Analysis of Human Breast Cancer Cells

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Exploratory data analysis

Download and import data:

```
fna.data <- "WisconsinCancer.csv"
wisc.df <- read.csv(fna.data, row.names = 1)</pre>
```

Lets make a new data.frame that omits the first column:

```
wisc.data <- wisc.df[, -1]
```

We can put the data from the first column into a separate vector

```
diagnosis <- as.factor(wisc.df$diagnosis)</pre>
```

Q1. How many observations are in this dataset?

```
nrow(wisc.data)
```

[1] 569

- There are 569 rows in wisc.data
 - Q2. How many of the observations have a malignant diagnosis?

```
table(wisc.df$diagnosis)
```

```
B M
357 212
```

- 212 observations have a malignant diagnosis
 - Q3. How many variables/features in the data are suffixed with _mean?

```
colnames(wisc.data)
```

```
[1] "radius_mean"
                                "texture mean"
 [3] "perimeter_mean"
                                "area_mean"
 [5] "smoothness_mean"
                                "compactness_mean"
 [7] "concavity_mean"
                                "concave.points_mean"
 [9] "symmetry_mean"
                                "fractal_dimension_mean"
[11] "radius_se"
                                "texture_se"
[13] "perimeter_se"
                                "area_se"
[15] "smoothness_se"
                                "compactness_se"
[17] "concavity_se"
                                "concave.points_se"
[19] "symmetry_se"
                                "fractal_dimension_se"
[21] "radius_worst"
                                "texture_worst"
[23] "perimeter_worst"
                                "area_worst"
[25] "smoothness_worst"
                                "compactness_worst"
[27] "concavity_worst"
                                "concave.points_worst"
[29] "symmetry_worst"
                                "fractal dimension worst"
```

Now we can use grep() to find the column names that contain _mean

```
grep("_mean", colnames(wisc.data))
[1] 1 2 3 4 5 6 7 8 9 10
```

And now we can use length() to find how many matches there are

```
length(grep("_mean", colnames(wisc.data)))
```

[1] 10

• 10 are suffixed with _mean

Principal Component Analysis

Check the column means and standard deviations to check if the data should be scaled

colMeans(wisc.data)

radius_mean	texture_mean	perimeter_mean
1.412729e+01	1.928965e+01	9.196903e+01
area_mean	${\tt smoothness_mean}$	${\tt compactness_mean}$
6.548891e+02	9.636028e-02	1.043410e-01
concavity_mean	concave.points_mean	symmetry_mean
8.879932e-02	4.891915e-02	1.811619e-01
<pre>fractal_dimension_mean</pre>	radius_se	texture_se
6.279761e-02	4.051721e-01	1.216853e+00
perimeter_se	area_se	smoothness_se
2.866059e+00	4.033708e+01	7.040979e-03
compactness_se	concavity_se	concave.points_se
2.547814e-02	3.189372e-02	1.179614e-02
symmetry_se	fractal_dimension_se	radius_worst
2.054230e-02	3.794904e-03	1.626919e+01
texture_worst	perimeter_worst	area_worst
2.567722e+01	1.072612e+02	8.805831e+02
smoothness_worst	${\tt compactness_worst}$	concavity_worst
1.323686e-01	2.542650e-01	2.721885e-01
concave.points_worst	symmetry_worst	${\tt fractal_dimension_worst}$
1.146062e-01	2.900756e-01	8.394582e-02

apply(wisc.data, 2, sd)

