UNIT I ELECTRONIC MATERIALS

INTRODUCTION

Materials can be broadly classified into three types based on conductivity. They are,

- 1. Conductors (Example: metals),
- 2. Semi conductors (Example: germanium, silicon) and
- 3. Insulators (Example: wood, mica, glass).

CONDUCTORS:

- Conductivity is the ability or power to conduct or transmit heat, electricity, or sound.
- Conductors are materials that electricity easily passes through, that do not resist the flow of electricity.
- Examples are copper, aluminum, steel, silver, gold, electrolytes. Not all materials conduct electricity equally well.

CLASSIFICATION OF CONDUCTORS:

Conducting materials are classified into three categories

1. Zero Resistivity materials:

These materials conduct electricity with zero resistance below transition temperature.

2. Low Resistivity materials:

These materials have very high electrical conductivity.

3. High Resistivity materials:

These materials have high resistivity and low temperature co-efficient of resistance.

Basic Terminologies

1. Bound Electrons:

All the valence electrons in an isolated atom are bound to their parent nuclei are called as bound electrons.

2. Free electrons:

Electrons which moves freely or randomly in all directions in the absence of external field.

3. Drift Velocity

If no electric field is applied on a conductor, the free electrons move in random directions. They collide with each other and also with the positive ions. Since the motion is completely random, average velocity in any direction is zero. If a constant electric field is established inside a conductor, the electrons experience a force F = -eE due to which they move in the direction opposite to direction of the field. These electrons undergo frequent collisions with positive ions. In each such collision, direction of motion of electrons undergoes random changes. As a result, in addition to the random motion, the electrons are subjected to a very slow directional motion. This motion is called drift and the average velocity of this motion is called **drift velocity vd.**

4. Electric Field (E):

The electric field E of a conductor having uniform cross section is defined as the potential drop (V) per unit length (l).

i.e.,
$$E = V/1 V/m$$

5. Current density (J):

It is defined as the current per unit area of cross section of an imaginary plane holded normal to the direction of the flow of current in a current carrying conductor.

$$J = I/A Am-2$$

6. Fermi level

Fermi level is the highest filled energy level at 0 K.

7. Fermi energy

Energy corresponding to Fermi level is known as Fermi energy.

Electron Theory of metals:

The electron theory of metals explain the following concepts

- → Structural, electrical and thermal properties of materials.
- → Elasticity, cohesive force and binding in solids.
- → Behaviour of conductors, semi conductors, insulators etc.

So far three electron theories have been proposed.

1. Classical Free electron theory:

- It is a macroscopic theory.
- Proposed by Drude and Loretz in 1900.
- It explains the free electrons in lattice

- It obeys the laws of classical mechanics.

2. Quantum Free electron theory:

- It is a microscopic theory.
- Proposed by Sommerfield in 1928.
- It explains that the electrons moves in a constant potential.
- It obeys the Quantum laws.

3. Brillouin Zone theory or Band theory:

- Proposed by Bloch in 1928.
- It explains that the electrons moves in a periodic potential.
- It also explains the mechanism of semiconductivity,
 based on bands and hence called band theory.

CLASSICAL FREE ELECTRON THEORY OF METALS:

This theory was developed by Drude and Lorentz during 1900 All the atoms are composed of and hence is also known as Drude-Lorentz theory. According to this theory, a metal consists of electrons which are free to move about in the crystal like molecules of a gas in a container. Mutual repulsion between electrons is ignored and hence potential energy is taken as zero. Therefore the total energy of the electron is equal to its kinetic energy.

Postulates of Classical free electron theory:

- 1. All the atoms are composed of atoms. Each atom have central nucleus around which there are revolving electrons.
- **2.** The electrons are free to move in all possible directions about the whole volume of metals.
- **3.** In the absence of an electric field the electrons move in random directions making collisions from time to time with positive ions which are fixed in the lattice or other free electrons. All the collisions are elastic i.e.; no loss of energy.
- **4.** When an external field is applied the free electrons are slowly drifting towards the positive potential.
- **5.** Since the electrons are assumed to be a perfect gas they obey classical kinetic theory of gasses.
- **6.** Classical free electrons in the metal obey Maxwell-Boltzmann statistics.

Drawbacks of Classical free electron theory:

- 1) According to this theory, r is proportional to ÖT. But experimentally it was found that r is proportional to T.
 - 2) According to this theory, K/sT = L, a constant (Wiedemann-Franz law) for all temperatures. But this is not true at low temperatures.
 - 3) The theoretically predicted value of specific heat of a metal does not agree with the experimentally obtained value.

