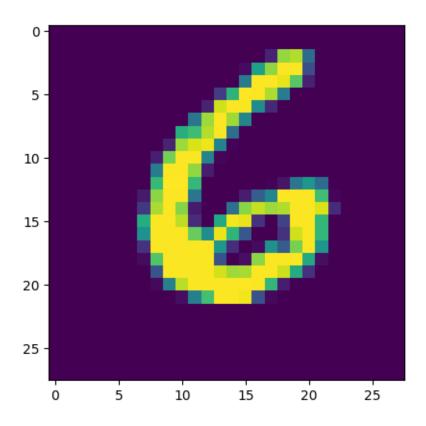
Mnist

September 22, 2024

```
[35]: import tensorflow
      from tensorflow import keras
      from tensorflow.keras import Sequential
      from tensorflow.keras.layers import
       →Dense,Flatten,Conv2D,MaxPooling2D,Dropout,BatchNormalization
 [3]: (X_train,y_train),(X_test,y_test)=keras.datasets.mnist.load_data()
     Downloading data from https://storage.googleapis.com/tensorflow/tf-keras-
     datasets/mnist.npz
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 [4]: X_train.shape
 [4]: (60000, 28, 28)
 [5]: X_test.shape
 [5]: (10000, 28, 28)
 [6]: y_test.shape
 [6]: (10000,)
 [7]: import matplotlib.pyplot as plt
      plt.imshow(X_train[90])
```