radius_mean	texture_mean	perimeter_mean
3.524049e+00	4.301036e+00	2.429898e+01
area_mean	smoothness_mean	compactness_mean
3.519141e+02	1.406413e-02	5.281276e-02
concavity_mean	concave.points_mean	symmetry_mean
7.971981e-02	3.880284e-02	2.741428e-02
fractal_dimension_mean	radius_se	texture_se
7.060363e-03	2.773127e-01	5.516484e-01
perimeter_se	area_se	smoothness_se
2.021855e+00	4.549101e+01	3.002518e-03
compactness_se	concavity_se	concave.points_se
1.790818e-02	3.018606e-02	6.170285e-03
symmetry_se	fractal_dimension_se	radius_worst
8.266372e-03	2.646071e-03	4.833242e+00
texture_worst	perimeter_worst	area_worst

```
6.146258e+00 3.360254e+01 5.693570e+02 smoothness_worst compactness_worst concavity_worst 2.283243e-02 1.573365e-01 2.086243e-01 concave.points_worst symmetry_worst fractal_dimension_worst 6.573234e-02 6.186747e-02 1.806127e-02
```

We need to scale with scale = TRUE argument in prcomp()

```
wisc.pr <- prcomp(wisc.data, scale = TRUE)
summary(wisc.pr)</pre>
```

Importance of components:

```
PC1
                                  PC2
                                          PC3
                                                  PC4
                                                          PC5
                                                                  PC6
                                                                           PC7
Standard deviation
                       3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172
Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251
Cumulative Proportion
                       0.4427 \ 0.6324 \ 0.72636 \ 0.79239 \ 0.84734 \ 0.88759 \ 0.91010
                           PC8
                                   PC9
                                          PC10
                                                 PC11
                                                         PC12
                                                                 PC13
                                                                          PC14
Standard deviation
                       0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
Cumulative Proportion
                       0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
                          PC15
                                  PC16
                                           PC17
                                                   PC18
                                                           PC19
                                                                   PC20
                                                                           PC21
Standard deviation
                       0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
Cumulative Proportion
                       0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
                          PC22
                                  PC23
                                          PC24
                                                  PC25
                                                          PC26
                                                                  PC27
                                                                           PC28
Standard deviation
                       0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
Cumulative Proportion
                       0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
                          PC29
                                   PC30
Standard deviation
                       0.02736 0.01153
Proportion of Variance 0.00002 0.00000
Cumulative Proportion
                       1.00000 1.00000
```

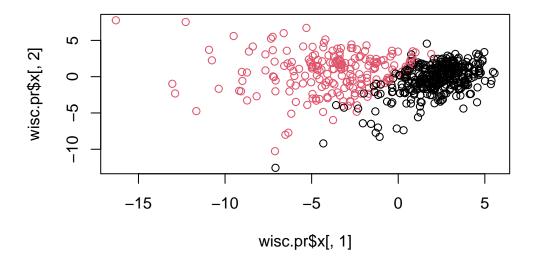
- Q4. From your results, what proportion of the original variance is captured by the first principal components (PC1)?
- Proportion of variance for PC1 = 44.27%
 - Q5. How many principal components (PCs) are required to describe at least 70% of the original variance in the data?
- 3 PCs are required to get at least 70% of the original variance.

Q6. How many principal components (PCs) are required to describe at least 90% of the original variance in the data?

 $\bullet\,$ 7 PCs are required to get at least 90% of the original variance.

Lets make a PC plot (aka "score plot" or "PC1 vs PC2")

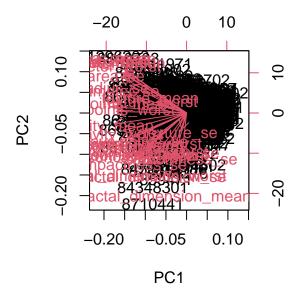
```
plot(wisc.pr$x[, 1], wisc.pr$x[, 2], col = diagnosis)
```



Interpreting PCA Results

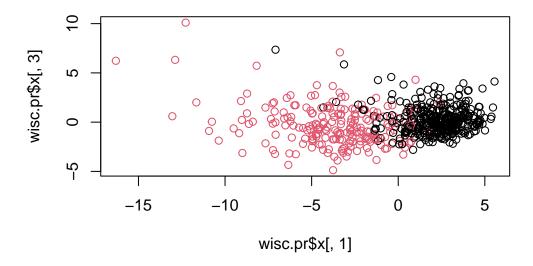
Create a biplot:

biplot(wisc.pr)



