

# Lab Brief

## Course - Statistical Learning

Covariance, Variance and Mean

# Tools

- R/R Studio
- Pen and Paper

# Problem Statement

## Question No 1: (To be solved using R)

Let  $X_1, X_2, X_3, X_4, X_5$  be independent  $U(0, 1)$  random variables. Let  $X = X_1 + X_2 + X_3$  and  $Y = X_3 + X_4 + X_5$ . Use the `runif()` function to simulate 1000 trials of each of these variables. Use these to estimate  $\text{Cov}(X, Y)$ .

## Question No 2

The random variable  $X$  takes values  $-1, 0, 1$  with probabilities  $1/8, 2/8, 5/8$  respectively.

- (a) Compute  $E(X)$ .
- (b) Give the pmf of  $Y = X^2$  and use it to compute  $E(Y)$ . [PMF - Probability Mass Function]
- (c) Instead, compute  $E(X^2)$  directly from an extended table.
- (d) Compute  $\text{Var}(X)$ .

## Reference Links -

1. PMF - [https://www.probabilitycourse.com/chapter3/3\\_1\\_3\\_pmf.php](https://www.probabilitycourse.com/chapter3/3_1_3_pmf.php)

# Steps

1.Solve Question 1 using R.

You can use `set.seed()`, `runif()`, `matrix()` and `cov()` functions in R to solve it.

2.Use R or Pen/Paper to solve Question 2 given in the previous slide.

# Learning Outcomes

You will learn how to --

- To use R to calculate data distribution parameters like covariance.
- Calculate mean and variance of given data-points.

## Submission -

- Each question carries 5 marks.
- Submit R code and your outputs with comments and necessary details in a pdf/doc file.
- Format of file name should be -- YourName\_LAB\_SL.extension