

# Ques: GCD of 2 numbers

$a$  &  $b$

for loop se dono ka HCF nikalo.

12 , 16

↓

4

12 → 1, 2, 3, 4, 6, 12

16 → 1, 2, 4, 8, 16

# Ques: GCD of 2 numbers

$$\begin{array}{r}
 24 \overline{) 60} \\
 \underline{48} \\
 12
 \end{array}
 \quad
 \begin{array}{r}
 24 \overline{) 12} \\
 \underline{24} \\
 0
 \end{array}$$

$$\begin{array}{r}
 13 \overline{) 41} \\
 \underline{39} \\
 2
 \end{array}
 \quad
 \begin{array}{r}
 13 \overline{) 2} \\
 \underline{13} \\
 1
 \end{array}
 \quad
 \begin{array}{r}
 2 \overline{) 1} \\
 \underline{2} \\
 0
 \end{array}$$

$$\begin{array}{cc}
 a & b \\
 \downarrow & \downarrow \\
 b \% a & a
 \end{array}$$

# Ques: GCD of 2 numbers

$$\begin{array}{r}
 29 \overline{) 41} \\
 \underline{29} \phantom{0} \\
 12
 \end{array}
 \begin{array}{r}
 2 \\
 29 \overline{) 29} \\
 \underline{29} \\
 0
 \end{array}
 \begin{array}{r}
 2 \\
 5 \overline{) 12} \\
 \underline{10} \\
 2
 \end{array}
 \begin{array}{r}
 2 \\
 2 \overline{) 5} \\
 \underline{4} \\
 1
 \end{array}
 \begin{array}{r}
 2 \\
 2 \overline{) 2} \\
 \underline{2} \\
 0
 \end{array}
 \begin{array}{r}
 2 \\
 2 \overline{) 2} \\
 \underline{2} \\
 0
 \end{array}
 \begin{array}{r}
 2 \\
 2 \overline{) 2} \\
 \underline{2} \\
 0
 \end{array}$$

$$hcf(a, b) = hcf(b \% a, a)$$

$$gcd(29, 41) \rightarrow gcd(12, 29)$$



**Ques:** GCD of 2 numbers

$$\begin{aligned} \gcd(41, 24) &\rightarrow \gcd(24 \% 41, 41) \\ &\quad \gcd(24, 41) \end{aligned}$$

