

Draw the following DFA using table filling algorithm where A is the start state and C, F and I are the final states.

$\delta$	0	1
$\rightarrow$ A	B	E
B	*C	*F
*C	D	H
D	E	H
E	*F	*I
*F	G	B
G	H	B
H	*I	*C
*I	A	E

STEP-1: Cross down all the combinations of Final and Non-Final states in the table.

B								
C*	X	X						
D			X					
E			X					
F*	X	X		X	X			
G			X			X		
H			X			X		
I*	X	X		X	X		X	X
	A	B	C*	D	E	F*	G	H

STEP-2: Check all the '0' and '1' input combinations of the non crossed states

	0	1
A	B	E
B	*C	*F

Non-Final – Non-Final  
Final – Final

So, this combination is not possible.

	0	1
A	B	E
D	E	H

Non-Final – Non-Final  
Non-Final – Non-Final

So, this combination is possible.

	0	1
A	B	E
E	*F	*I

Non-Final – Non-Final  
Final – Final

So, this combination is not possible.

	0	1
A	B	E
G	H	B

Non-Final – Non-Final  
Non-Final – Non-Final

So, this combination is possible.

	0	1
A	B	E
H	*I	*C

Non-Final – Non-Final  
Final – Final

So, this combination is not possible.

	0	1
B	*C	*F
D	E	H

Final – Final  
Non-Final – Non-Final

So, this combination is not possible.

	0	1
B	*C	*F
E	*F	*I

Final – Final  
Final – Final

So, this combination is possible.

	0	1
B	*C	*F
G	H	B

Final – Final  
Non-Final – Non-Final

So, this combination is not possible.

	0	1
B	*C	*F
H	*I	*C

Final – Final

Final – Final

So, this combination is possible.

	0	1
*C	D	H
*F	G	B

Non-Final – Non-Final

Non-Final – Non-Final

So, this combination is possible.

	0	1
*C	D	H
*I	A	E

Non-Final – Non-Final

Non-Final – Non-Final

So, this combination is possible.

	0	1
D	E	H
E	*F	*I

Non-Final – Non-Final

Final – Final

So, this combination is not possible.

	0	1
D	E	H
G	H	B

Non-Final – Non-Final

Non-Final – Non-Final

So, this combination is possible.

	0	1
D	E	H
H	*I	*C

Non-Final – Non-Final

Final – Final

So, this combination is not possible.

	0	1
E	*F	*I
G	H	B

Final – Final

Non-Final – Non-Final

So, this combination is not possible.

	0	1
E	*F	*I
H	*I	*C

Final – Final

Final – Final

So, this combination is possible.

	0	1
*F	G	B
*I	A	E

Non-Final – Non-Final

Non-Final – Non-Final

So, this combination is possible

	0	1
G	H	B
H	*I	*C

Non-Final – Non-Final

Final – Final

So, this combination is not possible.

B	X							
C*	X	X						
D		X	X					
E	X		X	X				
F*	X	X		X	X			
G		X	X		X	X		
H	X		X	X		X	X	
I*	X	X		X	X		X	X
	A	B	C*	D	E	F*	G	H

