Assignment 2

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Question 1

$$(p \to q) \land (p \to r) \equiv p \to (q \land r)$$

Solution:

$$(p \to q) \land (p \to r) \equiv (\neg p \lor q) \land (\neg p \lor r)$$

$$\equiv \neg p \lor (q \land r)$$

$$\equiv p \to (q \land r)$$

Conditional Disjunction Equivalence

By the First Distributive Law

Conditional Conjunction Equivalence

Question 2

$$p \wedge p \equiv p$$

Solution:

$$p \equiv p \wedge T$$

$$\equiv p \wedge (p \vee \neg p)$$

$$\equiv (p \wedge p) \vee (p \wedge \neg p)$$

$$\equiv (p \wedge p) \vee F$$

$$\equiv p \wedge p$$

By the First Identity Law
By the First Negation Law
By the Second Distributive Law
By the Second Negation Law
By the Second Identity Law

Question 3

- 1. $\exists x N(x)$
- 2. $\forall x N(x)$
- 3. $\neg \exists x N(x)$
- 4. $\exists x \neg N(x)$
- 5. $\neg \forall x N(x)$
- 6. $\forall x \neg N(x)$

Solution:

- 1. There are some students in my school that have visited North Dakota
- 2. All students in my school have visited North Dakota
- 3. $\neg \exists x N(x) \equiv \forall x \neg N(x)$. All the students in my class have not visited North Dakota
- 4. There are some students in my school that have not visited North Dakota
- 5. $\neg \forall x N(x) \equiv \exists x \neg N(x)$. There are some students in my school that have not visited North Dakota
- 6. All the students in my class have not visited North Dakota