

Machine Learning - Module 04

Regularization

Summary: Today you will fight overfitting! You will discover the concepts of regularization and how to implement it into the algorithms you already saw until now.

Notions and ressources

Notions of the module

Regularization, overfitting. Regularized loss function, regularized gradient descent. Regularized linear regression. Regularized logistic regression.

Useful Ressources

You are strongly advise to use the following resource: Machine Learning MOOC - Stanford Here are the sections of the MOOC that are relevant for today's exercises:

Week 3

Solving the Problem of Overfitting

- Classification (Video + Reading)
- Hypothesis Representation (Video + Reading)
- Decision Boundary (Video + Reading)

Logistic Regression Model

- Cost Function (Video + Reading)
- ullet Simplified Cost Function and Gradient Descent (Video + Reading)

Multiclass Classification

- \bullet Mutliclass Classification: One-vs-all (Video + Reading)
- Review (Reading + Quiz)

Common Instructions

- The version of Python recommended to use is 3.7, you can check the version of Python with the following command: python -V
- The norm: during this piscine, it is recommended to follow the PEP 8 standards, though it is not mandatory. You can install pycodestyle which is a tool to check your Python code.
- The function eval is never allowed.
- The exercises are ordered from the easiest to the hardest.
- Your exercises are going to be evaluated by someone else, so make sure that your variable names and function names are appropriate and civil.
- Your manual is the internet.
- You can also ask questions in the #bootcamps channel in the 42AI or 42born2code.
- If you find any issue or mistakes in the subject please create an issue on 42AI repository on Github.
- We encourage you to create test programs for your project even though this work won't have to be submitted and won't be graded. It will give you a chance to easily test your work and your peers' work. You will find those tests especially useful during your defence. Indeed, during defence, you are free to use your tests and/or the tests of the peer you are evaluating.
- Submit your work to your assigned git repository. Only the work in the git repository will be graded. If Deepthought is assigned to grade your work, it will be run after your peer-evaluations. If an error happens in any section of your work during Deepthought's grading, the evaluation will stop.

Contents

1	Exercise 00	4
II	Exercise 01	6
III	Exercise 02	11
IV	Exercise 03	13
V	Exercise 04	15
VI	Exercise 05	21
VII	Exercise 06	25
VIII	Exercise 07	28
IX	Exercise 08	30
X	Exercise 09	32
ΧI	Conclusion - What you have learnt	34

Chapter I

Exercise 00

	Exercise: 00	
/	Polynomial models II	
Turn-in directory : ex	00/	/
Files to turn in : polynomial_model_extended.py		
Forbidden functions: sklearn		

Objective

Create a function that takes a matrix X of dimensions $(m \times n)$ and an integer p as input, and returns a matrix of dimension $(m \times (np))$. For each column x_j of the matrix X, the new matrix contains x_j raised to the power of k, for k = 1, 2, ..., p:

$$x_1 \mid \ldots \mid x_n \mid x_1^2 \mid \ldots \mid x_n^2 \mid \ldots \mid x_1^p \mid \ldots \mid x_n^p$$

Instructions

In the polynomial_model_extended.py file, write the following function as per the instructions given below:

```
def add_polynomial_features(x, power):
    """Add polynomial features to matrix x by raising its columns to every power in the range
    of 1 up to the power given in argument.
Args:
    x: has to be an numpy.array, where x.shape = (m,n) i.e. a matrix of shape m * n.
    power: has to be a positive integer, the power up to which the columns of matrix x
    are going to be raised.
Return:
    - The matrix of polynomial features as a numpy.array, of shape m * (np),
    containg the polynomial feature values for all training examples.
    - None if x is an empty numpy.array.
    - None if x or power is not of the expected type.
Raises:
    This function should not raise any Exception.
"""
... Your code ...
```

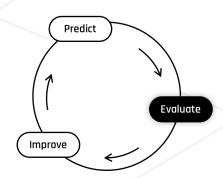
Examples

Chapter II

Exercise 01

Interlude

Fighting Overfitting... With Regularization



In the **module07**, we talked about the problem of **overfitting** and the necessity of splitting the dataset into a **training set** and a **test set** in order to spot it. However, being able to detect overfitting does not mean being able to avoid it. To address this important issue, it is time to introduce you to a new technique: **regularization**. If you remember well, overfitting happens because the model takes advantage of irrelevant signals in the training data. The basic idea behind regularization is to **penalize the model for putting too much weight on certain** (usually heavy polynomial) **features**. We do this by adding an extra term in the loss function:

regularized loss function = loss function +
$$\frac{\lambda}{2m} \sum_{j=1}^{n} \theta_j^2$$

By doing so, we are encouraging the model to keep its θ values as small as **possible**. Indeed, the values of θ themselves are now taken into account when calculating the loss.