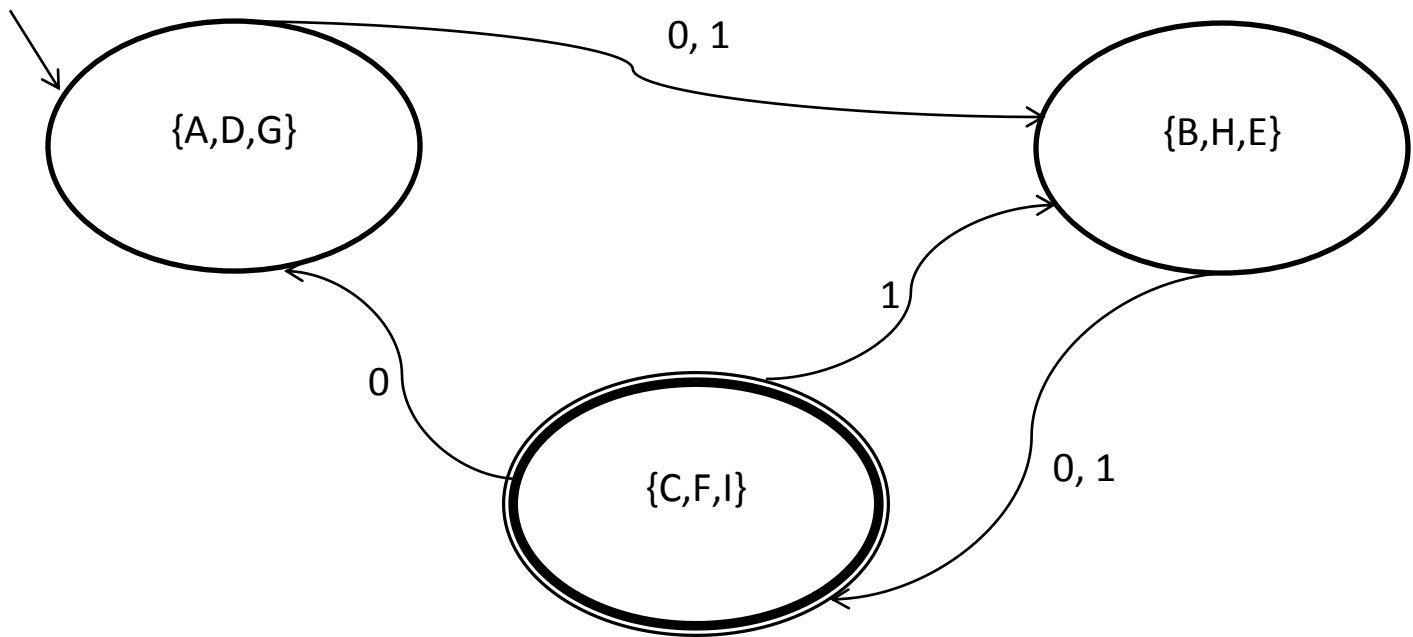
STEP 3: List the remaining pairs

$\{A,D\}, \{A,G\}, \{D,G\} \rightarrow \{A,D,G\}$

$\{B,E\}, \{B,H\}, \{E,H\} \rightarrow \{B,H,E\}$

$\{C,F\}, \{C,I\}, \{F,I\} \rightarrow \{C,F,I\}$

STEP 4: Transition Diagram



Consider the following transition table and minimize the states.

$\delta$	0	1
$\rightarrow q1$	$q2$	$^*q3$
$q2$	$^*q3$	$^*q5$
$^*q3$	$q4$	$^*q3$
$q4$	$^*q3$	$^*q5$
$^*q5$	$q2$	$^*q5$

STEP-1: Cross down all the combinations of Final and Non-Final states in the table.

$q2$				
$q3^*$	X	X		
$q4$			X	
$q5^*$	X	X		X
	$q1$	$q2$	$q3^*$	$q4$

STEP-2: Check all the '0' and '1' input combinations of the non crossed states

	0	1
$q1$	$q2$	$^*q3$
$q2$	$^*q3$	$^*q5$

Non-Final – Final

Final – Final

So, this combination is not possible.

	0	1
$q1$	$q2$	$^*q3$
$q4$	$^*q3$	$^*q5$

Non-Final – Final

Final – Final

So, this combination is not possible.

	0	1
$q2$	$^*q3$	$^*q5$
$q4$	$^*q3$	$^*q5$

Final – Final

Final – Final

So, this combination is possible.