[7]: <matplotlib.image.AxesImage at 0x7b20bbb09960>



```
[8]: X_train= X_train.reshape(-1, 28, 28, 1).astype('float32') / 255.0
     X_test = X_test.reshape(-1, 28, 28, 1).astype('float32') / 255.0
[9]: X_train[0]
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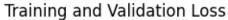
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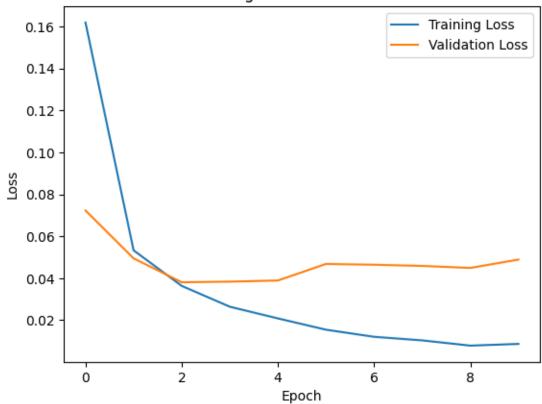
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[10]: X_train, X_val = X_train[:-10000], X_train[-10000:]
      y_train, y_val = y_train[:-10000], y_train[-10000:]
[11]: X_train.shape
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[11]: (50000, 28, 28, 1)
[12]: y_train
[12]: array([5, 0, 4, ..., 8, 4, 8], dtype=uint8)
[13]: # Build a simple CNN model with regularization
      model = Sequential()
      # Add layers to the model
      model.add(Conv2D(32, (3, 3), activation='relu', input_shape=(28, 28, 1)))
      model.add(MaxPooling2D((2, 2)))
      model.add(Conv2D(64, (3, 3), activation='relu'))
      model.add(MaxPooling2D((2, 2)))
      model.add(Flatten())
      model.add(Dense(64, activation='relu'))
     model.add(Dense(10, activation='softmax'))
     /usr/local/lib/python3.10/dist-
     packages/keras/src/layers/convolutional/base_conv.py:107: UserWarning: Do not
     pass an `input_shape`/`input_dim` argument to a layer. When using Sequential
     models, prefer using an `Input(shape)` object as the first layer in the model
     instead.
       super().__init__(activity_regularizer=activity_regularizer, **kwargs)
[14]: model.summary()
     Model: "sequential"
      Layer (type)
                                              Output Shape
                                                                                   Ш
      →Param #
       conv2d (Conv2D)
                                              (None, 26, 26, 32)
                                                                                       Ш
      →320
      max pooling2d (MaxPooling2D)
                                              (None, 13, 13, 32)
                                                                                       1.1
      → 0
      conv2d_1 (Conv2D)
                                              (None, 11, 11, 64)
                                                                                    Ш
      max_pooling2d_1 (MaxPooling2D)
                                              (None, 5, 5, 64)
                                                                                       Ш
      → 0
      flatten (Flatten)
                                              (None, 1600)
                                                                                       Ш
      □ 0
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```
(None, 64)
      dense (Dense)
      (None, 10)
      dense_1 (Dense)
                                                                                      Ш
      ⇔650
      Total params: 121,930 (476.29 KB)
      Trainable params: 121,930 (476.29 KB)
      Non-trainable params: 0 (0.00 B)
[15]: optimizer = tensorflow.keras.optimizers.Adam(learning rate=0.001)
[16]: model.compile(loss = "sparse_categorical_crossentropy",optimizer = optimizer,__
       →metrics=['accuracy'])
[17]: history = model.fit(X train, y train, epochs=10, validation_data=(X_val, y_val))
     Epoch 1/10
     1563/1563
                           64s 40ms/step -
     accuracy: 0.8957 - loss: 0.3627 - val_accuracy: 0.9790 - val_loss: 0.0723
     Epoch 2/10
     1563/1563
                           50s 32ms/step -
     accuracy: 0.9832 - loss: 0.0552 - val_accuracy: 0.9859 - val_loss: 0.0495
     Epoch 3/10
     1563/1563
                           48s 31ms/step -
     accuracy: 0.9891 - loss: 0.0360 - val_accuracy: 0.9889 - val_loss: 0.0381
     Epoch 4/10
     1563/1563
                           83s 31ms/step -
     accuracy: 0.9916 - loss: 0.0247 - val_accuracy: 0.9896 - val_loss: 0.0384
     Epoch 5/10
     1563/1563
                           81s 31ms/step -
     accuracy: 0.9936 - loss: 0.0190 - val_accuracy: 0.9894 - val_loss: 0.0389
     Epoch 6/10
     1563/1563
                           48s 31ms/step -
     accuracy: 0.9956 - loss: 0.0135 - val_accuracy: 0.9880 - val_loss: 0.0468
     Epoch 7/10
     1563/1563
                           83s 31ms/step -
     accuracy: 0.9960 - loss: 0.0108 - val_accuracy: 0.9885 - val_loss: 0.0464
     Epoch 8/10
     1563/1563
                           47s 30ms/step -
     accuracy: 0.9974 - loss: 0.0081 - val_accuracy: 0.9894 - val_loss: 0.0459
     Epoch 9/10
     1563/1563
                           87s 33ms/step -
```

```
accuracy: 0.9972 - loss: 0.0077 - val_accuracy: 0.9888 - val_loss: 0.0449
     Epoch 10/10
     1563/1563
                           47s 30ms/step -
     accuracy: 0.9976 - loss: 0.0071 - val_accuracy: 0.9894 - val_loss: 0.0489
[18]: \#history = model.fit(X_train, y_train, epochs=10, validation_data=(X_val, u)
       \rightarrow y_val), batch_size=32)
      # Plotting the training and validation loss
      import matplotlib.pyplot as plt
      plt.plot(history.history['loss'], label='Training Loss')
      plt.plot(history.history['val_loss'], label='Validation Loss')
      plt.title('Training and Validation Loss')
      plt.xlabel('Epoch')
      plt.ylabel('Loss')
      plt.legend()
      plt.show()
```





```
[19]: test_loss, test_accuracy = model.evaluate(X_test, y_test)
      print(f"Test Accuracy: {test_accuracy*100:.2f}%")
     313/313
                           3s 9ms/step -
     accuracy: 0.9895 - loss: 0.0402
     Test Accuracy: 99.18%
     Batch Noramlization and its usage:
     Code after applying drop out layer
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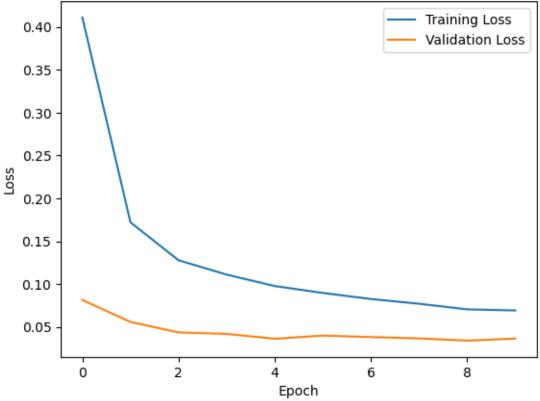
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[26]: model_with_drop_out = Sequential()
      # Input and first convolutional layer
      model_with_drop_out.add(Conv2D(32, (3, 3), activation='relu', input_shape=(28, __
       <sup>4</sup>28, 1)))
      model_with_drop_out.add(MaxPooling2D((2, 2)))
      model_with_drop_out.add(Dropout(0.25))
```

```
# Second convolutional layer
      model_with_drop_out.add(Conv2D(64, (3, 3), activation='relu'))
      model_with_drop_out.add(MaxPooling2D((2, 2)))
      model_with_drop_out.add(Dropout(0.25))
      model_with_drop_out.add(Flatten())
      model_with_drop_out.add(Dense(64, activation='relu'))
      model with drop out.add(Dropout(0.5))
     model_with_drop_out.add(Dense(10, activation='softmax'))
     /usr/local/lib/python3.10/dist-
     packages/keras/src/layers/convolutional/base_conv.py:107: UserWarning: Do not
     pass an `input_shape`/`input_dim` argument to a layer. When using Sequential
     models, prefer using an `Input(shape)` object as the first layer in the model
     instead.
       super().__init__(activity_regularizer=activity_regularizer, **kwargs)
[27]: optimizer = tensorflow.keras.optimizers.Adam(learning_rate=0.001)
[28]: model_with_drop_out.compile(loss = "sparse_categorical_crossentropy",optimizer_
       ⇔= optimizer, metrics=['accuracy'])
[29]: history_with_dropout = model_with_drop_out.fit(X_train, y_train, epochs=10,_u
       ⇔validation_data=(X_val, y_val))
     Epoch 1/10
     1563/1563
                           64s 40ms/step -
     accuracy: 0.7611 - loss: 0.7232 - val_accuracy: 0.9759 - val_loss: 0.0815
     Epoch 2/10
     1563/1563
                           55s 35ms/step -
     accuracy: 0.9425 - loss: 0.1841 - val_accuracy: 0.9832 - val_loss: 0.0559
     Epoch 3/10
     1563/1563
                           82s 35ms/step -
     accuracy: 0.9616 - loss: 0.1337 - val accuracy: 0.9876 - val loss: 0.0437
     Epoch 4/10
     1563/1563
                           82s 35ms/step -
     accuracy: 0.9654 - loss: 0.1131 - val accuracy: 0.9879 - val loss: 0.0419
     Epoch 5/10
                           82s 35ms/step -
     1563/1563
     accuracy: 0.9689 - loss: 0.0972 - val_accuracy: 0.9897 - val_loss: 0.0363
     Epoch 6/10
     1563/1563
                           54s 35ms/step -
     accuracy: 0.9735 - loss: 0.0851 - val_accuracy: 0.9897 - val_loss: 0.0400
```

