

Neural Networks

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ARTIFICIAL NEURAL NETWORKS

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CHAPTER 2

DEEP COMPUTER VISION AND CONVOLUTIONAL NEURAL NETWORKS (CNNs)

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Chapter 1

Artificial Neural Networks

An Artificial Neural Network (ANN) is a computational model that is inspired by the way biological neural networks in the human brain work. It is composed of a large number of highly interconnected processing elements (neurons) working in unison to solve specific problems. ANNs, like people, learn by example and are thus capable of solving unsupervised as well as supervised learning tasks.

1.1 Biological Neurons

Artificial Neural Networks being inspired by biological neural networks are composed of neurons, thus to understand the decision designs of ANNs we must first understand the biological neuron. Neurons are made up of three parts, the *soma* or the cell body, the *axon* and *dendrites*. A neuron is a specialized cell responsible for the creation and transportation of short electrical impulses called *action potentials* / AP / signals, used to communicate with other neurons with the overarching goal of transmitting information throughout the body. Through this vast network of neurons, the brain is able to perform highly complex computations. Research shows that neurons in the brain are organized in consecutive layers with each layer performing a specific task. This is the basis of the design of ANNs.

1.2 Logical Computation with Neurons

The Artificial Neuron is designed on this framework of the biological neuron, with a simple ANN proposed by McCulloch and Pitts, having one or more binary inputs and one binary output. The artificial neuron activates its output when more than a certain number of its inputs are active, allowing for simple computation of logical functions, such as propositional logic. For example a simple neuron designed to perform the logical AND operation:

Let the output neuron be *C* and take two input neuron *A* and *B*. As the neuron *C* always requires two input signals to give an output signal we can then require the two input signals to only give one output signal if activated. This would in turn require both neurons *A* and *B* to be activated to give an output signal for neuron *C*, thus performing the logical AND operation.

1.3 The Perceptron

A simple ANN, based on a artificial neuron called a *threshold logic unit* (TLU) / *linear threshold unit* (LTU). It inputs and outputs numbers and each input connection is associated with a weight. The TLU first computes a linear function of its inputs

$$z = w_1x_1 + \dots + w_nx_n + b = \mathbf{w}^T \mathbf{x} + b$$

Where the model parameters are the input weights \mathbf{w} and b is the bias term

It then applies a **step function** to the result

$$h_w(\mathbf{x}) = \text{step}(z)$$

A common step function used in perceptrons is the *Heavyside step function*, and the *sign function* defined:

$$\text{heavyside}(z) = \begin{cases} 0 & \text{if } z < 0 \\ 1 & \text{if } z \geq 0 \end{cases}$$

$$\text{sgn}(z) = \begin{cases} -1 & \text{if } z < 0 \\ 0 & \text{if } z = 0 \\ +1 & \text{if } z > 0 \end{cases}$$

A perceptron is composed of one or more TLUs organized in a single layer, where every TLU is connected to every input. Such a layer is called a fully **connected layer** or a **dense layer**, and the inputs constitute the **input layer**. As the final layer of TLU's produce the output this layer is called the **output layer**.

Using linear algebra the outputs of nodes in the output layers, for several instances at once, i.e.:

$$h_{W,b}(X) = \phi(XW + b)$$

Where:

- W is a matrix containing all the connection weights, with one row per unit and one column per node.
- X is a matrix containing the input features, with one row per instance and one column per feature, where each instance is a data point.
- b is the bias vector that contains all the bias terms, one entry per neuron, where each entry in b is broadcasted across the rows of XW .
- ϕ is the **activation function**, but when the artificial neurons are TLUs this is termed as the step function

The perceptron training algorithm is largely inspired by Hebb's rule, which suggests that when neurons on either side of a synapse or in the case of artificial neurons connection, fire together the connection between them is strengthened. This results in the strengthening of connections that help reduce the error in the output layer.

The perceptron is fed one training instance at a time and for each instance it makes predictions. For every output neuron that produced a wrong prediction, it reinforces the connection weights from the inputs that would have contributed to the correct prediction. The rule is as follows:

$$w_{i,j}^{\text{next step}} = w_{i,j} + \eta(y_j - \hat{y}_j)x_i$$

Where:

- $w_{i,j}$ is the connection weight between the i th input neuron and the j th neuron.
- x_i is the i th input value of the current training instance.
- \hat{y}_j is the output of the j th output neuron for the current training instance.
- y_j is the target output of the j th output neuron for the current training instance.
- η is the learning rate.

The decision boundary of each output neuron is linear, so perceptrons are incapable of learning complex patterns (just like logistic regression classifiers). However, if the training instances are linearly separable, Rosenblatt demonstrated that this algorithm would converge to a solution. This is called the **perceptron convergence theorem**.

```
[1]: import sys

!{sys.executable} -m pip install pydot
```

```
Requirement already satisfied: pydot in
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (2.0.0)
Requirement already satisfied: pyparsing≥3 in
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from pydot) (3.1.2)
```

```
[notice] A new release of pip is
available: 24.2 -> 24.3.1
[notice] To update, run:
pip install --upgrade pip
```

```
[2]: import numpy as np
      from sklearn.datasets import load_iris
      from sklearn.linear_model import Perceptron

      iris = load_iris(as_frame=True)
      X = iris.data[["petal length (cm)", "petal width (cm)"]].values
      y = iris.target == 0

      per = Perceptron(random_state=42)
      per.fit(X, y)

      XNew = [[2, 0.5], [3, 1]]
      per.predict(XNew)
```

```
[2]: array([ True, False])
```

1.4 Multilayer Perceptron (MLP) and Backpropagation

An MLP is composed of one input layer, one or more layers of TLUs called *hidden layers* and one output layer, also comprised of TLUs. Layers close the input layers are called the *lower layers* and those close to the output layers are called *upper layers*.

When signals only flow from the input layer across, hidden layers and finally stopping at the output layers, i.e one direction, the resulting architecture is called a **Feedforward Neural Network (FNN)**.

When an ANN contains a deep stack of hidden layers, it is called a **Deep Neural Network (DNN)**. A deep stack is when the number of hidden layers is large, typically more than 10.

Using the *reverse-mode automatic differentiation / reverse-mode autodiff* algorithm the gradient of a ANN's error in relation to the parameters it's given can be computed. Using this gradient it is possible to perform gradient descent to find the optimal weights and biases for the ANN, i.e. the parameters that minimize the error. This combination of both the reverse-mode autodiff and gradient descent is called **Backpropagation**.

Going into detail the Backpropagation algorithm is as follows:

- A mini-batch (for example 32 instances) of the training data is used at a time, and the algorithm goes through the full training data several times. Each time through the full training data is called an **epoch**.
- Each mini-batch enters the network through the input layer, then the output of the all the neurons in the first hidden layer is computed for each instance in the mini-batch. The result is then passed to the subsequent hidden layer and computed so on until the output layer is reached. This is called a **forward pass**, where the model makes predictions but all the intermediate results between hidden layers are stored for use in the backwards pass.
- The algorithm then calculates the model's output error, using a loss function that compares the result to the desired output of the network for the given parameters and returns the measure of the error.

- Then it computes how much each output bias and each connection to the output layer contributed to the error, by analytically applying the chain rule.
- The algorithm then measures how much of these error contributions came from each connection in the layer below, again using the chain rule, working backwards until it reaches the input layer. This is called the **backward / reverse pass**.
- Finally the algorithm performs a gradient descent step to tweak all the connections in the network, using the error contributions computed earlier. This is called the **gradient descent step**.

In order for Backpropagation to work properly it needs a gradient to work with, thus the step functions normally used in single layer perceptrons are replaced with differentiable functions, such as the **logistic / sigmoid function**, **hyperbolic tangent function** and the **rectified linear unit function (ReLU)**, defined below:

$$\text{sigmoid}(z) = \frac{1}{1 + \exp(-z)}$$

$$\tanh(z) = 2\sigma(2z) - 1$$

$$\text{ReLU}(z) = \max(0, z)$$

1.5 Regression MLPs

Hyperparameter	Typical Value
# hidden layers	Depends on the problem typically 1 - 5
# neurons per hidden layer	Depends on the problem typically 10 - 100
# output neurons	1 per prediction dimension
hidden activation	ReLU
output activation	None, or ReLU/ softplus if positive outputs or sigmoid / tanhn if bounded
Loss function	MSE, or huber if outliers

```
[3]: from sklearn.datasets import fetch_california_housing
from sklearn.neural_network import MLPRegressor
from sklearn.pipeline import Pipeline, make_pipeline
from sklearn.preprocessing import StandardScaler
from sklearn.metrics import root_mean_squared_error
from sklearn.model_selection import train_test_split

housing = fetch_california_housing()
XTrainFull, XTest, yTrainFull, yTest = train_test_split(
    housing.data, housing.target, random_state=42
)
XTrain, XValid, yTrain, yValid = train_test_split(
    XTrainFull, yTrainFull, random_state=42
)

mlpReg = MLPRegressor(
    hidden_layer_sizes=[50, 50, 50], random_state=42, activation="relu"
)
mlpRegPipe = make_pipeline(StandardScaler(), mlpReg)
```

```
mlpRegPipe.fit(XTrain, yTrain)
```

```
/home/mads/.pyenv/versions/ai/lib/python3.12/site-  
packages/sklearn/neural_network/_multilayer_perceptron.py:697: UserWarning:  
Training interrupted by user.
```

```
warnings.warn("Training interrupted by user.")
```

```
[3]: Pipeline(steps=[('standardscaler', StandardScaler()),  
                      ('mlpregressor',  
                       MLPRegressor(hidden_layer_sizes=[50, 50, 50],  
                                    random_state=42))])
```

```
[ ]: preds = mlpRegPipe.predict(XValid)  
rmse = root_mean_squared_error(yValid, preds)  
rmse
```

```
[ ]: 0.5053326657968522
```

1.6 Classification MLPs

For binary classification the output neuron has to have a bounded activation function like sigmoid so the output will be a number between 0 and 1, which can be interpreted as the estimated probability of the positive class. The estimated probability of the negative class is equal to one minus that number.

For multilabel binary classification the output layer should have one output neuron per class, and each neuron should have a sigmoid activation function, where the first neuron predicts the probability of the first class, the second neuron the probability of the second class and so on.

If each instance can only belong to one category out of all the possible categories, then the output layer should have one neuron per class and use the **softmax** activation function for the whole output layer. This ensures that the sum of all the estimated class probabilities for each instance is equal to one, and that the estimated class probabilities are all non-negative.

Hyperparameter	Binary Classification	Multilabel Binary Classification	Multiclass Classification
# hidden layers	Typically 1 - 5 layers, depending on the task	Typically 1 - 5 layers, depending on the task	Typically 1 - 5 layers, depending on the task
# output neurons	1	1 per binary label	1 per class
Output activation	Sigmoid	Sigmoid	Softmax
Loss function	Cross-entropy	Cross-entropy	Cross-entropy

```
[ ]: from sklearn.datasets import load_iris  
from sklearn.neural_network import MLPClassifier  
from sklearn.metrics import classification_report, ConfusionMatrixDisplay  
  
iris = load_iris()  
XTrainFull, XTest, yTrainFull, yTest = train_test_split(  
    iris.data, iris.target, random_state=42  
)  
XTrain, XValid, yTrain, yValid = train_test_split(  
    XTrainFull, yTrainFull, random_state=42  
)
```

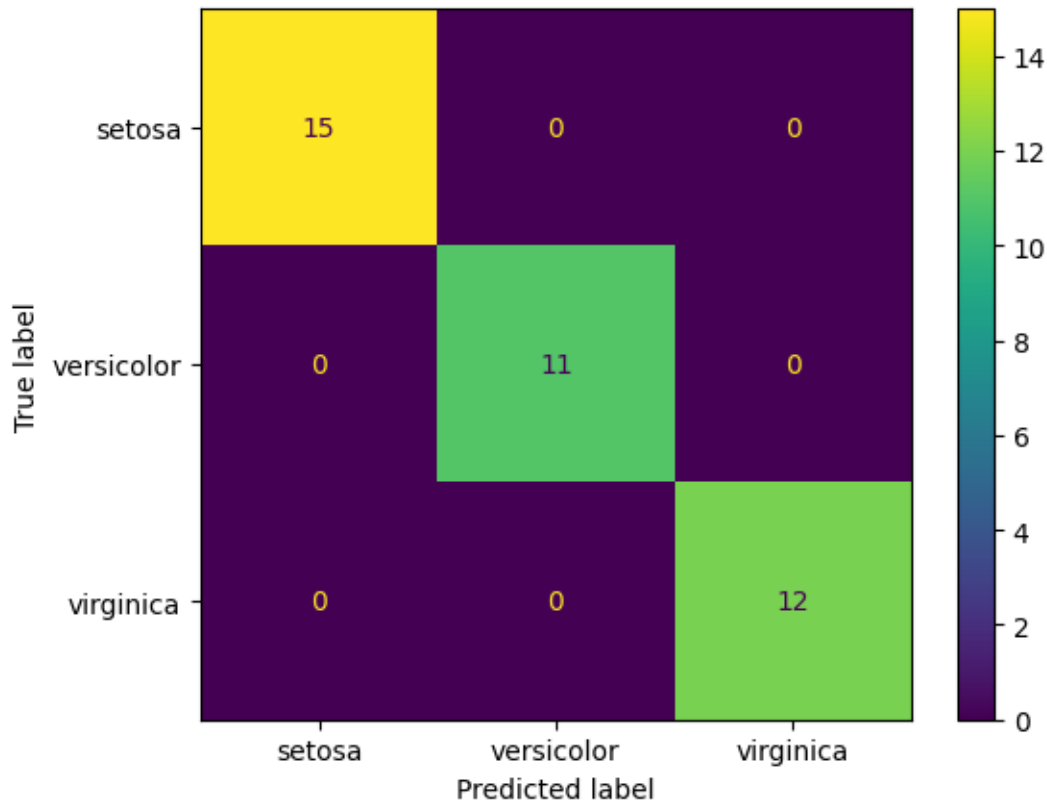
```
mlpCls = MLPClassifier(hidden_layer_sizes=[10], max_iter=10000,
    random_state=42)
mlpClsPipe = make_pipeline(StandardScaler(), mlpCls)
mlpClsPipe.fit(XTrain, yTrain)
```

```
[ ]: Pipeline(steps=[('standardscaler', StandardScaler()),
    ('mlpclassifier',
    MLPClassifier(hidden_layer_sizes=[10], max_iter=10000,
    random_state=42))])
```

```
[ ]: preds = mlpClsPipe.predict(XTest)
print(classification_report(yTest, preds))
ConfusionMatrixDisplay.from_predictions(yTest, preds, display_labels=iris.
    target_names)
```

	precision	recall	f1-score	support
0	1.00	1.00	1.00	15
1	1.00	1.00	1.00	11
2	1.00	1.00	1.00	12
accuracy			1.00	38
macro avg	1.00	1.00	1.00	38
weighted avg	1.00	1.00	1.00	38

```
[ ]: <sklearn.metrics._plot.confusion_matrix.ConfusionMatrixDisplay at
0x72e040109430>
```

1.7 Implementing MLPs in Keras

1.7.1 Building an Image Classifier using the Sequential API

```
[ ]: import tensorflow as tf
```

```
fmnist = tf.keras.datasets.fashion_mnist.load_data()
(XTrainFull, yTrainFull), (XTest, yTest) = fmnist
```

```
cutoff = -5000
```

```
XTrain, yTrain = XTrainFull[:cutoff], yTrainFull[:cutoff]
```

```
XValid, yValid = XTrainFull[cutoff:], yTrainFull[cutoff:]
```

```
XTrain.shape
```

```
2024-07-23 12:14:52.971955: I tensorflow/core/util/port.cc:113] oneDNN custom
operations are on. You may see slightly different numerical results due to
floating-point round-off errors from different computation orders. To turn them
off, set the environment variable 'TF_ENABLE_ONEDNN_OPTS=0'.
```

```
2024-07-23 12:14:52.980310: I external/local_tsl/tsl/cuda/cudart_stub.cc:32]
Could not find cuda drivers on your machine, GPU will not be used.
```

```
2024-07-23 12:14:53.063492: I external/local_tsl/tsl/cuda/cudart_stub.cc:32]
Could not find cuda drivers on your machine, GPU will not be used.
```

```
2024-07-23 12:14:53.161670: E
external/local_xla/xla/stream_executor/cuda/cuda_fft.cc:479] Unable to register
```

```

cuFFT factory: Attempting to register factory for plugin cuFFT when one has
already been registered
2024-07-23 12:14:53.250069: E
external/local_xla/xla/stream_executor/cuda/cuda_dnn.cc:10575] Unable to
register cuDNN factory: Attempting to register factory for plugin cuDNN when one
has already been registered
2024-07-23 12:14:53.250963: E
external/local_xla/xla/stream_executor/cuda/cuda_blas.cc:1442] Unable to
register cuBLAS factory: Attempting to register factory for plugin cuBLAS when
one has already been registered
2024-07-23 12:14:53.390184: I tensorflow/core/platform/cpu_feature_guard.cc:210]
This TensorFlow binary is optimized to use available CPU instructions in
performance-critical operations.
To enable the following instructions: AVX2 AVX512F AVX512_VNNI FMA, in other
operations, rebuild TensorFlow with the appropriate compiler flags.
2024-07-23 12:14:54.502765: W
tensorflow/compiler/tf2tensorrt/utils/py_utils.cc:38] TF-TRT Warning: Could not
find TensorRT

```

```
[ ]: (55000, 28, 28)
```

```

[ ]: XTrain, XValid, XTest = XTrain / 255.0, XValid / 255.0, XTest / 255.0
classNames = [
    "T-shirt/top",
    "Trouser",
    "Pullover",
    "Dress",
    "Coat",
    "Sandal",
    "Shirt",
    "Sneaker",
    "Bag",
    "Ankle boot",
]

def name(x):
    return classNames[x]

name(yTrain[0])

```

```
[ ]: 'Ankle boot'
```

```

[ ]: # Set random seed for reproducible results
tf.keras.utils.set_random_seed(42)

# Create a Sequential model a single stack of layers connected sequentially
cls = tf.keras.Sequential()

# The first layer, an Input layer, added to the model with shape
# 28x28, needed to determine the shape of the weight matrix of the
# first hidden layer

