
Lab2Simons.m

Table of Contents

Problem 1	1
Problem 2	1
Problem 3	2
Problem 4	2
Problem 5	2

@author Madilyn Simons

Problem 1

Perform four different fixed-point iteration methods of computing $25^{1/3}$

```
fixedPointIterationA();
fixedPointIterationB();
fixedPointIterationC();
fixedPointIterationD();

fprintf('\nMethods in order from fastest convergence to slowest: ');
fprintf('B, D, A\n');
fprintf('NB: Method C does not converge to a sufficient approximation
\n\n');
```

```
n: 135 p135: 2.7589241758 |error|: 0.0000000001
n: 9 p9: 2.7589241764 |error|: 0.0000000001
n: 2 p2: 0.0000000000 |error|: 0.0000000001
n: 37 p37: 2.7589241764 |error|: 0.0000000001
```

```
Methods in order from fastest convergence to slowest: B, D, A
NB: Method C does not converge to a sufficient approximation
```

Problem 2

Use Newton's Method to find an approximation of $25^{1/3}$ correct to within 10^{-10} .

```
NewtonMethod();

fprintf('\nThe Bisection Method takes 31 iterations to approximate
25^(1/3)\n');
fprintf('Newtons Method takes 9 iterations to approximate
25^(1/3)\n');
fprintf('Newtons method approximates 25^(1/3) %.f%% faster than the
Bisection method\n\n', 100*(31-9)/31);

n: 9 p9: 2.9240177382 |error|: 0.0000000001
```

*The Bisection Method takes 31 iterations to approximate $25^{(1/3)}$
Newtons Method takes 9 iterations to approximate $25^{(1/3)}$
Newtons method approximates $25^{(1/3)}$ 71% faster than the Bisection
method*

Problem 3

Use Newton's method to find the time, accurate to within 10^{-5} s that it takes for an object falling from 300 ft to hit the ground.

```
t = FallingObject();  
  
fprintf('\nThe object takes %.5f seconds to hit the ground\n', t);  
  
n: 5 t5: 6.00373 |error|: 0.00001
```

The object takes 6.00373 seconds to hit the ground

Problem 4

Use Newton's method to calculate how much of a drug should be administered to a patient given the maximum safe concentration and equation for concentration of drug in the bloodstream, how long it takes to reach that concentration, and when to administer a second dose.

```
[hours, minutes] = MaxDrugConcentration();  
  
fprintf('\n%.5f units of medicine should be injected to reach\n',  
    exp(1)/3);  
fprintf('the max safe concentration after %d hours.\n', 3);  
fprintf('The second injection should be injected\n');  
fprintf('%d hours and %d minutes later.\n', hours, minutes);  
  
n: 4 t4: 11.07790 |error|: 0.00001
```

*0.906094 units of medicine should be injected to reach
the max safe concentration after 3 hours.
The second injection should be injected
11 hours and 5 minutes later.*

Problem 5

Use Newton's method to approximate the zero of the function $f(x) = x^2 - 2xe^{-x} + e^{-2x}$ to within 10^{-8}

```
x = NewtonsMethod2();  
fprintf('\nx = %.8f\n', x);  
  
n: 13 p13: 0.56714329 |error|: 0.00000001  
  
x = 0.56714329
```

Published with MATLAB® R2018b