$$[a \% b = a \text{ (if } a < b)]$$

$$\text{lcm}(a, b) = \frac{a * b}{\gcd(a, b)}$$

$O(\log(\min(a, b)))$

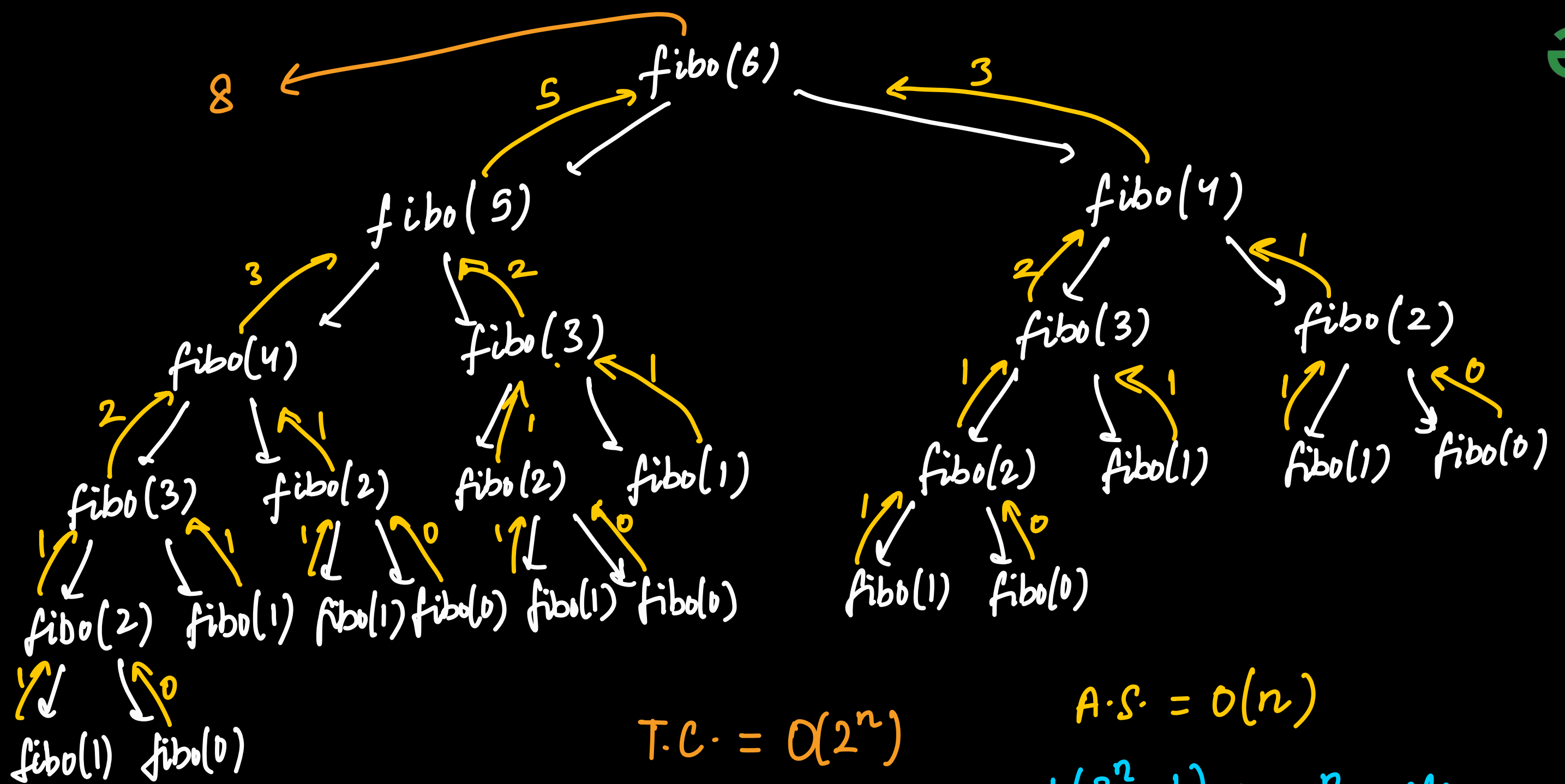
# Ques: nth Fibonacci Number

0	1	1	2	3	5	8	13	21	34	55	89	.	.
0	1	2	3	4	5	6	7	8	9	10	11		

```

int fibo(n){
    if(n <= 1) return n;
    return fibo(n-1) + fibo(n-2);
}

