Media Engineering and Technology Faculty German University in Cairo



Bachelor Thesis Title

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Supervisors: Sup 1

 $\mathrm{Sup}\ 2$

Sup 3

Submission Date: XX July, 20XX

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Τ	This is to certify that:				
(i)	the thesis comprises only my original work toward the Bachelor Degree				
(ii) due acknowlegement has been made in the text to all other material used					
	Maggie Ezzat Gamil Gaid XX July, 20XX				

Acknowledgments

Text

Abstract

Abstact

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Introduction

Natural Language Processing (NLP) and contextual analysis techniques have matured greatly over the last decade, with applications rising in many industries. The evolution of transport network operators to more automation requires an AI-enabled control center room. In this project, we aim to enhance the capability of our system, enabling it to understand human speech from vehicle driver input and trigger dispatcher actions automatically. As such, an AI dispatcher agent needs to understand a message/call from a driver in order to trigger the necessary action.

A second valuable application of such NLP engine, is increased automation inside the control center. As such, an artificially-intelligent (AI) dispatcher agent needs to understand a message/call from a driver in order to trigger the necessary action.

Literature Review

2.1 Natural Language Processing

Natural Languages refer to languages written and spoken by human beings. They are English, German, French, etc. Humans can easily learn and understand such languages. On the other hand, computers have difficulty understanding these languages because of the ambiguity problem, as computers understand structured and unambiguous programming languages.

Natural Language Processing (NLP) is a field which aims at enhancing the human-computer interaction by giving computers the ability to understand natural languages. It encompasses two sub-fields: Natural Language Generation (NLG) and Natural Language Understanding (NLU). NLG targets making computers generate human-like sentences. NLU focuses on semantics extraction or building a comprehension of the intent. For quite a long time, NLP researches have been striving to build ASR systems and language models for narrowing down the gap between humans and machines.

In this Literature Review, two sub-domains are explored: Speech Recognition and Text Analytics, but at the beginning a quick review of the widely popular Artificial Neural Networks is elaborated in the next section.

2.2 Artificial Neural Networks

Artificial Neural Network (ANN)s are models of computation modeled after the biological neural networks that constitute the human brain. In early researches of Neural Networks, biological resemblance was emphasized [15] [16] [8], however, nowadays it is obvious that ANNs have little in common compared to biological neural networks. That is due to the biological emphasis being abandoned in favor of achieving satisfying computational results.

The basic building block of ANNs are "neurons", commonly called nodes. The set of nodes are connected to each other with weighted edges, with the weights of the edges resembling the strength of the "synapses" between the neurons as suggested by the original biological model. The neurons are represented diagrammatically by drawing them as circles, and the weighted edges as arrows connecting them. Each node has an activation function associated with it, which takes as input a weighted sum of its input nodes (Figure 2.1).

The most popular activation functions are the sigmoid function $\sigma(z) = \frac{1}{1+e^-z}$, the tanh function $\phi(z) = \frac{e^z - e - z}{e^z + e^-z}$, and the Re-Lu function l(z) = max(0, z). The activation function at the output nodes is considered to be task-specific. However, the most popular ones are the softmax function $\sigma(\mathbf{z})_i = \frac{e^{z_i}}{\sum_{j=1}^K e^{z_j}}$ for i = 1, ..., K and $\mathbf{z} = (z_1, ..., z_K) \in \mathbb{R}^K$, the sigmoid function, or simple linear functions.

There exist many variations of ANNs, the simplest form of them are those whose edges do not form any cycles. These are called Feed Forward Neural Networks.

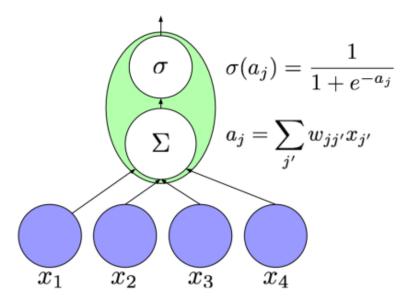


Figure 2.1: A neuron represented as a circle and the weighted edges as arrows. The activation function is a function of the sum of the weighted edges. [?]

2.2.1 Feed Forward Neural Networks

The most popular form of Feed Forward Neural Network (FNN)s is the Multi Layer Perceptrons (MLP)s [20] [24] [5]. With the absence of cycles, the nodes are arranged into layers, as seen in Figure 2.2, where the layers are classified as an input layer, one or many hidden layers, and an output layer.

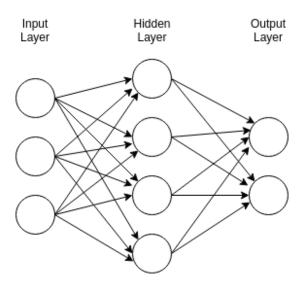


Figure 2.2: A simple Feed Forward Neural Network consisting of an input layer, one hidden layer, and an output layer

The input to FNNs is applied to the input layer. Values of nodes in a given layer, are successively calculated using the values of nodes in the lower layer, until the output is generated at the highest layer: the output layer. This is known as the "Forward pass". Neural Networks learn by looking at input examples without being explicitly programmed any hard-coded rules about the required task. The learning process is achieved by continuously modifying the weights to minimize an error represented by a loss function $L(\hat{y}, y)$, which measures the distance between the output y (predicted value of y) and the actual value of y (ground-truth).

The algorithm for training neural networks is back-propagation [20]. Back-propagation uses the

chain rule to calculate the derivative of the loss function $L(\widehat{y}, y)$ with respect to each parameter in the network. The parameters (weights) are then adjusted in the direction of less error by an optimization algorithm called gradient descent. This is known as the "Backward Pass"

Sequence Models and the Problem with FNNs

A distinctive feature of the FNNs is the "independence assumption". That is the presented examples (data points) are assumed to be independent of each other, rendering the FNNs unable to correctly represent input or output sequences with dependencies either in time or space. Examples are words forming sentences, letters forming words, frames of video, snippets of audio clips, DNA sequences, etc. FNNs knows no concept of context when analyzing the given examples, they simply are unable to capture dependencies. With the context being a crucial element when analyzing sequences, a simple solution that addresses that matter is the "time-window" solution, i.e. collect the data from either side of the current input into a window. The fact that the range of useful context (either on the left or the right) vary widely from sequence to sequence and in most cases is unknown makes this approach not very efficient. For example, a model trained using a finite-length context window of length n could never be trained to answer the simple question, "what was the data point seen n+1 time steps ago?"

Another problem with FNNs is that they treat inputs and outputs as "fixed-length vectors". Some representations, such as sentences can not be represented in such way. Some solutions such as "padding" assume a maximum-length for the inputs and/or outputs. Such approach is not a general one. Thus, it was required to extend these powerful and successful models to better suit the sequential nature of some data, and that is where the Recurrent Neural Networks came into picture.

2.2.2 Recurrent Neural Networks

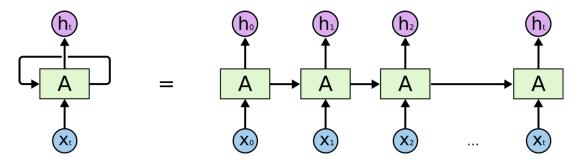


Figure 2.3: A Recurrent Neural Network

ANNs containing cycles are referred to as recursive, or recurrent neural networks. Recurrent Neural Network (RNN)s are models which have the ability to pass information learnt across past data points, while processing sequential data points one by one. Thus they can model inputs and outputs which are correlated either in time or space. They are considered to be neural networks possessing memory.

