

DBMS Assignment-2

Q1 a) $R(A, B, C, D, E)$

$$F = \{A \rightarrow B, B \rightarrow C, C \rightarrow D\}$$

$$AE^+ = ABCD$$

⇒ Only 1 CK ie- AE

b) $R(A, B, C, D, E)$

$$F = \{AD \rightarrow C, B \rightarrow A, C \rightarrow E, E \rightarrow BD\}$$

$$AD^+ = ADCB$$

$$BD^+ = BDACE$$

$$E^+ = EBPAC$$

$$C^+ = CEBDA$$

$$D^+ = D$$

$$A^+ = A$$

$$B^+ = BA$$

So, there are 4 CK ie-
AD, BD, E, C

c) $R(A, B, C, D, E, F, G, H, I, J)$

$$FD = \{ABD \rightarrow E, AB \rightarrow G, B \rightarrow F, C \rightarrow I, CJ \rightarrow H, G \rightarrow H\}$$

$$ABD^+ = ABDEGH$$

$$AB^+ = ABGFH$$

$$B^+ = BF$$

$$C^+ = CJI$$

$$CJ^+ = CJH$$

$$G^+ = HG$$

⇒ 1 candidate key
ie- (ABCD)

d) $R(ABCDCH)$

$$F = \{A \rightarrow B, B \rightarrow D, E \rightarrow C, D \rightarrow A\}$$

$$A^+ = \{A, B\}$$

$$B^+ = \{B, C, D, A\}$$

$$E^+ = \{E, C\}$$

$$D^+ = \{A, D, B\}$$

$$BCH^+ = \{B, C, D, E, A, H\}$$

$$AEH^+ = \{A, B, E, C, H, D\}$$

$$DEH^+ = \{D, E, H, A, B, C\}$$

So 3 CK are there i.e. - BEH, AEH, DEH.

Q2 ~~$ABAH \rightarrow B$~~ (Trivial)

$$\begin{array}{l} A \rightarrow B \\ A \rightarrow C \end{array}$$

i) $FD = \{A \rightarrow BC, CD \rightarrow E, E \rightarrow C, D \rightarrow AEH, ABH, DH \rightarrow BC\}$

$$A \rightarrow B$$

$$A \rightarrow C$$

$$E \rightarrow C$$

$$D \rightarrow A$$

$$D \rightarrow E$$

$$D \rightarrow H$$

$$AH \rightarrow D$$

$$D^+ = \{A, E, H, D, B, C\}$$

$$A^+ = ABC$$

So minimal cover is -

$$A \rightarrow B$$

$$A \rightarrow C$$

$$E \rightarrow C$$

$$D \rightarrow A$$

$$D \rightarrow E$$

$$D \rightarrow H$$

$$AH \rightarrow D$$

So minimal cover is -

$$\left\{ \begin{array}{l} A \rightarrow B, A \rightarrow C, E \rightarrow C, D \rightarrow A, D \rightarrow E, D \rightarrow H, \\ AH \rightarrow D \end{array} \right\}$$

ii) $F(AB \rightarrow C, C \rightarrow A, BC \rightarrow D, ADC \rightarrow, BE \rightarrow C, EC \rightarrow F, EC \rightarrow A, CF \rightarrow B, CF \rightarrow H, D \rightarrow E)$

$$AB \rightarrow C$$

$$C \rightarrow A$$

$$BC \rightarrow D$$

$$DC \rightarrow B$$

$$BE \rightarrow C$$

$$EC \rightarrow F$$

$$CF \rightarrow D$$

$$D \rightarrow E$$

$$AD^+ = ADE$$

$$DC^+ = DCEAFB$$

$$CF^+ = CFDCAF$$

$$BE^+ = BED$$

$$BC^+ = BCA$$

$$BE^+ = BE$$

$$CF^+ = CFA$$

$$EC = EC$$

$$EF = CA$$

Canonical Cover-

$AB \rightarrow C, C \rightarrow A, BC \rightarrow D, DC \rightarrow B, BE \rightarrow C, EC \rightarrow F,$
 $CF \rightarrow D, D \rightarrow E$

Q3a) $FD_1 = \{ A \rightarrow C, (AC \rightarrow D), E \rightarrow AD, E \rightarrow H \} \rightarrow \times$

$FD_2 = \{ A \rightarrow C, E \rightarrow A, E \rightarrow D, E \rightarrow H \}$
 $(A \rightarrow H)$