```

```

cls.add(tf.keras.layers.Input(shape=[28, 28]))

# A Flatten layer to convert the input images into 1D arrays
cls.add(tf.keras.layers.Flatten())

# A Dense layer with 300 neurons, using the ReLU activation function
# Each Dense layer manages it's own weight matrix containing the connection_
  ↳ weights
# between neurons and their inputs
cls.add(tf.keras.layers.Dense(300, activation="relu"))

# A second Dense layer with 100 neurons, also using the ReLU activation_
  ↳ function
cls.add(tf.keras.layers.Dense(100, activation="relu"))

# A final Dense layer as the output layer with 10 neurons, one per category
# And using the softmax activation function as classes are exclusive
cls.add(tf.keras.layers.Dense(10, activation="softmax"))
cls.summary()

```

Model: "sequential"

Layer (type)	Output Shape	Param #
flatten (Flatten)	(None, 784)	0
dense (Dense)	(None, 300)	235,500
dense_1 (Dense)	(None, 100)	30,100
dense_2 (Dense)	(None, 10)	1,010

Total params: 266,610 (1.02 MB)

Trainable params: 266,610 (1.02 MB)

Non-trainable params: 0 (0.00 B)

These steps can be condensed as seen below with the first **Input** layer dropped and the **input_shape** specified in the first layer

```

[ ]: cls = tf.keras.Sequential(
    [
        tf.keras.layers.Input(shape=[28, 28]),
        tf.keras.layers.Flatten(),
        tf.keras.layers.Dense(300, activation="leaky_relu"),
        tf.keras.layers.Dense(100, activation="leaky_relu"),

```

Model: "sequential_1"

Total params: 266,610 (1.02 MB)

Trainable params: 266,610 (1.02 MB)

Non-trainable params: 0 (0.00 B)

```
[<Flatten name=flatten_1, built=True>,  
<Dense name=dense_3, built=True>,  
<Dense name=dense_4, built=True>,  
<Dense name=dense_5, built=True>]
```

11

```
0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0.,
0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0.,
0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0.,
0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., dtype=float32)
```

1.7.1.1 Compiling the Model


```
[ ]: # Loss - Specifies the loss function to use when minimizing the value of the_
      ↳loss function
# Optimize - Specifies the optimization algorithm to use in reducing the loss_
      ↳function
# Metrics - Specifies other metrics to monitor during training and testing
cls.compile(
    loss="sparse_categorical_crossentropy",
    optimizer=tf.keras.optimizers.SGD(),
    metrics=["accuracy"],
)
```


- We use **sparse_categorical_crossentropy** loss as we have sparse labels, for each instance there is just a target class index from 0 to 9, and the classes are exclusive. If we instead had one target probability per class for each instance for example when using One Hot Encoding, we would use **categorical_crossentropy** loss. When doing binary classification or multilabel binary classification we would use the **binary_crossentropy** loss
- The optimizer **sgd** stands for *Stochastic Gradient Descent*, and means the model will be trained using this gradient descent variant. The **sgd** optimizer will perform the backpropagation algorithm. When using the **sdg** optimizer it is important to set a learning rate, this can be done by passing **tf.keras.optimizers.SGD(learning_rate=x)** where **x** is the learning rate


1.7.1.2 Training and Evaluating the Model


```
[ ]: hist = cls.fit(XTrain, yTrain, epochs=30, validation_data=(XValid, yValid))
```


```
Epoch 1/30
1719/1719 ————— 3s 2ms/step -
accuracy: 0.6862 - loss: 0.9684 - val_accuracy: 0.8304 - val_loss: 0.5021
Epoch 2/30
1719/1719 ————— 3s 2ms/step -
accuracy: 0.8262 - loss: 0.5073 - val_accuracy: 0.8400 - val_loss: 0.4540
Epoch 3/30
1719/1719 ————— 3s 1ms/step -
accuracy: 0.8420 - loss: 0.4570 - val_accuracy: 0.8466 - val_loss: 0.4333
Epoch 4/30
1719/1719 ————— 3s 2ms/step -
accuracy: 0.8505 - loss: 0.4295 - val_accuracy: 0.8470 - val_loss: 0.4207
Epoch 5/30
1719/1719 ————— 3s 2ms/step -
accuracy: 0.8570 - loss: 0.4097 - val_accuracy: 0.8506 - val_loss: 0.4106
Epoch 6/30
1719/1719 ————— 3s 2ms/step -
accuracy: 0.8618 - loss: 0.3941 - val_accuracy: 0.8528 - val_loss: 0.4020
Epoch 7/30
1719/1719 ————— 3s 2ms/step -
accuracy: 0.8670 - loss: 0.3810 - val_accuracy: 0.8552 - val_loss: 0.3963
```


Epoch 8/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8704 - loss: 0.3696 - val_accuracy: 0.8564 - val_loss: 0.3912


Epoch 9/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8732 - loss: 0.3596 - val_accuracy: 0.8582 - val_loss: 0.3856


Epoch 10/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8758 - loss: 0.3507 - val_accuracy: 0.8602 - val_loss: 0.3817


Epoch 11/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8784 - loss: 0.3426 - val_accuracy: 0.8634 - val_loss: 0.3768


Epoch 12/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8806 - loss: 0.3350 - val_accuracy: 0.8644 - val_loss: 0.3739


Epoch 13/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8829 - loss: 0.3280 - val_accuracy: 0.8654 - val_loss: 0.3708


Epoch 14/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8845 - loss: 0.3213 - val_accuracy: 0.8658 - val_loss: 0.3687


Epoch 15/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8863 - loss: 0.3152 - val_accuracy: 0.8668 - val_loss: 0.3667


Epoch 16/30
1719/1719  **3s** 1ms/step -
accuracy: 0.8884 - loss: 0.3093 - val_accuracy: 0.8666 - val_loss: 0.3629


Epoch 17/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8900 - loss: 0.3037 - val_accuracy: 0.8674 - val_loss: 0.3609


Epoch 18/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8918 - loss: 0.2984 - val_accuracy: 0.8678 - val_loss: 0.3598


Epoch 19/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8938 - loss: 0.2934 - val_accuracy: 0.8686 - val_loss: 0.3590


Epoch 20/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8958 - loss: 0.2885 - val_accuracy: 0.8686 - val_loss: 0.3580

Epoch 21/30
1719/1719  **3s** 2ms/step -
accuracy: 0.8979 - loss: 0.2838 - val_accuracy: 0.8700 - val_loss: 0.3593

Epoch 22/30
1719/1719  **3s** 2ms/step -
accuracy: 0.9001 - loss: 0.2792 - val_accuracy: 0.8694 - val_loss: 0.3567

Epoch 23/30
1719/1719  **3s** 2ms/step -
accuracy: 0.9014 - loss: 0.2748 - val_accuracy: 0.8704 - val_loss: 0.3590

Epoch 24/30
1719/1719  **3s** 1ms/step -
accuracy: 0.9030 - loss: 0.2707 - val_accuracy: 0.8722 - val_loss: 0.3579

Epoch 25/30
1719/1719  **3s** 2ms/step -
accuracy: 0.9044 - loss: 0.2666 - val_accuracy: 0.8722 - val_loss: 0.3559

```

Epoch 26/30
1719/1719 ————— 3s 2ms/step -
accuracy: 0.9056 - loss: 0.2627 - val_accuracy: 0.8712 - val_loss: 0.3577
Epoch 27/30
1719/1719 ————— 3s 2ms/step -
accuracy: 0.9070 - loss: 0.2589 - val_accuracy: 0.8710 - val_loss: 0.3560
Epoch 28/30
1719/1719 ————— 3s 2ms/step -
accuracy: 0.9086 - loss: 0.2552 - val_accuracy: 0.8714 - val_loss: 0.3571
Epoch 29/30
1719/1719 ————— 3s 2ms/step -
accuracy: 0.9099 - loss: 0.2516 - val_accuracy: 0.8722 - val_loss: 0.3569
Epoch 30/30
1719/1719 ————— 3s 2ms/step -
accuracy: 0.9115 - loss: 0.2480 - val_accuracy: 0.8730 - val_loss: 0.3553

```

```

[ ]: import matplotlib.pyplot as plt
from sklearn.metrics import classification_report, ConfusionMatrixDisplay

def classStats(actuals, preds, classNames):
    print(classification_report(actuals, preds))
    fig, ax = plt.subplots(figsize=(10, 6))
    ConfusionMatrixDisplay.from_predictions(
        actuals, preds, display_labels=classNames, ax=ax
    )

preds = cls.predict(XTest)
preds = preds.argmax(axis=1)

classStats(yTest, preds, classNames)

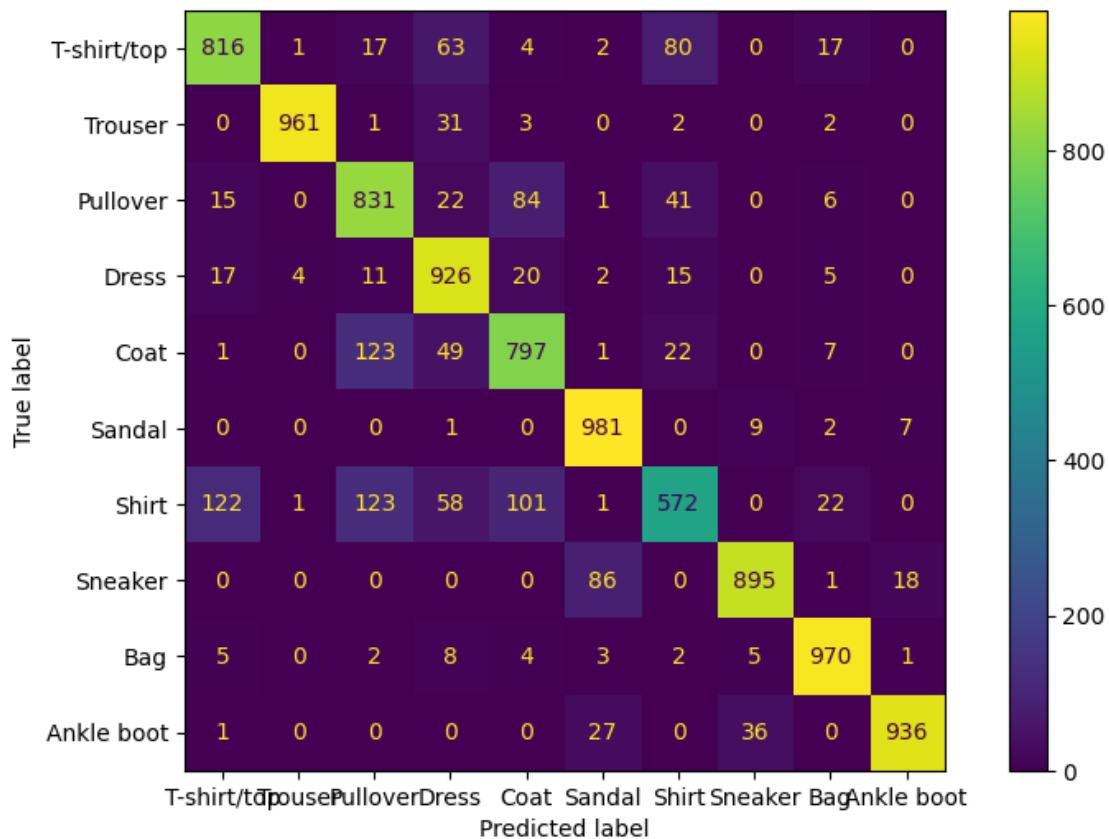
```

```

313/313 ————— 0s 972us/step

```

	precision	recall	f1-score	support
0	0.84	0.82	0.83	1000
1	0.99	0.96	0.98	1000
2	0.75	0.83	0.79	1000
3	0.80	0.93	0.86	1000
4	0.79	0.80	0.79	1000
5	0.89	0.98	0.93	1000
6	0.78	0.57	0.66	1000
7	0.95	0.90	0.92	1000
8	0.94	0.97	0.95	1000
9	0.97	0.94	0.95	1000
accuracy			0.87	10000
macro avg	0.87	0.87	0.87	10000
weighted avg	0.87	0.87	0.87	10000



If the training data was very skewed, with over/under-representation of some classes you can set the **class_weight** argument in the **fit** method to give a larger weight to underrepresented classes and a smaller weight to overrepresented classes. This is used when computing loss during training, so the model gives more importance to underrepresented classes. If per instance weights are needed the **sample_weight** argument can be used. When both **class_weight** and **sample_weight** are used the weights are multiplied. For example if you wanted to give more weight to more recent data you could use **sample_weight** and if you wanted to give more weight to underrepresented classes you could use **class_weight**.

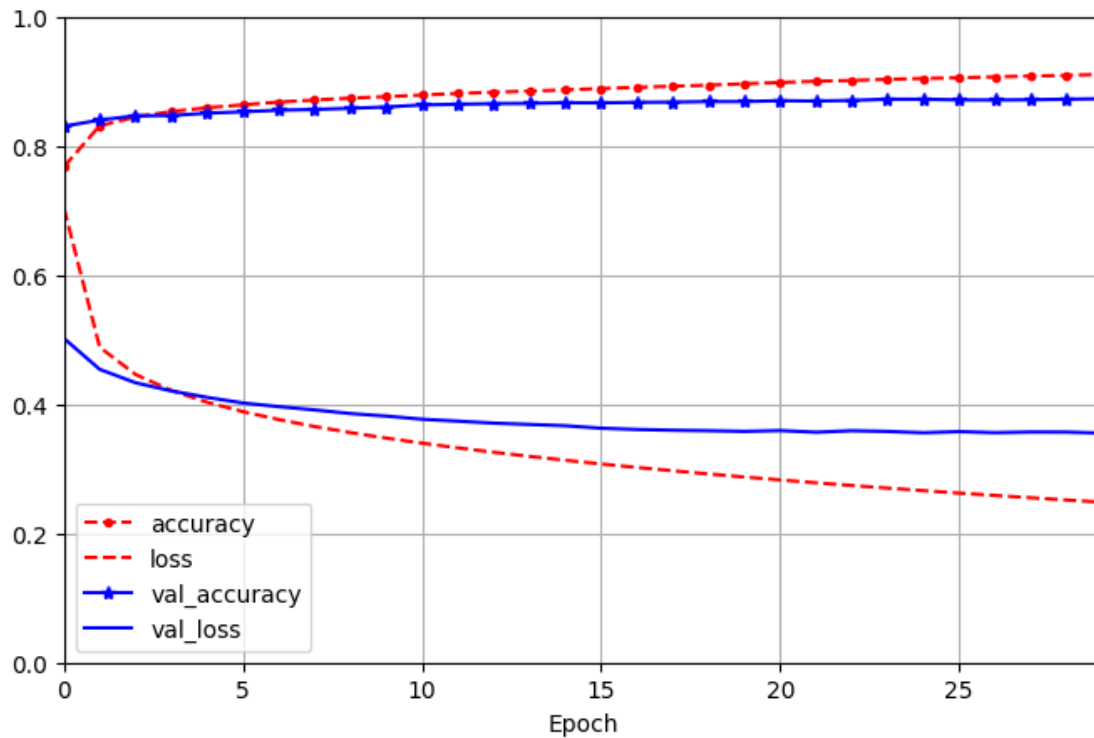
The **fit()** method returns a **History** object containing the training parameters (**history.params**), the list of epochs it went through (**history.epoch**) and a dictionary (**history.history**) containing the loss and extra metrics it measured at the end of each epoch on the training set and on the validation set. You can use the **history.history** dictionary to plot the learning curves.

```
[ ]: import pandas as pd

pd.DataFrame(hist.history).plot(
    figsize=(8, 5),
    xlim=[0, 29],
    ylim=[0, 1],
    grid=True,
    xlabel="Epoch",
    style=["r--.", "r--", "b-*", "b-"],
)
```



```
[ ]: <Axes: xlabel='Epoch'>
```



```
[ ]: hist = cls.fit(XTrain, yTrain, epochs=5, validation_data=(XValid, yValid))
```

```
Epoch 1/5
1719/1719 ————— 3s 2ms/step -
accuracy: 0.9135 - loss: 0.2446 - val_accuracy: 0.8724 - val_loss: 0.3561
Epoch 2/5
1719/1719 ————— 3s 1ms/step -
accuracy: 0.9147 - loss: 0.2414 - val_accuracy: 0.8734 - val_loss: 0.3570
Epoch 3/5
1719/1719 ————— 3s 1ms/step -
accuracy: 0.9158 - loss: 0.2381 - val_accuracy: 0.8736 - val_loss: 0.3571
Epoch 4/5
1719/1719 ————— 3s 2ms/step -
accuracy: 0.9167 - loss: 0.2350 - val_accuracy: 0.8730 - val_loss: 0.3584
Epoch 5/5
1719/1719 ————— 3s 2ms/step -
accuracy: 0.9178 - loss: 0.2319 - val_accuracy: 0.8734 - val_loss: 0.3590
```

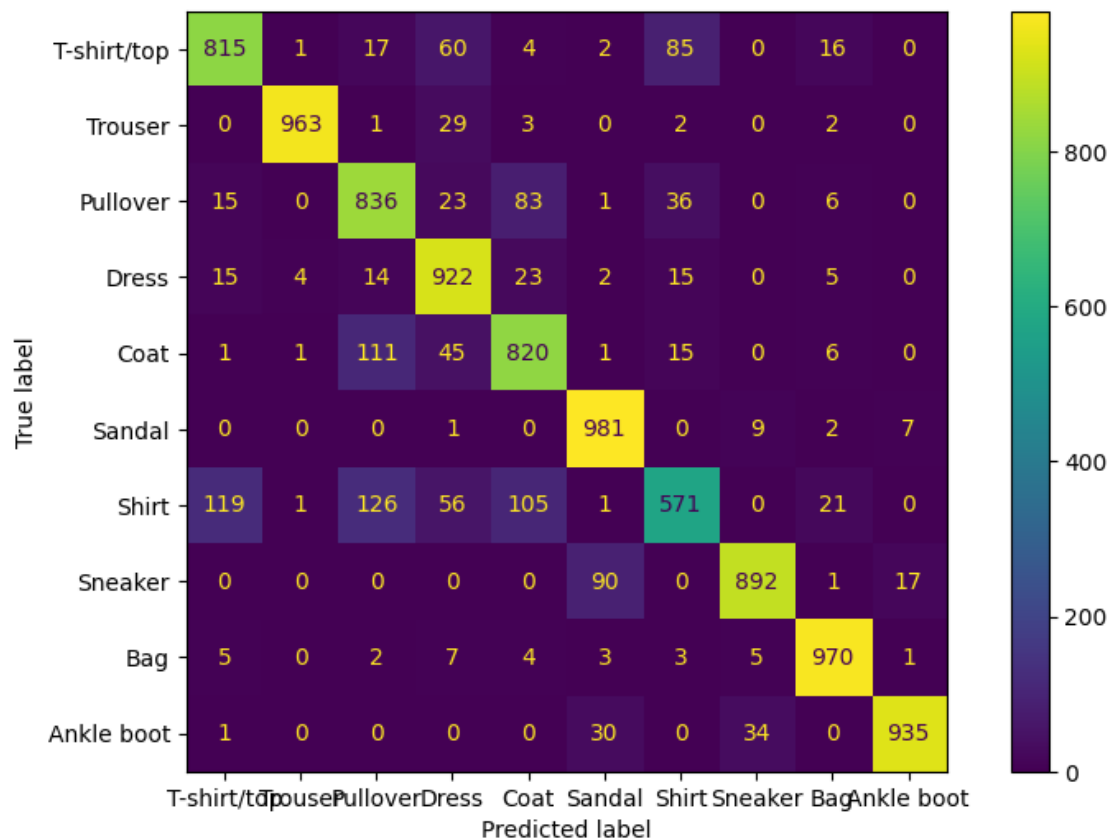
```
[ ]: preds = cls.predict(XTest)
     preds = preds.argmax(axis=1)

     display(cls.evaluate(XTest, yTest))
     classStats(yTest, preds, classNames)
```

```
313/313 ————— 0s 903us/step
```

