

Inter-generational conflict and the declining labor share

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Since World War II

1. Appearance of the **baby-boomers' cohort** in many OECD countries
2. **Declining labor income share** since the entry of the boomers on the labor market
 - ▶ Biased technical change, institutions, globalization ?

How does age structure affect the income allocation between capital and labor in high-income countries ?

Why would this matter ?

⇒ Aging population in many OECD countries

< Old-age dependency ratio figure >

What do we know ?

- Population aging affects the labor share **through capital accumulation**
 - ▶ Schmidt and Vosen (2013)
- **Biased technical change** is the long-run response of firms to thwart **workers empowerment**
 - ▶ Caballero and Hammour (1998); Blanchard (1997); Bentolila and Saint-Paul (2003); Acemoglu (2002); Karabarbounis and Neiman (2014)
- **Inter-generational conflict** over the public budget allocation
 - ▶ Gonzalez-Eiras and Niepelt (2012); Lancia and Prarolo (2012); Busemeyer et al. (2009); Sørensen (2013); Jäger and Schmidt (2016)

What I do ?

1. OLG model focusing on two elements:
 - ▶ **Direct cohort effect:** factor accumulation
 - ▶ **Indirect policy mechanism:** age-structure determines labor market institutions
2. **Calibration** to analyze the co-movement between labor share and age-structure
 - ▶ France and the United-States
3. **Quantify** the role of population growth and survival rate

Outline

- 1 Introduction
- 2 Theoretical Framework
- 3 Main results
- 4 Conclusion

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1 Introduction

2 Theoretical Framework

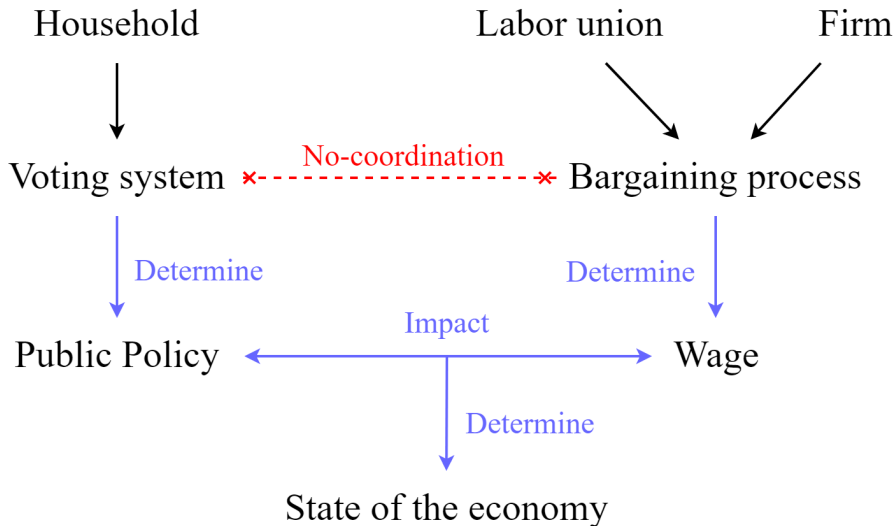
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Overlapping generations model

- **Standard 2-period OLG model** with logarithmic utility function and CES production function
 - ▶ Closed economy and capital fully depreciates between two periods
 - ▶ Perfect annuities market
- Each cohort: continuum of homogeneous agents
 - ▶ Young households: supply labor inelastically, earn income, pay taxes, consume and save for retirement
 - ▶ Old households: consume the return on their savings, pay taxes and derive utility from government health spending

Diagram of the model



Public policy preferences

- **Age-related conflict** in the public policy:
 - ▶ Young households desire more unemployment benefit (b)
 - ▶ Old households desire more health spending (h)
 - ▶ Both desire less taxes (τ)
- Solved with **probabilistic voting**: public policy depends on...
 1. Macroeconomic variables (*wage rate, unemployment rate, etc.*)
 2. Preference for government health spending
 3. Weight of the young generation within the social welfare function (η_t)

$$\eta_t = \frac{n_t}{p_t} \frac{1 + \alpha p_{t+1}}{\omega}$$

n population growth

p survival rate

α discount rate

ω relative per-capita influence
of old households

- Maximization program characterizing equilibrium policy choices in period t :

$$\begin{aligned} \max_{\{\tau_t, b_t, h_t\} \geq 0} \quad & \ln(1 - \tau_t) + \beta \ln h_t + \eta_t \ln [(1 - u_t)(1 - \tau_t)w_t + u_t b_t] + \dots \\ \text{s.t.} \quad & \tau_t Y_t = b_t u_t N_t^y + h_t N_t^o \end{aligned}$$

