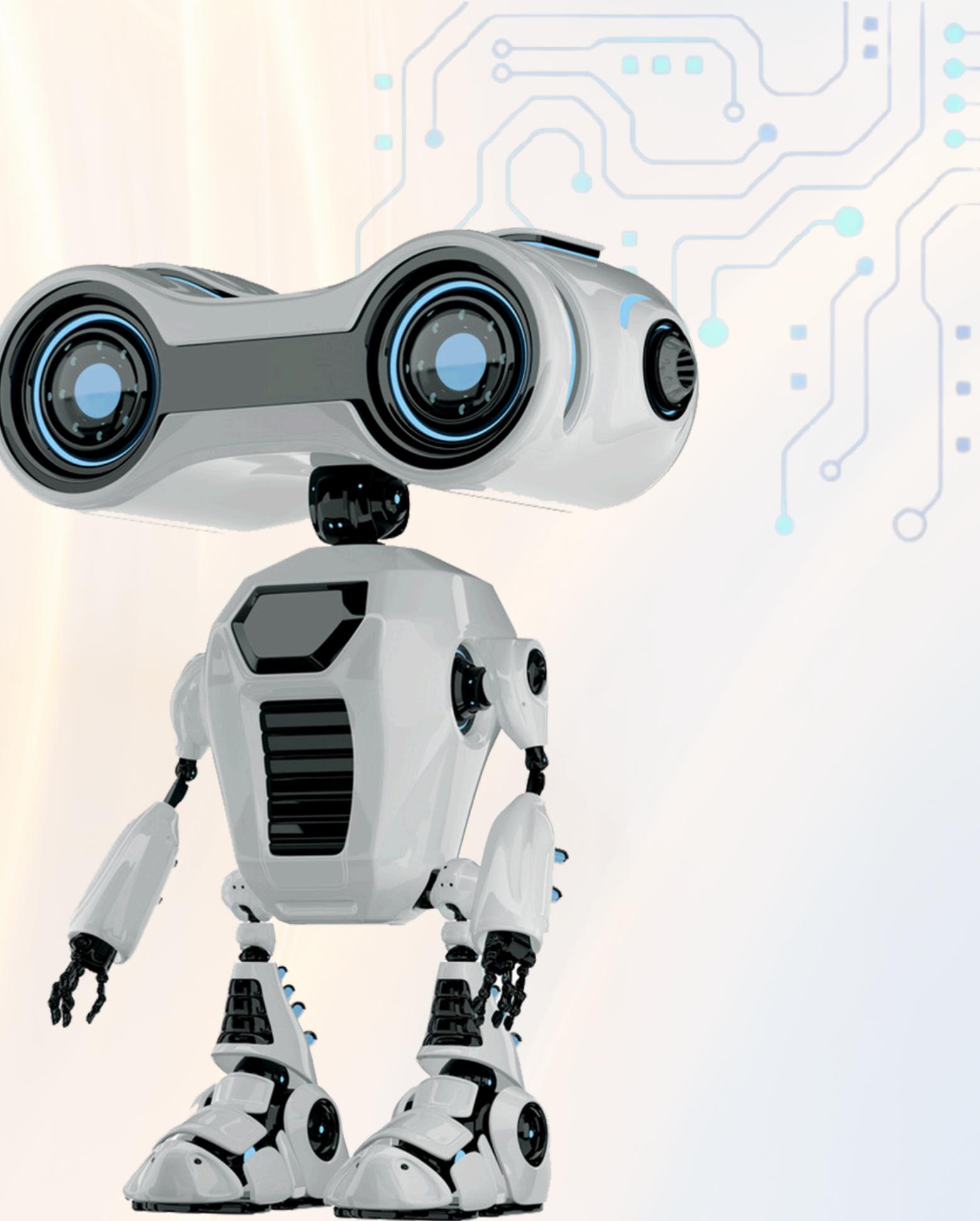