	0	1
q3	q4	*q3
*q5	q2	*q5

Non-Final – Final

Non- Final – Final

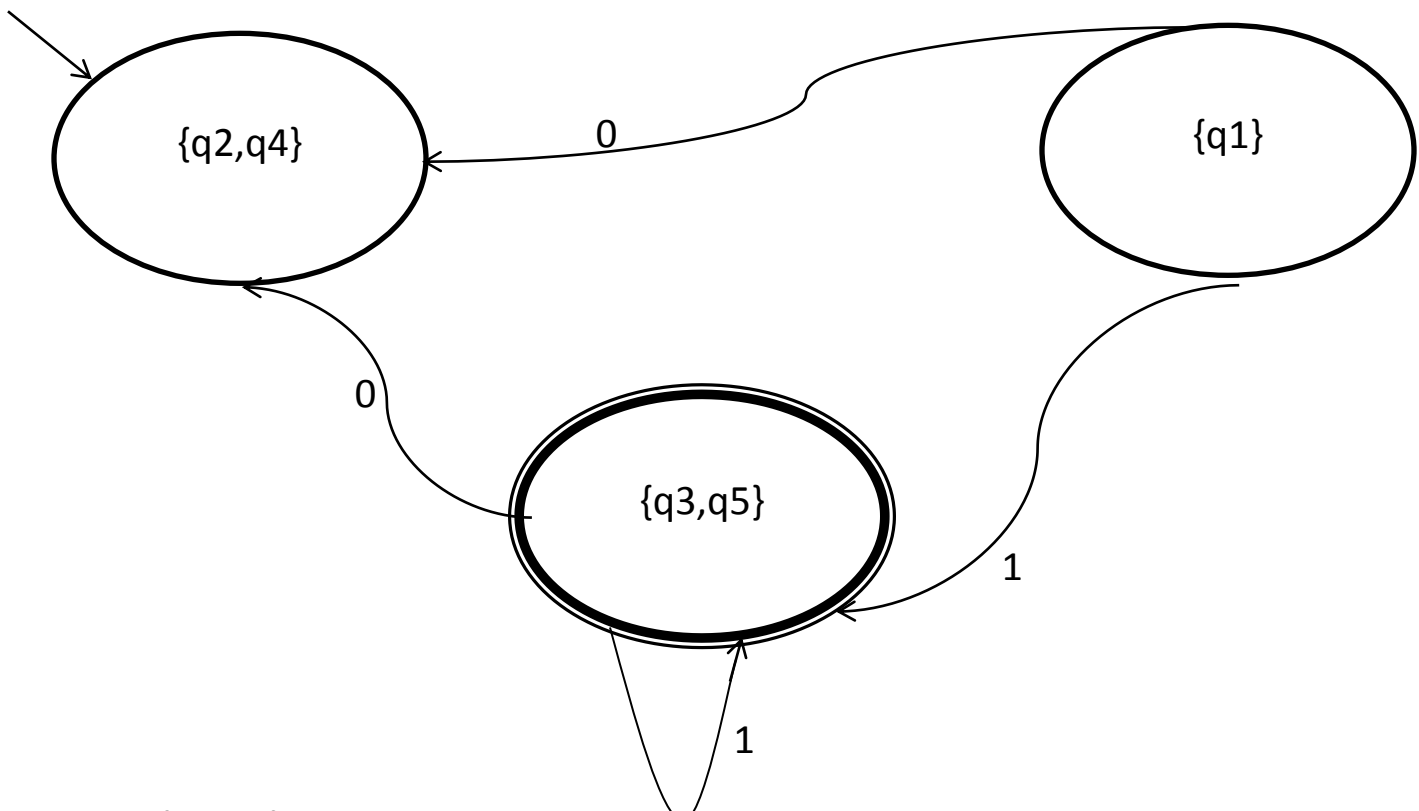
So, this combination is possible.

q2	X			
q3*	X	X		
q4	X		X	
q5*	X	X		X
	q1	q2	q3*	q4

STEP 3: List the remaining pairs

{q2,q4}, {q3,q5}, {q1}

STEP 4: Transition Diagram



Since, {q2,q4} reach the same destination, they are equivalent.

Since, {q3,q5} reach the different destination, they are not equivalent.

Consider the following transition table and minimize the states.

$\delta$	0	1
$\rightarrow$ q1	q2	*q6
q2	q1	*q3
*q3	q2	q4
q4	q4	q2
q5	q4	q5
*q6	q5	q4

STEP-1: Cross down all the combinations of Final and Non-Final states in the table.

q2					
q3*	X	X			
q4			X		
q5			X		
q6*	X	X		X	X
	q1	q2	q3*	q4	q5

STEP-2: Check all the '0' and '1' input combinations of the non crossed states

	0	1
q1	q2	*q6
q2	q1	*q3

Non-Final – Final

Non-Final – Final

So, this combination is possible.

	0	1
q1	q2	*q6
q4	q4	q2

Non-Final – Final

Non-Final – Non-Final

So, this combination is not possible.

	0	1
q1	q2	*q6
q5	q4	q5

Non-Final – Final

Non-Final – Non-Final



So, this combination is not possible.

	0	1
q2	q1	*q3
q4	q4	q2

Non-Final – Final

Non-Final – Non-Final

So, this combination is not possible.