$AC^+ = ACH$

$A^+ = ACD$

Not Equivalent

b) $FD_1 = \{ A \rightarrow C, AC \rightarrow D, E \rightarrow A, E \rightarrow H \}$
 $FD_2 = \{ A \rightarrow H, E \rightarrow C, E \rightarrow H \}$

is FD_1 covered by FD_2

$A^+ = AH$ (not FD_2)

Not Equivalent

Q-8 $R(ABCD)$

	$AB \rightarrow C$	$AB \rightarrow D$	$D \rightarrow A$
BCNF	✓	✓	✓
3NF			
2NF			
1NF			

$$AB^+ = ABCD$$

$$DB^+ = DBAC$$

So, 2CK, Prime(ABD)

(3NF)

ABC	ABD	
$AB \rightarrow C$	$AB \rightarrow D$	(BCNF)
BCNF	$D \rightarrow A$	(3NF)

So, 3NF

Q.7 $R(ABCDF)$

	$AB \rightarrow C$	$BC \rightarrow A$	$AC \rightarrow B$
BCNF			
3NF			
2NF		✓	✓
1NF	✓		

$$AB^+ = ABCD$$

$$ABDE \rightarrow CK$$

So,

(ABCDE)

ABC

BCDE

$$AB \rightarrow C$$

$$BC \rightarrow A$$

$$AC \rightarrow B$$

$$BC^+ = CBA$$

↳ CK

$(ABC) \cup (BCDE) \rightarrow \{ AB \rightarrow C, BC \rightarrow A, AC \rightarrow B \}$
 So, BCNF

Q5 $R = (A B C D E G)$

$F = \{ AB \rightarrow C, BC \rightarrow A, AC \rightarrow B, B \rightarrow D, E \rightarrow G, AD \rightarrow E \}$

F_1
 ABC

F_2
 BD

F_3
 $ADEG$

$AB \rightarrow C$
 $BC \rightarrow A$
 $AC \rightarrow B$

$B \rightarrow D$

$E \rightarrow G$
 $AD \rightarrow E$

$F_1 \cap F_2 = B$
 $B^+ = B, D$ so CK of F_2
 $ABC \cap ADEG = AD$
 $AD^+ = ADEG \rightarrow$ CK of F_3 so lossy

$AB \rightarrow C$
 $E \rightarrow G$

$BC \rightarrow A$
 $AD \rightarrow E$

$AC \rightarrow B$ $B \rightarrow D$

ABC

ADE

$ADEG$

$AB \rightarrow C$
 $BC \rightarrow A$
 $AC \rightarrow B$

$E \rightarrow G$
 $AD \rightarrow E$

$ABC \cap ADEG = A$
 $A^+ = A =$ lossy

Q6 i) $R(AB CDEGH)$

$FD = \{AB \rightarrow C, AC \rightarrow B, AD \rightarrow E, B \rightarrow D, BC \rightarrow A, E \rightarrow G\}$

$AB \cup BC \cup ABDE \cup EG$

$\{AB \rightarrow D, AD \rightarrow E, AB \rightarrow G, B \rightarrow D, E \rightarrow G\}$

$F = \{AB \rightarrow C, AC \rightarrow B, AD \rightarrow E, B \rightarrow D, BC \rightarrow A, E \rightarrow G\}$

$AB^+ = ABDEG$

→ This decomp. is not preserved & lossy & is missing.

W) ABC
 $AB \rightarrow C$
 $AC \rightarrow B$
 $BC \rightarrow A$

$ACDE$
 $AD \rightarrow E$
 $AC \rightarrow D, E$

ADG
 $AD \rightarrow G$

→ $AB \rightarrow C, AC \rightarrow B, BC \rightarrow A, AD \rightarrow E, AC \rightarrow DE, AD \rightarrow G$

To see

$B \rightarrow D, E \rightarrow G$

Q-4

$R(A, B, C, D)$

$$F = \{A \rightarrow B, B \rightarrow C, C \rightarrow D\}$$

$$D = \{AB, BC, CD\}$$

$$AB \Rightarrow A \rightarrow B$$

$$BC \Rightarrow B \rightarrow C, C \rightarrow$$

$$CD \Rightarrow C \rightarrow D, D \rightarrow C$$

$$B \rightarrow A$$

$$C \rightarrow B \quad (C \rightarrow D, D \rightarrow B)$$

$$D \rightarrow C \quad (D \rightarrow B, B \rightarrow C)$$

$$AB \cup BC \cup CD$$

$$\{A \rightarrow B, B \rightarrow C, C \rightarrow B\}$$

$$D^+ = DCB$$