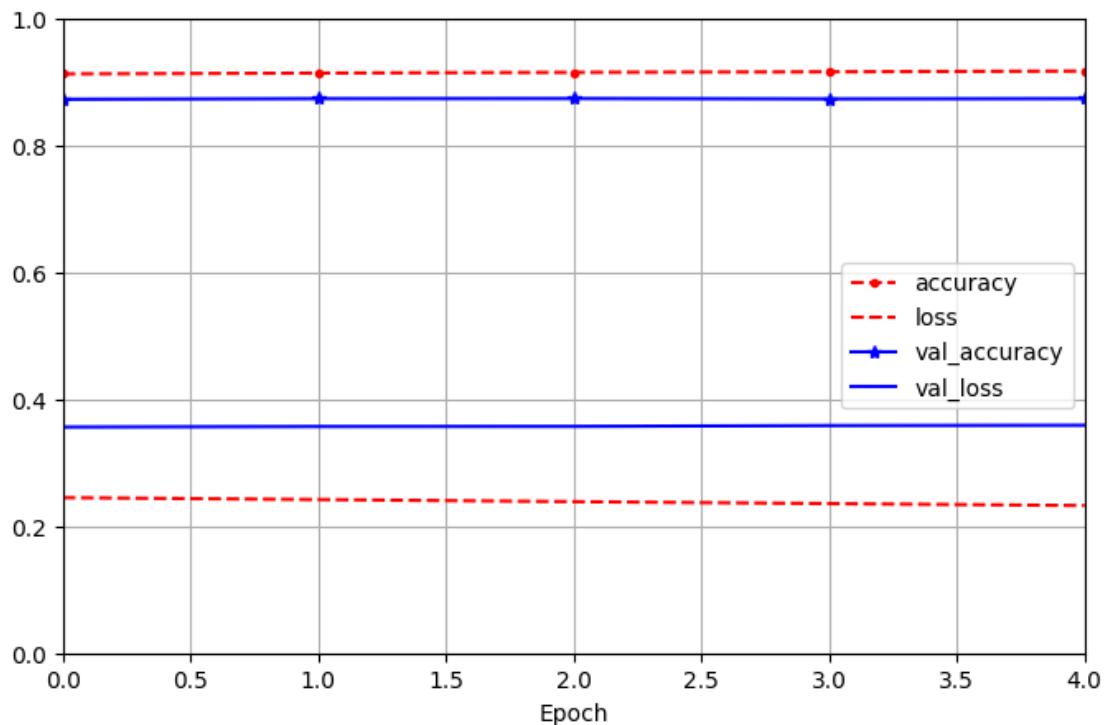
313/313 ————— 0s 829us/step -
accuracy: 0.8727 - loss: 0.3713
[0.3727381229400635, 0.8705000281333923]

	precision	recall	f1-score	support
0	0.84	0.81	0.83	1000
1	0.99	0.96	0.98	1000
2	0.76	0.84	0.79	1000
3	0.81	0.92	0.86	1000
4	0.79	0.82	0.80	1000
5	0.88	0.98	0.93	1000
6	0.79	0.57	0.66	1000
7	0.95	0.89	0.92	1000
8	0.94	0.97	0.96	1000
9	0.97	0.94	0.95	1000
accuracy			0.87	10000
macro avg	0.87	0.87	0.87	10000
weighted avg	0.87	0.87	0.87	10000



```
[ ]: pd.DataFrame(hist.history).plot(
    figsize=(8, 5),
    xlim=[0, 4],
    ylim=[0, 1],
    grid=True,
    xlabel="Epoch",
    style=["r--.", "r--", "b-*", "b-"],
)
```

```
[ ]: <Axes: xlabel='Epoch'>
```



1.7.2 Building a Regression MLP using the Sequential API

```
[ ]: tf.keras.utils.set_random_seed(42)

housing = fetch_california_housing()
XTrainFull, XTest, yTrainFull, yTest = train_test_split(
    housing.data, housing.target, random_state=42
)
XTrain, XValid, yTrain, yValid = train_test_split(
    XTrainFull, yTrainFull, random_state=42
)
```

```
[ ]: norm = tf.keras.layers.Normalization()

reg = tf.keras.Sequential(
```

```
[
    tf.keras.layers.Input(shape=XTrain.shape[1:]),
    norm,
    tf.keras.layers.Dense(50, activation="relu"),
    tf.keras.layers.Dense(50, activation="relu"),
    tf.keras.layers.Dense(50, activation="relu"),
    tf.keras.layers.Dense(1),
]
```

```
[ ]: opt = tf.keras.optimizers.Adam(learning_rate=1e-3)
reg.compile(loss="mse", optimizer=opt, metrics=["RootMeanSquaredError"])
```

```
[ ]: reg.summary()
```

Model: "sequential_2"

Layer (type)	Output Shape	Param #
normalization (Normalization)	(None, 8)	17
dense_6 (Dense)	(None, 50)	450
dense_7 (Dense)	(None, 50)	2,550
dense_8 (Dense)	(None, 50)	2,550
dense_9 (Dense)	(None, 1)	51

Total params: 5,618 (21.95 KB)

Trainable params: 5,601 (21.88 KB)

Non-trainable params: 17 (72.00 B)

```
[ ]: norm.adapt(XTrain)
hist = reg.fit(XTrain, yTrain, epochs=20, validation_data=(XValid, yValid))
```

Epoch 1/20


363/363  1s 1ms/step -


RootMeanSquaredError: 1.2143 - loss: 1.5762 - val_RootMeanSquaredError: 0.6527 - val_loss: 0.4261


Epoch 2/20


363/363  0s 944us/step -


RootMeanSquaredError: 0.6372 - loss: 0.4066 - val_RootMeanSquaredError: 0.5933 - val_loss: 0.3521


Epoch 3/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.6074 - loss: 0.3692 - val_RootMeanSquaredError: 0.6970 -
 val_loss: 0.4858


Epoch 4/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5922 - loss: 0.3509 - val_RootMeanSquaredError: 0.7863 -
 val_loss: 0.6183


Epoch 5/20
363/363  0s 995us/step -
 RootMeanSquaredError: 0.5808 - loss: 0.3375 - val_RootMeanSquaredError: 1.1434 -
 val_loss: 1.3074


Epoch 6/20
363/363  0s 994us/step -
 RootMeanSquaredError: 0.5719 - loss: 0.3272 - val_RootMeanSquaredError: 1.3506 -
 val_loss: 1.8242


Epoch 7/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5658 - loss: 0.3202 - val_RootMeanSquaredError: 0.7185 -
 val_loss: 0.5162


Epoch 8/20
363/363  0s 989us/step -
 RootMeanSquaredError: 0.5564 - loss: 0.3096 - val_RootMeanSquaredError: 0.8469 -
 val_loss: 0.7172


Epoch 9/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5513 - loss: 0.3040 - val_RootMeanSquaredError: 0.6418 -
 val_loss: 0.4119


Epoch 10/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5463 - loss: 0.2985 - val_RootMeanSquaredError: 0.6756 -
 val_loss: 0.4564


Epoch 11/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5426 - loss: 0.2944 - val_RootMeanSquaredError: 0.7295 -
 val_loss: 0.5321

Epoch 12/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5396 - loss: 0.2912 - val_RootMeanSquaredError: 1.0084 -
 val_loss: 1.0169





Epoch 13/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5377 - loss: 0.2891 - val_RootMeanSquaredError: 0.6520 -
 val_loss: 0.4251

Epoch 14/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5341 - loss: 0.2853 - val_RootMeanSquaredError: 1.0415 -
 val_loss: 1.0847

Epoch 15/20
363/363  0s 974us/step -
 RootMeanSquaredError: 0.5318 - loss: 0.2828 - val_RootMeanSquaredError: 0.7899 -
 val_loss: 0.6239

Epoch 16/20
363/363  0s 1ms/step -


```

RootMeanSquaredError: 0.5298 - loss: 0.2807 - val_RootMeanSquaredError: 1.1863 -
val_loss: 1.4073
Epoch 17/20
363/363  0s 979us/step -
RootMeanSquaredError: 0.5282 - loss: 0.2790 - val_RootMeanSquaredError: 0.5334 -
val_loss: 0.2845
Epoch 18/20
363/363  0s 953us/step -
RootMeanSquaredError: 0.5241 - loss: 0.2748 - val_RootMeanSquaredError: 0.5660 -
val_loss: 0.3204
Epoch 19/20
363/363  0s 946us/step -
RootMeanSquaredError: 0.5215 - loss: 0.2720 - val_RootMeanSquaredError: 0.5181 -
val_loss: 0.2684
Epoch 20/20
363/363  0s 953us/step -
RootMeanSquaredError: 0.5194 - loss: 0.2698 - val_RootMeanSquaredError: 0.5378 -
val_loss: 0.2893

```

```
[ ]: mse, rmse = reg.evaluate(XTest, yTest)
```

```

162/162  0s 603us/step -
RootMeanSquaredError: 0.5235 - loss: 0.2742

```

```
[ ]: XNew = XTest[:3]
      preds = reg.predict(XNew)
      preds.round(2)
```

```
1/1  0s 51ms/step
```

```
[ ]: array([[0.47],
           [1.2 ],
           [4.8 ]], dtype=float32)
```

1.7.3 Building Complex Models using the Functional API

An example of a non-sequential neural network is a *Wide & Deep* neural network, where all or part of the inputs are connected directly to the output layer. This makes it possible for the network to learn both deep patterns (using the deep path) and simple rules (through the short path). In contrast a regular MLP forces all the data to flow through the deep path, thus simple patterns in the data may end up being distorted by this sequence of transformations.

```
[ ]: from functools import partial
      from tensorflow.keras.layers import Normalization, Dense, Concatenate, Input

      hidLay = partial(Dense, units=30, activation="relu")

      normLayer = Normalization()
      hidLay1 = hidLay()
      hidLay2 = hidLay()
      concatLayer = Concatenate()
      outputLayer = Dense(1)

      input_ = Input(shape=XTrain.shape[1:])
      normed = normLayer(input_)
```

```

hid1 = hidLay1(normed)
hid2 = hidLay2(hid1)
concat = concatLayer([normed, hid2])
output = outputLayer(concat)

regWide = tf.keras.Model(inputs=[input_], outputs=[output])
regWide.summary()

```

Model: "functional_7"

Layer (type)	Output Shape	Param #	Connected to
input_layer_3 (InputLayer)	(None, 8)	0	-
normalization_1 (Normalization)	(None, 8)	17	input_layer_3[0]...
dense_10 (Dense)	(None, 30)	270	normalization_1[...
dense_11 (Dense)	(None, 30)	930	dense_10[0][0]
concatenate (Concatenate)	(None, 38)	0	normalization_1[... dense_11[0][0]
dense_12 (Dense)	(None, 1)	39	concatenate[0][0]

Total params: 1,256 (4.91 KB)

Trainable params: 1,239 (4.84 KB)

Non-trainable params: 17 (72.00 B)

- First we create five layers: a **Normalization** layer to standardize inputs, two **Dense** layers with 30 neurons each using the ReLU activation function, a **Concatenate** layer, and one more **Dense** layer with a single output layer without any activation function.
- Next we create an **Input** object, specifying the shape and dtype of the inputs. This is used as a function, passing it the inputs.
- Then we pass the **Normalization** layer just like a function, passing the **Input** layer. The passing of layers as arguments to other layers only serves to connect them together.
- We pass **normed** to **hidLay1**, which outputs **hid1** and we pass **hid1** to **hidLay2**, which outputs **hid2**.
- So far all the connections have been sequential, but then we use **concatLayer** to concatenate the input and second hidden layer's output
- Then pass **concat** to the **outputLayer** which finally gives us **output**.

- Finally we create a Keras model, specifying which inputs and outputs to use.

```
[ ]: opt = tf.keras.optimizers.Adam(learning_rate=1e-3)
regWide.compile(loss="mse", optimizer=opt, metrics=["RootMeanSquaredError"])
```

```
[ ]: normLayer.adapt(XTrain)
hist = regWide.fit(XTrain, yTrain, epochs=20, validation_data=(XValid,
↪yValid))
```

```
Epoch 1/20
363/363 ————— 1s 1ms/step -
RootMeanSquaredError: 1.4678 - loss: 2.2793 - val_RootMeanSquaredError: 2.9178 -
val_loss: 8.5133
Epoch 2/20
363/363 ————— 0s 882us/step -
RootMeanSquaredError: 0.7139 - loss: 0.5107 - val_RootMeanSquaredError: 1.7047 -
val_loss: 2.9059
Epoch 3/20
363/363 ————— 0s 900us/step -
RootMeanSquaredError: 0.6398 - loss: 0.4096 - val_RootMeanSquaredError: 1.0166 -
val_loss: 1.0334
Epoch 4/20
363/363 ————— 0s 945us/step -
RootMeanSquaredError: 0.6173 - loss: 0.3812 - val_RootMeanSquaredError: 0.6176 -
val_loss: 0.3815
Epoch 5/20
363/363 ————— 0s 939us/step -
RootMeanSquaredError: 0.6050 - loss: 0.3662 - val_RootMeanSquaredError: 0.5938 -
val_loss: 0.3526
Epoch 6/20
363/363 ————— 0s 910us/step -
RootMeanSquaredError: 0.5967 - loss: 0.3562 - val_RootMeanSquaredError: 0.5811 -
val_loss: 0.3377
Epoch 7/20
363/363 ————— 0s 890us/step -
RootMeanSquaredError: 0.5902 - loss: 0.3485 - val_RootMeanSquaredError: 0.5746 -
val_loss: 0.3301
Epoch 8/20
363/363 ————— 0s 884us/step -
RootMeanSquaredError: 0.5838 - loss: 0.3409 - val_RootMeanSquaredError: 0.5665 -
val_loss: 0.3209
Epoch 9/20
363/363 ————— 0s 909us/step -
RootMeanSquaredError: 0.5788 - loss: 0.3351 - val_RootMeanSquaredError: 0.5610 -
val_loss: 0.3147
Epoch 10/20
363/363 ————— 0s 883us/step -
RootMeanSquaredError: 0.5745 - loss: 0.3302 - val_RootMeanSquaredError: 0.5579 -
val_loss: 0.3113
Epoch 11/20
363/363 ————— 0s 878us/step -
RootMeanSquaredError: 0.5712 - loss: 0.3264 - val_RootMeanSquaredError: 0.5627 -
val_loss: 0.3166
Epoch 12/20
```



```

363/363 ██████████ 0s 884us/step -
RootMeanSquaredError: 0.5684 - loss: 0.3232 - val_RootMeanSquaredError: 0.5619 -
val_loss: 0.3158
Epoch 13/20
363/363 ██████████ 0s 883us/step -
RootMeanSquaredError: 0.5652 - loss: 0.3196 - val_RootMeanSquaredError: 0.6016 -
val_loss: 0.3620
Epoch 14/20
363/363 ██████████ 0s 875us/step -
RootMeanSquaredError: 0.5624 - loss: 0.3164 - val_RootMeanSquaredError: 0.5646 -
val_loss: 0.3187
Epoch 15/20
363/363 ██████████ 0s 876us/step -
RootMeanSquaredError: 0.5596 - loss: 0.3133 - val_RootMeanSquaredError: 0.7858 -
val_loss: 0.6175
Epoch 16/20
363/363 ██████████ 0s 957us/step -
RootMeanSquaredError: 0.5574 - loss: 0.3108 - val_RootMeanSquaredError: 0.6477 -
val_loss: 0.4196
Epoch 17/20
363/363 ██████████ 0s 937us/step -
RootMeanSquaredError: 0.5553 - loss: 0.3084 - val_RootMeanSquaredError: 1.1061 -
val_loss: 1.2234
Epoch 18/20
363/363 ██████████ 0s 915us/step -
RootMeanSquaredError: 0.5533 - loss: 0.3063 - val_RootMeanSquaredError: 0.6701 -
val_loss: 0.4490
Epoch 19/20
363/363 ██████████ 0s 897us/step -
RootMeanSquaredError: 0.5516 - loss: 0.3044 - val_RootMeanSquaredError: 1.7290 -
val_loss: 2.9895
Epoch 20/20
363/363 ██████████ 0s 954us/step -
RootMeanSquaredError: 0.5539 - loss: 0.3069 - val_RootMeanSquaredError: 1.9701 -
val_loss: 3.8811

```

```
[ ]: regWide.evaluate(XTest, yTest)
```

```

162/162 ██████████ 0s 544us/step -
RootMeanSquaredError: 0.5631 - loss: 0.3174

```

```
[ ]: [0.31699109077453613, 0.5630196332931519]
```

In passing different subsets of features along different paths in the network multiple inputs could be used.

```

[ ]: inputWide = Input(shape=[5], name="inputWide")
    inputDeep = Input(shape=[6], name="inputDeep")

    normLayerWide = Normalization()
    normLayerDeep = Normalization()

    normWide = normLayerWide(inputWide)
    normDeep = normLayerDeep(inputDeep)

```

```

hid1 = hidLay()(normDeep)
hid2 = hidLay()(hid1)

concat = tf.keras.layers.concatenate([normWide, hid2])

output = Dense(1, name="output")(concat)

regWide = tf.keras.Model(inputs=[inputWide, inputDeep], outputs=[output])
regWide.summary()

```

Model: "functional_9"

Layer (type)	Output Shape	Param #	Connected to
inputDeep (InputLayer)	(None, 6)	0	-
normalization_3 (Normalization)	(None, 6)	13	inputDeep[0][0]
inputWide (InputLayer)	(None, 5)	0	-
dense_13 (Dense)	(None, 30)	210	normalization_3[...]
normalization_2 (Normalization)	(None, 5)	11	inputWide[0][0]
dense_14 (Dense)	(None, 30)	930	dense_13[0][0]
concatenate_1 (Concatenate)	(None, 35)	0	normalization_2[...] dense_14[0][0]
output (Dense)	(None, 1)	36	concatenate_1[0]...