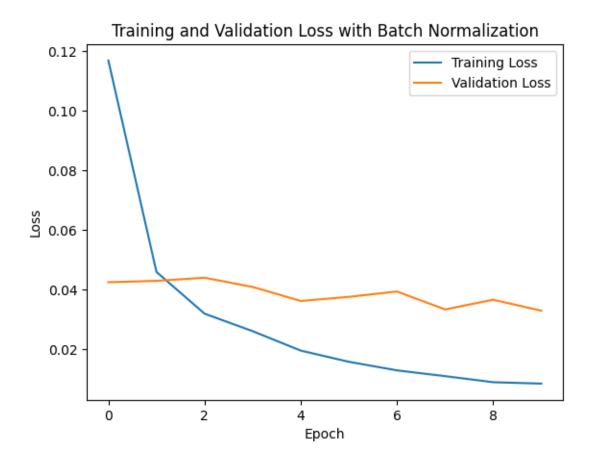
```
Epoch 7/10
     1563/1563
                           54s 35ms/step -
     accuracy: 0.9747 - loss: 0.0823 - val accuracy: 0.9902 - val loss: 0.0382
     Epoch 8/10
     1563/1563
                           54s 35ms/step -
     accuracy: 0.9767 - loss: 0.0777 - val_accuracy: 0.9905 - val_loss: 0.0367
     Epoch 9/10
     1563/1563
                           82s 35ms/step -
     accuracy: 0.9792 - loss: 0.0692 - val_accuracy: 0.9914 - val_loss: 0.0341
     Epoch 10/10
     1563/1563
                           54s 35ms/step -
     accuracy: 0.9799 - loss: 0.0671 - val accuracy: 0.9902 - val loss: 0.0365
[32]: import matplotlib.pyplot as plt
      plt.plot(history_with_dropout.history['loss'], label='Training Loss')
      plt.plot(history_with_dropout.history['val_loss'], label='Validation Loss')
      plt.title('Training and Validation Loss with drop out layer')
      plt.xlabel('Epoch')
      plt.ylabel('Loss')
      plt.legend()
      plt.show()
```





```
[33]: test_loss, test_accuracy = model_with_drop_out.evaluate(X_test, y_test)
      print(f"Test Accuracy: {test_accuracy*100:.2f}%")
     313/313
                         3s 10ms/step -
     accuracy: 0.9899 - loss: 0.0323
     Test Accuracy: 99.17%
[37]: model_with_BN = Sequential()
      # Add layers to the model
      model_with_BN.add(Conv2D(32, (3, 3), activation='relu', input_shape=(28, 28, u)
       →1)))
      model_with_BN.add(BatchNormalization())
      model_with_BN.add(MaxPooling2D((2, 2)))
      model_with_BN.add(Conv2D(64, (3, 3), activation='relu'))
      model_with_BN.add(BatchNormalization())
      model_with_BN.add(MaxPooling2D((2, 2)))
      model_with_BN.add(Flatten())
      model with BN.add(Dense(64, activation='relu'))
      model_with_BN.add(BatchNormalization())
      model_with_BN.add(Dense(10, activation='softmax'))
[38]: optimizer = tensorflow.keras.optimizers.Adam(learning_rate=0.001)
[39]: model_with_BN.compile(loss = "sparse_categorical_crossentropy",optimizer = ___
       ⇔optimizer, metrics=['accuracy'])
[40]: history_with_BN = model_with_BN.fit(X_train, y_train, epochs=10,__
       →validation_data=(X_val, y_val))
     Epoch 1/10
     1563/1563
                           91s 56ms/step -
     accuracy: 0.9294 - loss: 0.2394 - val_accuracy: 0.9877 - val_loss: 0.0425
     Epoch 2/10
                           70s 45ms/step -
     1563/1563
     accuracy: 0.9879 - loss: 0.0431 - val_accuracy: 0.9873 - val_loss: 0.0430
     Epoch 3/10
     1563/1563
                           81s 44ms/step -
     accuracy: 0.9911 - loss: 0.0291 - val_accuracy: 0.9876 - val_loss: 0.0440
     Epoch 4/10
     1563/1563
                           82s 44ms/step -
     accuracy: 0.9924 - loss: 0.0226 - val_accuracy: 0.9889 - val_loss: 0.0410
     Epoch 5/10
     1563/1563
                           83s 45ms/step -
     accuracy: 0.9943 - loss: 0.0189 - val_accuracy: 0.9892 - val_loss: 0.0363
     Epoch 6/10
```

```
1563/1563
                           82s 44ms/step -
     accuracy: 0.9952 - loss: 0.0147 - val_accuracy: 0.9894 - val_loss: 0.0376
     Epoch 7/10
     1563/1563
                           82s 44ms/step -
     accuracy: 0.9964 - loss: 0.0114 - val_accuracy: 0.9902 - val_loss: 0.0394
     Epoch 8/10
     1563/1563
                           72s 46ms/step -
     accuracy: 0.9972 - loss: 0.0095 - val_accuracy: 0.9916 - val_loss: 0.0334
     Epoch 9/10
     1563/1563
                           79s 44ms/step -
     accuracy: 0.9975 - loss: 0.0079 - val accuracy: 0.9902 - val loss: 0.0367
     Epoch 10/10
     1563/1563
                           82s 44ms/step -
     accuracy: 0.9980 - loss: 0.0064 - val_accuracy: 0.9908 - val_loss: 0.0330
[41]: import matplotlib.pyplot as plt
      plt.plot(history_with_BN.history['loss'], label='Training Loss')
      plt.plot(history_with_BN.history['val_loss'], label='Validation Loss')
      plt.title('Training and Validation Loss with Batch Normalization')
      plt.xlabel('Epoch')
      plt.ylabel('Loss')
      plt.legend()
      plt.show()
```



```
[42]: test_loss, test_accuracy = model_with_BN.evaluate(X_test, y_test) print(f"Test Accuracy: {test_accuracy*100:.2f}%")
```