- Q7. What stands out to you about this plot? Is it easy or difficult to understand? Why?
- This plot is very difficult to understand since it is all smushed together in a small plot and every point is labeled.
 - Q8. Generate a similar plot for principal components 1 and 3. What do you notice about these plots?

```
plot(wisc.pr$x[, 1], wisc.pr$x[, 3], col = diagnosis)
```



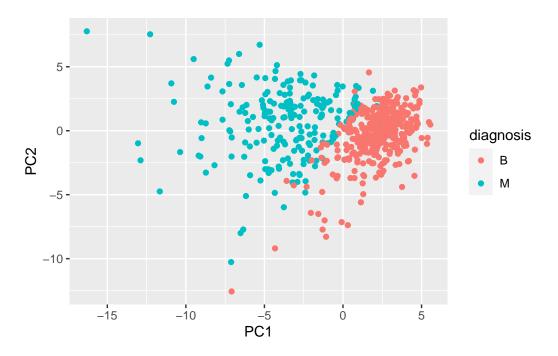
• The plots for PR1 vs PR2 and PR1 vs PR3 are very similar. They both have two groups that are close together around (0,0).

Now lets make a data.frame to use ggplot:

```
df <- as.data.frame(wisc.pr$x)
df$diagnosis <- diagnosis</pre>
```

Now load ggplot2 package and make a scatterplot colored by diagnosis:

```
library(ggplot2)
ggplot(df) +
  aes(PC1, PC2, col = diagnosis) +
  geom_point()
```



Variance explained

Calculate the variance of each component.

```
pr.var <- wisc.pr$sdev^2
head(pr.var)

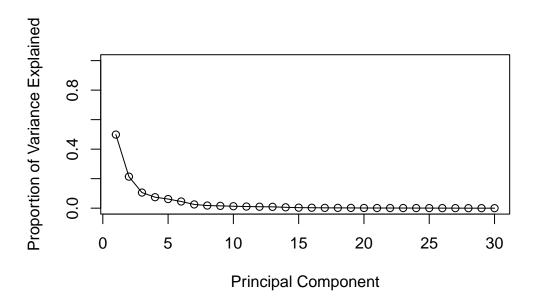
[1] 13.281608 5.691355 2.817949 1.980640 1.648731 1.207357</pre>
```

Calculate the variance explained by each principal component by dividing by the total variance explained of all principal components.

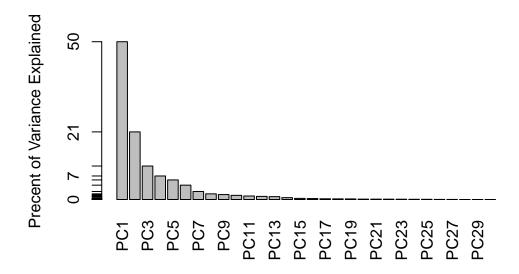
```
pve <- pr.var/sum(head(pr.var))</pre>
```

Plot the variance explained for each principal component.

```
plot(pve, xlab = "Principal Component",
    ylab = "Proportion of Variance Explained",
    ylim = c(0, 1), type = "o")
```



Alternative scree plot of the same data:



Communicating PCA Results

- Q9. For the first principal component, what is the component of the loading vector (i.e. wisc.pr\$rotation[,1]) for the feature concave.points_mean?
- It would be concave.points_mean(pr.var[1])
 - Q10. What is the minimum number of principal components required to explain 80% of the variance of the data?

[1] 0.8183569

• 3 PCs are required to explain 80% of the variance.

