

1. The Wave Function

1.1 The Schrödinger Equation

$$i\hbar \frac{\partial \Psi}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2 \Psi}{\partial x^2} + V\Psi$$

Solve for the particle's wave function $\Psi(x, t)$

$$\hbar = \frac{h}{2\pi} = 1.054572 \times 10^{-34} \text{ Js}$$

1.2 The Statistical Interpretation

$$\int_a^b |\Psi(x, t)|^2 dx = \{\text{P of finding the particle btwn } a \text{ and } b, \text{ at } t\}$$

1.3 Probability

$$\text{Standard deviation: } \sigma = \sqrt{\langle j^2 \rangle - \langle j \rangle^2}$$

$$\text{Expectation value of } x \text{ given } \Psi: \langle x \rangle = \int x |\Psi|^2 dx$$

1.4 Normalization

$$\int_{-\infty}^{+\infty} |\Psi(x, t)|^2 dx = 1$$

1.5 Momentum

For a particle in state Φ , the expectation value of x is

Other: **Blackbody Spectrum**

$$E = hv = \hbar\omega$$

The wave number k is $k = 2\pi/\lambda = \omega/c$

Only two spin states occur (quantum number m is +1 or -1).

$$\rho(\omega) = \frac{\hbar\omega^3}{\pi^2 c^3 (e^{\hbar\omega/k_b T} - 1)}$$

$$\text{Wien displacement law: } \lambda_{\max} = \frac{2.90 \times 10^{-3} \text{ mK}}{T}$$