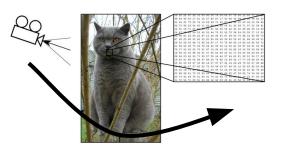
# Lecture 3: Loss functions and Optimization

# Administrative

A1 is due Jan 20 (Wednesday). ~9 days left Warning: Jan 18 (Monday) is Holiday (no class/office hours)

# Recall from last time... Challenges in Visual Recognition

Camera pose



Illumination



Deformation



Occlusion



Background clutter



Intraclass variation



This is a very difficult problem
We must be robust to all these variations.
State of the art can solve these problems

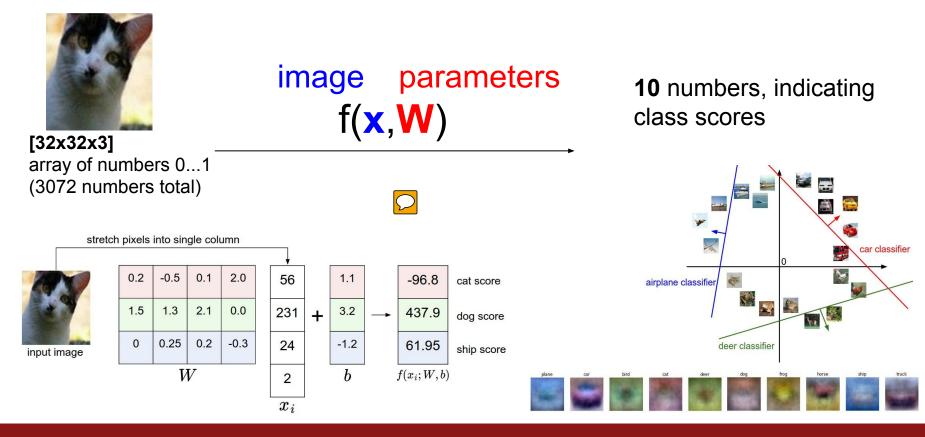
Recall from last time... data-driven approach, kNN We cant explicitly hard code these classifiers so we have to train them from data. airplane automobile train data test data deer fold 2 fold 3 fold 4 fold fold 5 test data dog frog horse Cross-validation on k ship truck the data NN classifier 5-NN classifier 0.28 E 0.27 0.26

bird cat

0.25

0.24

#### Recall from last time... Linear classifier



## Recall from last time... Going forward: Loss function/Optimization







airplane	-3.45	-0.51	3.42
automobile	-8.87	6.04	4.64
bird	0.09	5.31	2.65
cat	2.9	-4.22	5.1
deer	4.48	-4.19	2.64
dog	8.02	3.58	5.55
frog	3.78	4.49	<mark>-4.34</mark>
horse	1.06	-4.37	-1.5
ship	-0.36	-2.09	-4.79
truck	-0.72	-2.93	6.14

#### TODO:

- Define a **loss function** that quantifies our unhappiness with the scores across the training data.
- Come up with a way of efficiently finding the parameters that minimize the loss function. (optimization)







3.2 cat

1.3



4.9 5.1 car -1.7 2.0 frog

2.5 -3.1

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cat **3.2** 

1.3

2.2

car **5.1** 

4.9

2.5

frog **-1.7** 

.7 2.0

-3.1

#### **Multiclass SVM loss:**

Given an example  $(x_i, y_i)$  where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s=f(x_i,W)$ 

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$









2.2

cat

car

frog

Losses:

**3.2** 5.1

-1.7

2.9

1.3

**4.9** 2.5

2.0 **-3.1** 

#### **Multiclass SVM loss:**

Given an example  $(x_i, y_i)$  where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s = f(x_i, W)$ 

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

$$= \max(0, 5.1 - 3.2 + 1)$$

$$+ \max(0, 1.7, 3.2 + 1)$$

$$+\max(0, -1.7 - 3.2 + 1)$$

- $= \max(0, 2.9) + \max(0, -3.9)$
- = 2.9 + 0
- = 2.9







cat	3.2	1.3	2.2
car	5.1	4.9	2.5
frog	-1.7	2.0	-3.1
Losses:	2.9	0	

#### Multiclass SVM loss:

Given an example  $(x_i, y_i)$  where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s=f(x_i,W)$ 

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

- $= \max(0, 1.3 4.9 + 1)$
- $+\max(0, 2.0 4.9 + 1)$
- $= \max(0, -2.6) + \max(0, -1.9)$
- = 0 + (
- = 0







cat	3.2	1.3	2.2
car	5.1	4.9	2.5
frog	-1.7	2.0	-3.1
Losses:	2.9	0	10.9

#### Multiclass SVM loss:

Given an example  $(x_i, y_i)$  where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s = f(x_i, W)$ 

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

$$= \max(0, 2.2 - (-3.1) + 1) + \max(0, 2.5 - (-3.1) + 1)$$

- $= \max(0, 5.3) + \max(0, 5.6)$
- = 5.3 + 5.6
- = 10.9







cat	3.2	1.3	2.2
car	5.1	4.9	2.5
frog	-1.7	2.0	-3.1
Losses:	2.9	0	10.9

#### **Multiclass SVM loss:**

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s = f(x_i, W)$ 

the SVM loss has the form:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

and the full training loss is the mean over all examples in the training data:

$$L = rac{1}{N} \sum_{i=1}^N L_i$$

$$L = (2.9 + 0 + 10.9)/3$$
  
= **4.6**







cat	3.2	1.3	2.2
car	5.1	4.9	2.5
frog	-1.7	2.0	-3.1
Losses:	2.9	0	10.9

#### **Multiclass SVM loss:**

Given an example  $(x_i, y_i)$  where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s=f(x_i,W)$ 

the SVM loss has the form:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

Q: what if the sum was instead over all classes?







cat	3.2	1.3	2.2
car	5.1	4.9	2.5
frog	-1.7	2.0	-3.1
Losses:	2.9	0	10.9

## **Multiclass SVM loss:**

Given an example  $(x_i, y_i)$  where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s=f(x_i,W)$ 

the SVM loss has the form:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

Q2: what if we used a mean instead of a sum here?







