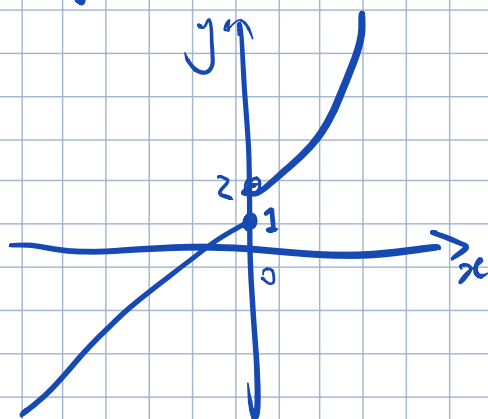


Problem Class Week 2

(2) Injection



$$x_1 \neq x_2 \Rightarrow f(x_1) \neq f(x_2)$$

$$y = f(x_1) = f(x_2) \Rightarrow x_1 = x_2$$

Surjection

$$\forall y \exists x \quad y = f(x)$$

A weird point around 0.

$$x_1 \leq 0 < x_2.$$

$$x_1 + 1 = x_2^2 + 2$$

$$x_2^2 + 2 > 2$$

$$x_1 + 1 \leq 1$$

$$x_1 \neq x_2.$$

Injective

$$y = 1.5$$

$$x > 0$$

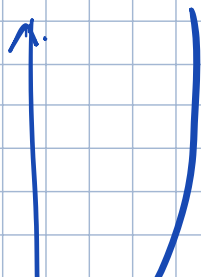
$$f(x) > 2$$

$$x \leq 0$$

$$f(x) \leq 1$$

Not surjective

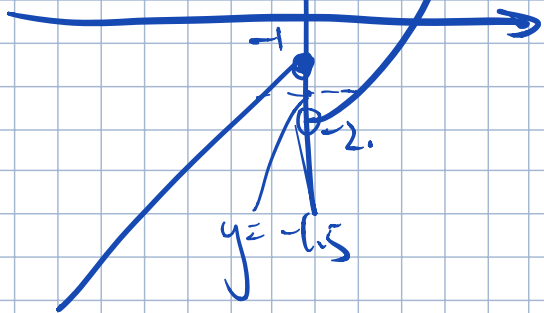
(3).



$$x_1 - 1 = -1.5$$

$$x_1 = -0.5$$

$$x_2^2 = 2 = 1.5$$



$$x_2 = 2 - (-1.5)$$

$$x_2^2 = 0.5$$

$$x_2 = \sqrt{0.5}$$

Not injective