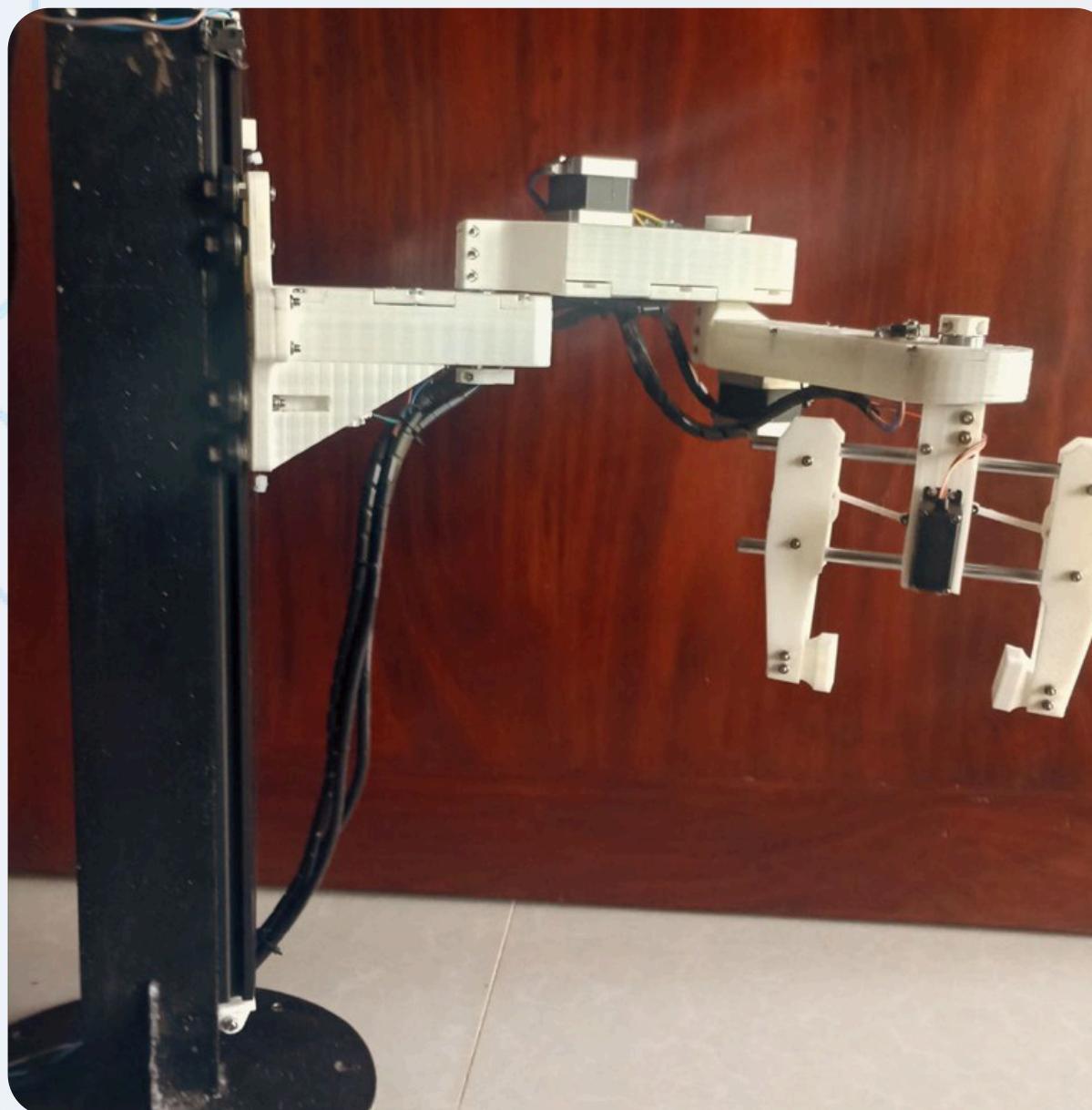


