

# Polynomial from Roots (Assignment)

## ■ Problem Statement

We are given polynomial roots in **JSON format**, where each root is expressed in a specific base (binary, octal, decimal, hexadecimal, etc.).

The task is to:

1. Parse the JSON input.
2. Convert each root into a **decimal integer**.
3. Use exactly **k roots** (where  $k = \text{degree} + 1$ ) to form the polynomial.
4. Expand the polynomial into standard form:

$$P(x) = a_m x^m + a_{m-1} x^{m-1} + \dots + a_0$$

5. Output the coefficients  $[a_m, a_{m-1}, \dots, a_0]$ .

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## ■■ Approach

1. **Parse JSON Input**
  - Extract  $n$  (total roots given) and  $k$  (minimum required).
  - Collect the first  $k$  roots.
2. **Convert Roots**
  - Each root has a "base" and "value".
  - Convert to decimal using base conversion.

Example:

"2": { "base": "2", "value": "111" }

→ Decimal = 7.

3. **Form Polynomial**
  - Build polynomial as:  
 $(x - r_1)(x - r_2)\dots(x - r_k)$
4. **Expand Polynomial**
  - Multiply step by step to compute coefficients.
  - Handle large numbers using BigInteger (Java) or equivalent.
5. **Output**
  - Print coefficients as a list.

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## ■■ Example

### *Input*

```
{  
  "keys": {  
    "n": 4,  
    "k": 3  
  },  
  "1": {  
    "base": "10",  
    "value": "4"  
  },  
  "2": {  
    "base": "2",  
    "value": "111"  
  },  
  "3": {  
    "base": "10",  
    "value": "12"  
  },  
  "6": {  
    "base": "4",  
    "value": "213"  
  }  
}
```

### *Conversion*

- Root 1: 4
- Root 2: 7
- Root 3: 12

### *Polynomial*

$$(x - 4)(x - 7)(x - 12) = x^3 - 23x^2 + 160x - 336$$

## ***Output***

[1, -23, 160, -336]

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## **■ How to Run**

1. Clone the repo:

```
git clone https://github.com/username/repo-name.git
cd repo-name
```

2. Compile and run (Java example):

```
javac PolynomialFromRoots.java
java PolynomialFromRoots input.json
```

3. The program will print polynomial coefficients.

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## **■ Repository Structure**

repo-name

- PolynomialFromRoots.java # Main source code
- input.json # Sample test case input
- README.md # Project documentation
- output.txt # Output from program

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## **■ Deliverables**

- Source code implementation.
- Sample input JSON.
- Output file/screenshot.
- README with explanation.