 λ (called lambda) is the parameter through which you can modulate how reglarization should impact the model's construction.

- If $\lambda = 0$, there is no regularization (as we did until now).
- If λ is very large, it will drive all the θ parameters to 0.



In the regularization term, the sum starts at j=1 because we do NOT want to penalize the value of θ_0 (the y-intercept, which doesn't depend on a feature).

Be carefull!

Machine Learning was essentially developed by computer scientists (not mathematicians). This can cause problems when we try to represent things mathematically. For example: using the θ_0 notation to represent the y-intercept makes things easy when we apply the linear algebra trick, **but** it completly messes up the overall matrix notation! According to that notation, the X' matrix has the following properties:

- its rows, $x'^{(i)}$, follow the mathematical indexing: starting at 1.
- its columns, x'_{i} , follow the computer science indexing: starting at 0.

$$X' = \underbrace{\begin{bmatrix} 1 & x_1^{(1)} & \dots & x_n^{(1)} \\ \vdots & \vdots & \ddots & \vdots \\ 1 & x_1^{(m)} & \dots & x_n^{(m)} \end{bmatrix}}_{j = 0, \dots, n} = \begin{bmatrix} x_0^{(1)} & x_1^{(1)} & \dots & x_n^{(1)} \\ \vdots & \vdots & \ddots & \vdots \\ x_0^{(m)} & x_1^{(m)} & \dots & x_n^{(m)} \end{bmatrix} }_{j = 1, \dots, m}$$

It's precisely for this reason that you keep seeing that X' is of dimension $(m \times (n+1))$.

Terminology

The regularization technique we are introducing here is named L_2 regularization, because it adds the squared L_2 norm of the θ vector to the loss function. The L_2 norm of a given vector x, written

$$L_2(x) = ||x||_2 = \sqrt{\sum_i x_i^2} L_2(x)^2 = ||x||_2^2 = \sum_i x_i^2$$

is its euclidean norm (i.e. the sum of the components squared).

There is an infinite variety of norms that could be used as regularization terms, depending on the desired regularization effect. Here, we will only use L_2 , the most common one.



The notation \sum_i means: "the sum for all i" There is no need to give explicitly the start and the end of the summation index if we want to sum over all the values of i. However, it is better to do it anyway because it forces us to be sure of what we are doing. And in our case, we do not want to sum over θ_0 ...

Our old friend vectorization ...

It is not a surprise, we can use vectorization to calculate $\sum_{j=1}^{n} \theta_{j}^{2}$ more efficiently. It could be a good exercise for you to try to figure it out by yourself. We suggest you give it a try and then check the answer on the next page.

Answers to the Vectorization Problem

So, how do you vectorize the following?

$$\sum_{i=j}^{n} \theta_j^2$$

It's very similar to a **dot product** of θ with itself. The only problem here is to find a way to not take θ_0 into account.

Let's construct a vector θ' with the following rules :

$$\theta'_0 = 0$$
 $\theta'_j = \theta_j \quad \text{for } j = 1, \dots, n$

In other words:

$$\theta' = \begin{bmatrix} 0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix}$$

This way, we can perform the dot product without having θ_0 interfering in our calculations:

$$\theta' \cdot \theta' = \begin{bmatrix} 0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix} \cdot \begin{bmatrix} 0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix}$$

$$= 0 \cdot 0 + \theta_1 \cdot \theta_1 + \dots + \theta_n \cdot \theta_n$$

$$= \sum_{j=1}^n \theta_j^2$$

A	Exercise: 01	
/	L2 Regularization	
Turn-in directory : $ex01/$		
Files to turn in: 12	_reg.py	
Forbidden functions	: sklearn	

Objective

You must implement the following formulas as functions:

Iterative

$$L_2(\theta)^2 = \sum_{j=1}^n \theta_j^2$$

Where:

• θ is a vector of dimension (n+1).