- 4) This theory fails to explain ferromagnetism, superconductivity, photoelectric effect, Compton Effect and black body radiation.
- 5) It is a macroscopic theory.
- 6) Dual nature is not explained.
- 7) Atomic fine spectra could not be accounted.

Merits of Classical Free Eletron Theory:

- 1. It is used to verify Ohm's law.
- 2. The electrical and thermal conductivities of metals can be explained.
- **3.** It is used to derive Wiedemann- Franz law
- **4.** It is used to explain the optical properties of metals.

Drawbacks of Classical Free Electron Theory:

- 1. It is a macroscopic theory.
- 2. It cannot explain the electrical conductivity of semiconductors and insulators properly.
- **3.** Dual nature is not explained.
- **4.** It cannot explain the Compton effect, Photo-electric effect.
- **5.** The theoritical and experimental values of specific heat are not matched.
- **6.** Atomic fine spectra could not be accounted.

7. Different types of magnetisms could not be explained satisfactorily by this theory.

Wiedmann-Franz law:

The ratio of thermal conductivity to electrical conductivity of a metal is directly proportional to absolute temperature.

K/s is proportional to T Or, K/sT = L, a constant called Lorentz number.

Quantum free electron theory:

- Classical free electron theory could not explain many physical properties.
- ➤ In 1928, Sommerfeld developed a new theory applying quantum mechanical concepts and Fermi-Dirac statistics to the free electrons in the metal. This theory is called quantum free electron theory.
- Classical free electron theory permits all electrons to gain energy. But quantum free electron theory permits only a fraction of electrons to gain energ

Description of Electrical Conductivity of a metal based on Described theory.

Consider a metal piece of length 'L' and area of cross-section A'. An electric field 'L' is applied to the metal piece.

The state of the s

The electrons are accelerated with a drift velocity Vd in a direction opposite to that of the applied field. Due to this field, the force experienced by the electrons can

be given as, F=eE --- w

where, $e \rightarrow charge$ of an electron $E \rightarrow applied$ electric field

From Newton's Second law of motion,

F = ma - - - - - - - (2)

is a -> acceleration

m -> mass of the electron.

Equating (1) \$ (2),

 $\ell E = ma \frac{33n}{m}$

: a = ef/m - - - - (3)

We know acceleration in terms of drift velocity and relaxation tone is given as, acceleration = duft Velocity Vd

selaxation tone T $a = \frac{\sqrt{a}}{T}$ equating eqn (3) and (4), er/m = Va $V_d = \frac{eET}{m}$ We know, Current density, J = 5-E - - - - - - (b) Current density in terms of dreft velocity is given as J = ne Vd - - - - (7) Substituting equ (3) in equ (7) $J = ne \frac{eEE}{m}$ $= \frac{ne^{\varphi}E\overline{b}}{m}$ $\sqrt{\frac{1}{E}} = \frac{ne^{\varphi}\overline{b}}{m} \qquad (8)$

We know the exputsion for electrical Conductivity.

: Ego (8) is the equation for electrical Conductivity

from this equation. We can fond that with increase of election Concentration in, the conductivity of increases. As m' increases, the motion of election becomes slow and hence the conductivity of decreases.

Verification of Ohm's law:

We know that, the Current Density, 9 = 1/1.

$$\mathcal{J} = \sigma \mathcal{E} A \qquad \left(\begin{array}{c} \cdot \cdot \cdot \cdot \mathcal{J} = \sigma \mathcal{E} \end{array} \right)$$

$$= \sigma - (\frac{V_{1}}{I})A \qquad \left(\cdots F \cdot \frac{V_{1}}{I} \right)$$

$$= \left(\frac{\sigma - A}{I} \right) V$$

$$= \left(\frac{A}{eI}\right)V \qquad \left(\frac{A}{eI}\right)$$

At part A!

: - Ohm's law is Verified.

Derivation of Thermal conductivity:

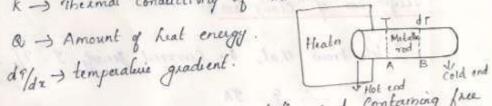
Desiration of Thermal Conductivity (k):

Thermal conductivity of a metal is defined as The amount of heat (a) conducted per unit time (t) through the material having unit area of cross section (A) maintaining at unit temperature gradient (d9/dx).

$$k = \frac{-\alpha}{d^{q}/dx}$$

. Q = - K. de/dx Wim k-1.

k -> Thermal conductivity of material.