Hierarchical Clustering

First scale the wisc.data data and assign to data.scaled Then calculate the distances between all pairs of observations in the new scaled dataset and assign to data.dist

```
data.scaled <- scale(wisc.data)
data.dist <- dist(data.scaled)</pre>
```

Create a hierarchical clustering model using complete linkage. Assign to wisc.hclust

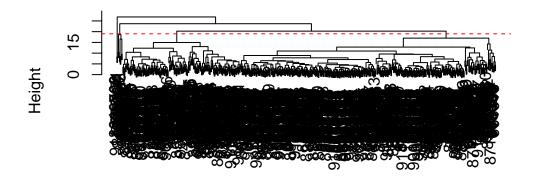
```
wisc.hclust <- hclust(data.dist)</pre>
```

Results of Hierarchical Clustering

Q11. Using the plot() and abline() functions, what is the height at which the clustering model has 4 clusters?

```
plot(wisc.hclust)
abline(h = 19, col = "red", lty = 2)
```

Cluster Dendrogram



data.dist hclust (*, "complete")

• Height = 19

Select number of clusters

Use cutree() to cut the tree so that it has 4 clusters. Assign the output to the variable wisc.hclust.clusters

```
wisc.hclust.clusters <- cutree(wisc.hclust, k = 4)</pre>
```

We can use the table() function to compare the cluster membership to the actual diagnoses.

```
table(wisc.hclust.clusters, diagnosis)
```

```
diagnosis
wisc.hclust.clusters B M
1 12 165
2 2 5
3 343 40
4 0 2
```

- Q12. Can you find a better cluster vs diagnoses match by cutting into a different number of clusters between 2 and 10?
- You can find other matches when cutting into different numbers of clusters, but there is no way to know what number of clusters is best to use.

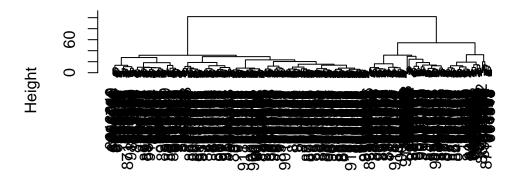
Using different methods

There are number of different "methods" we can use to combine points during the hierarchical clustering procedure. These include "single", "complete", "average", and "ward.D2"

Q13. Which method gives your favorite results for the same data.dist dataset? Explain your reasoning.

```
plot(hclust(data.dist, method = "ward.D2"))
```

Cluster Dendrogram



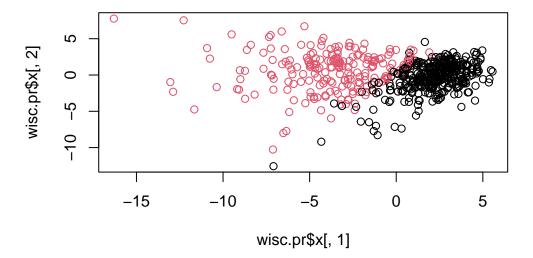
data.dist hclust (*, "ward.D2")

• The "ward.D2" method is my favorite because it gives a very clear cutoff point for clustering.

Combine PCA with Clustering

I want to cluster in "PC space"

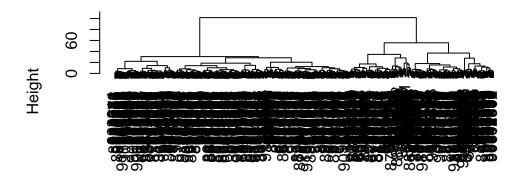
```
plot(wisc.pr$x[, 1], wisc.pr$x[, 2], col = diagnosis)
```



The $\verb|hclust()|$ function wants a distance matrix as input...