Vectorized

$$L_2(\theta)^2 = \theta' \cdot \theta'$$

Where:

• θ' is a vector of dimension (n+1), constructed using the following rules:

$$\theta'_0 = 0
\theta'_j = \theta_j \quad \text{for } j = 1, \dots, n$$

Instructions

In the 12_reg.py file, write the following function as per the instructions given below:

```
def iterative_12(theta):
    """Computes the L2 regularization of a non-empty numpy.array, with a for-loop.
    Args:
        theta: has to be a numpy.array, a vector of shape n' * 1.
    Return:
    The L2 regularization as a float.
    None if theta in an empty numpy.array.
    None if theta is not of the expected type.
    Raises:
    This function should not raise any Exception.
    """
    ... Your code ...

def 12(theta):
    """Computes the L2 regularization of a non-empty numpy.array, without any for-loop.
    Args:
        theta: has to be a numpy.array, a vector of shape n' * 1.
    Return:
        The L2 regularization as a float.
        None if theta in an empty numpy.array.
        None if theta is not of the expected type.
    Raises:
        This function should not raise any Exception.
    """
        ... Your code ...
```

Examples

```
x = np.array([[2],[ 14],[ -13],[ 5],[ 12],[ 4],[ -19]])
# Example 1:
iterative_l2(x)
# Output:
911.0

# Example 2:
12(x)
# Output:
911.0

y = np.array([[3],[0.5],[-6]])
# Example 3:
iterative_l2(y)
# Output:
36.25

# Example 4:
12(y)
# Output:
36.25
```

Chapter III

Exercise 02

A series series	Exercise: 02	
/	Regularized Linear Loss Function	/
Turn-in directory : ex	02/	
Files to turn in : line	ar_loss_reg.py	/
Forbidden functions : sklearn		

Objective

You must implement the following formula as a function:

$$J(\theta) = \frac{1}{2m} [(\hat{y} - y) \cdot (\hat{y} - y) + \lambda(\theta' \cdot \theta')]$$

Where:

- y is a vector of dimension m, the expected values,
- \hat{y} is a vector of dimension m, the predicted values,
- λ is a constant, the regularization hyperparameter,
- θ' is a vector of dimension n, constructed using the following rules:

$$\theta'_0 = 0
\theta'_j = \theta_j \quad \text{for } j = 1, \dots, n$$

Instructions

In the linear_loss_reg.py file, write the following function as per the instructions given below:

```
def reg_loss_(y, y_hat, theta, lambda_):
    """Computes the regularized loss of a linear regression model from two non-empty numpy.array,
    without any for loop. The two arrays must have the same shapes.

Args:
    y: has to be an numpy.array, a vector of shape m * 1.
    y_hat: has to be an numpy.array, a vector of shape m * 1.
    theta: has to be a numpy.array, a vector of shape n * 1.
    lambda_: has to be a float.

Return:
    The regularized loss as a float.
    None if y, y_hat, or theta are empty numpy.array.
    None if y and y_hat do not share the same shapes.
    None if y or y_hat is not of the expected type.

Raises:
    This function should not raise any Exception.

"""
    ... Your code ...
```



such situation is a good use case for decorators...

Examples

```
y = np.array([[2],[ 14],[ -13],[ 5],[ 12],[ 4],[ -19]])
y_hat = np.array([[3],[ 13],[ -11.5],[ 5],[ 11],[ 5],[ -20]])
theta = np.array([[1],[ 2.5],[ 1.5],[ -0.9]])

# Example 1:
reg_loss_(y, y_hat, theta, .5)
# Output:
0.8503571428571429

# Example 2:
reg_loss_(y, y_hat, theta, .05)
# Output:
0.5511071428571429

# Example 3:
reg_loss_(y, y_hat, theta, .9)
# Output:
1.116357142857143
```

Chapter IV

Exercise 03

4	Δ
42	MITTERS BILLIONES

Exercise: 03

Regularized Logistic Loss Function

Turn-in directory: ex03/

Files to turn in : logistic_loss_reg.py

Forbidden functions: sklearn

Objective

You must implement the following formula as a function:

$$J(\theta) = -\frac{1}{m} [y \cdot \log(\hat{y}) + (\vec{1} - y) \cdot \log(\vec{1} - \hat{y})] + \frac{\lambda}{2m} (\theta' \cdot \theta')$$

Where:

- \hat{y} is a vector of dimension m, the vector of predicted values,
- y is a vector of dimension m, the vector of expected values,
- $\vec{1}$ is a vector of dimension m, a vector full of ones,
- λ is a constant, the regularization hyperparameter,
- θ' is a vector of dimension n, constructed using the following rules:

$$\theta'_0 = 0
\theta'_j = \theta_j \quad \text{for } j = 1, \dots, n$$

Instructions

In the logistic_loss_reg.py file, write the following function as per the instructions given below:

```
def reg_log_loss_(y, y_hat, theta, lambda_, eps=1e-15):
    """Computes the regularized loss of a logistic regression model from two non-empty numpy.array,
    without any for loop. The two arrays must have the same shapes.
Args:
    y: has to be an numpy.array, a vector of shape m * 1.
        y_hat: has to be an numpy.array, a vector of shape m * 1.
        theta: has to be a numpy.array, a vector of shape n * 1.
        lambda_: has to be a float.
        eps: has to be a float, epsilon (default=1e-15).
Return:
        The regularized loss as a float.
        None if y, y_hat, or theta is empty numpy.array.
        None if y or y_hat have component ouside [0; 1]
        None if y and y_hat do not share the same shapes.
        None if y or y_hat is not of the expected type.
Raises:
        This function should not raise any Exception.
"""
        ... Your code ...
```



this is a good use case for decorators...

Examples

```
y = np.array([[1],[1],[0],[0],[1],[1],[0]])
y_hat = np.array([[.9],[.79],[.12],[.04],[.89],[.93],[.01]])
theta = np.array([[1],[2.5],[1.5],[-0.9]])

# Example 1:
reg_log_loss_(y, y_hat, theta, .5)
# Output:
0.40824105118138265

# Example 2:
reg_log_loss_(y, y_hat, theta, .05)
# Output:
0.10899105118138264

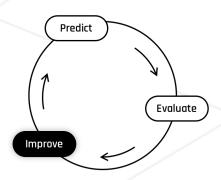
# Example 3:
reg_log_loss_(y, y_hat, theta, .9)
# Output:
0.6742410511813826
```

Chapter V

Exercise 04

Interlude

Regularized Gradient



To derive the gradient of the regularized loss function, $\nabla(J)$ you have to change a bit the formula of the unregularized gradient. Given the fact that we are not penalizing θ_0 , the formula will remain the same as before for this parameter. For the other parameters $(\theta_1, \ldots, \theta_n)$, we must add the partial derivative of the regularization term: $\lambda \theta_j$.

Therefore, we get:

$$\nabla(J)_0 = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

$$\nabla(J)_j = \frac{1}{m} \left(\sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \lambda \theta_j \right) \text{ for } j = 1, \dots, n$$

Where:

- $\nabla(J)_j$ is the jth component of the gradient vector $\nabla(J)$,
- \bullet m is the number of training examples used,
- $h_{\theta}(x^{(i)})$ is the model's prediction for the ith training example,
- $x^{(i)}$ is the feature vector of the ith training example,
- $y^{(i)}$ is the expected target value for the ith example,
- λ is a constant, the regularization hyperparameter,

• θ_i is the jth parameter of the θ vector.

Which can be vectorized as:

$$\nabla(J) = \frac{1}{m} [X'^{T}(h_{\theta}(X) - y) + \lambda \theta']$$

Where:

- $\nabla(J)$ is a vector of dimension (n+1) the gradient vector,
- \bullet m is the number of training examples used,
- X is a matrix of dimension $(m \times n)$, the design matrix,
- X' is a matrix of dimension $(m \times (n+1))$, the design matrix onto which a column of ones is added as a first column,
- y is a vector of dimension m, the vector of expected values,
- $h_{\theta}(X)$ is a vector of dimension m, the vector of predicted values,
- λ is a constant,
- θ is a vector of dimension (n+1), the parameter vector,
- θ' is a vector of dimension (n+1), constructed using the following rules:

$$\theta'_0 = 0
\theta'_j = \theta_j \quad \text{for } j = 1, \dots, n$$

Linear Gradient vs Logistic Gradient

As before, we draw your attention on the only difference between linear regression and logistic regression's gradient equations: the hypothesis function $h_{\theta}(X)$.

- In the linear regression: $h_{\theta}(X) = X'\theta$,
- In the logistic regression: $h_{\theta}(X) = \operatorname{sigmoid}(X'\theta)$.

