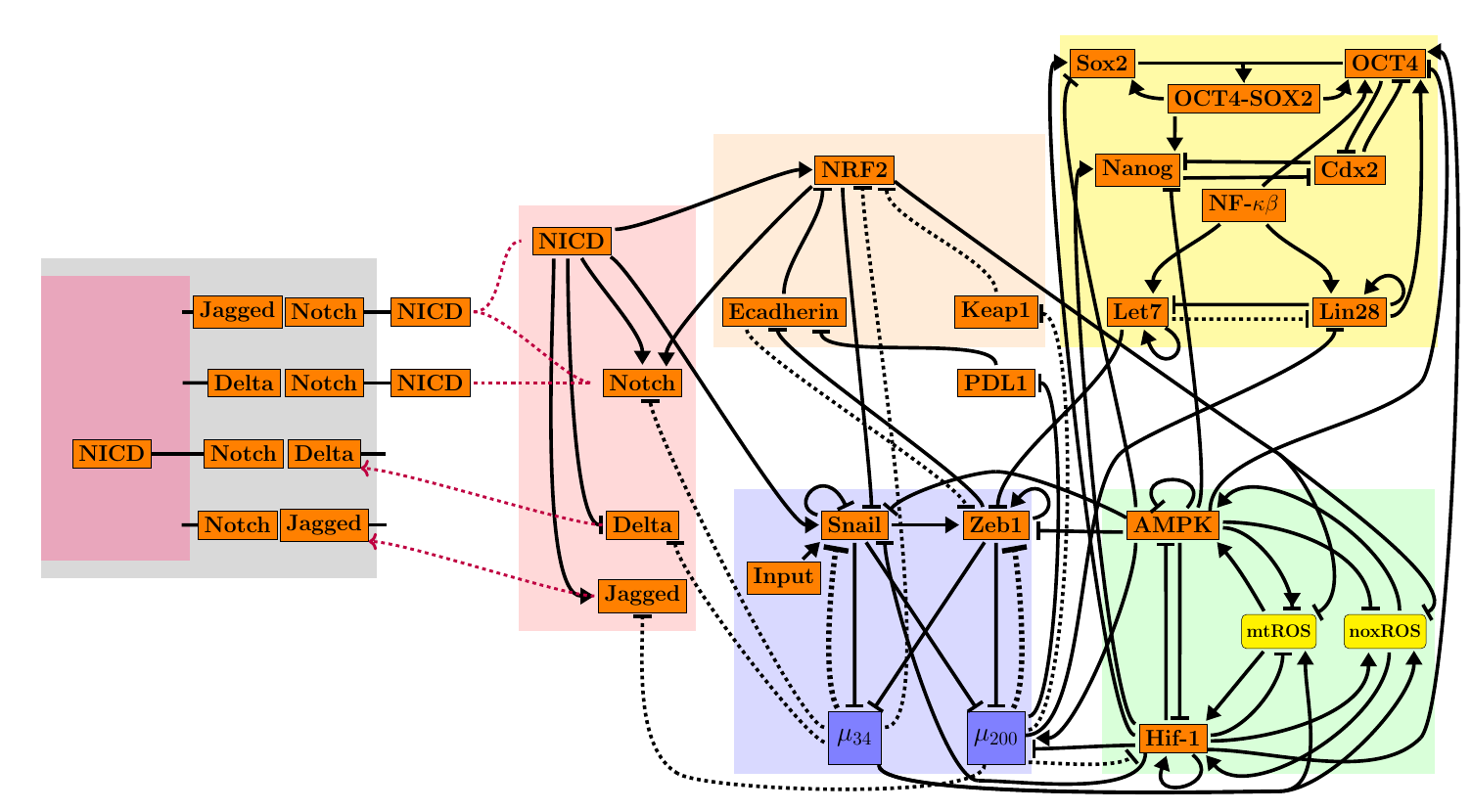
Our findings indicate that all else being equal, undergoing EMT tends to correlate with using additional glycolysis.(Madeline, which of our results support this? Please clarify) Our result is consistent with a recent pan-cancer study based on TCGA (TCGA? Please clarify) and in agreement with other studies [29] [69] (Please elaborate “other studies”). The result is somewhat surprising given the widespread impression that primary tumors often exhibit the Warburg effect, possibly because of their need to limit the amount of ATP produced in favor of maximizing biomass production and growth (see [77] and references therein). However, this finding is consistent with the general idea that moving from E to E/M is connected with increasing stemness, and stem-like capabilities often rely on glycolysis. It is also consistent with HIF-1 activation diminishing OXPHOS while driving EMT. Note that this tendency might be over-ridden for cells that actually have to have sufficient energy production to enable motility, such as leader cells. One possibility is that the basic Warburg effect corresponds to the transition between E-O to E-W/O when cells first become malignant and then as the cells undergo EMT they tend to switch to more and more W until reaching a mesenchymal-like E/M state with mostly W. Then as cells become even more mesenchymal and fully differentiated, they revert back to using mostly OXPHOS. Resolution of this issue must await a more precise idea of the phrase ‘all else being equal”. We have only considered EMT-inducing signals that act on SNAIL and ignored other external signals in this study. For example, the connection between EMT and metabolism also could depend on details of the TME such as the level of oxygen. Mesenchymal cells that reduce proliferation and have to traverse the ECM should switch to more OXPHOS, whereas ones that become quiescent in a hypoxic metastatic niche should favor glycolysis. Notably, in its current form, our model is unable to explain the cases wherein low glycolysis metabolism is correlated with EMT. However, extending the model to explicitly include the coupling with the metabolic pathways [80] may be able to explain the low glycolysis states of Ref. [69].

One important metabolic regulator of EMT emerges from our analysis is ROS. Our results suggest that ROS is critical for the metabolic activation of EMT. (Please use 1-2 sentences summarize our modeling results of ROS on the coupling, we may not need to distinguish mtROS from noxROS). In agreement with our results, recent experimental work has posited that ROS can drive EMT [72], and control cancer invasiveness [73,74]. Another important regulator of both metabolism and EMT is HIF-1. It is generally accepted that HIF-1 is a master regulator of glycolysis [22] and EMT [9]. Our results suggest the mtROS/HIF-1 axis is critical to stabilize the highly aggressive coupled E/M-W/O state. The connection between the mtROS/HIF-1 axis and cancer aggressiveness has also been indicated [75] (What is the connection? Please clarify). Additionally, both mtROS and HIF-1 are controlled by the miRNAs of the EMT network, and , confirming the importance of miRNAs in mediating the coupling of EMT and metabolism [76].

While we have tried to ensure our parameters are within biologically relevant ranges (utilizing values from literature whenever available), one limitation of this study is knowing how these results are translatable to experimental cancer studies. For example, the significance of the mtROS/HIF-1 feedback loop should be experimentally tested by e.g., modulating ROS level via antioxidant factors such as NRF2, or modulating hypoxia to perturb HIF-1. Overall, the importance of external signaling in our model is in conceptual agreement with a hypothesis by Sciacovelli and Frezza that, in an adverse tumor microenvironment, metabolic reprogramming drives EMT to allow cells to find more favorable metabolic niches [42].

In line with the above, this work is merely a first step, and it is quite likely that incorporating additional pathways especially the ones that regulate cell motility, may be necessary to improve our understanding of EMT-metabolism coupling. Previous work has shown that cancer cells can transition from collective migration of E/M cells to individual migration via amoeboid cells, via the regulation of the RHO-ROCK signaling network [9,81]. Inclusion of the RHO-ROCK signaling could provide a detailed understanding of how metabolism is coupled to different modes of cancer cell migration.

The overall goal of this project is toward understanding all the inter-related apects of cancer metastasis. Previous studies coupling EMT, stemness, with Notch signaling have shown that therapy resistance and increased metastatic potential are associated with stem-like hybrid E/M cells [85–87]. Furthermore, these couplings also resulted in unexpected behaviors such as the co-localization of hybrid E/M cells [85] and a tunable stemness window [86]. Studying individual gene regulatory network modules, even in the presence of signals, is unable to give a thorough understanding of the network properties. Therefore, to understand how various cancer traits are correlated, and potentially identify key regulators, multiple network modules and their crosstalk should be studied concurrently.



**Figure 10: The coupled networks of cancer metastasis.** Here we include the core EMT circuit, metabolism circuit, stemness circuit, KEAP1-NRF2 pathway, Notch signaling pathway, and the immune system biomarker PDL1. The crosstalk identified here may provide a novel set of cancer phenotypes and targets. (Please add name to each module in the figure, metabolism, EMT, immune response etc.)

**Acknowledgements**

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