Total params: 1,200 (4.70 KB)

Trainable params: 1,176 (4.59 KB)

Non-trainable params: 24 (104.00 B)

- Each **Dense** layer is created and called on the same line as is common practice. However this isn't done with the **Normalization** layers as a reference to the layer is needed for adaptation.
- Used **tf.keras.layers.concatenate** to concatenate the inputs and the output of the second hidden layer.

- We specified two inputs when creating the model as there are two inputs.

```
[ ]: opt = tf.keras.optimizers.Adam(learning_rate=1e-3)
regWide.compile(loss="mse", optimizer=opt, metrics=["RootMeanSquaredError"])
```












```
[ ]: XTrainWide, XTrainDeep = XTrain[:, :5], XTrain[:, 2:]
XValidWide, XValidDeep = XValid[:, :5], XValid[:, 2:]
XTestWide, XTestDeep = XTest[:, :5], XTest[:, 2:]
XNewWide, XNewDeep = XTestWide[:3], XTestDeep[:3]

normLayerWide.adapt(XTrainWide)
normLayerDeep.adapt(XTrainDeep)

hist = regWide.fit(
    (XTrainWide, XTrainDeep),
    yTrain,
    validation_data=((XValidWide, XValidDeep), yValid),
    epochs=20,
)
```

```
Epoch 1/20
363/363 ————— 1s 1ms/step -
RootMeanSquaredError: 1.7786 - loss: 3.2631 - val_RootMeanSquaredError: 0.9088 -
val_loss: 0.8260
Epoch 2/20
363/363 ————— 0s 953us/step -
RootMeanSquaredError: 0.8502 - loss: 0.7241 - val_RootMeanSquaredError: 0.9169 -
val_loss: 0.8408
Epoch 3/20
363/363 ————— 0s 930us/step -
RootMeanSquaredError: 0.7640 - loss: 0.5841 - val_RootMeanSquaredError: 0.8662 -
val_loss: 0.7503
Epoch 4/20
363/363 ————— 0s 943us/step -
RootMeanSquaredError: 0.7125 - loss: 0.5081 - val_RootMeanSquaredError: 0.9910 -
val_loss: 0.9821
Epoch 5/20
363/363 ————— 0s 946us/step -
RootMeanSquaredError: 0.6711 - loss: 0.4506 - val_RootMeanSquaredError: 0.9600 -
val_loss: 0.9216
Epoch 6/20
363/363 ————— 0s 959us/step -
RootMeanSquaredError: 0.6402 - loss: 0.4101 - val_RootMeanSquaredError: 0.8299 -
val_loss: 0.6888
Epoch 7/20
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.6181 - loss: 0.3821 - val_RootMeanSquaredError: 1.3156 -
val_loss: 1.7309
Epoch 8/20
363/363 ————— 0s 973us/step -
RootMeanSquaredError: 0.6084 - loss: 0.3702 - val_RootMeanSquaredError: 1.4480 -
val_loss: 2.0968
Epoch 9/20
363/363 ————— 0s 1ms/step -
```


```

RootMeanSquaredError: 0.6010 - loss: 0.3612 - val_RootMeanSquaredError: 1.2405 -
val_loss: 1.5388
Epoch 10/20
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5949 - loss: 0.3541 - val_RootMeanSquaredError: 1.3897 -
val_loss: 1.9313
Epoch 11/20
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5920 - loss: 0.3506 - val_RootMeanSquaredError: 1.3386 -
val_loss: 1.7919
Epoch 12/20
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5907 - loss: 0.3490 - val_RootMeanSquaredError: 1.2488 -
val_loss: 1.5596
Epoch 13/20
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5863 - loss: 0.3438 - val_RootMeanSquaredError: 0.9414 -
val_loss: 0.8862
Epoch 14/20
363/363  0s 980us/step -
RootMeanSquaredError: 0.5836 - loss: 0.3407 - val_RootMeanSquaredError: 0.9483 -
val_loss: 0.8992
Epoch 15/20
363/363  0s 966us/step -
RootMeanSquaredError: 0.5806 - loss: 0.3372 - val_RootMeanSquaredError: 0.9576 -
val_loss: 0.9170
Epoch 16/20
363/363  0s 914us/step -
RootMeanSquaredError: 0.5799 - loss: 0.3364 - val_RootMeanSquaredError: 1.0987 -
val_loss: 1.2072
Epoch 17/20
363/363  0s 933us/step -
RootMeanSquaredError: 0.5794 - loss: 0.3357 - val_RootMeanSquaredError: 1.0939 -
val_loss: 1.1966
Epoch 18/20
363/363  0s 903us/step -
RootMeanSquaredError: 0.5778 - loss: 0.3339 - val_RootMeanSquaredError: 1.2056 -
val_loss: 1.4534
Epoch 19/20
363/363  0s 914us/step -
RootMeanSquaredError: 0.5776 - loss: 0.3337 - val_RootMeanSquaredError: 1.1802 -
val_loss: 1.3928
Epoch 20/20
363/363  0s 926us/step -
RootMeanSquaredError: 0.5764 - loss: 0.3323 - val_RootMeanSquaredError: 1.2530 -
val_loss: 1.5700

```

```
[ ]: mseTest = regWide.evaluate((XTestWide, XTestDeep), yTest)
```

```

162/162  0s 557us/step -
RootMeanSquaredError: 0.5803 - loss: 0.3369

```

```
[ ]: preds = regWide.predict((XNewWide, XNewDeep))
```

```

1/1  0s 52ms/step

```

There are also cases where you may want to have multiple outputs:

- The task demands it, like locating and classifying, the main object in a picture, which is both a regression and classification task
- You have multiple independent tasks based on the same data. For example performing *multitask classification* on pictures of faces, using one output to classify the person's facial expression and another output to identify if the person is wearing glasses or not.
- As a regularization technique. For example you may want to add an auxiliary output to a network architecture to ensure the underlying part of the network learns something useful on it's own, without relying on the rest of the network.

```
[ ]: aux = Dense(1, name="aux")(hid2)
regWide = tf.keras.Model(
    inputs={"inputDeep": inputDeep, "inputWide": inputWide}, outputs=[output, _
    ↪aux]
)
opt = tf.keras.optimizers.Adam(learning_rate=1e-3)
regWide.compile(
    loss={"output": "mse", "aux": "mse"},
    loss_weights={"output": 0.9, "aux": 0.1},
    optimizer=opt,
    metrics=["RootMeanSquaredError", "RootMeanSquaredError"],
)
regWide.summary()
```

Model: "functional_11"

Layer (type)	Output Shape	Param #	Connected to
inputDeep (InputLayer)	(None, 6)	0	-
normalization_3 (Normalization)	(None, 6)	13	inputDeep[0][0]
inputWide (InputLayer)	(None, 5)	0	-
dense_13 (Dense)	(None, 30)	210	normalization_3[...]
normalization_2 (Normalization)	(None, 5)	11	inputWide[0][0]
dense_14 (Dense)	(None, 30)	930	dense_13[0][0]
concatenate_1 (Concatenate)	(None, 35)	0	normalization_2[...] dense_14[0][0]
output (Dense)	(None, 1)	36	concatenate_1[0]...

aux (Dense)	(None, 1)	31	dense_14[0][0]
-------------	-----------	----	----------------

Total params: 1,231 (4.82 KB)

Trainable params: 1,207 (4.71 KB)

Non-trainable params: 24 (104.00 B)

Each output will need it's own loss function, so have to pass a list of losses. By default Keras assigns each loss an equal weight, but since we are more interested in the main output we can give it a higher weight.

```
[ ]: normLayerDeep.adapt(XTrainDeep)
normLayerWide.adapt(XTrainWide)

ytrains = {"output": yTrain, "aux": yTrain}
xtrains = {"inputDeep": XTrainDeep, "inputWide": XTrainWide}
xvals = {"inputDeep": XValidDeep, "inputWide": XValidWide}
yvals = {"output": yValid, "aux": yValid}
xtests = {"inputDeep": XTestDeep, "inputWide": XTestWide}
ytests = {"output": yTest, "aux": yTest}
hist = regWide.fit(
    xtrains,
    ytrains,
    epochs=20,
    validation_data=(xvals, yvals),
)
```

Epoch 1/20

363/363 ————— 1s 1ms/step -
 aux_RootMeanSquaredError: 1.3624 - loss: 0.4962 - output_RootMeanSquaredError:
 0.5801 - val_aux_RootMeanSquaredError: 0.9054 - val_loss: 0.5189 -
 val_output_RootMeanSquaredError: 0.6967

Epoch 2/20

363/363 ————— 0s 1ms/step -
 aux_RootMeanSquaredError: 0.8021 - loss: 0.3629 - output_RootMeanSquaredError:
 0.5758 - val_aux_RootMeanSquaredError: 0.7498 - val_loss: 0.6340 -
 val_output_RootMeanSquaredError: 0.8012

Epoch 3/20












363/363 ————— 0s 1ms/step -
 aux_RootMeanSquaredError: 0.7388 - loss: 0.3517 - output_RootMeanSquaredError:
 0.5745 - val_aux_RootMeanSquaredError: 0.9372 - val_loss: 0.7686 -
 val_output_RootMeanSquaredError: 0.8697

Epoch 4/20

363/363 ————— 0s 1ms/step -
 aux_RootMeanSquaredError: 0.7108 - loss: 0.3452 - output_RootMeanSquaredError:
 0.5722 - val_aux_RootMeanSquaredError: 1.2409 - val_loss: 1.1104 -
 val_output_RootMeanSquaredError: 1.0309

Epoch 5/20

363/363 ————— 0s 1ms/step -
 aux_RootMeanSquaredError: 0.6880 - loss: 0.3416 - output_RootMeanSquaredError:

0.5717 - val_aux_RootMeanSquaredError: 1.2655 - val_loss: 1.1496 -
val_output_RootMeanSquaredError: 1.0485
Epoch 6/20
363/363  0s 1ms/step -
aux_RootMeanSquaredError: 0.6728 - loss: 0.3397 - output_RootMeanSquaredError:
0.5719 - val_aux_RootMeanSquaredError: 1.1427 - val_loss: 1.1674 -
val_output_RootMeanSquaredError: 1.0733
Epoch 7/20
363/363  0s 1ms/step -
aux_RootMeanSquaredError: 0.6583 - loss: 0.3356 - output_RootMeanSquaredError:
0.5698 - val_aux_RootMeanSquaredError: 1.0255 - val_loss: 0.7857 -
val_output_RootMeanSquaredError: 0.8696
Epoch 8/20
363/363  0s 1ms/step -
aux_RootMeanSquaredError: 0.6489 - loss: 0.3334 - output_RootMeanSquaredError:
0.5688 - val_aux_RootMeanSquaredError: 1.0503 - val_loss: 0.8421 -
val_output_RootMeanSquaredError: 0.9017
Epoch 9/20
363/363  0s 1ms/step -
aux_RootMeanSquaredError: 0.6402 - loss: 0.3303 - output_RootMeanSquaredError:
0.5669 - val_aux_RootMeanSquaredError: 0.9851 - val_loss: 0.7459 -
val_output_RootMeanSquaredError: 0.8491
Epoch 10/20
363/363  0s 1ms/step -
aux_RootMeanSquaredError: 0.6334 - loss: 0.3282 - output_RootMeanSquaredError:
0.5657 - val_aux_RootMeanSquaredError: 1.0902 - val_loss: 0.8345 -
val_output_RootMeanSquaredError: 0.8917
Epoch 11/20
363/363  0s 1ms/step -
aux_RootMeanSquaredError: 0.6283 - loss: 0.3269 - output_RootMeanSquaredError:
0.5651 - val_aux_RootMeanSquaredError: 1.0446 - val_loss: 0.7880 -
val_output_RootMeanSquaredError: 0.8685
Epoch 12/20
363/363  0s 1ms/step -
aux_RootMeanSquaredError: 0.6251 - loss: 0.3268 - output_RootMeanSquaredError:
0.5654 - val_aux_RootMeanSquaredError: 1.1686 - val_loss: 0.9666 -
val_output_RootMeanSquaredError: 0.9603
Epoch 13/20
363/363  0s 1ms/step -
aux_RootMeanSquaredError: 0.6209 - loss: 0.3254 - output_RootMeanSquaredError:
0.5644 - val_aux_RootMeanSquaredError: 1.1490 - val_loss: 0.9162 -
val_output_RootMeanSquaredError: 0.9334
Epoch 14/20
363/363  0s 1ms/step -
aux_RootMeanSquaredError: 0.6200 - loss: 0.3270 - output_RootMeanSquaredError:
0.5661 - val_aux_RootMeanSquaredError: 1.0984 - val_loss: 0.9250 -
val_output_RootMeanSquaredError: 0.9454
Epoch 15/20
363/363  0s 1ms/step -
aux_RootMeanSquaredError: 0.6149 - loss: 0.3236 - output_RootMeanSquaredError:
0.5634 - val_aux_RootMeanSquaredError: 1.0322 - val_loss: 0.7635 -
val_output_RootMeanSquaredError: 0.8544
Epoch 16/20
363/363  0s 1ms/step -

```

aux_RootMeanSquaredError: 0.6116 - loss: 0.3220 - output_RootMeanSquaredError:
0.5623 - val_aux_RootMeanSquaredError: 1.0857 - val_loss: 0.8371 -
val_output_RootMeanSquaredError: 0.8940
Epoch 17/20
363/363 ————— 0s 1ms/step -
aux_RootMeanSquaredError: 0.6103 - loss: 0.3216 - output_RootMeanSquaredError:
0.5620 - val_aux_RootMeanSquaredError: 1.0779 - val_loss: 0.7986 -
val_output_RootMeanSquaredError: 0.8708
Epoch 18/20
363/363 ————— 0s 1ms/step -
aux_RootMeanSquaredError: 0.6108 - loss: 0.3229 - output_RootMeanSquaredError:
0.5632 - val_aux_RootMeanSquaredError: 0.9940 - val_loss: 0.8047 -
val_output_RootMeanSquaredError: 0.8856
Epoch 19/20
363/363 ————— 0s 1ms/step -
aux_RootMeanSquaredError: 0.6059 - loss: 0.3202 - output_RootMeanSquaredError:
0.5612 - val_aux_RootMeanSquaredError: 0.9897 - val_loss: 0.7214 -
val_output_RootMeanSquaredError: 0.8323
Epoch 20/20
363/363 ————— 0s 1ms/step -
aux_RootMeanSquaredError: 0.6049 - loss: 0.3183 - output_RootMeanSquaredError:
0.5594 - val_aux_RootMeanSquaredError: 1.0551 - val_loss: 0.6691 -
val_output_RootMeanSquaredError: 0.7872

```

```

[ ]: evalRes = regWide.evaluate(xtests, ytests)
      mainLoss, wSumLoss, mainRmse = evalRes

```

```

162/162 ————— 0s 628us/step -
aux_RootMeanSquaredError: 0.6172 - loss: 0.3291 - output_RootMeanSquaredError:
0.5685

```

```

[ ]: xnews = {"inputWide": XNewWide, "inputDeep": XNewDeep}
      preds = regWide.predict(xnews)
      preds = dict(zip(regWide.output_names, preds))
      preds

```

```

1/1 ————— 0s 57ms/step

```

```

[ ]: {'output': array([[0.47618163],
                      [0.71396697],
                      [3.7181835 ]], dtype=float32),
      'aux': array([[0.4587401],
                    [0.685268 ],
                    [3.588437 ]], dtype=float32)}

```

1.7.4 Using Subclassing API to build Dynamic Models

The **Sequential** and **Functional** APIs are declarative, meaning you declare the layers and how they are connected, then you pass the data to the model and it does the rest. The **Subclassing** API is more dynamic, allowing you to do pretty much anything you want. With this approach you inherit from the **Model** class, create layers in the constructor and use them to perform the computations in the **call()** method. For example creating an instance of the **WideAndDeepModel** class gives an equivalent model to the one created using the **Functional** API.


```
[ ]: class WideAndDeepModel(tf.keras.Model):
    def __init__(self, units=30, activation="relu", **kwargs):
        super().__init__(**kwargs)
        self.normLayerWide = Normalization()
        self.normLayerDeep = Normalization()
        self.hiddLayer1 = Dense(units=units, activation=activation)
        self.hiddLayer2 = Dense(units=units, activation=activation)
        self.mainOut = Dense(1)
        self.auxOut = Dense(1)

    def call(self, inputs):
        inputWide, inputDeep = inputs
        normWide = self.normLayerWide(inputWide)
        normDeep = self.normLayerDeep(inputDeep)
        hidd1 = self.hiddLayer1(normDeep)
        hidd2 = self.hiddLayer2(hidd1)
        concat = tf.keras.layers.concatenate([normWide, hidd2])
        output = self.mainOut(concat)
        auxOutput = self.auxOut(hidd2)
        return output, auxOutput

wideAndDeep = WideAndDeepModel(name="WideAndDeep")
```

```
[ ]: opt = tf.keras.optimizers.Adam(learning_rate=1e-3)
wideAndDeep.compile(
    loss="mse",
    loss_weights=[0.9, 0.1],
    optimizer=opt,
    metrics=["RootMeanSquaredError", "RootMeanSquaredError"],
)
wideAndDeep.normLayerDeep.adapt(XTrainDeep)
wideAndDeep.normLayerWide.adapt(XTrainWide)

wideAndDeep.summary()
```

Model: "WideAndDeep"

Layer (type)	Output Shape	Param #
normalization_4 (Normalization)	?	11
normalization_5 (Normalization)	?	13
dense_15 (Dense)	?	0 (unbuilt)
dense_16 (Dense)	?	0 (unbuilt)
dense_17 (Dense)	?	0 (unbuilt)

dense_18 (Dense)	?	0 (unbuilt)
------------------	---	-------------

Total params: 24 (104.00 B)

Trainable params: 0 (0.00 B)

Non-trainable params: 24 (104.00 B)

```
[ ]: hist = wideAndDeep.fit(
    (XTrainWide, XTrainDeep),
    ytrains,
    epochs=20,
    validation_data=((XValidWide, XValidDeep), yvals),
)
```

Epoch 1/20

363/363 ————— 2s 2ms/step -

RootMeanSquaredError: 1.6283 - RootMeanSquaredError_1: 1.8672 - loss: 2.8192 -
val_RootMeanSquaredError: 1.1792 - val_RootMeanSquaredError_1: 3.6576 -
val_loss: 2.5892