η_t the weight of the young generation within the social welfare function :

$$\eta_t = \frac{n_t}{p_t} \frac{1 + \alpha p_{t+1}}{\omega}$$

- Focusing on the interior solution, first order conditions give :

$$\begin{aligned}\frac{b_t}{(1 - \tau_t)w_t} &= \frac{1 - u_t}{u_t} \left(\eta_t \frac{1 - \theta_t}{\theta_t} - 1 \right) \\ \tau_t &= 1 - [(1 - \theta_t)(1 + \beta + \eta_t)]^{-1} \\ h_t &= \left(\tau_t \frac{Y_t}{N_t^y} - b_t u_t \right) \frac{n_t}{p_t}\end{aligned}$$

Wage bargaining

- Right-to-manage model *à la* Nickell & Andrews (1983) :
 - ▶ Single union that represents workers and bargains only over wages
 - ▶ Employer retains the prerogative to hire and fire
- Maximization program characterizing equilibrium wage bargaining :

$$\begin{aligned} \max_{w_t > 0} \quad & \{ (L_t [U_t^{y,e} - U_t^{y,u}])^\gamma (Y_t - w_t L_t)^{1-\gamma} \}, \quad \gamma \in (0, 1) \\ \text{s.t.} \quad & U_t^{y,e} - U_t^{y,u} = (1 + \alpha p_{t+1}) \ln \left[\frac{(1 - \tau_t) w_t}{b_t} \right] \end{aligned}$$

- From the first-order condition :

$$k_t(X_t) = \left[\frac{1-\phi}{\phi} \frac{1-\gamma(1-\sigma)}{\gamma} \frac{X_t}{1-\sigma X_t} \right]^{\frac{\sigma}{\sigma-1}}$$

where $X_t = \ln \left[\frac{(1-\tau_t)w_t}{b_t} \right]$ is the value-added to be employed in utility terms.

Equilibrium

- Using first order conditions from the voting and wage bargaining, the **capital-to-labor ratio (k) at the equilibrium** solves :

$$X_t = \ln \left(\frac{\frac{N_t^y}{K_t} k_t - 1}{\frac{\phi}{1-\phi} k_t^{\frac{\sigma-1}{\sigma}} \eta_t - 1} \right) \quad (1)$$

$$X_t = \left(\sigma + \frac{1-\phi}{\phi} \frac{1-\gamma(1-\sigma)}{\gamma} k_t^{\frac{1-\sigma}{\sigma}} \right)^{-1} \quad (2)$$

- Uniqueness of the equilibrium : [► Details](#)

Comparative statics : public policy and households

- The longer you expect to live, the more you save : $\frac{\partial S_t}{\partial p_{t+1}} > 0$
- Young households desire...
 - ▶ more redistribution : $\frac{\partial \tau_t}{\partial \eta_t} > 0$
 - ▶ a higher unemployment replacement rate : $\frac{\partial \frac{b_t}{(1-\tau_t)w_t}}{\partial \eta_t} > 0$
- Unemployment benefits increases the labor income share : $\frac{\partial \theta_t}{\partial b_t} > 0$

Comparative statics : labor share

- Labor share : $\theta_t = \frac{w_t L_t}{Y_t} = \left(1 + \frac{\phi}{1-\phi} k_t^{\frac{\sigma-1}{\sigma}}\right)^{-1}$
- Comparative statics :

$$\left\{ \frac{\partial w_t}{\partial k_t} > 0, \quad \frac{\partial(Y_t/L_t)}{\partial k_t} > 0, \quad \frac{\partial \theta_t}{\partial k_t} \leq 0 \right\}, \quad \sigma \geq 1$$

- It implies that :

$$\left\{ \frac{\partial w_t}{\partial k_t} \leq \frac{\partial(Y_t/L_t)}{\partial k_t} \right\}, \quad \sigma \geq 1$$

- Finally,

$$\frac{\partial \theta_t}{\partial X_t} < 0, \quad \forall \sigma \in \mathbb{R}_+^* \setminus \{1\}$$

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Conclusion