2.2 3.2 1.3 cat 4.9 2.5 5.1 car -3.1 -1.7 2.0 frog

# Multiclass SVM loss:

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s = f(x_i, W)$ 

the SVM loss has the form:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

# Q3: what if we used

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)^2$$



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10.9

2.9

Losses:







 cat
 3.2
 1.3
 2.2

 car
 5.1
 4.9
 2.5

 frog
 -1.7
 2.0
 -3.1

 Losses:
 2.9
 0
 10.9

## **Multiclass SVM loss:**

Given an example  $(x_i, y_i)$  where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s=f(x_i,W)$ 

the SVM loss has the form:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

Q4: what is the min/max possible loss?







cat	3.2	1.3	2.2
car	5.1	4.9	2.5
frog	-1.7	2.0	-3.1
Losses:	2.9	0	10.9

#### Multiclass SVM loss:

Given an example  $(x_i, y_i)$  $x_i$  the image and where  $y_i^*$  the (integer) label, where

and using the shorthand for the scores  $s = f(x_i, W)$ vector:

the SVM loss has the form:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

Q5: usually at initialization W are small numbers, so all s ~= 0. What is the loss?

## Example numpy code:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

```
def L i vectorized(x, y, W):
  scores = W.dot(x)
 margins = np.maximum(0, scores - scores[y] + 1)
  margins[y] = 0
  loss i = np.sum(margins)
  return loss i
```

$$f(x,W) = Wx$$

$$L = rac{1}{N} \sum_{i=1}^{N} \sum_{j 
eq y_i} \max(0, f(x_i; W)_j - f(x_i; W)_{y_i} + 1)$$



## There is a bug with the loss:

$$f(x,W) = Wx$$
  $L = rac{1}{N} \sum_{i=1}^N \sum_{j 
eq y_i} \max(0,f(x_i;W)_j - f(x_i;W)_{y_i} + 1)$ 

## There is a bug with the loss:

$$f(x,W) = Wx$$
  $L = rac{1}{N} \sum_{i=1}^N \sum_{j 
eq y_i} \max(0,f(x_i;W)_j - f(x_i;W)_{y_i} + 1)$ 

E.g. Suppose that we found a W such that L = 0. Is this W unique?









	Wite-	The second second	
cat	3.2	1.3	2.2
car	5.1	4.9	2.5
frog	-1.7	2.0	-3.1
Losses:	2.9	0	

# $L_i = \sum_{j eq y_i} \max(0, s_j - s_{y_i} + 1)$

#### Before:

$$= \max(0, 1.3 - 4.9 + 1) + \max(0, 2.0 - 4.9 + 1) = \max(0, -2.6) + \max(0, -1.9) = 0 + 0$$

#### With W twice as large:

= 
$$max(0, 2.6 - 9.8 + 1)$$
  
+ $max(0, 4.0 - 9.8 + 1)$   
=  $max(0, -6.2) + max(0, -4.8)$   
=  $0 + 0$ 

= 0

# Weight Regularization

\lambda = regularization strength (hyperparameter)

$$L=rac{1}{N}\sum_{i=1}^{N}\sum_{j
eq y_i}\max(0,f(x_i;W)_j-f(x_i;W)_{y_i}+1)+\lambda R(W)$$

## In common use:



# L2 regularization

$$R(W) = \sum_k \sum_l W_{k,l}^2$$

L1 regularization

$$R(W) = \sum_k \sum_l |W_{k,l}|$$

Elastic net (L1 + L2)

$$R(W) = \sum_{k} \sum_{l} \beta W_{k,l}^2 + |W_{k,l}|$$

Max norm regularization (might see later)

Dropout (will see later)

# L2 regularization: motivation

$$egin{aligned} x &= [1,1,1,1] \ & w_1 &= [1,0,0,0] \ & w_2 &= [0.25,0.25,0.25,0.25] \end{aligned}$$

$$w_1^T x = w_2^T x = 1$$



cat **3.2** 

car 5.1

frog -1.7



scores = unnormalized log probabilities of the classes.

$$s=f(x_i;W)$$

cat **3.2** 

car 5.1

frog -1.7



scores = unnormalized log probabilities of the classes.

$$P(Y=k|X=x_i)=rac{e^{s_k}}{\sum_j e^{s_j}}$$
 where  $egin{aligned} oldsymbol{s}=oldsymbol{f(x_i;W)} \end{aligned}$ 

$$s = f(x_i; W)$$

3.2 cat

5.1 car

-1.7 frog



scores = unnormalized log probabilities of the classes.

$$P(Y=k|X=x_i)=rac{e^{s_k}}{\sum_j e^{s_j}}$$

where 
$$s=f(x_i;W)$$

3.2 cat

car

5.1

-1.7 frog

Softmax function



scores = unnormalized log probabilities of the classes.

$$P(Y=k|X=x_i)=rac{e^{s_k}}{\sum_j e^{s_j}}$$
 where  $egin{aligned} oldsymbol{s}=oldsymbol{f(x_i;W)} \end{aligned}$ 