Consider a uniform metallic sod Containing free elections. One end of the rod is healed using a healer. Let A and B be the two cross. Actions of temperature T and (T-dT) Separated by a distance of mean free pot (A). Fleat (Cows from hot end A' to the cold end B'

During the collision, the elections near A lose their Kinetic energy and the elections near B gain the energy. At point A:

Average kindle energy of election = 1/2 mv = 3/2 kg (0 ---- Olmi fee a Very of When, k -> Bollgmann's Constant

P -> Pemperature at A

At Point B:

Hence the Excess kinetic energy carried out by election from

A to B.

= 3/2 k7 - 3/2 k(7-d7)

= 3/2 k9 - 3/2 k9 + 3/2 kd9

116) = 3/2 k d9 - ---- (3)

Let us assume that the electrons will flow in all 6 directions with equal probability. If in is the free electron density and v is the thermal velocity, number of electrons carrying unit area per unit time from A to B = 1/2 TV --- (1)

Excess of energy carried from A to & for unit area in unit time - 1/2 nv x 3/2 kd7

= 1/4 nvkd9 ---- (5)

Illy, the deficiency of energy carried from B to A for unit area in unit time = -1/4 nv kd? ... (6) Hence, the net energy hansferred from A to B per unit area per unit time, Q = 1/4 nv kd? - [-1/4 nv kd?]

: Q = 1/2 nv kdp We know, Thermal Conductivity, Q = K [dr] [: dx = d] By compairing eqn (7) and eqn (0), k [d%] = 1/2 DV Kd9 Fox metals, relexation time (I) = Collesion time (Te) : T = Tc = 2/2 Substituting eqn. (10) in (9) ∴ k = ½ nvktv k = 1/2 ny kt (10) Egn (11) is the classical expression for thermal conductivity. Wiedemann - Frang Law : The Ratio between the thermal conductivity and The electrical conductively of a metal is desectly proportional to the absolute temperature of the metal.

The ratio is constant for all metals in a given ling.

Substituting egn (5) in egn (4),

$$\frac{k}{e} = \frac{3}{3} \frac{k!}{e^2}$$

$$= \frac{3}{2} \frac{k!}{e^2}$$

$$= \frac{3}{2} (\frac{k}{e})^2 \qquad (6)$$

When, L = 3/2 (K/e) is a Constant and it is known as Lorentz Number.

Loxentz - Number:

The sales between the thermal conductivity (k) to be product of electerical conductivity (o) and absolute temperature (P) of the metal is a constant. The constant value is known as Lorentz number.

Lorenty Number (1) = K

According to classical theory.

Substituting, k = 1.38 x 10 3 9 k , e = 1.6021 x 10 9 Coulomb

- Blog . John . .

$$L = \frac{3}{4} \left(\frac{1.88 \times 10^{-43}}{1.60 \times 10^{19}} \right)^{2}$$

L = 1.112 x 10 W SL K?

Hence it was found that he classical value of Loverty number is only half of he experimental value if $L = 2.24 \times 10^8 \, \text{W.D.k.}$. This discrepancy in the experimental and theoretical value of Lovertz number is he failure of classical theory.

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Fermi-Dirac Statistics:

There are three statistics

- 1. Maxwell- Boltzmann statistics
- Deals with particles which has no spin
 - Eg: Gaseous particles
 - 2. Bose-Einstein statistics
- Deals with particles which has integral spin
 - Eg: Photons
 - 3. Fermi-Dirac statistics
 - Deals with particles which has half integral spin
 - Also known as Fermions
 - Eg: Electrons

Fermi - Duac Statisties Distribution function:

to calculate the probability of an electron occupying a certain energy livel.

* The distribution of electrons among the different energy levels as a function of temperature is known as fermi-Dirac distribution function.

$$F(E) = \frac{1}{1 + \exp\left((E - E_F)/k^q\right)}$$

Where,

Ef - fermi enegy

k -> Boltzmann Constant

7 -> Pemperalure in k.

The probability value F(F) lies between 0 and 1

-> If F(F)=1, the energy level is occupied by an electron

-> If F(F) =0, the energy level is vacant

→ If F(F) = 0.5 or 1/2, then there is a 50% chance for funding the electron in the energy level.