```

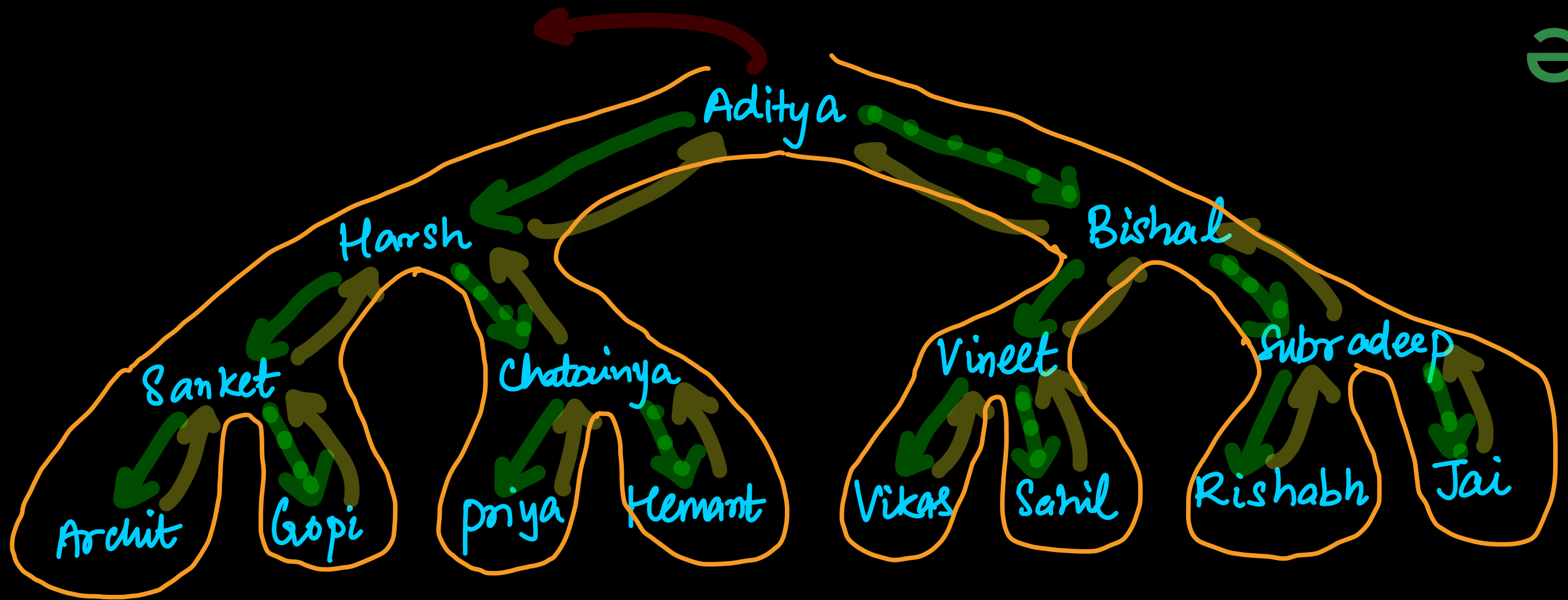


$$T.C. = O(2^n)$$

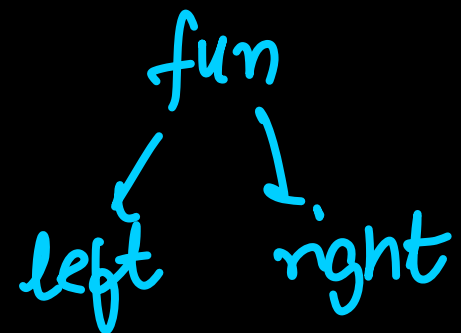
$$A.S. = O(n)$$