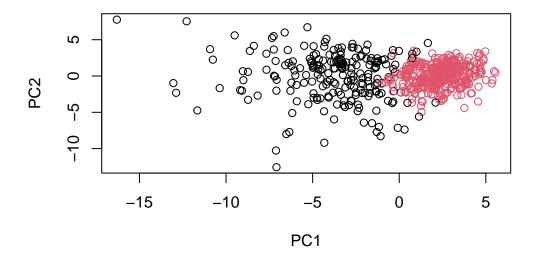
```
d <- dist(wisc.pr$x[, 1:7])
wisc.pr.hclust <- hclust(dist(wisc.pr$x[, 1:7]), method = "ward.D2")
plot(wisc.pr.hclust)</pre>
```

Cluster Dendrogram

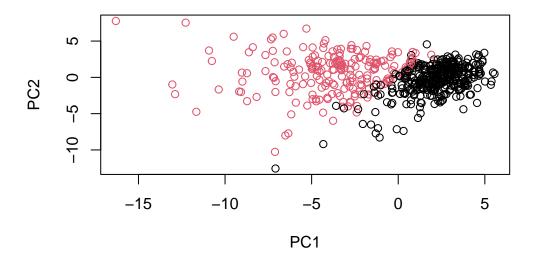


dist(wisc.pr\$x[, 1:7]) hclust (*, "ward.D2")

Find my cluster membership vector with cutree().



plot(wisc.pr\$x[,1:2], col=diagnosis)



Use the distance along the first 7 PCs for clustering

```
wisc.pr.hclust <- hclust(dist(wisc.pr$x[, 1:7]), method="ward.D2")</pre>
```

Cut this hierarchical clustering model into 2 clusters and assign the results to wisc.pr.hclust.clusters

```
wisc.pr.hclust.clusters <- cutree(wisc.pr.hclust, k=2)</pre>
```

Using table(), compare the results from your new hierarchical clustering model with the actual diagnoses.

Q15. How well does the newly created model with four clusters separate out the two diagnoses?

```
table(wisc.pr.hclust.clusters, diagnosis)
```

```
diagnosis
wisc.pr.hclust.clusters B M
1 28 188
2 329 24
```

- The new model does a pretty decent job of separating the two diagnoses. However, a somewhat high proportion of malignant diagnoses are seen in cluster 2, meaning it would be difficult to tell whether or not a sample is malignant or benign based on the plot alone.
 - Q16. How well do the k-means and hierarchical clustering models you created in previous sections (i.e. before PCA) do in terms of separating the diagnoses? Again, use the table() function to compare the output of each model (wisc.km\$cluster and wisc.hclust.clusters) with the vector containing the actual diagnoses.

```
table(wisc.hclust.clusters, diagnosis)
```

```
diagnosis
wisc.hclust.clusters B M
1 12 165
2 2 5
3 343 40
4 0 2
```

```
table(wisc.df$diagnosis)
```

```
B M
357 212
```

• The hierarchical clustering model did a pretty good job at separating the diagnoses, but there is a somewhat high proportion of malignant diagnoses in clusters 2, 3, and 4 that would make it difficult to tell if a sample is benign or malignant from looking at the data alone.

Sensitivity/Specificity

Q17. Which of your analysis procedures resulted in a clustering model with the best specificity? How about sensitivity?

Sensitivity:

```
table(wisc.hclust.clusters, diagnosis)

diagnosis
wisc.hclust.clusters B M
1 12 165
2 2 5
3 343 40
4 0 2
```

165/212

[1] 0.7783019

```
table(wisc.pr.hclust.clusters, diagnosis)
```

```
diagnosis
wisc.pr.hclust.clusters B M
1 28 188
2 329 24
```

188/212

[1] 0.8867925

• wisc.pr.hclust.clusters had the highest sensitivity.

Specificity:

```
table(wisc.hclust.clusters, diagnosis)
```

diagnosis wisc.hclust.clusters B M 1 12 165 2 2 5 3 343 40 4 0 2

343/357

[1] 0.9607843

```
table(wisc.pr.hclust.clusters, diagnosis)
```

diagnosis wisc.pr.hclust.clusters B M 1 28 188 2 329 24

329/357

[1] 0.9215686

• wisc.hclust.clusters had the highest specificity.