
```
function p_current = NewtonsMethod2()
% Use Newton's method to approximate the zero of the function
%  $f(x) = x^2 - 2xe^{-x} + e^{-2x}$  to within  $10^{-8}$ 
% with  $p_0 = 0$ 
% Return the value of  $p_n$  for the approximation

% how many iterations it takes to approximate the zero of the function
how_many_iterations = 0;

% tolerance
TOL =  $10^{-8}$ ;

%  $p_{n-1}$ 
p_last = 0;

%  $p_n$ 
p_current = 1;

%  $f(x) = x^2 - 2xe^{-x} + e^{-2x}$ 
f = @(x) x^2 - 2*x*exp(-x) + exp(-2*x);

% the derivative of  $f(x)$ 
df = @(x) 2*x - 2*exp(-x);

% Until the error range is less than tolerance,
% we continue to apply Newton's method.
while abs((p_current - p_last)/p_current) >= TOL

    % set  $p_{n-1}$  to the last value of  $p_n$ 
    p_last = p_current;

    % calculate  $p_n = p_{n-1} - f(p_{n-1})/f'(p_{n-1})$ 
    p_current = p_last - f(p_last) / df(p_last);

    % increment how_many_iterations
    how_many_iterations = how_many_iterations + 1;

end

% print the results
fprintf("n: %d\t", how_many_iterations);
fprintf("p%d: %.8f\t", how_many_iterations, p_current);
fprintf("|error|: %.8f\n", TOL);

end

n: 13 p13: 0.56714329 |error|: 0.00000001

ans =

0.5671
```

Published with MATLAB® R2018b