313/313 4s 12ms/step - accuracy: 0.9893 - loss: 0.0361

Test Accuracy: 99.10%

1 Definition

Batch Noramlization and its usage:

Batch normalization is a technique which makes deep learning training more faster and stable. It consists of normalizing activation vectors from hidden layers using the mean and variance of the current batch. This is applied right before or after the nonlinear function

Drop out layer and its usage:

Dropout layer is a technique used to reduce overfitting of the model by dropping of some neurons randomly from hidden layer to avoid overfitting

2 Inferences:

I have trained the model without dropout layer, later with dropout layer and batch normalization layer.

observations:

1) Adding drop out layer does not make any significant change in the output and test accuracy is almost same i.e 99.17. Additionally training loss is initially higher in model with drop out compared with model without drop out layer

overfitting is not a concern, as test accuracy is same in both cases

2) Model trained with Batch Normalization significantly improves the model's performance by normalizing the inputs at each layer, which helps in stabilizing the training process. This is evident from the consistently lower training and validation losses compared to models without it. Such normalization reduces drastic shifts in input distribution—a common problem in deep networks—making training faster and more reliable. The close tracking of training and validation losses indicates that the model generalizes well and doesn't overfit, making Batch Normalization a highly effective strategy for enhancing neural network performance.

Model requires batch processing layer and doesn't require drop out based on the observations

[]:	
[42]:	