

Mandatory exercises for week 38

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S17

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Let $S = \{a, \clubsuit, 1\}$ and $T = \{1, 2\}$

a)

Determine $S \cap T$, $S \cup T$, $S \setminus T$, and $T \setminus S$

$S \cap T = \{1\}$ because 1 is the only element that is both in S and T.

$S \cup T = \{a, \clubsuit, 1, 2\}$ because it is the union of both sets.

$S \setminus T = \{a, \clubsuit\}$ because it is the set S minus the set T, and the remainder is this.

$T \setminus S = \{2\}$ because it is the set T minus the set S.

b)

$S \times S = \{(a, a), (a, \clubsuit), (a, 1), (\clubsuit, a), (\clubsuit, \clubsuit), (\clubsuit, 1), (1, a), (1, \clubsuit), (1, 1)\}$ because it is the cartesian product of S and S

$S \times T = \{(a, 1), (a, 2), (\clubsuit, 1), (\clubsuit, 2), (1, 1), (1, 2)\}$ it is the cartesian product of S and T ordered in such a way that $S \times T = \{(s, t)\}$

c)

The empty set \emptyset is not an element because it is a set. $(\pi, 4)$ is an element because the cartesian product in this case would contain, in the first position, all real numbers between 0 and 10, not including 10, and π is a real number between 1 and 10, and in the second position all the natural numbers are represented, and 4 is a natural number. $(\sqrt{2}, 10)$ is a member for the same reasons as $(\pi, 4)$. 0 is not an ordered pair and is therefore not an element of S. $(4, \pi)$ is not an element because π is not a natural number and $\{1, 2\}$ is not an element because it is a set, but it is a subset of S.

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$$p(x) = x^n + x^{n-1} + x^{n-2} + \dots + x^2 + x + 1, q(x) = x - 1$$

a)

$p \cdot q = (x^{n+1} - x^n) + (x^n - x^{n-1}) + \dots + (x^2 - x) + (x - 1) \Leftrightarrow \underline{x^{n+1} - 1}$ and the degree of $p \cdot q$ is equal to $n+1$ and the coefficient of $a_n=1$ and $a_0=-1$

b)

$p(x)$ with $n = 3$ is : $p(x) = x^3 + x^2 + x + 1$

$p \circ q = \underline{(x-1)^3 + (x-1)^2 + x - 1}$ which has a degree of 3

and $a_3 = 1, a_2 = -2, a_1 = 2, a_0 = -1$

$q \circ p = \underline{x^3 + x^2 + x}$ with degree of 3 and $a_3 = 1, a_2 = 1, a_1 = 1, a_0 = 0$