Epoch 2/20

363/363 ————— 0s 1ms/step -

RootMeanSquaredError: 0.8252 - RootMeanSquaredError_1: 1.0348 - loss: 0.7221 -
val_RootMeanSquaredError: 0.6714 - val_RootMeanSquaredError_1: 2.3543 -
val_loss: 0.9600

Epoch 3/20

363/363 ————— 0s 1ms/step -

RootMeanSquaredError: 0.6889 - RootMeanSquaredError_1: 0.8212 - loss: 0.4948 -
val_RootMeanSquaredError: 0.6514 - val_RootMeanSquaredError_1: 1.5066 -
val_loss: 0.6089

Epoch 4/20

363/363 ————— 0s 1ms/step -

RootMeanSquaredError: 0.6580 - RootMeanSquaredError_1: 0.7508 - loss: 0.4462 -
val_RootMeanSquaredError: 0.6222 - val_RootMeanSquaredError_1: 1.1765 -
val_loss: 0.4868

Epoch 5/20

363/363 ————— 0s 1ms/step -

RootMeanSquaredError: 0.6409 - RootMeanSquaredError_1: 0.7232 - loss: 0.4220 -
val_RootMeanSquaredError: 0.7048 - val_RootMeanSquaredError_1: 0.8662 -
val_loss: 0.5221

Epoch 6/20

363/363 ————— 0s 1ms/step -

RootMeanSquaredError: 0.6294 - RootMeanSquaredError_1: 0.7070 - loss: 0.4066 -
val_RootMeanSquaredError: 0.6411 - val_RootMeanSquaredError_1: 0.8654 -
val_loss: 0.4448

Epoch 7/20

363/363 ————— 0s 1ms/step -

RootMeanSquaredError: 0.6199 - RootMeanSquaredError_1: 0.6960 - loss: 0.3944 -
val_RootMeanSquaredError: 0.6753 - val_RootMeanSquaredError_1: 0.7255 -
val_loss: 0.4631

Epoch 8/20

363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.6132 - RootMeanSquaredError_1: 0.6871 - loss: 0.3858 -
val_RootMeanSquaredError: 0.6335 - val_RootMeanSquaredError_1: 0.7489 -
val_loss: 0.4173
Epoch 9/20
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.6076 - RootMeanSquaredError_1: 0.6790 - loss: 0.3784 -
val_RootMeanSquaredError: 0.6531 - val_RootMeanSquaredError_1: 0.6652 -
val_loss: 0.4281
Epoch 10/20
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.6028 - RootMeanSquaredError_1: 0.6717 - loss: 0.3722 -
val_RootMeanSquaredError: 0.5907 - val_RootMeanSquaredError_1: 0.7013 -
val_loss: 0.3633
Epoch 11/20
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5979 - RootMeanSquaredError_1: 0.6642 - loss: 0.3659 -
val_RootMeanSquaredError: 0.7426 - val_RootMeanSquaredError_1: 0.6442 -
val_loss: 0.5378
Epoch 12/20
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5944 - RootMeanSquaredError_1: 0.6580 - loss: 0.3613 -
val_RootMeanSquaredError: 0.8757 - val_RootMeanSquaredError_1: 0.7963 -
val_loss: 0.7536
Epoch 13/20
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5914 - RootMeanSquaredError_1: 0.6521 - loss: 0.3573 -
val_RootMeanSquaredError: 0.9340 - val_RootMeanSquaredError_1: 0.6333 -
val_loss: 0.8253
Epoch 14/20
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5879 - RootMeanSquaredError_1: 0.6464 - loss: 0.3529 -
val_RootMeanSquaredError: 0.9581 - val_RootMeanSquaredError_1: 1.1784 -
val_loss: 0.9650
Epoch 15/20
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5856 - RootMeanSquaredError_1: 0.6434 - loss: 0.3501 -
val_RootMeanSquaredError: 0.7951 - val_RootMeanSquaredError_1: 0.6387 -
val_loss: 0.6098
Epoch 16/20
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5814 - RootMeanSquaredError_1: 0.6365 - loss: 0.3448 -
val_RootMeanSquaredError: 1.0566 - val_RootMeanSquaredError_1: 1.1624 -
val_loss: 1.1398
Epoch 17/20
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5800 - RootMeanSquaredError_1: 0.6342 - loss: 0.3431 -
val_RootMeanSquaredError: 1.4174 - val_RootMeanSquaredError_1: 1.0021 -
val_loss: 1.9086
Epoch 18/20
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5801 - RootMeanSquaredError_1: 0.6311 - loss: 0.3427 -
val_RootMeanSquaredError: 1.5065 - val_RootMeanSquaredError_1: 1.2418 -
val_loss: 2.1968

```
Epoch 19/20
363/363 — 0s 1ms/step -
RootMeanSquaredError: 0.5793 - RootMeanSquaredError_1: 0.6276 - loss: 0.3415 -
val_RootMeanSquaredError: 1.1126 - val_RootMeanSquaredError_1: 0.6934 -
val_loss: 1.1622
Epoch 20/20
363/363 — 0s 1ms/step -
RootMeanSquaredError: 0.5742 - RootMeanSquaredError_1: 0.6232 - loss: 0.3356 -
val_RootMeanSquaredError: 1.4374 - val_RootMeanSquaredError_1: 1.8831 -
val_loss: 2.2141
```

```
[ ]: evalRes = wideAndDeep.evaluate((XTestWide, XTestDeep), ytests)
# mainLoss, wSumLoss, mainRmse = evalRes
evalRes
```

```
162/162 — 0s 781us/step -
RootMeanSquaredError: 0.5819 - RootMeanSquaredError_1: 0.6344 - loss: 0.3451
```

```
[ ]: [0.33926549553871155, 0.577087938785553, 0.577087938785553, 0.
↳ 6287933588027954]
```

```
[ ]: preds = regWide.predict((XNewDeep, XNewWide))
preds = dict(zip(regWide.output_names, preds))
preds
```

WARNING:tensorflow:5 out of the last 318 calls to <function TensorFlowTrainer.make_predict_function.<locals>.one_step_on_data_distributed at 0x72df9b333a60> triggered tf.function retracing. Tracing is expensive and the excessive number of tracings could be due to (1) creating @tf.function repeatedly in a loop, (2) passing tensors with different shapes, (3) passing Python objects instead of tensors. For (1), please define your @tf.function outside of the loop. For (2), @tf.function has reduce_retracing=True option that can avoid unnecessary retracing. For (3), please refer to https://www.tensorflow.org/guide/function#controlling_retracing and https://www.tensorflow.org/api_docs/python/tf/function for more details.

```
1/1 — 0s 64ms/step
```

```
[ ]: {'output': array([[0.47618163],
[0.71396697],
[3.7181835 ]], dtype=float32),
'aux': array([[0.4587401],
[0.685268 ],
[3.588437 ]], dtype=float32)}
```

1.7.5 Saving and Restoring a Model

When using the **Sequential** or **Functional** APIs you can save the model by calling the **save()** method. This will save the architecture, the model's parameters and the optimizer's parameters. You can also save the model's weights and optimizer's parameters separately by calling the **save_weights()** method. Calling the **export()** method on a function saves it as a TensorFlow **SavedModel**, which also saves the function's computation graph.

When using the **Subclassing** API you can only save the model's weights and optimizer's parameters by calling the **save_weights()** method.

```
[ ]: from pathlib import Path
```

```
modelPath = Path("./models")
modelPath.mkdir(exist_ok=True)

clsName = "FashionMNIST"
cls.save(modelPath / f"{clsName}.keras")
cls.export(modelPath / clsName)
```

INFO:tensorflow:Assets written to: models/FashionMNIST/assets

INFO:tensorflow:Assets written to: models/FashionMNIST/assets

Saved artifact at 'models/FashionMNIST'. The following endpoints are available:

* Endpoint 'serve'

args_0 (POSITIONAL_ONLY): TensorSpec(shape=(None, 28, 28), dtype=tf.float32, name='keras_tensor_11')

Output Type:

TensorSpec(shape=(None, 10), dtype=tf.float32, name=None)

Captures:

126304782520720: TensorSpec(shape=(), dtype=tf.resource, name=None)

126304782522832: TensorSpec(shape=(), dtype=tf.resource, name=None)

126304782522448: TensorSpec(shape=(), dtype=tf.resource, name=None)

126304782522256: TensorSpec(shape=(), dtype=tf.resource, name=None)

126304782523024: TensorSpec(shape=(), dtype=tf.resource, name=None)

126304782523600: TensorSpec(shape=(), dtype=tf.resource, name=None)

To load the model you can use the `load_model()` function, which will return a model identical to the one saved. If you only saved the model's weights you will need to create the model and then call the `load_weights()` method.

```
[ ]: fashionCls = tf.keras.models.load_model(modelPath / f"{clsName}.keras")
```

```
fmnist = tf.keras.datasets.fashion_mnist.load_data()
(XTrainFull, yTrainFull), (XTest, yTest) = fmnist
```

```
XTest = XTest / 255.0
```

```
preds = fashionCls.predict(XTest)
preds = preds.argmax(axis=1)
classStats(yTest, preds, classNames)
```

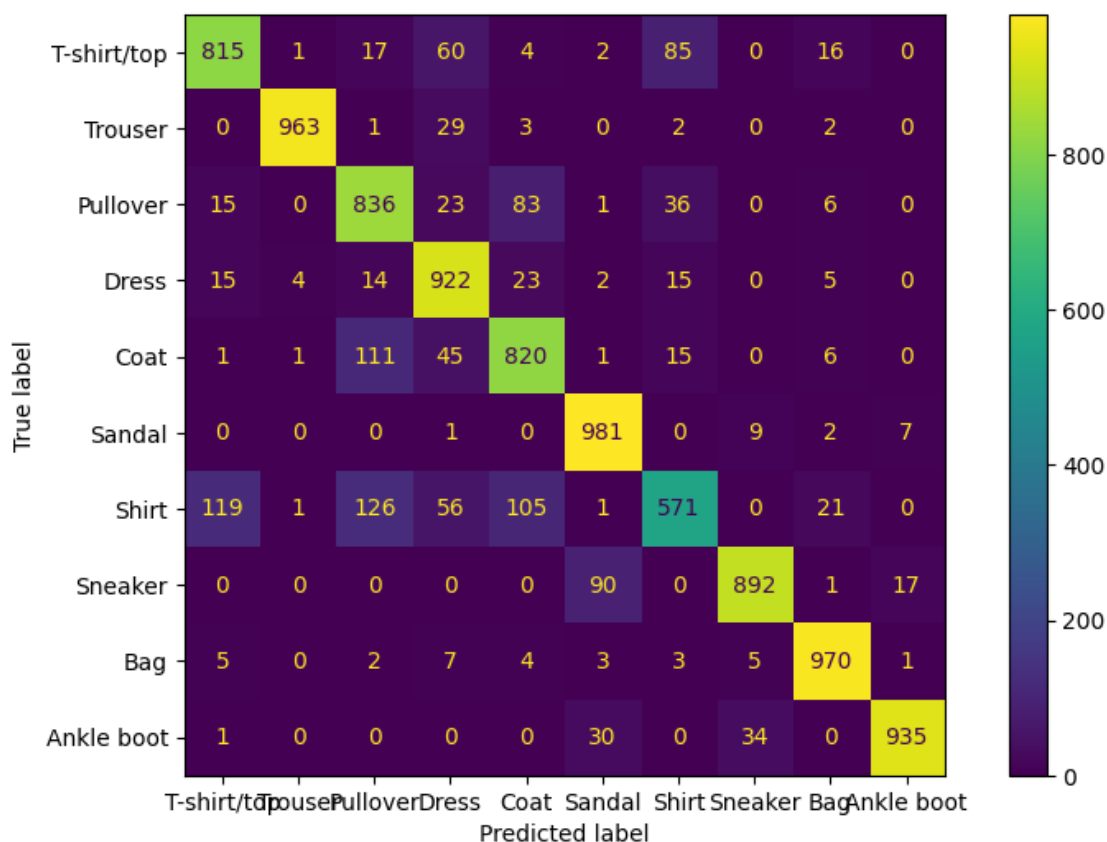
WARNING:tensorflow:6 out of the last 319 calls to <function TensorFlowTrainer.make_predict_function.<locals>.one_step_on_data_distributed at 0x72df9f97cb80> triggered tf.function retracing. Tracing is expensive and the excessive number of tracings could be due to (1) creating @tf.function repeatedly in a loop, (2) passing tensors with different shapes, (3) passing Python objects instead of tensors. For (1), please define your @tf.function outside of the loop. For (2), @tf.function has `reduce_retracing=True` option that can avoid unnecessary retracing. For (3), please refer to https://www.tensorflow.org/guide/function#controlling_retracing and https://www.tensorflow.org/api_docs/python/tf/function for more details.

WARNING:tensorflow:6 out of the last 319 calls to <function TensorFlowTrainer.make_predict_function.<locals>.one_step_on_data_distributed at 0x72df9f97cb80> triggered tf.function retracing. Tracing is expensive and the

excessive number of tracings could be due to (1) creating `@tf.function` repeatedly in a loop, (2) passing tensors with different shapes, (3) passing Python objects instead of tensors. For (1), please define your `@tf.function` outside of the loop. For (2), `@tf.function` has `reduce_retracing=True` option that can avoid unnecessary retracing. For (3), please refer to https://www.tensorflow.org/guide/function#controlling_retracing and https://www.tensorflow.org/api_docs/python/tf/function for more details.

313/313 ————— 0s 991us/step

	precision	recall	f1-score	support
0	0.84	0.81	0.83	1000
1	0.99	0.96	0.98	1000
2	0.76	0.84	0.79	1000
3	0.81	0.92	0.86	1000
4	0.79	0.82	0.80	1000
5	0.88	0.98	0.93	1000
6	0.79	0.57	0.66	1000
7	0.95	0.89	0.92	1000
8	0.94	0.97	0.96	1000
9	0.97	0.94	0.95	1000
accuracy			0.87	10000
macro avg	0.87	0.87	0.87	10000
weighted avg	0.87	0.87	0.87	10000

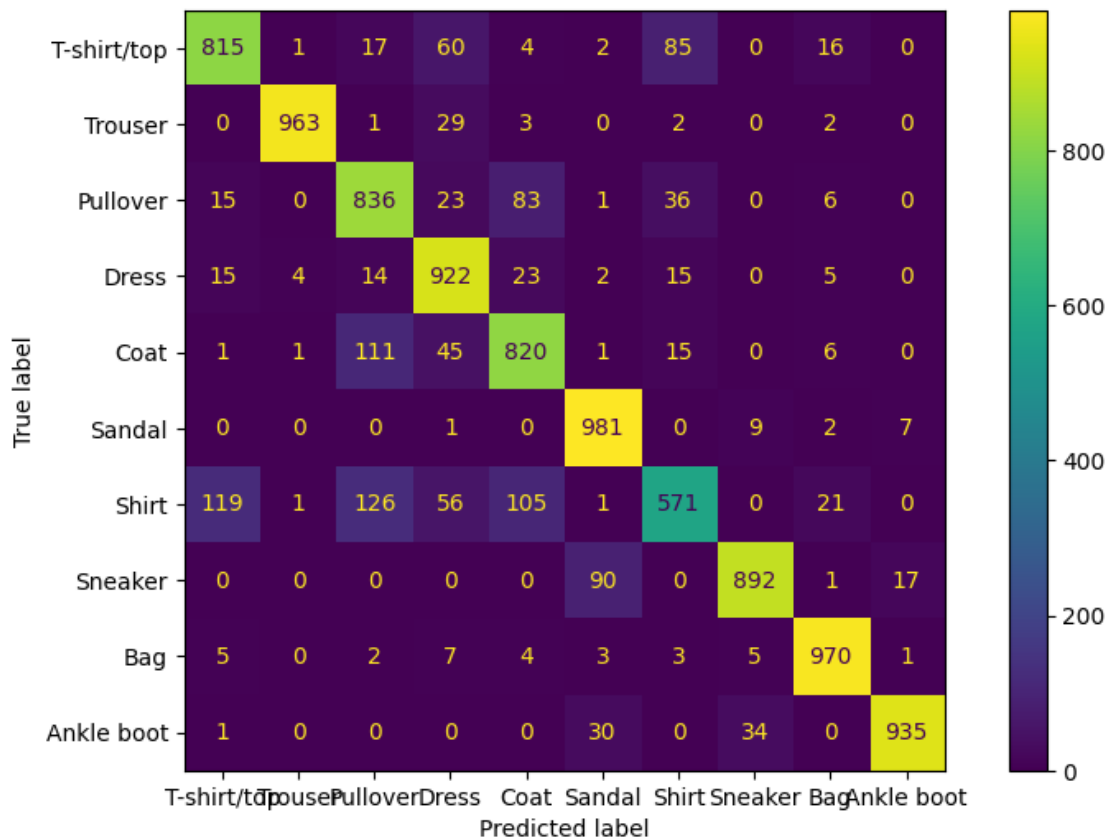


```
[ ]: pbFashion = tf.keras.layers.TFSMLayer(
    modelPath / clsName, call_endpoint="serving_default"
)

preds = pbFashion(XTest)
preds = np.array(preds["output_0"]).argmax(axis=1)

classStats(yTest, preds, classNames)
```

	precision	recall	f1-score	support
0	0.84	0.81	0.83	1000
1	0.99	0.96	0.98	1000
2	0.76	0.84	0.79	1000
3	0.81	0.92	0.86	1000
4	0.79	0.82	0.80	1000
5	0.88	0.98	0.93	1000
6	0.79	0.57	0.66	1000
7	0.95	0.89	0.92	1000
8	0.94	0.97	0.96	1000
9	0.97	0.94	0.95	1000
accuracy			0.87	10000
macro avg	0.87	0.87	0.87	10000
weighted avg	0.87	0.87	0.87	10000



You can also save and load weights using the `save_weights()` and `load_weights()` methods. This uses less disk space and is faster than saving the whole model, but you will need to save the model's architecture separately.