<u> </u>	Exercise: 04	
	Regularized Linear Gradient	
Turn-in directory	: ex04/	
Files to turn in:	reg_linear_grad.py	
Forbidden functio	ns: sklearn	

Objective

You must implement the following formulas as a functions for the **linear regression hypothesis**:

Iterative

$$\nabla(J)_0 = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

$$\nabla(J)_j = \frac{1}{m} \left(\sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \lambda \theta_j \right) \text{ for } j = 1, ..., n$$

Where:

- $\nabla(J)_i$ is the jth component of $\nabla(J)$,
- $\nabla(J)$ is a vector of dimension (n+1), the gradient vector,
- *m* is a constant, the number of training examples used,
- $h_{\theta}(x^{(i)})$ is the model's prediction for the ith training example,
- $x^{(i)}$ is the feature vector (of dimension n) of the ith training example, found in the ith row of the X matrix,
- X is a matrix of dimensions $(m \times n)$, the design matrix,
- $y^{(i)}$ is the ith component of the y vector,
- ullet y is a vector of dimension m, the vector of expected values,
- ullet λ is a constant, the regularization hyperparameter,
- θ_j is the jth parameter of the θ vector,
- θ is a vector of dimension (n+1), the parameter vector.

Vectorized

$$\nabla(J) = \frac{1}{m} [X'^{T}(h_{\theta}(X) - y) + \lambda \theta']$$

Where:

- $\nabla(J)$ is a vector of dimension (n+1), the gradient vector,
- m is a constant, the number of training examples used,
- X is a matrix of dimensions $(m \times n)$, the design matrix,
- X' is a matrix of dimensions $(m \times (n+1))$, the design matrix onto which a column of ones is added as a first column,
- X^{T} is the transpose of the matrix, with dimensions $((n+1) \times m)$,
- $h_{\theta}(X)$ is a vector of dimension m, the vector of predicted values,
- y is a vector of dimension m, the vector of expected values,
- λ is a constant, the regularization hyperparameter,
- θ is a vector of dimension (n+1), the parameter vector,
- θ' is a vector of dimension (n+1), constructed using the following rules:

$$\theta'_0 = 0$$
 $\theta'_j = \theta_j \quad \text{for } j = 1, \dots, n$

Instructions

In the reg_linear_grad.py file, write the following functions as per the instructions given below:

```
def reg_linear_grad(y, x, theta, lambda_):
      """Computes the regularized linear gradient of three non-empty numpy.array, with two for-loop. The three arrays must have compatible shapes.
        y: has to be a numpy.array, a vector of shape m * 1.
x: has to be a numpy.array, a matrix of dimesion m * n.
theta: has to be a numpy.array, a vector of shape (n + 1) * 1.
lambda_: has to be a float.
        None if y, x, or theta are empty numpy.array.

None if y, x or theta does not share compatibles shapes.

None if y, x or theta or lambda_ is not of the expected type.
     Raises:
     This function should not raise any Exception.
     ... Your code ...
def vec_reg_linear_grad(y, x, theta, lambda_):
      """Computes the regularized linear gradient of three non-empty numpy.array,
         without any for-loop. The three arrays must have compatible shapes.
        y: has to be a numpy.array, a vector of shape m * 1.
        x: has to be a numpy.array, a matrix of dimesion m * n. theta: has to be a numpy.array, a vector of shape (n + 1) * 1. lambda_: has to be a float.
     Return:
        A numpy.array, a vector of shape (n + 1) * 1, containing the results of the formula for all j.
        None if y, x, or theta are empty numpy.array.

None if y, x or theta does not share compatibles shapes.
        None if y, x or theta or lambda_ is not of the expected type.
     Raises:
      ... Your code ...
```



this is a good use case for decorators...

Examples

```
np.array([
reg_linear_grad(y, x, theta, 1)
array([[ -60.99
vec_reg_linear_grad(y, x, theta, 1)
array([[ -60.99
reg_linear_grad(y, x, theta, 0.5)
array([[ -60.99
vec_reg_linear_grad(y, x, theta, 0.5)
# Output:
array([[ -60.99
reg_linear_grad(y, x, theta, 0.0)
array([[ -60.99
      [-643.66428571]])
vec_reg_linear_grad(y, x, theta, 0.0)
array([[ -60.99
```

Chapter VI

Exercise 05

Q mea wants	Exercise: 05	
/	Regularized Logistic Gradient	
Turn-in directory : $ex05$	/	
Files to turn in : reg_logistic_grad.py		/
Forbidden functions: sk	learn	/