Effect of Pemperature on Fermi function:

in At P= OK

At Ok, the electrons are filled upto a maximum

energy level called fermi Energy level ff. All the energy level are empty.

Case in: At 9= ok and Exeq

$$F(F) = \frac{1}{1 + \overline{e}^{\infty}} = \frac{1}{1} = 1$$

level between Fermi energy level is 100%.

Case (in): At 9=0k and E>Ef.

$$F(E) = \frac{1}{1+e^{i\phi}} = \frac{1}{1+i\phi} = 0$$

This means that at 0 k, electrons are completely occupied below 'ff' and above 'ky electrons are unoccupied.

Case (iii): Af T= OK and f= Fg

$$F(E) = \frac{1}{1+1} = \frac{1}{2} = 0.5$$

The fermi-function at Ok Can also be graphically-

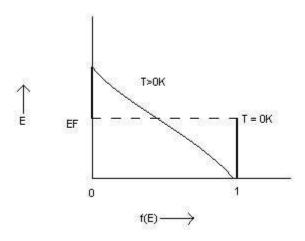
Electrons with formi energy move with fermi velicity and the same is related to he fermi temperature by the Relation,

1/2 m Vf = k9.

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Effect of temperature on Fermi-Dirac distribution function:

Fermi-Dirac distribution function is given by, f(E) = 1 / [1 + e(E - EF/KT)]At T=0K, for EEF, f(E)=0
At T=0K, for E=EF, f(E)=indeterminate
At T>0K, for E=EF, f(E)=1/2
All these results are depicted in the figure.



Importance of Fermi Energy:

- ◆ Fermi energy is used to seperate the vacant and filled states at
- 0 K
 - ◆ It is used to know the status of the electrons.

- ◆ Electrons are completely filled below fermi energy level and completely empty above the fermi level at 0 K
- ◆ Above 0 K some electrons absorb thermal energy and they jumps to the higher energy levels.

Density of States:

Density of states N(E)dE is defined as the number of energy states present per unit volume of a metal in an energy interval E and E+dE

No. of energy states available between E and E+dE in a metal piece

Density of states [N(E)dE] = -Volume of that metal piece

Desivation of Density of States (NCE) dE):

Figure shows a graph between number of States (NCE)) and energy (E). To fell the electrons in energy level, we must know the number of states present within he energy interval E and E+dE

Let us calculate the density of States in a cubical metal piece with bides a. Let $n_{\rm pl}$, $n_{\rm pl}$ and $n_{\rm pl}$ be the Coordinate axes. Draw the Sphere in these $E \rightarrow a_{\rm pl}$ with radius $n = n_{\rm pl}^2 + n_{\rm pl}^2 + n_{\rm pl}^2$ and Energy E.

Any change in na , my , ng will change E and hence the

The number of energy states within a sphere of radius is

$$n = \frac{1}{8} \left(\frac{4}{3} \sqrt{3} n^3 \right) - \dots = 0$$

: Number of available energy state between

=
$$\frac{1}{8} \left(\frac{4\pi}{3} \right) \left((n+dn)^3 - (n)^3 \right)$$

$$= \frac{18 \left[\frac{10}{3} \right] \left(n^3 + dn^3 + 3 n^3 dn + 3 n dn^4 - n^2 \right)}{8 \left[\frac{10}{3} \right] \left(n^3 + dn^3 + 3 n^3 dn + 3 n dn^4 - n^2 \right)}$$

Desivation of Density of States (NEE) dE):

Figure shows a graph between number of states (NCE) and energy (E). To fell the electrons in energy level, we must know the number of states present within he energy interval E and E+dE

Let us calculate the density of States in a cubical metal piece with bides a, Let n_x , n_y and n_g be the Coordinate axes. Draw the sphere in these $E \rightarrow$ axes with radius $n = n_x^2 + n_y^2 + n_z^2$ and Energy E.

Any change in na, my, ng will change & and hince the

The number of energy states wis

$$n = \frac{1}{8} \left[\frac{4}{3} \pi n^3 \right] - \cdots 0$$

. Number of available energy state between

It sphere of radius " and not on the " of Z(E) dE = 1/8 [41/3] (n+dn) - 1/8 [41/3] n3

= 1/8 [41/3] (n3+dn3+3n3 dn+3ndn4-n3)

$$= \frac{\pi}{4} \left(\frac{8ma^{2}}{K^{2}} \right)^{\frac{1}{2}} \left(\frac{8ma^{2}}{K^{2}} \right) E^{\frac{1}{2}} dE$$

$$= \frac{\pi}{4} \left(\frac{8ma^{2}}{K^{2}} \right)^{\frac{3}{2}} E^{\frac{1}{2}} dE$$

$$= \frac{\pi}{4} \left(\frac{8m}{K^{2}} \right)^{\frac{3}{2}} a^{\frac{3}{2}} E^{\frac{1}{2}} dE$$

The dinsity of States is equal to the number of states per unit volume in the range E and R+dE

$$4i N(E) dE = \frac{Z(E) dE}{V}$$

$$= \sqrt[3]{4} \left(\frac{8m}{R^2} \right)^{3/2} E^{1/3} dE - ... (7)$$

According to Pauli's exclusion principle, in each state two electrons can accompidate.

Density of States (NCE) dE) = \(\hat{\chi} \) (8m) 3/3 E to dE - (8)

$$= \frac{\pi}{4} \cdot \frac{1}{2} \left(\frac{8ma'}{h^2} \right)^{\frac{1}{2}} \left(\frac{8ma'}{h^2} \right) e^{\frac{1}{2}} dE$$

$$= \frac{\pi}{4} \left(\frac{8ma'}{h^2} \right)^{\frac{3}{2}} e^{\frac{1}{2}} dE$$

$$= \frac{\pi}{4} \left(\frac{8m}{h^2} \right)^{\frac{3}{2}} a^{\frac{3}{2}} e^{\frac{1}{2}} dE$$

$$= \frac{\pi}{4} \left(\frac{8m}{h^2} \right)^{\frac{3}{2}} a^{\frac{3}{2}} e^{\frac{1}{2}} dE$$

$$= \frac{\pi}{4} \left(\frac{8m}{h^2} \right)^{\frac{3}{2}} V e^{\frac{1}{2}} dE$$

$$= \frac{\pi}{4} \left(\frac{8m}{h^2} \right)^{\frac{3}{2}} V e^{\frac{1}{2}} dE$$

The dinsity of states is equal to the number of states

per unit volume in the range E and E+dE

$$i N(E) dE = \frac{Z(E) dE}{V}$$

$$= \sqrt[3]{4} \left(\frac{8m}{k^2} \right)^{3/2} E^{1/2} dE - ... (7)$$

According to Pauli's exclusion principle, in each state two electrons can accomodate.

Jensily of Stales
$$(N(E)dE) = \frac{\lambda}{2k} N(E)dE$$

$$= \frac{\lambda}{2} \left(\frac{8m/k^2}{k^2}\right)^{3/2} E^{1/2} dE$$

$$= \frac{\lambda}{2} \left(\frac{8m/k^2}{k^2}\right)^{3/2} E^{1/2} dE$$

$$= \frac{\lambda}{2k^3} \left(\frac{8m}{k^2}\right)^{3/2} E^{1/2} dE - (8)$$

The above equation represents the Fermi energy of electrons in solids at absolute gero.

When temperature increases, formi energy Eq is related with temperature as

$$E_f = E_{f_0} \left[1 - \frac{\lambda^2}{12} \left(\frac{kq}{E_{f_0}} \right)^3 \right]$$

when, Eto is fermi energy at ok.

Average Energy (Eare) of an Electron at Ok:

Average Energy Eave = Total Energy

Carrier Concentration

Total Energy, Fitot) = Spensity of states x Energy of an electron

$$\frac{F_{f_{0}}}{\int N(E) dE \times E}$$

$$\int \frac{\bar{\Lambda}}{2h^{3}} (8m)^{3/2} E^{3/2} E dE$$

$$- \frac{\bar{\Lambda}}{2h^{3}} (8m)^{3/2} \int E^{3/2} dE$$

Total Energy (Elot) =
$$\frac{\pi}{5h^3}$$
 (8m) $\frac{3/2}{E_{Fo}}$

From egn W,

$$N = \frac{\pi}{3h^3} (8m)^3 E_{f_0}^{3/3}$$

: Average Energy,

$$(E_{ave}) = \frac{\frac{\chi}{5h^3} (8m)^{3/2} E_{F_0}^{5/2}}{\frac{\chi}{3h^3} (8m)^{3/2} E_{F_0}^{5/2}}$$

$$= \frac{3}{5} E_{f_0}^{5/2} E_{f_0}^{-3/2}$$

.. The average energy of an electron at OK