1.7.6 Using Callbacks

The `fit()` method accepts a `callbacks` argument that lets you specify a list of objects that Keras will call at the start and end of training, at the start and end of each epoch, and even before and after processing each batch. For example the `ModelCheckpoint` callback saves checkpoints of your model at regular intervals during training, by default at the end of each epoch. You can also specify the `save_best_only=True` argument, which will only save your model when its performance on the validation set is the best so far. Another useful callback is the `EarlyStopping` callback, which interrupts training when it measures no progress on the validation set for a number of epochs, specified by the `patience` argument. This can be used in combination with the `ModelCheckpoint` callback to save the best model when training is interrupted.

```
[ ]: checkpoint = tf.keras.callbacks.ModelCheckpoint(
    modelPath / "wideAndDeep_checkpoints.weights.h5",
    save_weights_only=True,
    save_best_only=True,
)

earlyStop = tf.keras.callbacks.EarlyStopping(patience=10,
    ↪ restore_best_weights=True)
```



```

hist = wideAndDeep.fit(
    (XTrainWide, XTrainDeep),
    ytrains,
    epochs=100,
    validation_data=((XValidWide, XValidDeep), yvals),
    callbacks=[checkpoint, earlyStop],
)

```

Epoch 1/100

363/363  1s 1ms/step -

RootMeanSquaredError: 0.5747 - RootMeanSquaredError_1: 0.6264 - loss: 0.3366 -
 val_RootMeanSquaredError: 1.4027 - val_RootMeanSquaredError_1: 1.1160 -
 val_loss: 1.8953

Epoch 2/100

363/363  0s 1ms/step -

RootMeanSquaredError: 0.5740 - RootMeanSquaredError_1: 0.6212 - loss: 0.3352 -
 val_RootMeanSquaredError: 1.1059 - val_RootMeanSquaredError_1: 1.2985 -
 val_loss: 1.2692

Epoch 3/100

363/363  0s 1ms/step -

RootMeanSquaredError: 0.5696 - RootMeanSquaredError_1: 0.6184 - loss: 0.3303 -
 val_RootMeanSquaredError: 0.8283 - val_RootMeanSquaredError_1: 0.6903 -
 val_loss: 0.6651

Epoch 4/100

363/363  0s 1ms/step -

RootMeanSquaredError: 0.5668 - RootMeanSquaredError_1: 0.6135 - loss: 0.3268 -
 val_RootMeanSquaredError: 1.1103 - val_RootMeanSquaredError_1: 1.2245 -
 val_loss: 1.2595

Epoch 5/100

363/363  0s 1ms/step -

RootMeanSquaredError: 0.5663 - RootMeanSquaredError_1: 0.6134 - loss: 0.3263 -
 val_RootMeanSquaredError: 1.1915 - val_RootMeanSquaredError_1: 0.9500 -
 val_loss: 1.3680

Epoch 6/100

363/363  0s 1ms/step -

RootMeanSquaredError: 0.5672 - RootMeanSquaredError_1: 0.6127 - loss: 0.3271 -
 val_RootMeanSquaredError: 1.1928 - val_RootMeanSquaredError_1: 1.7316 -
 val_loss: 1.5802

Epoch 7/100

363/363  0s 1ms/step -

RootMeanSquaredError: 0.5652 - RootMeanSquaredError_1: 0.6150 - loss: 0.3254 -
 val_RootMeanSquaredError: 1.0477 - val_RootMeanSquaredError_1: 0.9157 -
 val_loss: 1.0717

Epoch 8/100

363/363  0s 1ms/step -












RootMeanSquaredError: 0.5640 - RootMeanSquaredError_1: 0.6093 - loss: 0.3234 -
 val_RootMeanSquaredError: 0.9953 - val_RootMeanSquaredError_1: 1.2899 -
 val_loss: 1.0580












Epoch 9/100

363/363  0s 1ms/step -

RootMeanSquaredError: 0.5618 - RootMeanSquaredError_1: 0.6086 - loss: 0.3211 -
 val_RootMeanSquaredError: 0.8066 - val_RootMeanSquaredError_1: 0.7483 -
 val_loss: 0.6415

Epoch 10/100












363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5605 - RootMeanSquaredError_1: 0.6058 - loss: 0.3195 -
 val_RootMeanSquaredError: 1.0338 - val_RootMeanSquaredError_1: 1.1420 -
 val_loss: 1.0923
 Epoch 11/100
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5602 - RootMeanSquaredError_1: 0.6051 - loss: 0.3191 -
 val_RootMeanSquaredError: 1.0583 - val_RootMeanSquaredError_1: 0.9010 -
 val_loss: 1.0893
 Epoch 12/100
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5602 - RootMeanSquaredError_1: 0.6042 - loss: 0.3190 -
 val_RootMeanSquaredError: 1.0585 - val_RootMeanSquaredError_1: 1.5290 -
 val_loss: 1.2422
 Epoch 13/100
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5583 - RootMeanSquaredError_1: 0.6050 - loss: 0.3172 -
 val_RootMeanSquaredError: 0.8286 - val_RootMeanSquaredError_1: 0.8183 -
 val_loss: 0.6848
 Epoch 14/100
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5570 - RootMeanSquaredError_1: 0.6013 - loss: 0.3154 -
 val_RootMeanSquaredError: 1.0213 - val_RootMeanSquaredError_1: 1.2052 -
 val_loss: 1.0840
 Epoch 15/100
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5569 - RootMeanSquaredError_1: 0.6009 - loss: 0.3153 -
 val_RootMeanSquaredError: 0.8784 - val_RootMeanSquaredError_1: 0.7932 -
 val_loss: 0.7573
 Epoch 16/100
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5558 - RootMeanSquaredError_1: 0.5988 - loss: 0.3139 -
 val_RootMeanSquaredError: 1.1506 - val_RootMeanSquaredError_1: 1.1822 -
 val_loss: 1.3312
 Epoch 17/100
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5559 - RootMeanSquaredError_1: 0.5979 - loss: 0.3139 -
 val_RootMeanSquaredError: 1.0621 - val_RootMeanSquaredError_1: 0.8752 -
 val_loss: 1.0919
 Epoch 18/100
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5556 - RootMeanSquaredError_1: 0.5972 - loss: 0.3135 -
 val_RootMeanSquaredError: 0.9998 - val_RootMeanSquaredError_1: 1.1077 -
 val_loss: 1.0223
 Epoch 19/100
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5537 - RootMeanSquaredError_1: 0.5960 - loss: 0.3115 -
 val_RootMeanSquaredError: 0.7957 - val_RootMeanSquaredError_1: 0.6926 -
 val_loss: 0.6177
 Epoch 20/100
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5523 - RootMeanSquaredError_1: 0.5938 - loss: 0.3098 -
 val_RootMeanSquaredError: 0.8167 - val_RootMeanSquaredError_1: 0.9693 -
 val_loss: 0.6943

Epoch 21/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5511 - RootMeanSquaredError_1: 0.5930 - loss: 0.3085 -
val_RootMeanSquaredError: 0.7157 - val_RootMeanSquaredError_1: 0.6734 -
val_loss: 0.5064
Epoch 22/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5507 - RootMeanSquaredError_1: 0.5922 - loss: 0.3081 -
val_RootMeanSquaredError: 0.9484 - val_RootMeanSquaredError_1: 0.9995 -
val_loss: 0.9095
Epoch 23/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5507 - RootMeanSquaredError_1: 0.5916 - loss: 0.3079 -
val_RootMeanSquaredError: 0.9413 - val_RootMeanSquaredError_1: 0.7843 -
val_loss: 0.8590
Epoch 24/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5508 - RootMeanSquaredError_1: 0.5910 - loss: 0.3080 -
val_RootMeanSquaredError: 0.9960 - val_RootMeanSquaredError_1: 1.3859 -
val_loss: 1.0848
Epoch 25/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5501 - RootMeanSquaredError_1: 0.5923 - loss: 0.3075 -
val_RootMeanSquaredError: 0.8405 - val_RootMeanSquaredError_1: 0.8404 -
val_loss: 0.7064
Epoch 26/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5493 - RootMeanSquaredError_1: 0.5898 - loss: 0.3064 -
val_RootMeanSquaredError: 0.8693 - val_RootMeanSquaredError_1: 1.0139 -
val_loss: 0.7829
Epoch 27/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5479 - RootMeanSquaredError_1: 0.5877 - loss: 0.3048 -
val_RootMeanSquaredError: 0.6776 - val_RootMeanSquaredError_1: 0.6298 -
val_loss: 0.4529
Epoch 28/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5471 - RootMeanSquaredError_1: 0.5865 - loss: 0.3038 -
val_RootMeanSquaredError: 0.8521 - val_RootMeanSquaredError_1: 0.9563 -
val_loss: 0.7450
Epoch 29/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5479 - RootMeanSquaredError_1: 0.5878 - loss: 0.3048 -
val_RootMeanSquaredError: 0.8346 - val_RootMeanSquaredError_1: 0.7558 -
val_loss: 0.6841
Epoch 30/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5471 - RootMeanSquaredError_1: 0.5859 - loss: 0.3038 -
val_RootMeanSquaredError: 0.9366 - val_RootMeanSquaredError_1: 1.2434 -
val_loss: 0.9441
Epoch 31/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5448 - RootMeanSquaredError_1: 0.5840 - loss: 0.3013 -
val_RootMeanSquaredError: 0.8158 - val_RootMeanSquaredError_1: 0.8978 -





```

val_loss: 0.6796
Epoch 32/100
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5447 - RootMeanSquaredError_1: 0.5843 - loss: 0.3012 -
val_RootMeanSquaredError: 0.8045 - val_RootMeanSquaredError_1: 0.7176 -
val_loss: 0.6339
Epoch 33/100
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5438 - RootMeanSquaredError_1: 0.5815 - loss: 0.3000 -
val_RootMeanSquaredError: 0.7032 - val_RootMeanSquaredError_1: 0.6171 -
val_loss: 0.4832
Epoch 34/100
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5430 - RootMeanSquaredError_1: 0.5816 - loss: 0.2993 -
val_RootMeanSquaredError: 0.8456 - val_RootMeanSquaredError_1: 0.9718 -
val_loss: 0.7380
Epoch 35/100
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5425 - RootMeanSquaredError_1: 0.5814 - loss: 0.2987 -
val_RootMeanSquaredError: 0.8133 - val_RootMeanSquaredError_1: 0.7557 -
val_loss: 0.6525
Epoch 36/100
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5425 - RootMeanSquaredError_1: 0.5816 - loss: 0.2988 -
val_RootMeanSquaredError: 0.6379 - val_RootMeanSquaredError_1: 0.7324 -
val_loss: 0.4199
Epoch 37/100
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5411 - RootMeanSquaredError_1: 0.5796 - loss: 0.2971 -
val_RootMeanSquaredError: 0.6410 - val_RootMeanSquaredError_1: 0.5897 -
val_loss: 0.4046
Epoch 38/100
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5406 - RootMeanSquaredError_1: 0.5794 - loss: 0.2967 -
val_RootMeanSquaredError: 0.6772 - val_RootMeanSquaredError_1: 0.8651 -
val_loss: 0.4876
Epoch 39/100
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5398 - RootMeanSquaredError_1: 0.5786 - loss: 0.2957 -
val_RootMeanSquaredError: 0.6132 - val_RootMeanSquaredError_1: 0.5858 -
val_loss: 0.3727
Epoch 40/100
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5395 - RootMeanSquaredError_1: 0.5785 - loss: 0.2955 -
val_RootMeanSquaredError: 0.9271 - val_RootMeanSquaredError_1: 1.3718 -
val_loss: 0.9618
Epoch 41/100
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5394 - RootMeanSquaredError_1: 0.5798 - loss: 0.2956 -
val_RootMeanSquaredError: 0.7829 - val_RootMeanSquaredError_1: 0.8517 -
val_loss: 0.6242
Epoch 42/100
363/363 ————— 0s 1ms/step -
RootMeanSquaredError: 0.5398 - RootMeanSquaredError_1: 0.5795 - loss: 0.2958 -

```

val_RootMeanSquaredError: 1.6921 - val_RootMeanSquaredError_1: 1.9738 -
val_loss: 2.9666
Epoch 43/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5454 - RootMeanSquaredError_1: 0.5854 - loss: 0.3021 -
val_RootMeanSquaredError: 0.8399 - val_RootMeanSquaredError_1: 0.7203 -
val_loss: 0.6867
Epoch 44/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5402 - RootMeanSquaredError_1: 0.5783 - loss: 0.2961 -
val_RootMeanSquaredError: 0.6235 - val_RootMeanSquaredError_1: 0.7759 -
val_loss: 0.4100
Epoch 45/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5377 - RootMeanSquaredError_1: 0.5763 - loss: 0.2935 -
val_RootMeanSquaredError: 0.5308 - val_RootMeanSquaredError_1: 0.5859 -
val_loss: 0.2879
Epoch 46/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5387 - RootMeanSquaredError_1: 0.5782 - loss: 0.2946 -
val_RootMeanSquaredError: 0.5518 - val_RootMeanSquaredError_1: 0.6495 -
val_loss: 0.3162
Epoch 47/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5365 - RootMeanSquaredError_1: 0.5752 - loss: 0.2922 -
val_RootMeanSquaredError: 0.5273 - val_RootMeanSquaredError_1: 0.5826 -
val_loss: 0.2842
Epoch 48/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5355 - RootMeanSquaredError_1: 0.5739 - loss: 0.2911 -
val_RootMeanSquaredError: 0.5395 - val_RootMeanSquaredError_1: 0.6340 -
val_loss: 0.3021
Epoch 49/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5342 - RootMeanSquaredError_1: 0.5731 - loss: 0.2897 -
val_RootMeanSquaredError: 0.5349 - val_RootMeanSquaredError_1: 0.6087 -
val_loss: 0.2945
Epoch 50/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5339 - RootMeanSquaredError_1: 0.5728 - loss: 0.2894 -
val_RootMeanSquaredError: 0.7951 - val_RootMeanSquaredError_1: 0.9697 -
val_loss: 0.6630
Epoch 51/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5341 - RootMeanSquaredError_1: 0.5732 - loss: 0.2896 -
val_RootMeanSquaredError: 0.8907 - val_RootMeanSquaredError_1: 0.9911 -
val_loss: 0.8122
Epoch 52/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5348 - RootMeanSquaredError_1: 0.5740 - loss: 0.2904 -
val_RootMeanSquaredError: 0.8140 - val_RootMeanSquaredError_1: 0.8948 -
val_loss: 0.6764
Epoch 53/100
363/363  0s 1ms/step -

```

RootMeanSquaredError: 0.5341 - RootMeanSquaredError_1: 0.5728 - loss: 0.2896 -
val_RootMeanSquaredError: 0.8266 - val_RootMeanSquaredError_1: 0.6926 -
val_loss: 0.6629
Epoch 54/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5347 - RootMeanSquaredError_1: 0.5731 - loss: 0.2902 -
val_RootMeanSquaredError: 0.8771 - val_RootMeanSquaredError_1: 0.9348 -
val_loss: 0.7798
Epoch 55/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5337 - RootMeanSquaredError_1: 0.5721 - loss: 0.2891 -
val_RootMeanSquaredError: 0.6440 - val_RootMeanSquaredError_1: 0.6874 -
val_loss: 0.4205
Epoch 56/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5320 - RootMeanSquaredError_1: 0.5709 - loss: 0.2874 -
val_RootMeanSquaredError: 0.8745 - val_RootMeanSquaredError_1: 0.9783 -
val_loss: 0.7840
Epoch 57/100
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5320 - RootMeanSquaredError_1: 0.5706 - loss: 0.2873 -
val_RootMeanSquaredError: 0.5890 - val_RootMeanSquaredError_1: 0.6695 -
val_loss: 0.3570

```

Custom callbacks can also be written by inheriting from `tf.keras.callbacks.Callback` for example the below callback prints the ratio between the validation loss and the training loss to detect overfitting

```

[ ]: class PrintValTrainRatioCallback(tf.keras.callbacks.Callback):
      def on_epoch_end(self, epoch, logs):
          ratio = logs["val_loss"] / logs["loss"]
          print(f" Epoch={epoch}, ratio={ratio:.2f}")





```

```

[ ]: hist = wideAndDeep.fit(
      (XTrainWide, XTrainDeep),
      ytrains,
      epochs=100,
      validation_data=((XValidWide, XValidDeep), yvals),
      callbacks=[checkpoint, earlyStop, PrintValTrainRatioCallback()],
      )















```

```

Epoch 1/100
362/363  0s 835us/step -
RootMeanSquaredError: 0.5355 - RootMeanSquaredError_1: 0.5743 - loss: 0.2911
Epoch=0, ratio=1.01
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5355 - RootMeanSquaredError_1: 0.5743 - loss: 0.2911 -
val_RootMeanSquaredError: 0.5353 - val_RootMeanSquaredError_1: 0.6181 -
val_loss: 0.2961
Epoch 2/100
319/363  0s 956us/step -
RootMeanSquaredError: 0.5350 - RootMeanSquaredError_1: 0.5733 - loss: 0.2905
Epoch=1, ratio=1.00
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5348 - RootMeanSquaredError_1: 0.5737 - loss: 0.2903 -
val_RootMeanSquaredError: 0.5352 - val_RootMeanSquaredError_1: 0.5826 -

```



```

val_loss: 0.2917
Epoch 3/100
348/363  0s 871us/step -
RootMeanSquaredError: 0.5347 - RootMeanSquaredError_1: 0.5735 - loss: 0.2902
Epoch=2, ratio=4.02
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5347 - RootMeanSquaredError_1: 0.5736 - loss: 0.2902 -
val_RootMeanSquaredError: 1.0613 - val_RootMeanSquaredError_1: 1.2585 -
val_loss: 1.1721
Epoch 4/100
305/363  0s 828us/step -
RootMeanSquaredError: 0.5361 - RootMeanSquaredError_1: 0.5748 - loss: 0.2917
Epoch=3, ratio=2.95
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5363 - RootMeanSquaredError_1: 0.5759 - loss: 0.2921 -
val_RootMeanSquaredError: 0.9299 - val_RootMeanSquaredError_1: 0.9716 -
val_loss: 0.8726
Epoch 5/100
357/363  0s 849us/step -
RootMeanSquaredError: 0.5358 - RootMeanSquaredError_1: 0.5751 - loss: 0.2915
Epoch=4, ratio=2.08
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5358 - RootMeanSquaredError_1: 0.5752 - loss: 0.2915 -
val_RootMeanSquaredError: 0.7694 - val_RootMeanSquaredError_1: 0.8887 -
val_loss: 0.6118
Epoch 6/100
315/363  0s 805us/step -
RootMeanSquaredError: 0.5345 - RootMeanSquaredError_1: 0.5726 - loss: 0.2900
Epoch=5, ratio=2.36
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5344 - RootMeanSquaredError_1: 0.5732 - loss: 0.2900 -
val_RootMeanSquaredError: 0.8325 - val_RootMeanSquaredError_1: 0.7989 -
val_loss: 0.6876
Epoch 7/100
308/363  0s 818us/step -
RootMeanSquaredError: 0.5340 - RootMeanSquaredError_1: 0.5722 - loss: 0.2894
Epoch=6, ratio=1.41
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5340 - RootMeanSquaredError_1: 0.5729 - loss: 0.2895 -
val_RootMeanSquaredError: 0.6307 - val_RootMeanSquaredError_1: 0.7347 -
val_loss: 0.4120
Epoch 8/100
316/363  0s 797us/step -
RootMeanSquaredError: 0.5330 - RootMeanSquaredError_1: 0.5708 - loss: 0.2883
Epoch=7, ratio=1.33
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5328 - RootMeanSquaredError_1: 0.5712 - loss: 0.2881 -
val_RootMeanSquaredError: 0.6210 - val_RootMeanSquaredError_1: 0.6084 -
val_loss: 0.3841
Epoch 9/100
313/363  0s 806us/step -
RootMeanSquaredError: 0.5321 - RootMeanSquaredError_1: 0.5700 - loss: 0.2874
Epoch=8, ratio=1.92
363/363  0s 1ms/step -