Kinematic Analysis of a Robot Arm

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Robotics Mini Project





Introduction

- The project involves the kinematic analysis of a SCARA (PRRR) robot arm with 4 DoF.
- Tasks include forward kinematics, inverse kinematics, Jacobian analysis, and a pick-and-place demonstration.
- Designed and built a functional SCARA robot with a gripper, powered by stepper motors, capable of holding objects up to 0.8 kg

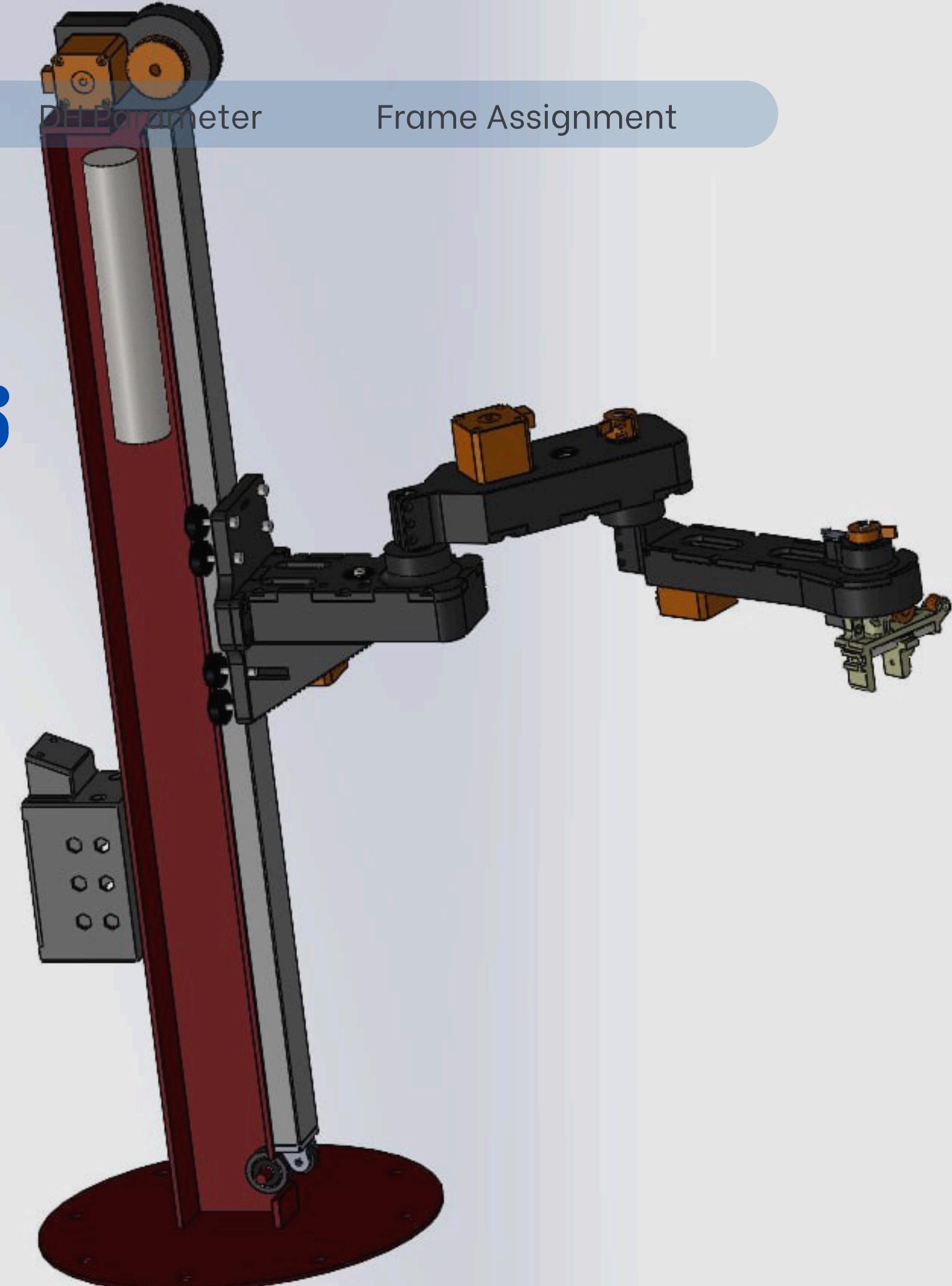
SCARA Robot Details

- Type: PRRR SCARA Robot with 4 DoF.
- Dimensions:
 - a₁=160 mm
 - a₂=220 mm
 - a₃=202 mm
 - d₄=60 mm
- Components:
 - Arduino Uno, CNC Shield, DRV8825 Drivers
 - NEMA 17 stepper motors, 3D-printed parts.
- 12V, 10A power supply.
- Functional gripper to handle round and square objects.