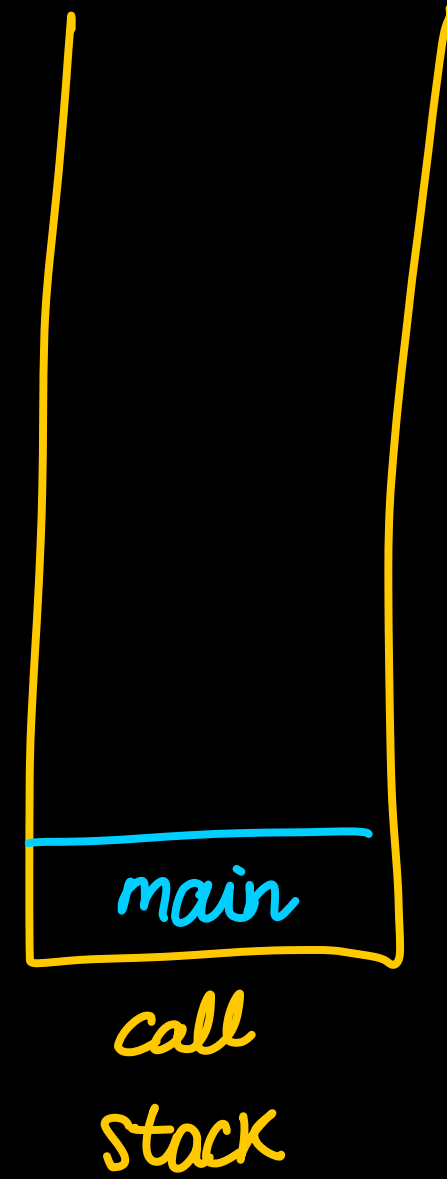
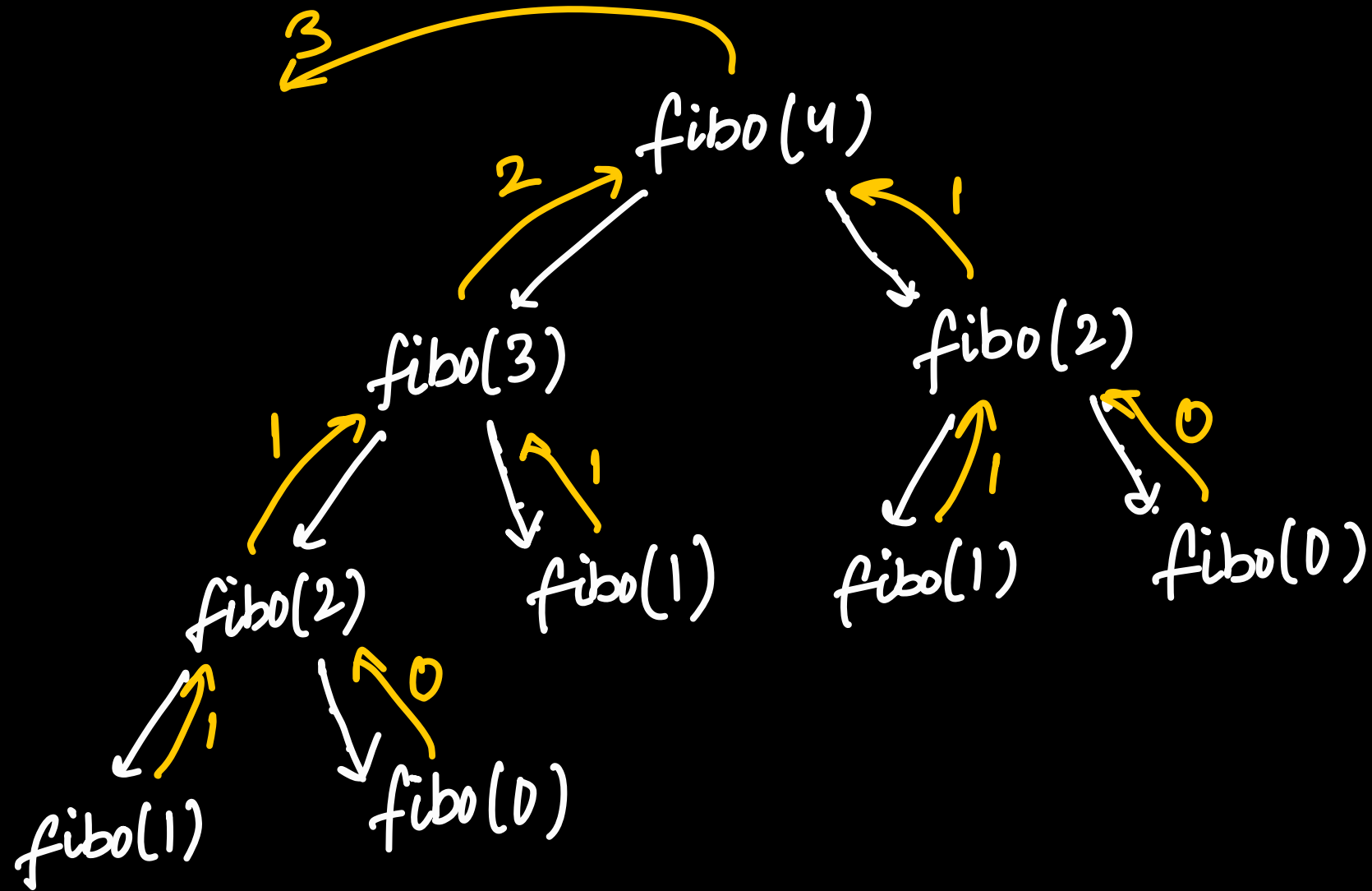
$$\underbrace{1 + 2 + 4 + 8 + 16 + \dots}_{n \text{ terms}}$$

$$\rightarrow \frac{1(2^n - 1)}{2 - 1} \approx 2^n \text{ calls}$$



Euler's Tour Tree



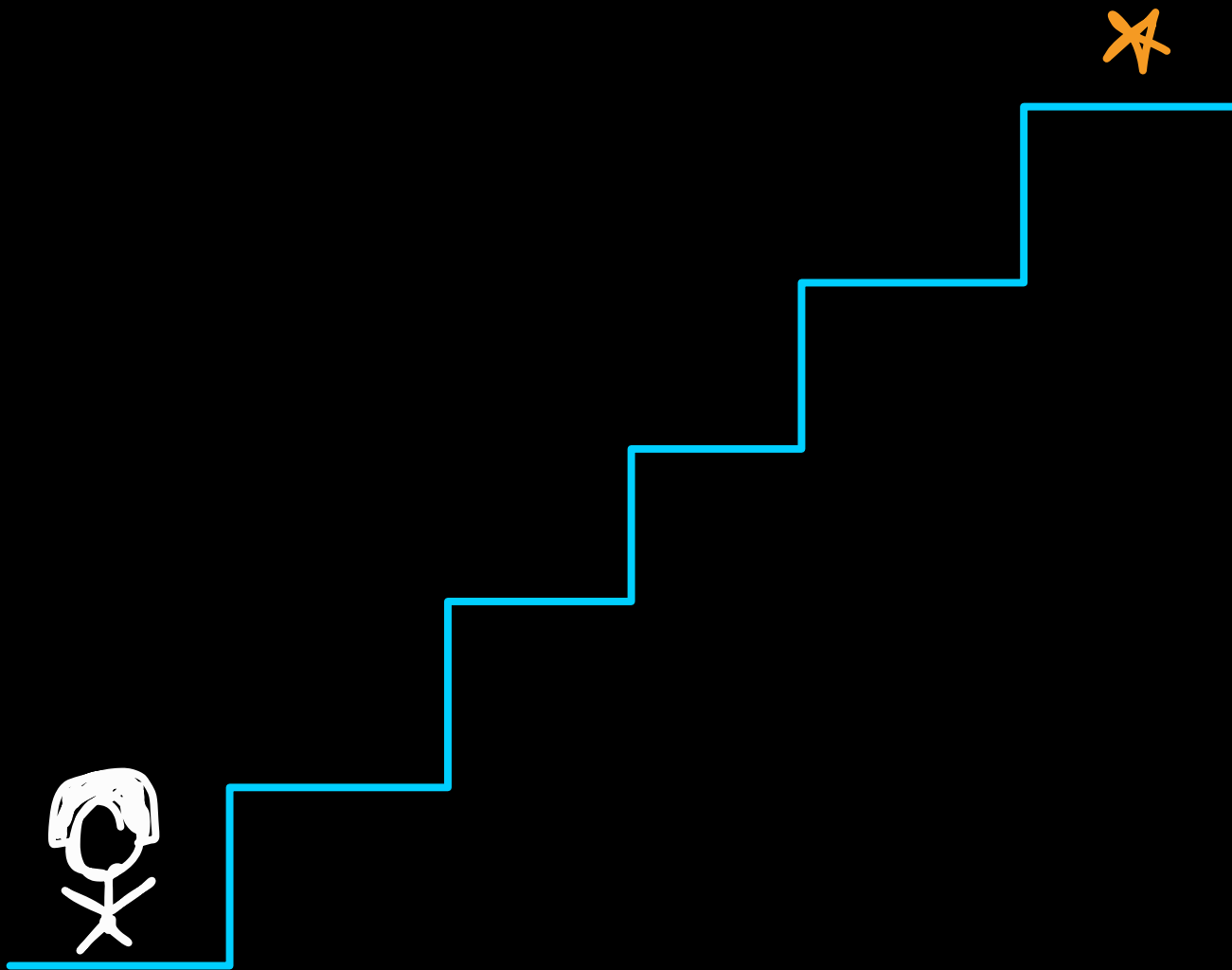




**Ques:** Ways to reach the n'th stair (Max 2 jumps)



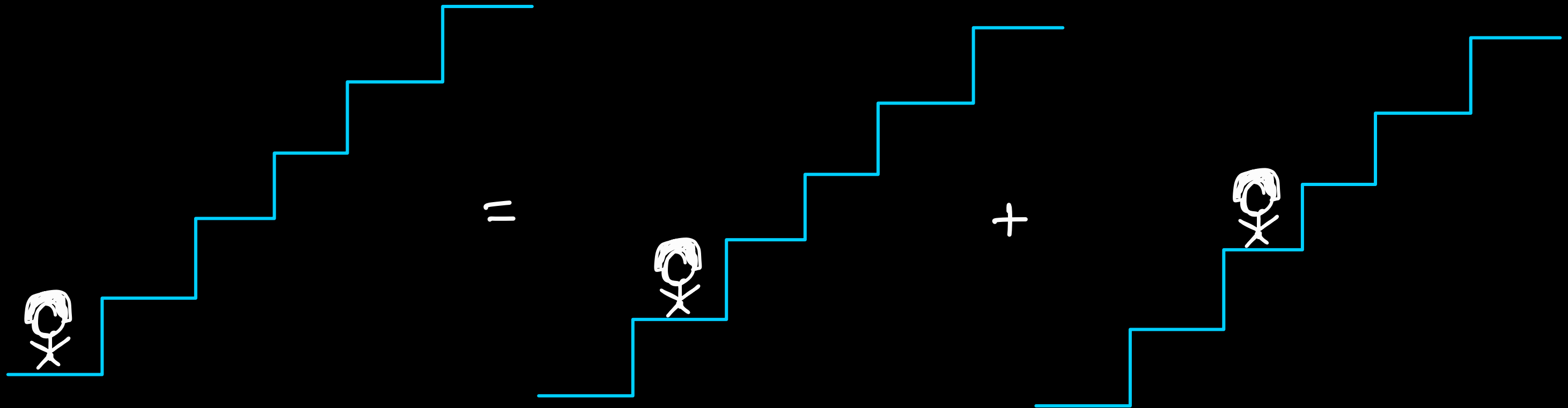
$n = 5$



1 1 1 1 1  
1 1 1 2  
1 1 2 1  
1 2 1 1  
1 2 2  
2 1 1 1  
2 1 2  
2 2 1

8 ways

# Ques: Ways to reach the n'th stair



$$\text{stair}(n) = \text{stair}(n-1) + \text{stair}(n-2)$$

$$\text{stair}(1) = 1, \text{stair}(2) = 2$$