

LEAN 4 CHEATSHEET

In the following table, *name* always refers to a name already known to Lean while *new_name* refers to a new name provided by the user; *expr* designates an expression, for example the name of an object in the context, an arithmetic expression that is a function of such objects, a hypothesis in the context, or a lemma applied to any of these. When one of these words appears twice in the same line, the appearances do not designate the same name or the same expression.

| Logical symbol | Appears in goal | Appears in hypothesis |
|------------------------------------|---|--|
| \forall (for all) | <code>intro new_name</code> | <code>apply expr</code> or <code>specialize name expr</code> |
| \exists (there exists) | <code>use expr</code> | <code>cases' expr with new_name new_name</code> |
| \rightarrow (implies) | <code>intro new_name</code> | <code>apply expr</code> or <code>specialize name expr</code> |
| \leftrightarrow (if and only if) | <code>constructor</code> | <code>rw [expr]</code> or <code>rw [← expr]</code> |
| \wedge (and) | <code>constructor</code> | <code>cases' expr with new_name new_name</code> |
| \vee (or) | <code>left</code> or <code>right</code> | <code>cases' expr with new_name new_name</code> |
| \neg (not) | <code>intro new_name</code> | <code>apply expr</code> or <code>specialize name expr</code> |

In the left-hand column of the following table, the parts in brackets are optional. The effect of these parts is also in brackets in the right-hand column. It is almost always a matter of specifying that a manipulation, which acts by default on the goal, must be performed rather on a certain hypothesis named *hyp*.

| Tactic | Effect |
|--|--|
| <code>exact expr</code> | assert that the goal can be satisfied by <i>expr</i> |
| <code>have new_name : fact</code> | introduce a name <i>new_name</i> asserting that <i>fact</i> is provable |
| <code>unfold name (at hyp)</code> | unfold the definition of <i>name</i> in the goal (or in the hypothesis <i>hyp</i>) |
| <code>convert name</code> | prove the goal by transforming it to an existing proposition <i>name</i> and create goals for propositions used in the transformation that were not proved automatically |
| <code>convert_to expr</code> | transform the goal into the expression <i>expr</i> and create additional goals for propositions used in the transformation that were not proved automatically |
| <code>rw [(←) expr] (at hyp)</code> | in the goal (or in the hypothesis <i>hyp</i>), replace the left-hand side (or the right-hand side, if \leftarrow is present) of the equality or equivalence <i>expr</i> by the other side |
| <code>rw [expr , expr] (at hyp)</code> | rewrite (parts of) the goal (or the hypothesis <i>hyp</i>), using given equalities/equivalences in the given order |
| <code>linarith</code> | prove the goal by a linear combination of hypotheses |
| <code>ring</code> | prove the goal by combining the axioms of a commutative (semi)ring |
| <code>library_search</code> | search for a single existing lemma which closes the goal, also using local hypotheses |
| <code>by_cases new_name : expr</code> | split the proof into two cases depending on whether <i>expr</i> is true or false, using <i>new_name</i> as name for this hypothesis |
| <code>by_contra new_name</code> | start a proof by contradiction, using <i>new_name</i> as name for the hypothesis that is the negation of the goal |
| <code>contrapose</code> | transform a goal of the form $expr \rightarrow expr$ into its contrapositive |
| <code>push_neg (at hyp)</code> | push negations in the goal (or in the hypothesis <i>hyp</i>) |
| <code>exfalso</code> | apply the rule <i>ex falso quod libet</i> (replaces the current goal by False) |