Objective

You must implement the following formulas as a functions for the **logistic regression hypothesis**:

Iterative

$$\nabla(J)_0 = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

$$\nabla(J)_j = \frac{1}{m} \left(\sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \lambda \theta_j \right) \text{ for } j = 1, ..., n$$

Where:

- $\nabla(J)_j$ is the jth component of $\nabla(J)$,
- $\nabla(J)$ is a vector of dimension (n+1), the gradient vector,
- \bullet m is a constant, the number of training examples used,
- $h_{\theta}(x^{(i)})$ is the model's prediction for the ith training example,
- $x^{(i)}$ is the feature vector of dimension n) of the ith training example, found in the ith row of the X matrix,
- X is a matrix of dimensions $(m \times n)$, the design matrix,

- $y^{(i)}$ is the ith component of the y vector,
- y is a vector of dimension m, the vector of expected values,
- λ is a constant, the regularization hyperparameter,
- θ_i is the jth parameter of the θ vector,
- θ is a vector of dimension (n+1), the parameter vector.

Vectorized

$$\nabla(J) = \frac{1}{m} [X'^{T}(h_{\theta}(X) - y) + \lambda \theta']$$

Where:

- $\nabla(J)$ is a vector of dimension (n+1), the gradient vector,
- ullet m is a constant, the number of training examples used,
- X is a matrix of dimensions $(m \times n)$, the design matrix,
- X' is a matrix of dimensions $(m \times (n+1))$, the design matrix onto which a column of ones is added as a first column,
- X^{T} is the transpose of the matrix, with dimensions $((n+1) \times m)$,
- $h_{\theta}(X)$ is a vector of dimension m, the vector of predicted values,
- y is a vector of dimension m, the vector of expected values,
- $\bullet~\lambda$ is a constant, the regularization hyperparameter,
- θ is a vector of dimension (n+1), the parameter vector,
- θ' is a vector of dimension (n+1), constructed using the following rules:

$$\theta'_0 = 0
\theta'_j = \theta_j \text{ for } j = 1, \dots, n$$

Instructions

In the reg_logistic_grad.py file, create the following function as per the instructions given below:

```
def reg_logistic_grad(y, x, theta, lambda_):
      """Computes the regularized logistic gradient of three non-empty numpy.array, with two for-loops. The three arrays must have compatible shapes.
        y: has to be a numpy.array, a vector of shape m * 1.
x: has to be a numpy.array, a matrix of dimesion m * n.
theta: has to be a numpy.array, a vector of shape (n + 1) * 1.
lambda_: has to be a float.
        None if y, x, or theta are empty numpy.array.

None if y, x or theta does not share compatibles shapes.

None if y, x or theta or lambda_ is not of the expected type.
     Raises:
     This function should not raise any Exception.
     ... Your code ...
def vec_reg_logistic_grad(y, x, theta, lambda_):
     """Computes the regularized logistic gradient of three non-empty numpy.array,
         without any for-loop. The three arrays must have compatible shapes.
        y: has to be a numpy.array, a vector of shape m * 1.
        x: has to be a numpy.array, a matrix of dimesion m * n. theta: has to be a numpy.array, a vector of shape (n + 1) * 1. lambda_: has to be a float.
     Return:
        A numpy.array, a vector of shape (n + 1) * 1, containing the results of the formula for all j.
        None if y, x, or theta are empty numpy.array.

None if y, x or theta does not share compatibles shapes.
        None if y, x or theta or lambda_ is not of the expected type.
     Raises:
      ... Your code ...
```



this is a good use case for decorators...

Examples

```
x = np.array([[0, 2, 3, 4],
reg_logistic_grad(y, x, theta, 1)
# Output:
array([[-0.55711039],
vec_reg_logistic_grad(y, x, theta, 1)
array([[-0.55711039],
       [-2.56737958],
      [-3.03924017]])
reg_logistic_grad(y, x, theta, 0.5)
array([[-0.55711039],
vec_reg_logistic_grad(y, x, theta, 0.5)
array([[-0.55711039],
reg_logistic_grad(y, x, theta, 0.0)
# Output:
array([[-0.55711039],
      [-3.27257351]])
vec_reg_logistic_grad(y, x, theta, 0.0)
array([[-0.55711039],
      [-2.10071291],
       [-3.27257351]])
```

Chapter VII

Exercise 06

Interlude

Linear Regression to the Next Level: Ridge Regression

Until now we only talked about L_2 regularization and its implication on the calculation of the loss function and gradient for both linear and logistic regression.