```



```

RootMeanSquaredError: 0.5320 - RootMeanSquaredError_1: 0.5705 - loss: 0.2873 -
val_RootMeanSquaredError: 0.7303 - val_RootMeanSquaredError_1: 0.8686 -
val_loss: 0.5555
Epoch 10/100
319/363  0s 796us/step -
RootMeanSquaredError: 0.5316 - RootMeanSquaredError_1: 0.5692 - loss: 0.2868
Epoch=9, ratio=1.00
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5315 - RootMeanSquaredError_1: 0.5697 - loss: 0.2867 -
val_RootMeanSquaredError: 0.5310 - val_RootMeanSquaredError_1: 0.5793 -
val_loss: 0.2873

```

1.7.7 Using TensorBoard for Visualization

TensorBoard is a browser-based application that allows you to visualize training stats. To use it you need to modify your program to output the data you want to visualize to special binary log files called *event files*. Each binary data record is called a *summary*. TensorBoard reads these files and displays the data.

```

[ ]: from time import strftime

def get_run_logdir(root_logdir="logs"):
    return Path(root_logdir) / strftime("run_%Y_%m_%d-%H_%M_%S")

run = get_run_logdir()

[ ]: norm = tf.keras.layers.Normalization()

reg = tf.keras.Sequential(
    [
        tf.keras.layers.Input(shape=XTrain.shape[1:]),
        norm,
        tf.keras.layers.Dense(50, activation="relu"),
        tf.keras.layers.Dense(50, activation="relu"),
        tf.keras.layers.Dense(50, activation="relu"),
        tf.keras.layers.Dense(1),
    ]
)

opt = tf.keras.optimizers.Adam(learning_rate=2e-3)

reg.compile(loss="mse", optimizer=opt, metrics=["RootMeanSquaredError"])

[ ]: tensorboard = tf.keras.callbacks.TensorBoard(run, profile_batch=(100, 200))
norm.adapt(XTrain)
hist = reg.fit(
    XTrain, yTrain, epochs=20, validation_data=(XValid, yValid),
    callbacks=[tensorboard]
)

```

Epoch 1/20


2024-07-23 12:17:51.013127: I
external/local_tsl/tsl/profiler/lib/profiler_session.cc:104] Profiler session


```

initializing.
2024-07-23 12:17:51.013162: I
external/local_tsl/tsl/profiler/lib/profiler_session.cc:119] Profiler session
started.
2024-07-23 12:17:51.013720: I
external/local_tsl/tsl/profiler/lib/profiler_session.cc:131] Profiler session
tear down.

172/363  0s 2ms/step -
RootMeanSquaredError: 1.1236 - loss: 1.3335


2024-07-23 12:17:52.373750: I
external/local_tsl/tsl/profiler/lib/profiler_session.cc:104] Profiler session
initializing.
2024-07-23 12:17:52.373790: I
external/local_tsl/tsl/profiler/lib/profiler_session.cc:119] Profiler session
started.
2024-07-23 12:17:52.545277: I
external/local_tsl/tsl/profiler/lib/profiler_session.cc:70] Profiler session
collecting data.
2024-07-23 12:17:52.574379: I
external/local_tsl/tsl/profiler/lib/profiler_session.cc:131] Profiler session
tear down.


319/363  0s 2ms/step -
RootMeanSquaredError: 0.9936 - loss: 1.0455


2024-07-23 12:17:52.576488: I
external/local_tsl/tsl/profiler/rpc/client/save_profile.cc:144] Collecting
XSpace to repository:
logs/run_2024_07_23-12_17_50/plugins/profile/2024_07_23_12_17_52/BM0-
end.xplane.pb


363/363  2s 3ms/step -
RootMeanSquaredError: 0.9689 - loss: 0.9941 - val_RootMeanSquaredError: 0.8554 -
val_loss: 0.7317
Epoch 2/20
363/363  0s 1ms/step -
RootMeanSquaredError: 0.6371 - loss: 0.4061 - val_RootMeanSquaredError: 0.5914 -
val_loss: 0.3498
Epoch 3/20
363/363  0s 1ms/step -
RootMeanSquaredError: 0.6099 - loss: 0.3722 - val_RootMeanSquaredError: 0.7210 -
val_loss: 0.5199
Epoch 4/20
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5902 - loss: 0.3486 - val_RootMeanSquaredError: 0.8382 -
val_loss: 0.7026
Epoch 5/20
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5776 - loss: 0.3337 - val_RootMeanSquaredError: 0.7712 -
val_loss: 0.5948
Epoch 6/20
363/363  0s 1ms/step -
RootMeanSquaredError: 0.5679 - loss: 0.3227 - val_RootMeanSquaredError: 0.7254 -
val_loss: 0.5261


```


Epoch 7/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5588 - loss: 0.3124 - val_RootMeanSquaredError: 0.5415 -
 val_loss: 0.2932


Epoch 8/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5496 - loss: 0.3022 - val_RootMeanSquaredError: 0.5793 -
 val_loss: 0.3356


Epoch 9/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5425 - loss: 0.2943 - val_RootMeanSquaredError: 0.5851 -
 val_loss: 0.3423


Epoch 10/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5413 - loss: 0.2931 - val_RootMeanSquaredError: 0.6448 -
 val_loss: 0.4158


Epoch 11/20
363/363  1s 2ms/step -
 RootMeanSquaredError: 0.5383 - loss: 0.2898 - val_RootMeanSquaredError: 0.5335 -
 val_loss: 0.2847


Epoch 12/20
363/363  1s 2ms/step -
 RootMeanSquaredError: 0.5339 - loss: 0.2851 - val_RootMeanSquaredError: 0.5682 -
 val_loss: 0.3228


Epoch 13/20
363/363  1s 1ms/step -
 RootMeanSquaredError: 0.5303 - loss: 0.2813 - val_RootMeanSquaredError: 0.6181 -
 val_loss: 0.3821


Epoch 14/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5291 - loss: 0.2800 - val_RootMeanSquaredError: 0.6360 -
 val_loss: 0.4045


Epoch 15/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5266 - loss: 0.2774 - val_RootMeanSquaredError: 0.5525 -
 val_loss: 0.3052

Epoch 16/20
363/363  1s 1ms/step -
 RootMeanSquaredError: 0.5225 - loss: 0.2730 - val_RootMeanSquaredError: 0.7503 -
 val_loss: 0.5630

Epoch 17/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5215 - loss: 0.2720 - val_RootMeanSquaredError: 0.5498 -
 val_loss: 0.3023

Epoch 18/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5259 - loss: 0.2766 - val_RootMeanSquaredError: 0.5276 -
 val_loss: 0.2783

Epoch 19/20
363/363  0s 1ms/step -
 RootMeanSquaredError: 0.5194 - loss: 0.2699 - val_RootMeanSquaredError: 0.5305 -
 val_loss: 0.2814

Epoch 20/20
363/363  0s 1ms/step -

```
RootMeanSquaredError: 0.5172 - loss: 0.2676 - val_RootMeanSquaredError: 0.5167 - val_loss: 0.2669
```

```
[ ]: %load_ext tensorboard
      %tensorboard --logdir=./logs
```

```
<IPython.core.display.HTML object>
```

1.7.8 Fine-Tuning Neural Network Hyperparameters

One option to determine the best hyperparameters for a neural network, is to convert it from a Keras model to a Scikit-Learn estimator, and using **GridSearchCV** or **RandomSearchCV** to fine tune the hyperparameters. For this you can use the **KerasRegressor** or **KerasClassifier** wrapper classes from SciKeras. But a better way is to use the **Keras Tuner** library.

1.7.8.1 Using Keras Tuner

```
[ ]: !{sys.executable} -m pip install keras-tuner
      import keras_tuner as kt
```

```
Collecting keras-tuner
```

```
  Downloading keras_tuner-1.4.7-py3-none-any.whl.metadata (5.4 kB)
```

```
Requirement already satisfied: keras in
```

```
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from keras-tuner) (3.3.3)
```

```
Requirement already satisfied: packaging in
```

```
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from keras-tuner) (24.1)
```

```
Requirement already satisfied: requests in
```

```
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from keras-tuner) (2.32.3)
```

```
Collecting kt-legacy (from keras-tuner)
```

```
  Downloading kt_legacy-1.0.5-py3-none-any.whl.metadata (221 bytes)
```

```
Requirement already satisfied: absl-py in
```

```
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from keras->keras-tuner) (2.1.0)
```

```
Requirement already satisfied: numpy in
```

```
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from keras->keras-tuner) (1.26.4)
```

```
Requirement already satisfied: rich in
```

```
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from keras->keras-tuner) (13.7.1)
```

```
Requirement already satisfied: namex in
```

```
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from keras->keras-tuner) (0.0.8)
```

```
Requirement already satisfied: h5py in
```

```
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from keras->keras-tuner) (3.11.0)
```

```
Requirement already satisfied: optree in
```

```
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from keras->keras-tuner) (0.11.0)
```

```
Requirement already satisfied: ml-dtypes in
```

```
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from keras->keras-tuner) (0.3.2)
```

```
Requirement already satisfied: charset-normalizer<4, ≥2 in
```

```

/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from
requests->keras-tuner) (3.3.2)
Requirement already satisfied: idna<4, ≥2.5 in
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from
requests->keras-tuner) (3.7)
Requirement already satisfied: urllib3<3, ≥1.21.1 in
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from
requests->keras-tuner) (2.2.2)
Requirement already satisfied: certifi≥2017.4.17 in
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from
requests->keras-tuner) (2024.6.2)
Requirement already satisfied: typing-extensions≥4.0.0 in
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from
optree->keras->keras-tuner) (4.12.2)
Requirement already satisfied: markdown-it-py≥2.2.0 in
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from
rich->keras->keras-tuner) (3.0.0)
Requirement already satisfied: pygments<3.0.0, ≥2.13.0 in
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from
rich->keras->keras-tuner) (2.18.0)
Requirement already satisfied: mdurl~=0.1 in
/home/mads/.pyenv/versions/ai/lib/python3.12/site-packages (from markdown-it-
py≥2.2.0->rich->keras->keras-tuner) (0.1.2)
Downloading keras_tuner-1.4.7-py3-none-any.whl (129 kB)
129.1/129.1 kB 440.2 kB/s eta 0:00:00 kB/s eta
0:00:01:01
Downloading kt_legacy-1.0.5-py3-none-any.whl (9.6 kB)
Installing collected packages: kt-legacy, keras-tuner
Successfully installed keras-tuner-1.4.7 kt-legacy-1.0.5

```

```

[ ]: def buildModel(hp):
    nHidden = hp.Int("n_hidden", min_value=0, max_value=8, default=2)
    nNeurons = hp.Int("n_neurons", min_value=16, max_value=256)
    learningRate = hp.Float(
        "learning_rate", min_value=1e-4, max_value=1e-2, sampling="log"
    )
    optimizer = hp.Choice("optimizer", values=["sgd", "adam"])

    if optimizer == "sgd":
        optimizer = tf.keras.optimizers.SGD(learning_rate=learningRate)
    else:
        optimizer = tf.keras.optimizers.Adam(learning_rate=learningRate)

    model = tf.keras.Sequential()
    model.add(tf.keras.layers.Flatten())
    for _ in range(nHidden):
        model.add(tf.keras.layers.Dense(nNeurons, activation="relu"))
    model.add(tf.keras.layers.Dense(10, activation="softmax"))
    model.compile(
        loss="sparse_categorical_crossentropy",
        optimizer=optimizer,
        metrics=["accuracy"],
    )

```

```
return model
```

```
[ ]:
```

Chapter 2

Deep Computer Vision and Convolutional Neural Networks (CNNs)

Convolutional Neural Networks are designed based on the way the human visual cortex perceives images with the neurons in the visual cortex being sensitive to small sub-regions of the visual field, called *receptive fields*. This is the basis of the design of CNNs, where the neurons in the first layer are connected to the pixels in the images in their receptive fields, and the neurons in the next layer are connected to the neurons in the previous layer, and so on

2.1 Convolutional Layers

Neurons in the first Convolutional layer are not connected to every pixel in the input image but instead only to pixels in their receptive fields. In turn each neuron in the second convolutional layer is connected only to neurons located within a small rectangle in the first layer. This architecture allows the network to concentrate on low-level features in the first hidden layer, then assemble them into higher-level features in the next hidden layer, and so on. The layers of a CNN are arranged in 2 dimensions in rows and in columns unlike the multi-layered perceptrons which are arranged in a single dimension.

A neuron located in row i , column j of a given layer is connected to the outputs of the neurons in the previous layer located in rows i to $i + f_h - 1$, columns j to $j + f_w - 1$, where f_h and f_w are the height and width of the receptive field. In order for a layer to have the same height and weight as the previous layer it is common to add zeros around the inputs, called *zero padding*. It is also possible to connect a large input layer to a much smaller layer by spacing out the receptive fields, thereby greatly reducing the model's computational complexity.

The horizontal or vertical step size from one receptive field to the next is called the *stride*. By increasing the stride the output layer will be smaller than the input layer, but the receptive field will be larger.

2.1.1 Filters

A neuron's weights can be represented as a small image the size of the receptive field. These weights can be termed as *filters* / *convolutional kernels* / *kernels*. These weights can be used to change what data the neuron actually takes in with entries in the filter being the parameters that the backpropagation algorithm can tweak. For example for a neuron with a receptive field of size 7x7, a filter could be a 7x7 matrix with all entries being 0 except for the 4th column which would be 1s. This filter would cause the neuron to detect everything in its receptive field except for the central vertical line, making it only sensitive to vertical lines.

Now if all the neurons in a layer use this vertical line filter (and the same bias term) an image passed to this layer would enhance the vertical lines in the image, while the horizontal lines would be blurred. Thus a layer full of neuron using the same filter outputs a **feature map**, which highlights the areas in an image that activate the filter the most.

During training the convolutional layer learns the most useful features for the task at hand, which above layers can then use to detect more complex patterns.

Employing the filter of a feature map the output of a neuron in a convolutional layer can be calculated as follows:

$$z_{i,j} = b + \sum_{u=0}^{f_h-1} \sum_{v=0}^{f_w-1} x_{i',j'} \times w_{u,v} \text{ with } \begin{cases} i' = i \times s_h + u \\ j' = j \times s_w + v \end{cases}$$

With:

- $z_{i,j}$ being the output of the neuron located in row i and column j in the convolutional layer
- b being the bias term for the neuron
- s_h and s_w being the vertical and horizontal strides
- f_h and f_w being the height and width of the receptive field
- $x_{i',j'}$ being the input of the neuron located in row i' and column j' in the previous layer
- $w_{u,v}$ being the connection weight between any neuron in the previous layer and the neuron located in row u and column v in the convolutional layer

2.1.2 Stacking Feature Maps

Convolution layers can have multiple filters and outputs one feature map per feature. CLs have one on neuron per pixel in each feature map, and all neurons within a given feature map share the same parameters, kernel and bias term. Neurons in different feature maps have different parameters, meaning the previous CL in the network neurons' receptive fields extend across the depth of the next CL, simultaneously applying all the filters to its input making it able to detect multiple features anywhere in its inputs.

Input layers are also composed of layers on per colour channel, usually coloured pictures have Red, Green and Blue layers. Specifically a neuron in the i th row, j th column and k feature map of a CL l is connected to the output neurons of the $l - 1$ CL in the rows $i \times s_h$ to $i \times s_h + f_h - 1$ and columns $j \times s_w$ to $j \times s_w + f_w - 1$, across all feature maps in later $l - 1$. Note that within a CL, all the neuron in the same row i and column j but in different feature maps are connected to the outputs of the same neurons in the previous layer. This leads to the output of a neuron in a feature map having the following equation:

$$z_{i,j,k} = b_k + \sum_{u=0}^{f_h-1} \sum_{v=0}^{f_w-1} \sum_{k'=0}^{f_n-1} x_{i',j',k'} \times w_{u,v,k',k} \text{ with } \begin{cases} i' = i \times s_h + u \\ j' = j \times s_w + v \end{cases}$$

With

- $z_{i,j,k}$ being the output of the neuron located in row i , column j in feature map k of the convolutional layer l
- s_h and s_w being the vertical and horizontal stride and f_w and f_h being the width and height of the receptive field
- f_n being the number of feature maps in the previous layer ($l - 1$)
- $x_{i',j',k'}$ being the output of the neuron located in layer $l - 1$, row i' , column j' and feature map k' or channel k' if the previous layer is the input layer.
- b_k being the bias term for the feature map k in layer l , which basically determines the brightness of feature map k
- $w_{u,v,k',k}$ being the connection weight between any neuron in feature map k of the layer l and its input located at row u , column v , relative to the neuron's receptive field, and feature map k'

```
[ ]: from sklearn.datasets import load_sample_images
```

```
images = load_sample_images()["images"]
images = tf.keras.layers.CenterCrop(height=70, width=120)(images)
images = tf.keras.layers.Rescaling(scale=1 / 255)(images)
images.shape
```

```
[ ]: TensorShape([2, 70, 120, 3])
```

```
[ ]: convLayer1 = tf.keras.layers.Conv2D(filters=32, kernel_size=7, padding="same")
fmaps = convLayer1(images)
fmaps.shape
```

```
[ ]: TensorShape([2, 70, 120, 32])
```

```
[ ]: kernels, biases = convLayer1.get_weights()
kernels.shape
```

```
[ ]: (7, 7, 3, 32)
```

```
[ ]: biases.shape
```

```
[ ]: (32,)
```

2.1.3 Activation functions

As the convolutional layers perform linear operations, and thus can only learn linear transformations of the input data, it is necessary to introduce non-linearity to the layers to allow the network to learn complex patterns. This is done by applying an activation function to the output of each neuron in the convolutional layer. The most common activation function used in CNNs is the **Rectified Linear Unit (ReLU)**, already defined above. This function is usually applied to the hidden convolutional layers of the network, but not to the output layer.