Want to maximize the log likelihood, or (for a loss function) to minimize the negative log likelihood of the correct class:

$$L_i = -\log P(Y=y_i|X=x_i)$$

cat **3.2** 

car 5.1

froq -1.7



scores = unnormalized log probabilities of the classes.

$$P(Y=k|X=x_i)=rac{e^{s_k}}{\sum_j e^{s_j}}$$
 where  $egin{aligned} oldsymbol{s}=oldsymbol{f(x_i;W)} \end{aligned}$ 

Want to maximize the log likelihood, or (for a loss function) to minimize the negative log likelihood of the correct class:

$$L_i = -\log P(Y=y_i|X=x_i)$$

in summary: 
$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$

cat **3.2** 

car 5.1

froq -1.7



$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$

cat **3.2** 

car 5.

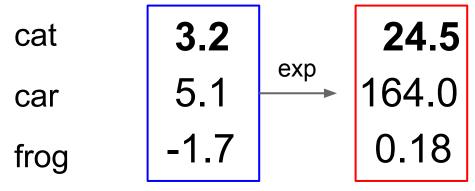
frog -1.

unnormalized log probabilities



$$L_i = -\log(rac{e^{sy_i}}{\sum_{j}e^{s_j}})$$

unnormalized probabilities

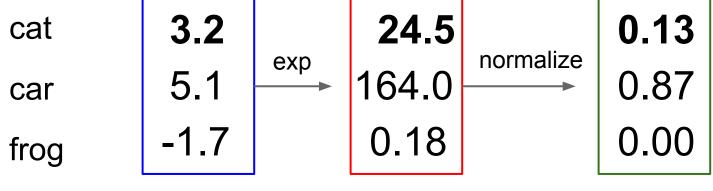


unnormalized log probabilities



$$L_i = -\log(rac{e^{sy_i}}{\sum_{j}e^{s_j}})$$

unnormalized probabilities



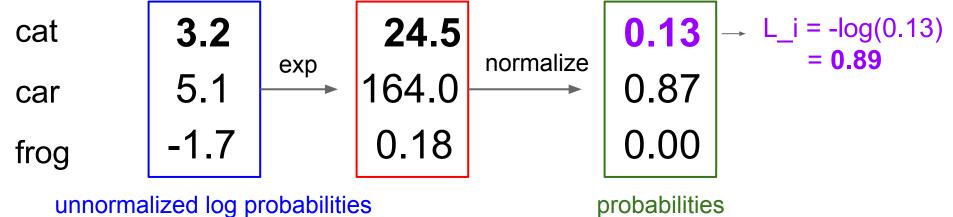
unnormalized log probabilities

probabilities



$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$

unnormalized probabilities

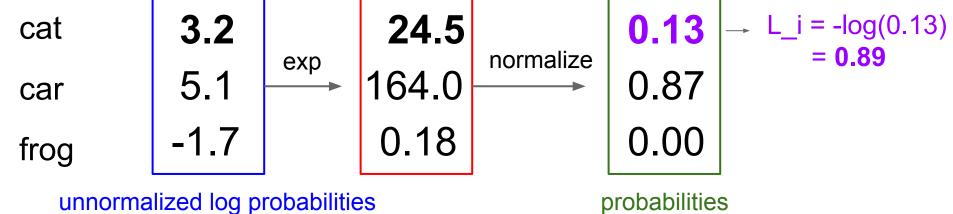




$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$

Q: What is the min/max possible loss L\_i?

unnormalized probabilities

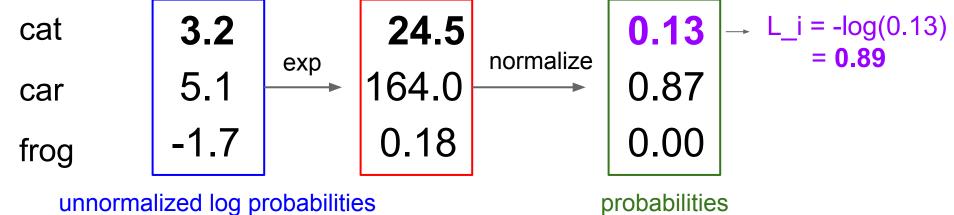


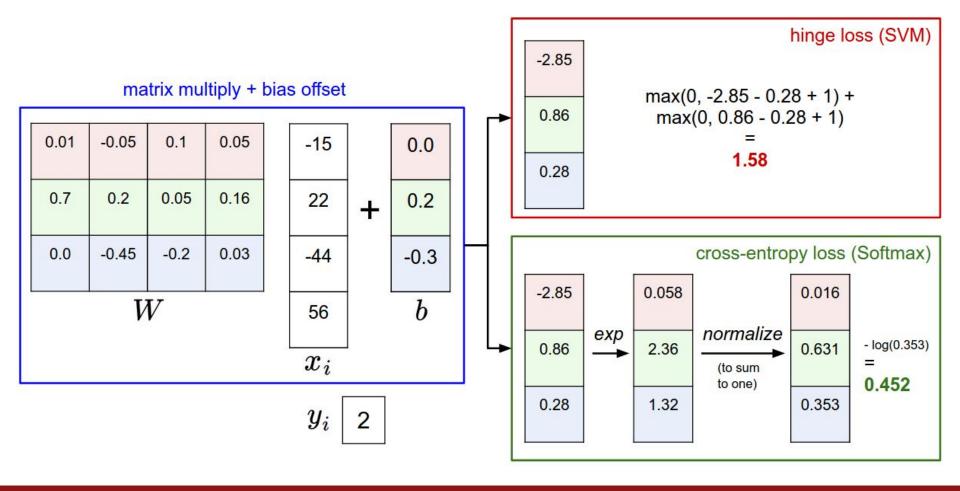


$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$

unnormalized probabilities

Q5: usually at initialization W are small numbers, so all s ~= 0. What is the loss?