Now it's time to use proper terminology: When we apply L_2 regularization on a linear regression model, the new model is called a **Ridge Regression** model. Besides that brand-new name, Ridge regression is nothing more than linear regression regularized with L_2 .

We suggest you watch this nice explanation very nice explanation of Ridge Regularization. By the way, this Youtube channel, StatQuest, is very good to help you understand the gist of a lot of machine learning concepts. You will not waste your time watching its statistics and machine learning playlists!

A some seconds	Exercise: 06	
	Ridge Regression	
Turn-in directory: $ex06/$		
Files to turn in : ridge.py		
Forbidden functions: sklearn		

Objective

Now it's time to implement your MyRidge class, similar to the class of the same name in sklearn.linear model.

Instructions

In the ridge.py file, create the following class as per the instructions given below: Your MyRidge class will have at least the following methods:

- __init__, special method, similar to the one you wrote in MyLinearRegression (module06),
- get_params_, which get the parameters of the estimator,
- set_params_, which set the parameters of the estimator,
- loss_, which return the loss between 2 vectors (numpy arrays),
- loss_elem_, which return a vector corresponding to the squared diffrence between 2 vectors (numpy arrays),
- predict_, which generates predictions using a linear model,
- \bullet ${\tt gradient}_,$ which calculates the vectorized regularized gradient,
- fit_, which fits Ridge regression model to a training dataset.



You should consider inheritance

The difference between MyRidge's loss_elem_, loss_, gradient_ and fit_ methods and MyLinearRegression's loss_elem_, loss_, gradient_ and fit_ methods implemented in module 06 is the use of a regularization term.



again, this is a good use case for decorators...

Chapter VIII

Exercise 07

A	Exercise: 07	
/	Practicing Ridge Regression	/
Turn-in director:	r: ex07/	/
Files to turn in : space_avocado.py, benchmark_train.py,		/
models.[csv/ym	l/pickle]	
Forbidden functi	ons: sklearn	/

Objective

It's training time! Let's practice our brand new Ridge Regression with a polynomial model.

Introduction

You have already used the dataset space_avocado.csv. The dataset is constituted of 5 columns:

- index: not relevant,
- weight: the avocado weight order (in ton),
- prod_distance: distance from where the avocado ordered is produced (in Mkm),
- time_delivery: time between the order and the receipt (in days),
- target: price of the order (in trantorian unit).

It contains the data of all the avocado purchase made by Trantor administration (guacamole is a serious business there).

Instructions

You have to explore different models and select the best you find. To do this:

- Split your space_avocado.csv dataset into a training, a cross-validation and a test sets.
- Use your polynomial features method on your training set.
- Consider several Linear Regression models with polynomial hypotheses with a maximum degree of 4.
- For each hypothesis consider a regularized factor ranging from 0 to 1 with a step of 0.2.
- Evaluate your models on the cross-validation set.
- Evaluate the best model on the test set.

According to your model evaluations, what is the best hypothesis you can get?

- Plot the evaluation curve which help you to select the best model (evaluation metrics vs models $+ \lambda$ factor).
- Plot the true price and the predicted price obtain via your best model with the different λ values (meaning the dataset + the 5 predicted curves).

The training of all your models can take a long time. Thus you need to train only the best one during the correction. But, you should return in benchmark_train.py the program which perform the training of all the models and save the parameters of the different models into a file. In models.[csv/yml/pickle] one must find the parameters of all the models you have explored and trained. In space_avocado.py train the model based on the best hypothesis you find and load the other models from models.[csv/yml/pickle]. Then evaluate the best model on the right set and plot the different graphics as asked before.

Chapter IX

Exercise 08

Interlude

Regularized Logistic Regression is still Logistic Regression

As opposed to linear regression, **regularized logistic regression is still called logistic regression**.