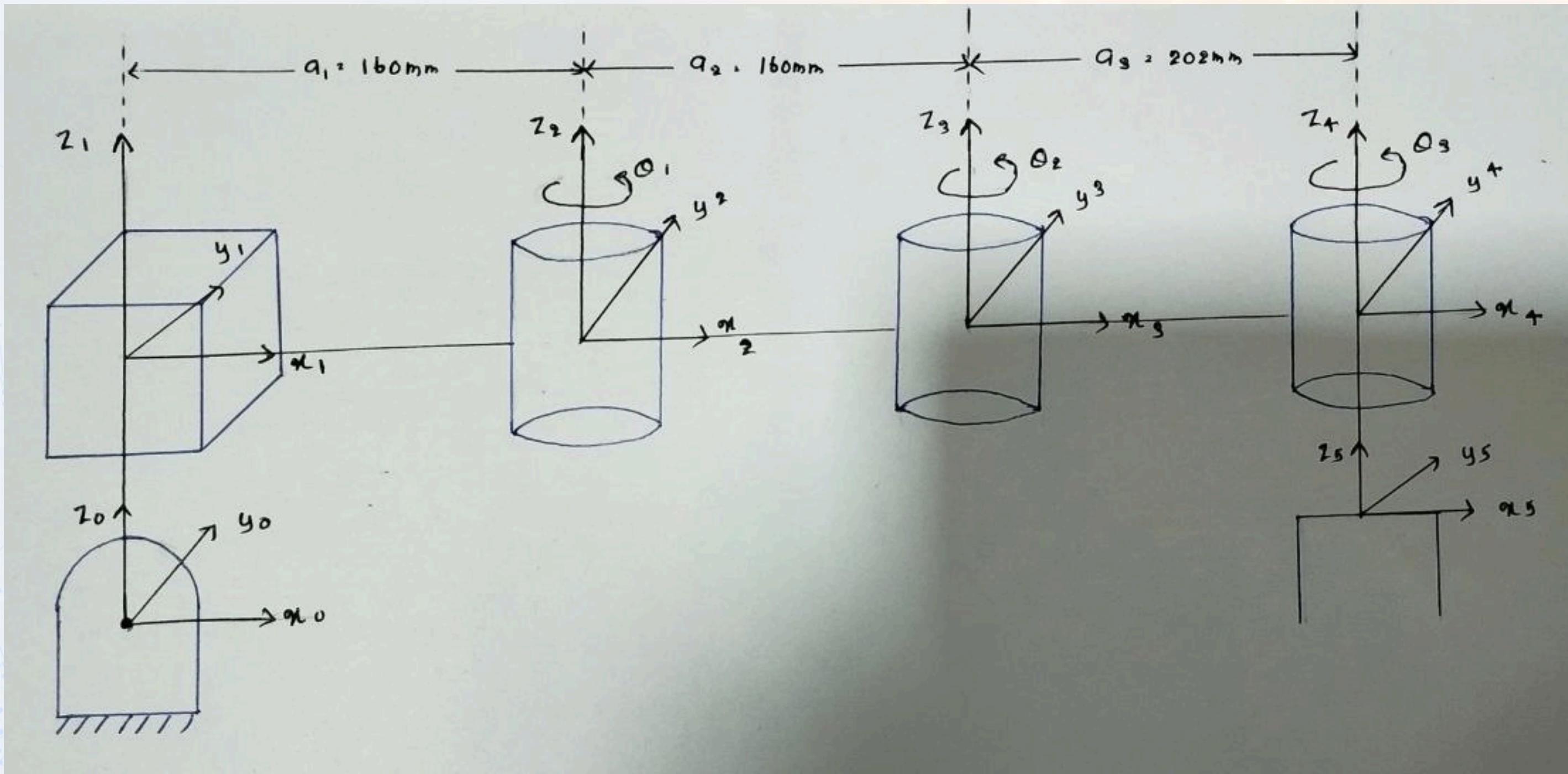
Robot Details

DH Parameter

Frame Assignment



SCARA Robot-Coordinate frame assignments



DH Parameter

Forward Kinematics

Inverse Kinematics

Denavit-Hartenberg (DH) Parameters

Joint (iii)	ai (mm)	ai	di(mm)	θi
1 (Prismatic)	0	0	d1(variable)	0
2 (Revolute)	160	0	0	θ1(variable)
3 (Revolute)	160	0	0	θ2(variable)
4 (Revolute)	202	0	0	θ3(variable)
5	0	0	60	0