	0	1
q2	q1	*q3
q5	q4	q5

Non-Final – Final

Non-Final – Non-Final

So, this combination is not possible.

	0	1
*q3	q2	q4
*q6	q5	q4

Non-Final – Non-Final

Non-Final – Non-Final

So, this combination is possible.

	0	1
q4	q4	q2
q5	q4	q5

Non-Final – Non-Final

Non-Final – Non-Final

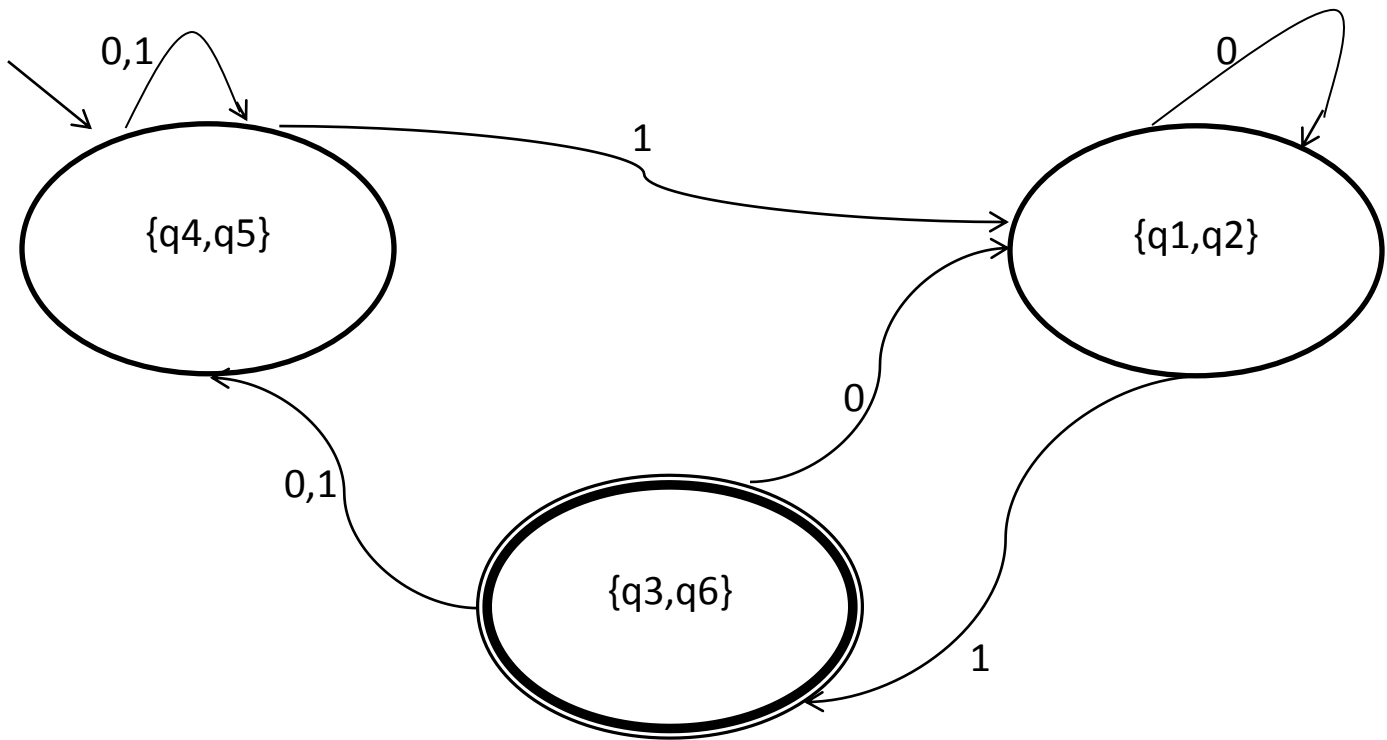
So, this combination is possible.

q2					
q3*	X	X			
q4	X	X	X		
q5	X	X	X		
q6*	X	X		X	X
	q1	q2	q3*	q4	q5

STEP 3: List the remaining steps

{q1, q2}, {q3,q6}, {q4,q5}

#### STEP 4: Transition Diagram



Since,  $\{q1, q2\}$ ,  $\{q4, q5\}$  and  $\{q3, q6\}$  reach the different destination, they are not equivalent.