

Apply Master's Theorem for the following recurrence relation.

1.  $T(n) = 8T\left(\frac{n}{2}\right) + 1000n^2$

According to Master's theorem,

if,  $f(n) = c * n^k$  where  $d \geq 0$  in recurrence and

$T(n) = aT\left(\frac{n}{b}\right) + f(n)$  then,

$$T(n) \in \theta(n^k) \quad \text{if } a < b^k$$

$$T(n) \in \theta(n^k \log n) \quad \text{if } a = b^k$$

$$T(n) \in \theta(n^{\log_b a}) \quad \text{if } a > b^k$$

Here  $a = 8$ ,  $b = 2$ ,  $k = 2$  and since  $a > b^k$

$$T(n) \in \theta(n^{\log_2 8}) \quad \approx \quad T(n) \in \theta(n^3)$$

2.  $T(n) = 2T\left(\frac{n}{2}\right) + n^2$

According to Master's theorem,

if,  $f(n) = c * n^k$  where  $d \geq 0$  in recurrence and

$T(n) = aT\left(\frac{n}{b}\right) + f(n)$  then,

$$T(n) \in \theta(n^k) \quad \text{if } a < b^k$$

$$T(n) \in \theta(n^k \log n) \quad \text{if } a = b^k$$

$$T(n) \in \theta(n^{\log_b a}) \quad \text{if } a > b^k$$

Here  $a = 2$ ,  $b = 2$ ,  $k = 2$  and since  $a < b^k$

$$T(n) \in \theta(n^2)$$

3.  $T(n) = 2T\left(\frac{n}{2}\right) + 10n$

According to Master's theorem,

if,  $f(n) = c * n^k$  where  $d \geq 0$  in recurrence and

$T(n) = aT\left(\frac{n}{b}\right) + f(n)$  then,

$$T(n) \in \theta(n^k) \quad \text{if } a < b^k$$

$$T(n) \in \theta(n^k \log n) \quad \text{if } a = b^k$$

$$T(n) \in \theta(n^{\log_b a}) \quad \text{if } a > b^k$$

Here  $a = 2$ ,  $b = 2$ ,  $k = 1$  and since  $a = b^k$

$$T(n) \in \theta(n \log n)$$