## Seriekobling af to modstande: R3=R1+R2

R1=2.4 kOhm+-5% ~U[2280;2520]

$$f_{r1}\left(r_{1}\right)\coloneqq\left\|\begin{array}{c} \text{if } 2280\leq r_{1}\leq 2520\\ \left\|\frac{1}{240}\right\|\\ \text{else}\\ \left\|\begin{array}{c} 0 \end{array}\right\|$$

R2=100 Ohm+-5% ~U[95;105]

$$f_{r2}\left(r_{2}\right)\coloneqq\left\|\begin{array}{c} \text{if } 95\leq r_{2}\leq105\\\\ \left\|\frac{1}{10}\\\\ \text{else}\\ \left\|\begin{array}{c} 0 \end{array}\right.\right\|$$

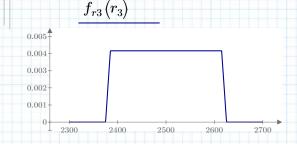
R3=R1+R2: 
$$f_{r3}\left(r_{3}\right) = \int_{0}^{\infty} f_{r1}\left(\rho\right) \cdot f_{r2}\left(r_{3}-\rho\right) d\rho$$

 $2280 \le \rho \le 2520 \quad \text{og} \quad r_3 - 105 \le \rho \le r_3 - 95 \quad \text{(}95 \le r_3 - \rho \le 105\text{)}$ 

$$f_{r3}\left(r_{3}\right)\coloneqq \left\|\begin{array}{l} \text{if } r_{3}<2375\\ 0\\ \text{else if } 2375\leq r_{3}<2385\\ \end{array}\right\|^{r_{3}-95}\\ \int \frac{1}{240}\cdot\frac{1}{10}\,\mathrm{d}\rho \qquad \qquad f_{r31}\left(r_{3}\right)\coloneqq \int \frac{1}{240}\cdot\frac{1}{10}\,\mathrm{d}\rho \to \frac{r_{3}}{2400}-\frac{95}{96}\\ \text{else if } 2385\leq r_{3}\leq 2615\\ \left\|\begin{array}{l} r_{3}-95\\ \int \frac{1}{240}\cdot\frac{1}{10}\,\mathrm{d}\rho \end{array}\right\|^{r_{3}-95}\\ \int \frac{1}{240}\cdot\frac{1}{10}\,\mathrm{d}\rho \qquad \qquad f_{r32}\left(r_{3}\right)\coloneqq \int \frac{1}{240}\cdot\frac{1}{10}\,\mathrm{d}\rho \to \frac{1}{240}\\ \text{else if } 2615< r_{3}\leq 2625\\ \left\|\begin{array}{l} \frac{2520}{r_{3}-105} \end{array}\right\|^{2520}\\ \int \frac{1}{240}\cdot\frac{1}{10}\,\mathrm{d}\rho \qquad \qquad f_{r33}\left(r_{3}\right)\coloneqq \int \frac{1}{240}\cdot\frac{1}{10}\,\mathrm{d}\rho \to \frac{35}{32}-\frac{r_{3}}{2400}\\ \text{else if } r_{3}>2625\\ \left\|\begin{array}{l} 0\\ \end{array}\right\|^{2520}\\ \end{array}$$

$$f_{r31}(r_3) \coloneqq \int \frac{1}{240} \cdot \frac{1}{10} d\rho \to \frac{r_3}{2400} - \frac{95}{96}$$

$$f_{r33}\left(r_{3}\right)\coloneqq\int_{r_{3}-105}^{2520}\frac{1}{240}\cdot\frac{1}{10}\,\mathrm{d}\rho\to\frac{35}{32}-\frac{r_{3}}{2400}$$



$$EZZ \coloneqq \int_{2375}^{2385} r_3^2 \cdot \left( \frac{r_3}{2400} - \frac{95}{96} \right) \mathrm{d}r_3 + \int_{2385}^{2615} r_3^2 \cdot \left( \frac{1}{240} \right) \mathrm{d}r_3 + \int_{2615}^{2625} r_3^2 \cdot \left( -\frac{r_3}{2400} + \frac{35}{32} \right) \mathrm{d}r_3 = 6.255 \cdot 10^6$$

$$EZ \coloneqq \int\limits_{2375}^{2385} r_3 \cdot \left( \frac{r_3}{2400} - \frac{95}{96} \right) \mathrm{d}r_3 + \int\limits_{2385}^{2615} r_3 \cdot \left( \frac{1}{240} \right) \mathrm{d}r_3 + \int\limits_{2615}^{2625} r_3 \cdot \left( -\frac{r_3}{2400} + \frac{35}{32} \right) \mathrm{d}r_3 = 2500$$

$$VarZ := EZZ - EZ^2 = 4808.333$$

$$\sigma_Z = \sqrt{VarZ} = 69.342$$

$$VarU_{2375;2625} = \frac{\left(2625 - 2375\right)^2}{12} = 5208.333$$

$$\sigma_U \coloneqq \sqrt{VarU_{2375;2625}} = 72.169 \quad > \sigma_Z$$

## Seriekobling af to modstande: R3=R1+R2

R1=1.25 kOhm+-5% ~U[1187.5;1312.5]

$$f_{r1}\left(r_{1}\right)\coloneqq\left|\begin{array}{c} \text{if } 1187.5\leq r_{1}\leq1312.5\\ \\ \left\|\begin{array}{c} \underline{1}\\ 125 \end{array}\right|\right|$$
 else 
$$\left\|\begin{array}{c} 0 \end{array}\right|$$