Forward Kinematics

- Transformation matrix for each joint:

$$\begin{bmatrix} C_\theta & -S_\theta C_\alpha & S_\theta S_\alpha & aC_\theta \\ S_\theta & C_\theta C_\alpha & -C_\theta S_\alpha & aS_\theta \\ 0 & S_\alpha & C_\alpha & d \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- End-effector transformation matrix:
 $T_4^0 = T_1^0 \times T_2^1 \times T_3^2 \times T_4^3$
- Position of the end-effector (x,y,z) calculated from the matrix.

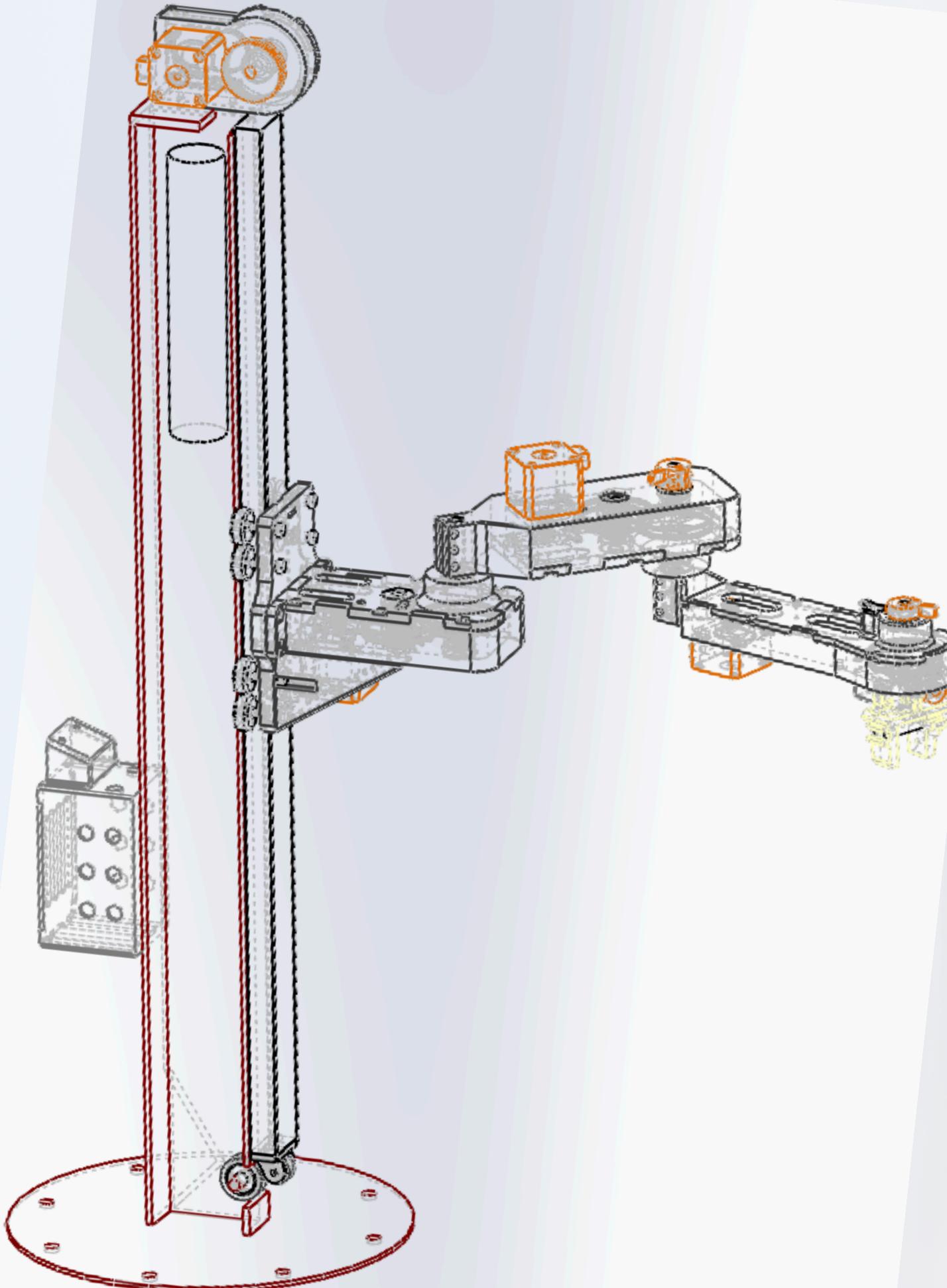


Forward Kinematics

For the end-effector position:

- $x = a_1 \sin(90) + a_2 \cos(\theta_1) + a_3 \cos(\theta_1 + \theta_2)$
- $x = 160 + 160 \cos(\theta_1) + 202 \cos(\theta_1 + \theta_2)$
- $y = a_1 \cos(90) + a_2 \sin(\theta_1) + a_3 \sin(\theta_1 + \theta_2)$
- $y = 0 + 160 \sin(\theta_1) + 202 \sin(\theta_1 + \theta_2)$
- $z = z_0 + d_1^*$

A_1	A_2	A_3	A_4	A_5
$A_1 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & d_1^* \\ 0 & 0 & 0 & 1 \end{bmatrix}$	$A_2 = \begin{bmatrix} c_1 & -s_1 & 0 & 160c_1 \\ s_1 & c_1 & 0 & 160s_1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$	$A_3 = \begin{bmatrix} c_2 & -s_2 & 0 & 160c_2 \\ s_2 & c_2 & 0 & 160s_2 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$	$A_4 = \begin{bmatrix} c_3 & -s_3 & 0 & 202c_3 \\ s_3 & c_3 & 0 & 202s_3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$	$A_5 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 60 \\ 0 & 0 & 0 & 1 \end{bmatrix}$



Inverse Kinematics

Manipulator Jacobian

GUI

Inverse Kinematics

Solve for θ_1 and θ_2 :

1. Projection on XY plane:

$$r = \sqrt{x^2 + y^2} \quad (\text{distance from origin in XY-plane}).$$

Use the law of cosines to solve for θ_2 :

$$\cos \theta_2 = \frac{r^2 - a_2^2 - a_3^2}{2a_2a_3}.$$

$$\theta_2 = \arccos(\cos \theta_2).$$

Solve for θ_1 using:

$$\theta_1 = \arctan 2(y, x) - \arctan 2\left(\frac{a_3 \sin \theta_2}{a_2 + a_3 \cos \theta_2}\right).$$

Manipulator Jacobian

Manipulator Jacobian

GUI

Homing

The Jacobian matrix is:

$$J = \begin{bmatrix} J_v \\ J_\omega \end{bmatrix},$$

Where:

$$J_v = [z_0 \quad z_1 \times (o_n - o_1) \quad z_2 \times (o_n - o_2) \quad z_3 \times (o_n - o_3)],$$

and:

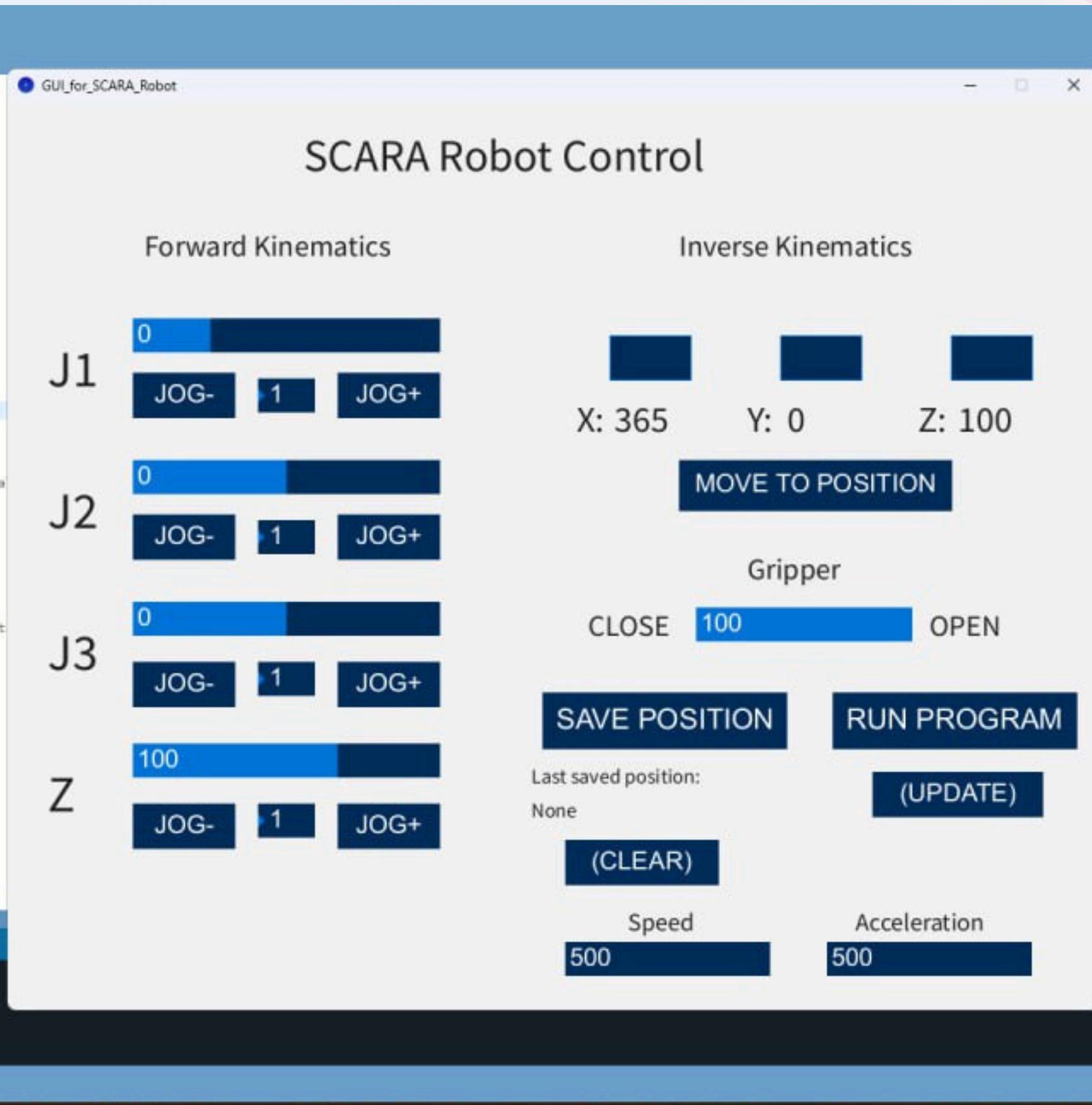
$$J_\omega = [\mathbf{0} \quad z_1 \quad z_2 \quad z_3].$$

$$J = \begin{bmatrix} (z_1^\circ, o_1) & z_1^\circ \times (t_4^\circ - t_1^\circ) & z_2^\circ \times (t_4^\circ - t_2^\circ) & z_3^\circ \times (t_5^\circ - t_3^\circ) \\ 0 & z_1^\circ & z_2^\circ & z_3^\circ \end{bmatrix}$$

GUI

Homing

Pick-and-Place Task



Graphical User Interface (GUI)

Provides an interactive interface for controlling the SCARA robot.

Key features include:

- Save positions and run predefined programs.
- Update, clear, and adjust speed and acceleration parameters.



Homing

- The robot resets to its base position before executing the task.

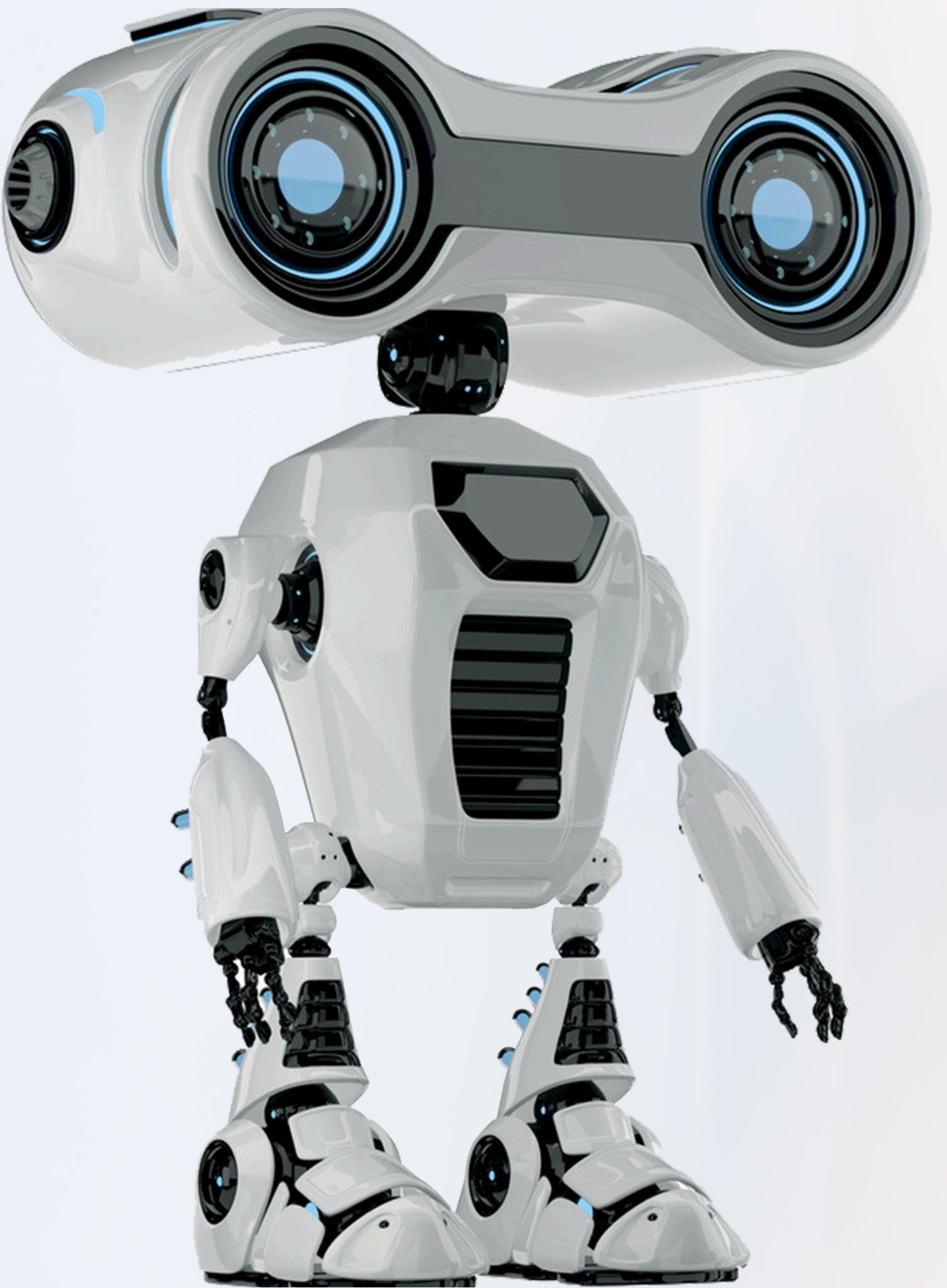
```
SCARA_Robot.ino
242
243 void homing() {
244     // Homing Stepper3
245     while (digitalRead(limitSwitch3) != 1) {
246         stepper3.setSpeed(-1100);
247         stepper3.runSpeed();
248         stepper3.setCurrentPosition(-1580); // When limit switch pressed set position to 0 steps
249     }
250     delay(20);
251
252     stepper3.moveTo(0);
253     while (stepper3.currentPosition() != 0) {
254         stepper3.run();
255     }
256
257     // Homing Stepper2
258     while (digitalRead(limitSwitch2) != 1) {
259         stepper2.setSpeed(1300);
260         stepper2.runSpeed();
261         stepper2.setCurrentPosition(4350); // When limit switch pressed set position to -5440 steps
262     }
263     delay(20);
264
265     stepper2.moveTo(0);
266     while (stepper2.currentPosition() != 0) {
267         stepper2.run();
268     }
269 }
```

In 13, Col 32 Arduino Uno on COM41 [not connected]



Pick and place task

- Pick a box from a given coordinate.
- Place it in a designated square.
- Record joint angles and end-effector positions



Questions?

Thank You!

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