Activation functions are applied on the whole layer at once, meaning that the same activation function is applied to all the neurons in the layer. This is done to ensure that the network can learn to detect different patterns in different parts of the image. Therefore the activation function augments the output of the neuron in the feature map k of the layer l as follows:

$$h_{i,j,k} = \text{ReLU}(z_{i,j,k})$$

And in the case of a convolutional layer with a single feature map:

$$h_{i,j} = \text{ReLU}(z_{i,j})$$

```
[ ]: convLayer1 = tf.keras.layers.Conv2D(
    filters=32, kernel_size=7, padding="same", activation="relu"
)
fmaps = convLayer1(images)
fmaps.shape
```

```
[ ]: TensorShape([2, 70, 120, 32])
```

```
[ ]: kernels, biases = convLayer1.get_weights()
kernels.shape
```



```
[ ]: (7, 7, 3, 32)
```

2.2 Pooling Layers

The goal of pooling layers is to subsample / shrink the input image in order to reduce the computational load, memory usage and the number of parameters. Just like convolutional layers each neuron in a pooling layer is only connected to a limited number of neurons in the previous layer in a receptive field, however a pooling layer has no weights, all it does is aggregate the inputs using an aggregation function such as the mean or the max. A pooling layer employing the max aggregation function is called a **max pooling layer**.

Other than reducing computations, memory usage, and the number of parameters, max pooling layers introduce some level of **invariance** to small translations. This means that if a small feature is slightly moved in the input image, the output of the max pooling layer may not change. This can be useful for detecting patterns in images, as the location of the pattern in the image will not matter. By inserting a max pooling layer after every convolutional layer, the network can learn to be invariant to small translations which can be useful for classification tasks.

Max Pooling is however very destructive, as it discards all the information except for the maximum value. This can be a problem for tasks that require precise localization. To address this issue, a common strategy is to add a convolutional layer with the same number of filters as the max pooling layer just before the max pooling layer. This way the network can learn to preserve the information that will be most useful to the max pooling layer.

Pooling can also be performed along the depth dimension instead of spatial dimensions which will allow the CNN to be invariant to various features, such as rotation and scaling.

```
[ ]: maxPool = tf.keras.layers.MaxPool2D(pool_size=2)
```

```
[ ]: class DepthPool(tf.keras.layers.Layer):
    def __init__(self, pool_size=2, **kwargs):
        super().__init__(**kwargs)
        self.pool_size = pool_size

    def call(self, inputs):
        shape = tf.shape(inputs)
        groups = shape[-1] // self.pool_size
        newShape = tf.concat([shape[:-1], [groups, self.pool_size]], axis=0)
        return tf.reduce_max(tf.reshape(inputs, newShape), axis=-1)
```

Another type of pooling layer used commonly is the *global average pooling layer*. This layer computes the mean of each entire feature map, like an average pooling layer using a pooling size of the entire feature map. This means the layer outputs a single number per feature map and per instance. Although this is very destructive it can be useful just before the output layer.

Keras does not have a Depth wise Max Pooling layer, but it can be implemented reshaping its inputs to split the channels into groups of the desired, size then using `tf.reduce_max()` to compute the max of each group. This implementation assumes that the stride is equal to the pooling size.

```
[ ]: globAvgPool = tf.keras.layers.GlobalAveragePooling2D()
globAvgPool(images)
```

```
[ ]: <tf.Tensor: shape=(2, 3), dtype=float32, numpy=
array([[0.64338624, 0.5971759 , 0.5824972 ],
       [0.76306933, 0.2601113 , 0.10849128]], dtype=float32)>
```

2.3 CNN Architectures

A typical CNN architecture consists of a few convolutional layers, each generally followed by a ReLU layer, then a pooling layer, then another few convolutional layers again followed by a ReLU, then another pooling layer, and so on. The image gets smaller and smaller as it goes through the network, but also getting deeper and deeper due to the increasing number of filters in each convolutional layer. At the top of the stack of convolutional layers a regular feedforward neural network is added, composed of a few fully connected layers (+ReLU), and the final layer outputs the prediction, potentially using a softmax activation function if the network is used for classification to output estimated class probabilities.

```
[ ]: from functools import partial

conv2DLayer = partial(
    tf.keras.layers.Conv2D,
    kernel_size=3,
    padding="same",
    activation="relu",
    kernel_initializer="he_normal",
)
ffLayer = partial(
    tf.keras.layers.Dense, activation="relu", kernel_initializer="he_normal"
)

cnnCls = tf.keras.Sequential(
    [
        tf.keras.layers.Input(shape=[28, 28, 1]),
        tf.keras.layers.Reshape(target_shape=(28, 28, 1)),
        conv2DLayer(filters=64, kernel_size=7),
        tf.keras.layers.MaxPool2D(),
        conv2DLayer(filters=128),
        conv2DLayer(filters=128),
        tf.keras.layers.MaxPool2D(),
        conv2DLayer(filters=256),
        conv2DLayer(filters=256),
        tf.keras.layers.MaxPool2D(),
        tf.keras.layers.Flatten(),
        ffLayer(units=128),
        tf.keras.layers.Dropout(0.5),
        ffLayer(units=64),
        tf.keras.layers.Dropout(0.5),
        tf.keras.layers.Dense(units=10, activation="softmax"),
    ]
)

cnnCls.summary()
```

Model: "sequential_4"

Layer (type)	Output Shape	Param #
reshape (Reshape)	(None, 28, 28, 1)	0

conv2d_2 (Conv2D)	(None, 28, 28, 64)	3,200
max_pooling2d_1 (MaxPooling2D)	(None, 14, 14, 64)	0
conv2d_3 (Conv2D)	(None, 14, 14, 128)	73,856
conv2d_4 (Conv2D)	(None, 14, 14, 128)	147,584
max_pooling2d_2 (MaxPooling2D)	(None, 7, 7, 128)	0
conv2d_5 (Conv2D)	(None, 7, 7, 256)	295,168
conv2d_6 (Conv2D)	(None, 7, 7, 256)	590,080
max_pooling2d_3 (MaxPooling2D)	(None, 3, 3, 256)	0
flatten_2 (Flatten)	(None, 2304)	0
dense_23 (Dense)	(None, 128)	295,040
dropout (Dropout)	(None, 128)	0
dense_24 (Dense)	(None, 64)	8,256
dropout_1 (Dropout)	(None, 64)	0
dense_25 (Dense)	(None, 10)	650

Total params: 1,413,834 (5.39 MB)

Trainable params: 1,413,834 (5.39 MB)

Non-trainable params: 0 (0.00 B)

- First we use the `partial()` function to defined a template Convolutional Layer, with a small kernel size of 3x3, a stride of 1, the `same` padding, and the ReLU activation function. This template can be used to create any number of layers in the CNN.
- Next we create the CNN with the first **Input** layer taking in images in array representation of size $28 \times 28 \times 1$ as the images in the Fashion MNIST dataset are of size 28×28 and are in greyscale, with a **Reshape** layer to ensure the images are of this size.
- The first CL is of size 64 with fairly large filters (7×7) which creates a 64 feature maps each of size 28×28 .
- Then we add a max pooling layer with a default pool size of 2, so it downscales the feature maps by a factor of 2, resulting in 64 feature maps of size 14×14 .
- We repeat the same structure twice, two convolutional layers followed by a max pooling layer, each adding

on more feature maps, deepening the network. For larger images this structure could be repeated using the number of repetitions hyperparameter. The number of filters double as we climb up the CNN toward the output layer (64, 128, 256), as the number of low-level features is usually much lower than the number of high-level features. It is common to double the number of filters after each pooling layer as the pooling layer reduces the size of the feature maps by 2 by default, so we can afford to double the number of filters in the next layer without increasing the computational load.

- Next is the fully connected network, composed of two dense hidden layers and a dense output layer. Since it is a classification task with 10 classes the output layer has 10 layers and uses the softmax activation function to determine the class probabilities of each class. We must flatten the inputs just before the first dense layer as it expects a 1D array of features for each instance. Two dropout layers with a dropout rate of 50% each have also been added to reduce overfitting.

```
[ ]: cnnCls.compile(
    loss="sparse_categorical_crossentropy",
    optimizer=tf.keras.optimizers.SGD(learning_rate=0.09),
    metrics=["accuracy"],
)
cnnCls.summary()
```

Model: "sequential_4"

Layer (type)	Output Shape	Param #
reshape (Reshape)	(None, 28, 28, 1)	0
conv2d_2 (Conv2D)	(None, 28, 28, 64)	3,200
max_pooling2d_1 (MaxPooling2D)	(None, 14, 14, 64)	0
conv2d_3 (Conv2D)	(None, 14, 14, 128)	73,856
conv2d_4 (Conv2D)	(None, 14, 14, 128)	147,584
max_pooling2d_2 (MaxPooling2D)	(None, 7, 7, 128)	0
conv2d_5 (Conv2D)	(None, 7, 7, 256)	295,168
conv2d_6 (Conv2D)	(None, 7, 7, 256)	590,080
max_pooling2d_3 (MaxPooling2D)	(None, 3, 3, 256)	0
flatten_2 (Flatten)	(None, 2304)	0
dense_23 (Dense)	(None, 128)	295,040
dropout (Dropout)	(None, 128)	0
dense_24 (Dense)	(None, 64)	8,256

dropout_1 (Dropout)	(None, 64)	0
dense_25 (Dense)	(None, 10)	650

Total params: 1,413,834 (5.39 MB)

Trainable params: 1,413,834 (5.39 MB)

Non-trainable params: 0 (0.00 B)

```
[ ]: (XTrainFull, yTrainFull), (XTest, yTest) = fmnist
```

```
cutoff = -5000
XTrain, yTrain = XTrainFull[:cutoff], yTrainFull[:cutoff]
XValid, yValid = XTrainFull[cutoff:], yTrainFull[cutoff:]
XTrain, XValid, XTest = XTrain / 255.0, XValid / 255.0, XTest / 255.0
```

```
[ ]: hist = cnnCls.fit(
    XTrain, yTrain, epochs=10, validation_data=(XValid, yValid),
    callbacks=[earlyStop]
)
```

Epoch 1/10

1719/1719 ————— 139s 80ms/step

- accuracy: 0.5495 - loss: 1.3179 - val_accuracy: 0.8574 - val_loss: 0.3831

Epoch 2/10

1719/1719 ————— 126s 73ms/step

- accuracy: 0.8277 - loss: 0.4989 - val_accuracy: 0.8796 - val_loss: 0.3222

Epoch 3/10

1719/1719 ————— 126s 74ms/step

- accuracy: 0.8636 - loss: 0.4064 - val_accuracy: 0.8856 - val_loss: 0.3119

Epoch 4/10

1719/1719 ————— 129s 75ms/step

- accuracy: 0.8835 - loss: 0.3529 - val_accuracy: 0.8986 - val_loss: 0.2883

Epoch 5/10

1719/1719 ————— 153s 89ms/step

- accuracy: 0.8931 - loss: 0.3190 - val_accuracy: 0.8998 - val_loss: 0.2791

Epoch 6/10

1719/1719 ————— 134s 78ms/step

- accuracy: 0.9003 - loss: 0.2929 - val_accuracy: 0.9014 - val_loss: 0.2730

Epoch 7/10

1719/1719 ————— 137s 80ms/step

- accuracy: 0.9076 - loss: 0.2740 - val_accuracy: 0.9080 - val_loss: 0.2695

Epoch 8/10


1719/1719 ————— 140s 82ms/step

- accuracy: 0.9158 - loss: 0.2537 - val_accuracy: 0.9062 - val_loss: 0.2746



Epoch 9/10

1719/1719 ————— 141s 82ms/step

- accuracy: 0.9201 - loss: 0.2383 - val_accuracy: 0.9018 - val_loss: 0.2827

Epoch 10/10
 1719/1719  140s 81ms/step
 - accuracy: 0.9214 - loss: 0.2274 - val_accuracy: 0.9084 - val_loss: 0.2856

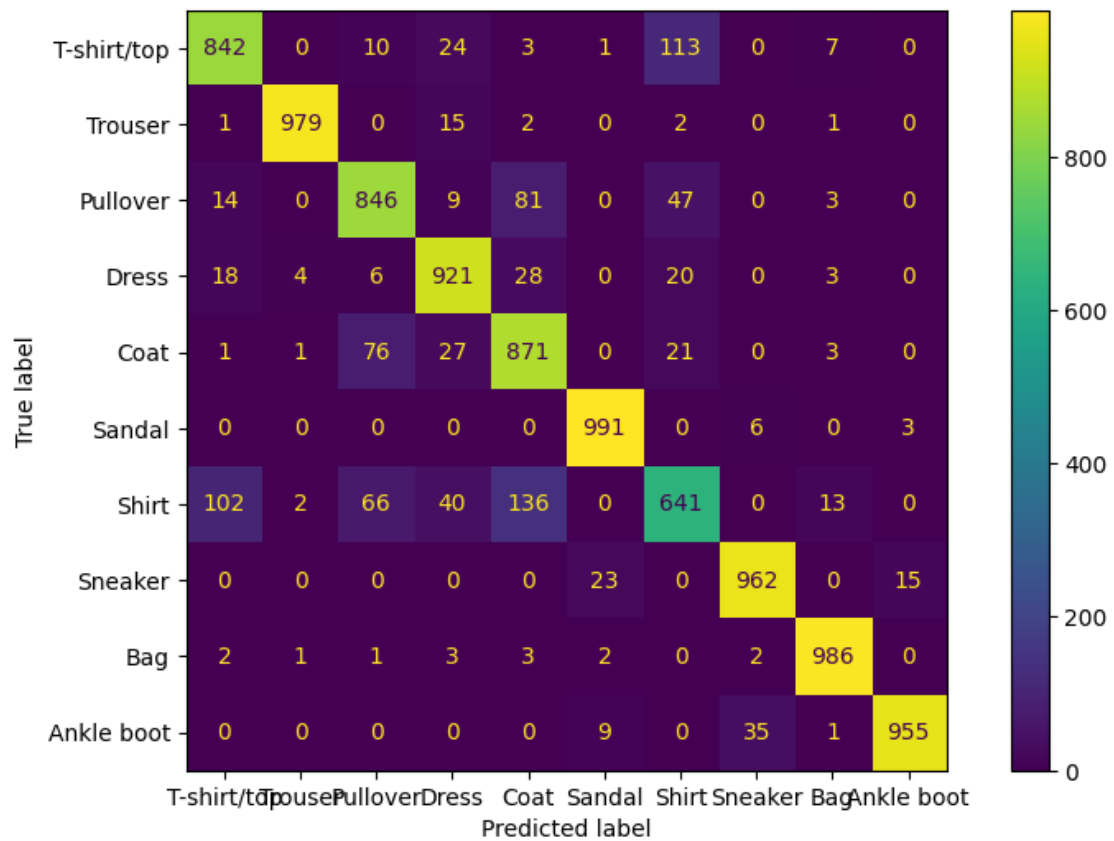
```
[ ]: preds = cnnCls.predict(XTest)
      preds = preds.argmax(axis=1)
      cnnCls.evaluate(XTest, yTest)
```

313/313  9s 27ms/step
 313/313  9s 28ms/step -
 accuracy: 0.8996 - loss: 0.3032

```
[ ]: [0.29478150606155396, 0.899399995803833]
```

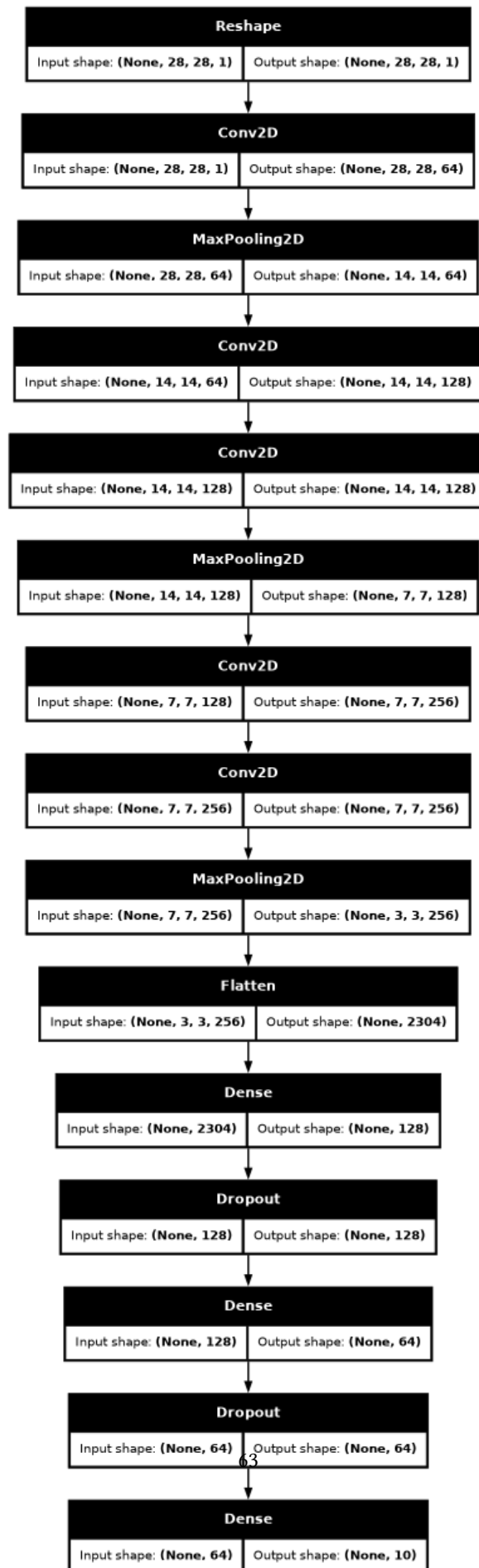
```
[ ]: classStats(yTest, preds, classNames)
```

	precision	recall	f1-score	support
0	0.86	0.84	0.85	1000
1	0.99	0.98	0.99	1000
2	0.84	0.85	0.84	1000
3	0.89	0.92	0.90	1000
4	0.77	0.87	0.82	1000
5	0.97	0.99	0.98	1000
6	0.76	0.64	0.70	1000
7	0.96	0.96	0.96	1000
8	0.97	0.99	0.98	1000
9	0.98	0.95	0.97	1000
accuracy			0.90	10000
macro avg	0.90	0.90	0.90	10000
weighted avg	0.90	0.90	0.90	10000



```
[ ]: tf.keras.utils.plot_model(cnnCls, show_shapes=True, dpi=50)
```

```
[ ]:
```



[]: