

Imperative style. vs. functional style
 calculus elegant.

Miranda Tuple. ("Ted", 23, False)
 $:: (\text{Char}) \rightarrow \text{num} \rightarrow \text{bool}$
 ("increment", inc) $:: (\text{Char}) \rightarrow \text{num} \rightarrow \text{num}$.

lazy evaluation. $\rightarrow g(x\ y) = 2$.
 $g(1, \text{!}0)$
 \downarrow
 never evaluated.

partial funcs.
 $f(x\ y) = x / y, \quad y \neq 0$.

polymorphic funcs don't evaluate some
 of the input.

three $:: * \rightarrow \text{num}$.
 three $x \rightarrow 3$

for different types, use $\#$, $\#\#$, $\#\#\#$

Non-exhaustive patterns

$f\ \text{True} = \text{False}$.
 $x = f\ \text{False}$ \times False not defined.

Patterns destroy laziness.

not lazy. $f. (x, 0) = x$.

$$\text{notlazy}_f(x, y) = x.$$

$$\text{notlazy}(5, \underline{1/0})$$

↓
evaluated to imp to 0

Duplicate param = equality test.

botheqnd $(x, x) \rightarrow \text{Bool.}$

$$(x, x) = \top$$

$$(x, y) = \text{F}$$

Recursive function creates loops.

$$f :: \text{num} \rightarrow [\text{char}]$$

$$f 0 = ""$$

$$f n = "x" ++ (f(n-1)), \text{ if } n > 0$$

$$= "x" ++ (f(n+1)), \text{ otherwise.}$$

Type Synonyms

$$\text{str} == [\text{char}].$$

$$\text{Coord} == (\text{num}, \text{num}, \text{num})$$

Lists.

$$x1 :: [\text{num}].$$

$$x1 = x :: [\text{lst}] \quad (\text{lst}, x)$$

$$\text{or } x1 = [\text{lst}, x].$$

Iterative list.

$[1..] = [1, 2, 3, \dots]$

list comprehension. $\rightarrow [n * n \mid n \in [1, 2, 3]]$
 $= [1, 4, 9]$

λ calculus

α . reduction. $\lambda x. E \rightarrow \lambda y. E[y/x]$
 \downarrow
all free occurrences
 $x \rightarrow y$

β reduction $(\lambda x. E) M \rightarrow E[M/x]$

η reduction. $\lambda x. (E \ x) \rightarrow E$

δ rules $+ \ x \quad (3+4) = 7$

Examples.

$\lambda x. (x+3) \ 5 \rightarrow \beta$ reduction
 $(5+3) \rightarrow \delta$ rules
 8

$\lambda y. ((\lambda x. (x+y)) \ 5) \ 3 \rightarrow$

$\lambda y. (5+y) \ 3 \rightarrow$

$5+3 \rightarrow$
 8

$$\begin{aligned}
 & (\lambda x. ((x\ 5) + (x\ 4)))\ (\lambda x. (x+3)) \rightarrow \\
 & ((\lambda x (x+3)\ 5) + ((\lambda x (x+3)\ 4))). \\
 & (5+3) + (4+3). \\
 & = 15.
 \end{aligned}$$

Mark Scan GC.

Triggered at `malloc()`. when free is low.

Program pause at GC.

Mark Garbage. Trace all live pointers
Scan. Garbage node available for re-use

We can compact to reduce fragmentation
every block has a "mark" bit