#### Softmax vs. SVM

$$L_i = -\log(rac{e^{sy_i}}{\sum_i e^{s_j}})$$

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

## Softmax vs. SVM

$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$

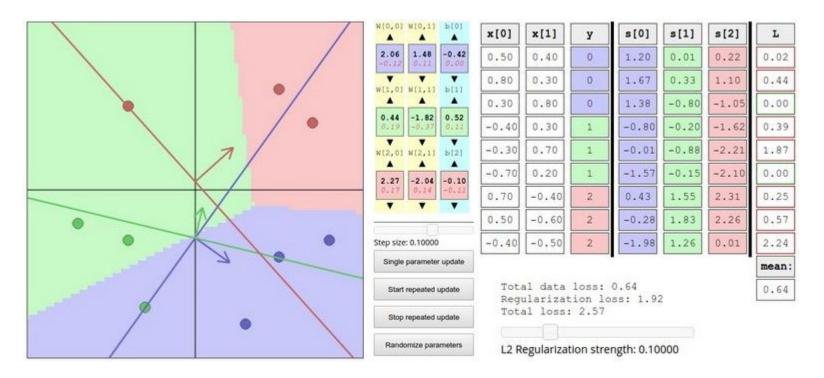
$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

assume scores:

and 
$$y_i = 0$$

Q: Suppose I take a datapoint and I jiggle a bit (changing its score slightly). What happens to the loss in both cases?

#### Interactive Web Demo time....



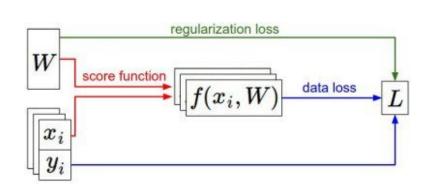
http://vision.stanford.edu/teaching/cs231n/linear-classify-demo/

## Optimization

#### Recap

- We have some dataset of (x,y)
- We have a **score function**:  $s=f(x;W)\stackrel{\text{e.g.}}{=}Wx$
- We have a **loss function**:

$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$
 SVM $L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$  $L = rac{1}{N} \sum_{i=1}^N L_i + R(W)$  Full loss



#### Strategy #1: A first very bad idea solution: Random search

```
# assume X train is the data where each column is an example (e.g. 3073 x 50,000)
# assume Y train are the labels (e.g. 1D array of 50,000)
# assume the function L evaluates the loss function
bestloss = float("inf") # Python assigns the highest possible float value
for num in xrange(1000):
 W = np.random.randn(10, 3073) * 0.0001 # generate random parameters
 loss = L(X train, Y train, W) # get the loss over the entire training set
 if loss < bestloss: # keep track of the best solution
   bestloss = loss
   bestW = W
 print 'in attempt %d the loss was %f, best %f' % (num, loss, bestloss)
# prints:
# in attempt 0 the loss was 9.401632, best 9.401632
# in attempt 1 the loss was 8.959668, best 8.959668
# in attempt 2 the loss was 9.044034, best 8.959668
# in attempt 3 the loss was 9.278948, best 8.959668
# in attempt 4 the loss was 8.857370, best 8.857370
# in attempt 5 the loss was 8.943151, best 8.857370
# in attempt 6 the loss was 8.605604, best 8.605604
# ... (trunctated: continues for 1000 lines)
```

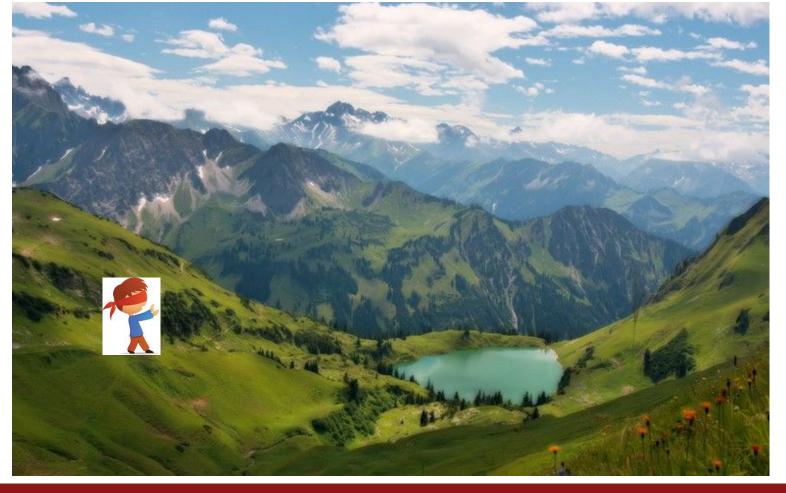
#### Lets see how well this works on the test set...

```
# Assume X_test is [3073 x 10000], Y_test [10000 x 1]
scores = Wbest.dot(Xte_cols) # 10 x 10000, the class scores for all test examples
# find the index with max score in each column (the predicted class)
Yte_predict = np.argmax(scores, axis = 0)
# and calculate accuracy (fraction of predictions that are correct)
np.mean(Yte_predict == Yte)
# returns 0.1555
```

15.5% accuracy! not bad! (SOTA is ~95%)