R2=1.25 kOhm+-5% ~U[1187.5;1312.5]

$$f_{r2}\left(r_{2}\right)\coloneqq\left|\begin{array}{c} \text{if } 1187.5\leq r_{2}\leq1312.5\\ \\ \left\|\begin{array}{c} 1\\ 125 \end{array}\right|\right|$$
 else 
$$\left\|\begin{array}{c} 0 \end{array}\right|$$

R3=R1+R2: 
$$f_{r3}\left(r_{3}\right)$$

$$f_{r3}(r_3) = \int_{-\infty}^{\infty} f_{r1}(\rho) \cdot f_{r2}(r_3 - \rho) ds$$

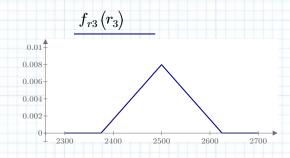
 $f_{r3}\left(r_{3}\right) = \int f_{r1}\left(\rho\right) \cdot f_{r2}\left(r_{3} - \rho\right) \,\mathrm{d}\rho \qquad 1187.5 \leq \rho \leq 1312.5 \quad \text{og } r_{3} - 1312.5 \leq \rho \leq r_{3} - 1187.5 \leq \rho \leq$ 

$$\begin{array}{c|c} f_{r3}\left(r_{3}\right)\coloneqq & \text{if } r_{3}<2375\\ & 0\\ & \text{else if } 2375\leq r_{3}\leq 2500\\ & & \left|\int_{1187.5}^{r_{3}-1187.5} \frac{1}{125} \,\mathrm{d}\rho\\ & & \text{else if } 2500\leq r_{3}\leq 2625\\ & & \left|\int_{1312.5}^{1312.5} \frac{1}{125} \,\mathrm{d}\rho\\ & & \left|\int_{r_{3}-1312.5}^{1312.5} \mathrm{d}\rho\\ & & \text{else if } r_{3}>2625\\ & & 0 \end{array}\right.$$

$$f_{r3}\left(r_{3}\right) \coloneqq \left\| \begin{array}{l} \text{if } r_{3} < 2375 \\ \left\| \begin{array}{l} 0 \\ \text{else if } 2375 \le r_{3} \le 2500 \end{array} \right\| \\ \left\| \begin{array}{l} f_{r31}\left(r_{3}\right) \coloneqq \int \frac{1}{125} \cdot \frac{1}{125} \, \mathrm{d}\rho \\ \left\| \begin{array}{l} \frac{1}{15625} \, \mathrm{d}\rho \end{array} \right\| \\ \left\| \begin{array}{l} \frac{1}{125} \cdot \frac{1}{125} \, \mathrm{d}\rho \end{array} \right\| \\ \left\| \begin{array}{l} f_{r3-1187.5} \\ \left\| \begin{array}{l} \frac{1}{125} \cdot \frac{1}{125} \, \mathrm{d}\rho \end{array} \right\| \\ \left\| \begin{array}{l} f_{r31}\left(r_{3}\right) \coloneqq \frac{1}{125^{2}} \cdot \left(r_{3}-1187.5-1187.5\right) \to \frac{r_{3}}{15625} -0.152 \end{array} \right\|$$

$$f_{r31}\left(r_{3}\right) \coloneqq \frac{1}{125^{2}} \cdot \left(r_{3} - 1187.5 - 1187.5\right) \to \frac{r_{3}}{15625} - 0.152$$

$$f_{r33}\left(r_3\right) \coloneqq \frac{1}{125^2} \cdot \left(1312.5 - \left(r_3 - 1312.5\right)\right) \to 0.168 - \frac{r_3}{15625}$$



$$EZZ \coloneqq \int\limits_{2375}^{2500} r_3^2 \cdot \left(\frac{r_3}{15625} - 0.152\right) \mathrm{d}r_3 + \int\limits_{2500}^{2625} r_3^2 \cdot \left(0.168 - \frac{r_3}{15625}\right) \mathrm{d}r_3 = 6.253 \cdot 10^6$$

$$EZ \coloneqq \int_{2375}^{2500} r_3 \cdot \left( \frac{r_3}{15625} - 0.152 \right) \mathrm{d}r_3 + \int_{2500}^{2625} r_3 \cdot \left( 0.168 - \frac{r_3}{15625} \right) \mathrm{d}r_3 = 2500$$

$$VarZ := EZZ - EZ^2 = 2604.167$$

$$\sigma_Z = \sqrt{VarZ} = 51.031$$

$$VarU_{2375;2625} := \frac{\left(2625 - 2375\right)^2}{12} = 5208.333$$

$$\sigma_U \coloneqq \sqrt{VarU_{2375;2625}} = 72.169 \quad > \sigma_Z$$