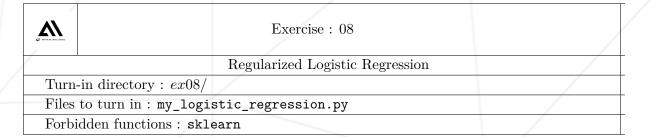
Working without regularization parameters can be considered simply as a special case where $\lambda=0.$

if $\lambda = 0$:

$$\nabla(J) = \frac{1}{m} [X'^T (h_{\theta}(X) - y) + \lambda \theta']$$

$$= \frac{1}{m} [X'^T (h_{\theta}(X) - y) + 0 \cdot \theta']$$

$$= \frac{1}{m} [X'^T (h_{\theta}(X) - y)]$$



Objective

In the last exercise, you implemented of a regularized version of the linear regression algorithm, called Ridge regression. Now it's time to update your logistic regression classifier as well! In the scikit-learn library, the logistic regression implementation offers a few regularization techniques, which can be selected using the parameter penalty (L_2 is default). The goal of this exercise is to update your old MyLogisticRegression class to take that into account.

Instructions

In the my_logistic_regression.py file, update your MyLogisticRegression class according to the following:

• add a penalty parameter which can take the following values: '12', 'none' (default value is '12').

```
class MyLogisticRegression():
    Description:
        My personnal logistic regression to classify things.
    """

        def __init__(self, theta, alpha=0.001, max_iter=1000, penalty='12'):
            self.alpha = alpha
            self.max_iter = max_iter
            self.theta = theta
            self.penalty=penalty
            ... Your code ...
... other methods ...
```

- update the fit_(self, x, y) method:
 - o if penalty == '12': use a regularized version of the gradient descent.
 - if penalty = 'none': use the unregularized version of the gradient descent from module08.



this is also a great use case for decorators...

Chapter X

Exercise 09

2 MINCHE BYTHERS	Exercise: 09
	Practicing Regularized Logistic Regression
Turn	-in directory: $ex09/$
Files	to turn in : solar_system_census.py, benchmark_train.py,
mode	ls.[csv/yml/pickle]
Forbi	idden functions: sklearn

Objective

It's training time! Let's practice our updated Logistic Regression with polynomial models.

Instructions

Split the Data

Take your solar_system_census.csv dataset and split it in a training set, a cross-validation set and a test set.

Training and benchmark

One part of your submission will be find in benchmark_train.py and models.[csv/yml/pickle] files. You have to:

- Train different regularized logistic regression models with a polynomial hypothesis of **degree 3**. The models will be trained with different λ values, ranging from 0 to 1. Use one-vs-all method.
- Evaluate the **f1 score** of each of the models on the cross-validation set. You can use the **f1_score** function that you wrote in the **ex11** of module08.
- Save the different models into a models.[csv/yml/pickle].

Solar system census program

The second and last part of your submission is in solar_system_census.py. You have to:

- Loads the differents models from models. [csv/yml/pickle] and train from scratch the best one.
- Visualize the performance of the different models with a bar plot showing the score of the models given their λ value.
- Print the **f1 score** of all the models calculated on the cross-validation set and the final score of the best model on the test set.
- Visualize the target values and the predicted values of the best model on the same scatterplot. Make some effort to have a readable figure.

Chapter XI

Conclusion - What you have learnt

The excercises serie is finished, well done! Based on all the knowledges tackled today, you should be able to discuss and answer the following questions:

- 1. Why do we use logistic hypothesis for a classification problem rather than a linear hypothesis?
- 2. What is the decision boundary?
- 3. In the case we decide to use a linear hypothesis to tackle a classification problem, why the classification of some data points can be modified by considering more examples (for example, extra data points with extrem ordinate)?
- 4. In a one versus all classification approach, how many logisitic regressor do we need to distinguish between N classes?
- 5. Can you explain the difference between accuracy and precision? What is the type I and type II errors?
- 6. What is the interest of the F1-score?

Contact

You can contact 42AI association by email: contact@42ai.fr You can join the association on 42AI slack and/or posutale to one of the association teams.

Acknowledgements

The modules Python & ML is the result of a collective work, we would like to thanks:

- Maxime Choulika (cmaxime),
- Pierre Peigné (ppeigne),
- Matthieu David (mdavid).

who supervised the creation, the enhancement and this present transcription.

- Amric Trudel (amric@42ai.fr)
- Benjamin Carlier (bcarlier@student.42.fr)
- Pablo Clement (pclement@student.42.fr)

for your investment for the creation and development of these modules.

- Richard Blanc (riblanc@student.42.fr)
- Solveig Gaydon Ohl (sgaydon-@student.42.fr)
- Quentin Feuillade Montixi (qfeuilla@student.42.fr)

who betatest the first version of the modules of Machine Learning.

This work is licensed under a Creative Commons "Attribution-NonCommercial-ShareAlike 4.0 International" license.