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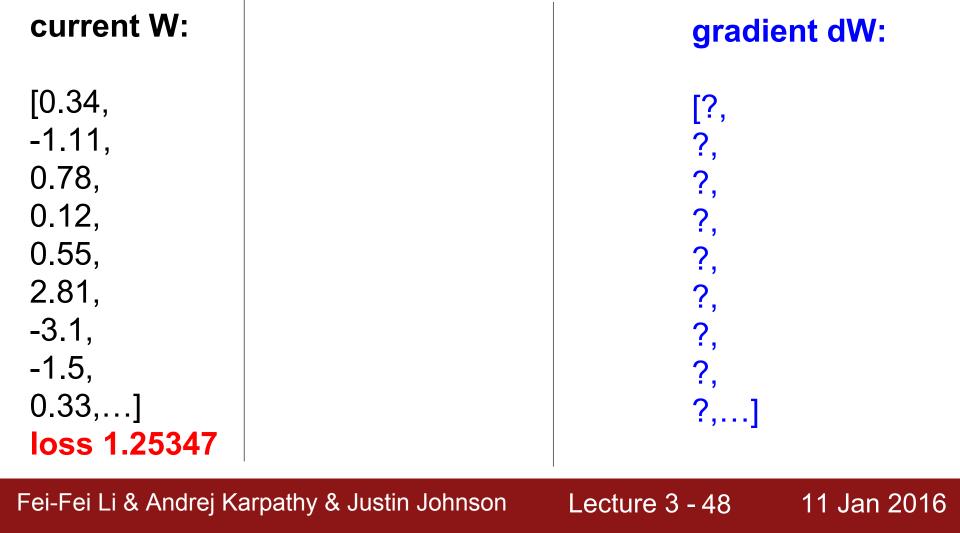
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#### Strategy #2: Follow the slope

In 1-dimension, the derivative of a function:

$$rac{df(x)}{dx} = \lim_{h o 0} rac{f(x+h) - f(x)}{h}$$

In multiple dimensions, the **gradient** is the vector of (partial derivatives).



current W:	W + h (first dim):	gradie	ent dW:
[0.34, -1.11, 0.78, 0.12, 0.55,	[0.34 + <b>0.0001</b> , -1.11, 0.78, 0.12, 0.55,	[?, ?, ?, ?,	
2.81, -3.1, -1.5, 0.33,] loss 1.25347	2.81, -3.1, -1.5, 0.33,] loss 1.25322	?, ?, ?, ?,]	
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#### W + h (first dim): gradient dW: [0.34 + 0.0001][0.34,**[-2.5**, -1.11, -1.11, 0.78, 0.78, 0.12, 0.12, (1.25322 - 1.25347)/0.00010.55, 0.55, = -2.52.81, 2.81, $\frac{df(x)}{dx} = \lim_{x \to 0} \frac{f(x+h) - f(x)}{f(x+h)}$ -3.1, -3.1, -1.5, -1.5, 0.33,...0.33,...?,...] loss 1.25347 loss 1.25322 Fei-Fei Li & Andrej Karpathy & Justin Johnson Lecture 3 - 50 11 Jan 2016

current W:

current W:	W + h (second dim):	gradie	nt dW:
[0.34, -1.11, 0.78, 0.12, 0.55, 2.81, -3.1, -1.5, 0.33,]	[0.34, -1.11 + <b>0.0001</b> , 0.78, 0.12, 0.55, 2.81, -3.1, -1.5, 0.33,]	[-2.5, ?, ?, ?, ?, ?, ?, ?, ?,]	
loss 1.25347	loss 1.25353 arpathy & Justin Johnson	Lecture 3 - 51	11 Jan 2

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#### gradient dW: [0.34,[0.34,[-2.5, -1.11, -1.11 + 0.00010.6, 0.78, 0.78, 0.12, 0.12, 0.55, 0.55, (1.25353 - 1.25347)/0.00012.81, 2.81, = 0.6-3.1, -3.1, -1.5, -1.5, 0.33,...0.33,...] ?,...] loss 1.25353 loss 1.25347 Fei-Fei Li & Andrej Karpathy & Justin Johnson Lecture 3 - 52 11 Jan 2016

W + h (second dim):

current W:

current W:	W + h (third dim):	gradient dW:
[0.34,	[0.34,	[-2.5,
-1.11,	-1.11,	0.6,
0.78,	0.78 + <b>0.0001</b> ,	?,
0.12,	0.12,	?,
0.55,	0.55,	?,
2.81,	2.81,	?,
-3.1,	-3.1,	?,
-1.5,	-1.5,	?,
0.33,]	0.33,]	?,]
loss 1.25347	loss 1.25347	
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#### gradient dW: [0.34,[0.34,[-2.5, -1.11, -1.11, 0.6, 0.78 + 0.00010.78, 0.12, 0.12, 0.55, 0.55, (1.25347 - 1.25347)/0.00012.81, 2.81, = 0-3.1, -3.1, $\frac{df(x)}{dx} = \lim \frac{f(x+h) - f(x)}{dx}$ -1.5, -1.5, 0.33,...0.33,...] loss 1.25347 loss 1.25347

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**W** + **h** (third dim):

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current W:

## Evaluation the gradient numerically

$$rac{df(x)}{dx} = \lim_{h o 0} rac{f(x+h) - f(x)}{h}$$

```
def eval numerical gradient(f, x):
  a naive implementation of numerical gradient of f at x
  - f should be a function that takes a single argument
  - x is the point (numpy array) to evaluate the gradient at
 fx = f(x) # evaluate function value at original point
 grad = np.zeros(x.shape)
 h = 0.00001
 # iterate over all indexes in x
 it = np.nditer(x, flags=['multi index'], op flags=['readwrite'])
 while not it.finished:
   # evaluate function at x+h
    ix = it.multi index
    old value = x[ix]
    x[ix] = old value + h # increment by h
    fxh = f(x) # evalute f(x + h)
   x[ix] = old value # restore to previous value (very important!)
    # compute the partial derivative
    grad[ix] = (fxh - fx) / h # the slope
    it.iternext() # step to next dimension
  return grad
```

# Evaluation the gradient numerically

$$rac{df(x)}{dx} = \lim_{h o 0} rac{f(x+h) - f(x)}{h}$$

- approximate
- very slow to evaluate

```
def eval numerical gradient(f, x):
  a naive implementation of numerical gradient of f at x
  - f should be a function that takes a single argument
  - x is the point (numpy array) to evaluate the gradient at
 fx = f(x) # evaluate function value at original point
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 while not it.finished:
   # evaluate function at x+h
    ix = it.multi index
    old value = x[ix]
    x[ix] = old value + h # increment by h
    fxh = f(x) # evalute f(x + h)
   x[ix] = old value # restore to previous value (very important!)
    # compute the partial derivative
    grad[ix] = (fxh - fx) / h # the slope
    it.iternext() # step to next dimension
  return grad
```

$$egin{aligned} L &= rac{1}{N} \sum_{i=1}^{N} L_i + \sum_k W_k^2 \ L_i &= \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1) \ s &= f(x; W) = Wx \end{aligned}$$

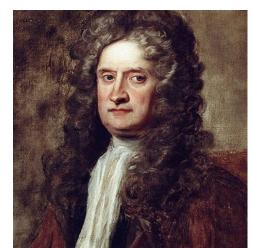
want  $\nabla_W L$ 

$$L = \frac{1}{N} \sum_{i=1}^{N} L_i + \sum_k W_k^2$$

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

$$s = f(x; W) = Wx$$

want  $\nabla_W L$ 

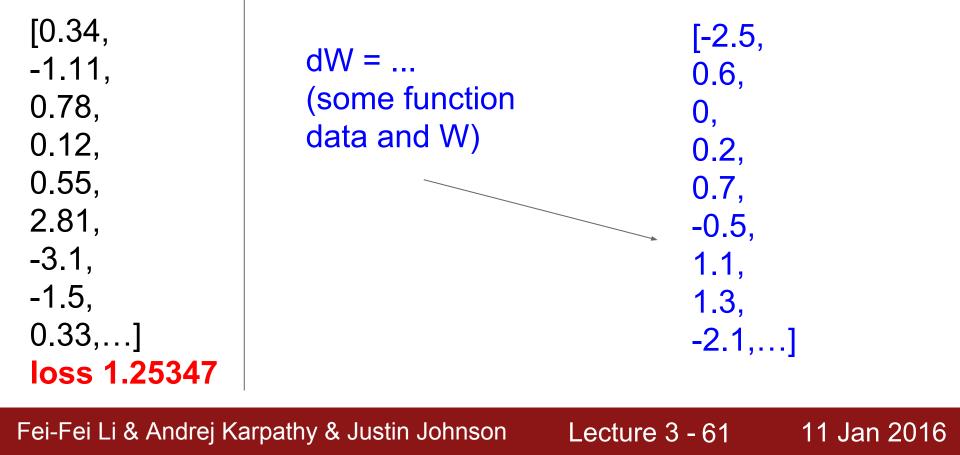




$$L=rac{1}{N}\sum_{i=1}^{N}L_i+\sum_k W_k^2$$
  $L_i=\sum_{j
eq y_i}\max(0,s_j-s_{y_i}+1)$   $s=f(x;W)=Wx$  want  $abla_W L$  Calculus

$$egin{aligned} L &= rac{1}{N} \sum_{i=1}^N L_i + \sum_k W_k^2 \ L_i &= \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1) \ s &= f(x; W) = Wx \end{aligned}$$

$$\nabla_W L = \dots$$



gradient dW:

current W:

#### In summary:

- Numerical gradient: approximate, slow, easy to write
- Analytic gradient: exact, fast, error-prone

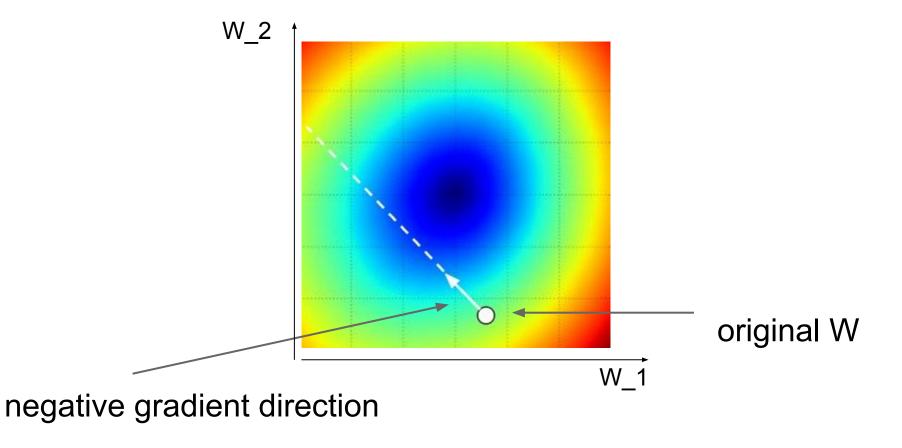
=>

<u>In practice:</u> Always use analytic gradient, but check implementation with numerical gradient. This is called a **gradient check.** 

#### **Gradient Descent**

```
# Vanilla Gradient Descent

while True:
    weights_grad = evaluate_gradient(loss_fun, data, weights)
    weights += - step_size * weights_grad # perform parameter update
```



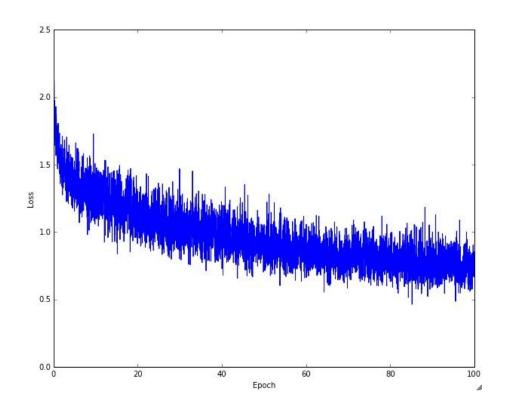
#### Mini-batch Gradient Descent

only use a small portion of the training set to compute the gradient.

```
# Vanilla Minibatch Gradient Descent

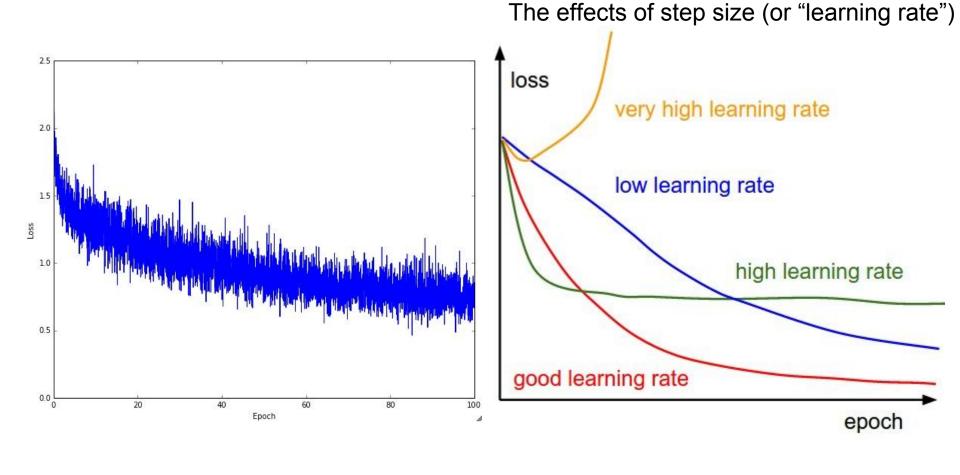
while True:
    data_batch = sample_training_data(data, 256) # sample 256 examples
    weights_grad = evaluate_gradient(loss_fun, data_batch, weights)
    weights += - step_size * weights_grad # perform parameter update
```

Common mini-batch sizes are 32/64/128 examples e.g. Krizhevsky ILSVRC ConvNet used 256 examples



Example of optimization progress while training a neural network.

(Loss over mini-batches goes down over time.)



#### Mini-batch Gradient Descent

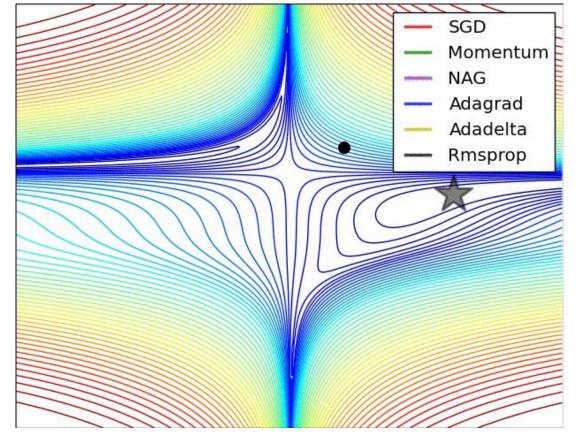
only use a small portion of the training set to compute the gradient.

```
Vanilla Minibatch Gradient Descent
while True:
  data batch = sample training data(data, 256) # sample 256 examples
  weights grad = evaluate gradient(loss fun, data batch, weights)
  weights += - step size * weights grad # perform parameter update
```

Common mini-batch sizes are 32/64/128 examples e.g. Krizhevsky ILSVRC ConvNet used 256 examples

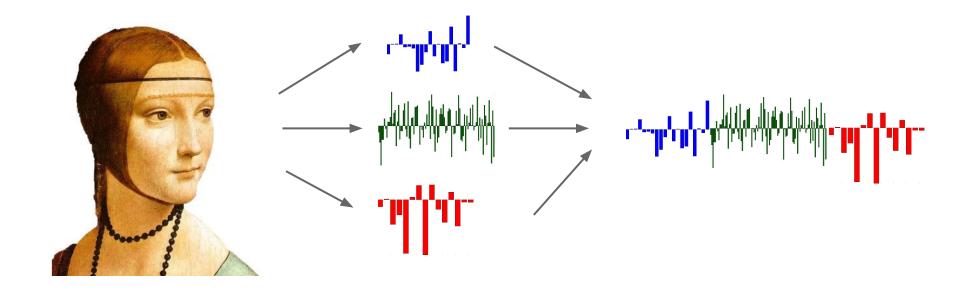
we will look at more fancy update formulas (momentum, Adagrad, RMSProp, Adam, ...)

The effects of different update form formulas

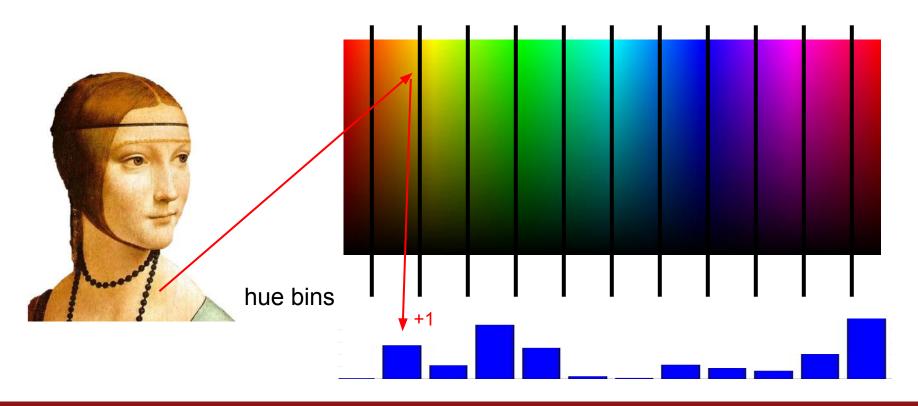


(image credits to Alec Radford)

### Aside: Image Features

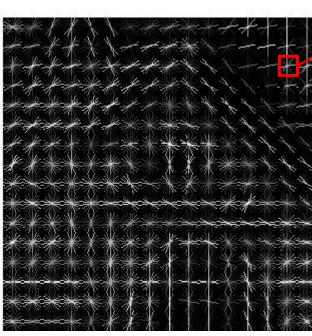


## Example: Color (Hue) Histogram



#### Example: HOG/SIFT features



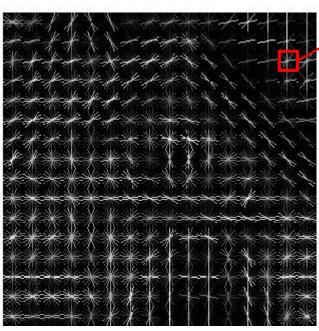


8x8 pixel region, quantize the edge orientation into 9 bins

(image from vlfeat.org)

#### Example: HOG/SIFT features

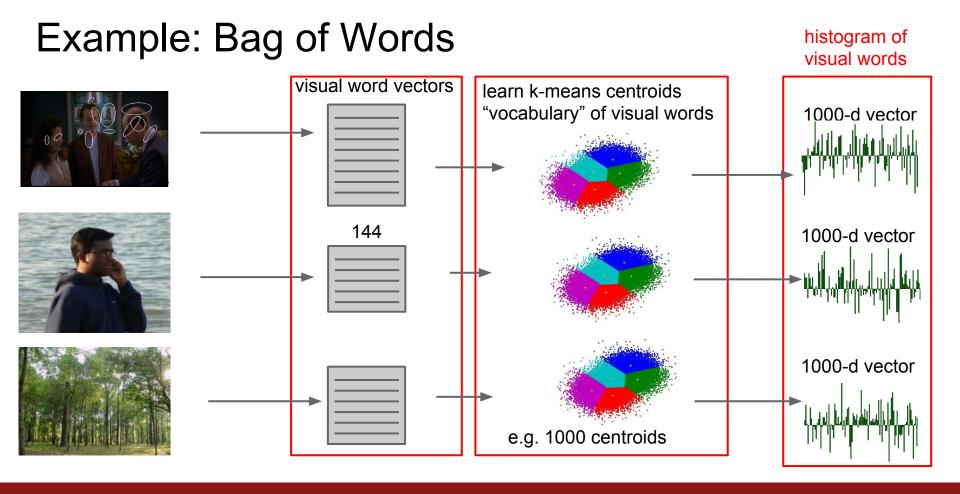


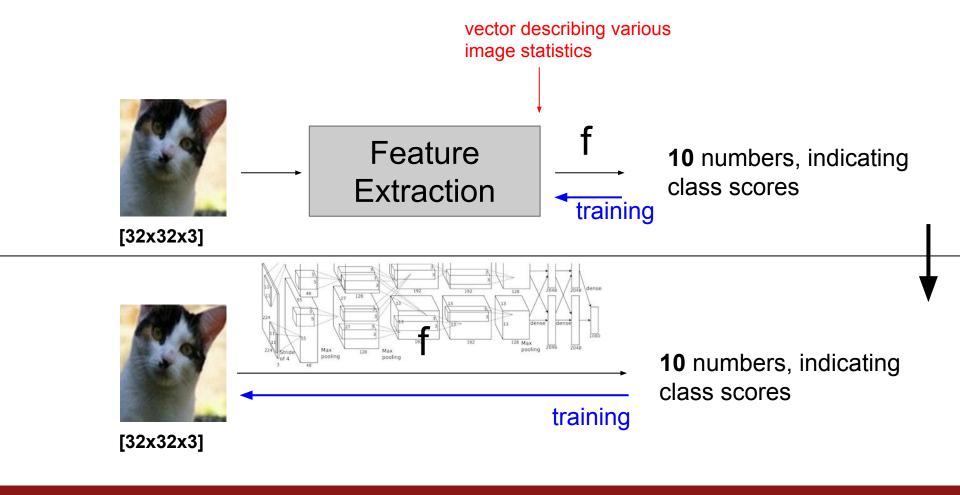


8x8 pixel region, quantize the edge orientation into 9 bins

Many more: GIST, LBP, Texton, SSIM, ...

(image from vlfeat.org)





## **Next class:**

Becoming a backprop ninja and Neural Networks (part 1)