The RNNs have the following architecture: each hidden layer - commonly referred to as "hidden state" - has two sources of inputs, which are the present data point, and information from the hidden state of the past data point (Figure 2.3). This is how contextual information is propagated across the hidden states of the sequential data points. Equation 2.1 explains how each hidden state nodes values are calculated. Each hidden state $\mathbf{h_t}$ is a function of the present data point \mathbf{x} multiplied by some weight matrix W^x and the previous hidden state $\mathbf{h_{t-1}}$ multiplied by some weight matrix W^h and some bias term $\mathbf{b_h}$. The weight matrices are used to determine how much importance is given to both the present data point and the past hidden state. The output $\widehat{\mathbf{y_t}}$ at time step t is given by

equation 2.2, where $\hat{\mathbf{y_t}}$ is obtained by applying the softmax function to the hidden state $\mathbf{h_t}$ multiplied by some weight matrix W^y and adding to it some bias term $\mathbf{b_y}$. Similar to the vanilla ANNs, the weights are continuously adjusted to minimize a cost function. This is done using an algorithm called Backpropagation Through Time (BPTT) [25]

$$\mathbf{h_t} = \phi(W^x \mathbf{x} + W^h \mathbf{h_{t-1}} + \mathbf{b_h}) \tag{2.1}$$

$$\widehat{\mathbf{y_t}} = softmax(W^y \mathbf{h_t} + \mathbf{b_y}) \tag{2.2}$$

Bidirectional RNNs

A slight variation of the RNNs is the Bidirectional Recurrent Neural Network (BRNN)s [21]. The BRNNs have a slight different architecture which allows it to take into consideration information not only from the present and the past input but also from the future input. Note that by past, present, and future, we not only refer to temporal sequences, but also sequences which have a strong emphasis of the order, but bear no explicit notion of time; this is actually the case with natural languages. In BRNNs each hidden layer is duplicated into two layers (Figure 2.4), one layer takes as inputs the present data point and information from the past data point. This is referred to as the "forward direction". The other layer takes as input the present data point and information from the future data point. This is referred to as the "backward direction". The BRNNs are fully described by equations 2.3, 2.4 and 2.5, where $\mathbf{h_t^{< f>}}$ represents the forward direction of the hidden layers and $\mathbf{h}_{\mathbf{t}}^{<\mathbf{b}>}$ represents the backward direction of the hidden layers. The predicted value $\widehat{\mathbf{y}}_{\mathbf{t}}$ is now a function of both the forward and the backward direction. Considering information from both sides of the sequence instead of the left side only adds much power to the network as the context is understood much better. Consider the following example: "She said, 'Teddy bears are on sale.", "She said, 'Teddy Roosevelt was an amazing president'" On these two examples, considering "Teddy" as the current data point, the left sequence is the same, however, the right sequence is crucial in understanding the context. Thus for an application like named-entity recognition, using BRNNs adds much gain. One drawback about BRNNs is that the entire sequence is needed before any predictions can be made, therefore for real-time systems it is a bit slow as it introduces some delay.

$$\mathbf{h}_{\mathbf{t}}^{\langle \mathbf{f} \rangle} = \phi(W^{xf}\mathbf{x} + W^{hf} \mathbf{h}_{\mathbf{t-1}}^{\langle \mathbf{f} \rangle} + \mathbf{b}_{\mathbf{hf}})$$
(2.3)

$$\mathbf{h_t^{}} = \phi(W^{xb}\mathbf{x} + W^{hb} \mathbf{h_{t+1}^{}} + \mathbf{b_{hb}})$$
(2.4)

$$\widehat{\mathbf{y_t}} = softmax(W^{yf} \ \mathbf{h_t^{< f}}) + W^{yb} \ \mathbf{h_t^{< b}} + \mathbf{b_y})$$
(2.5)

Problems with RNNs

TODO: vanishing and exploding gradients [12] [13] [4]

Long Short-Term Memory

Long Short-Term Memory (LSTM) [14] is a variation of vanilla RNNs which was designed as a solution to the vanishing gradients problem. The main idea was to replace the ordinary node with a "memory cell". The cell uses "gates" in order to make decisions about which information to keep and which to discard. It has three gates: output, input, and forget gate, which are analogous to read,

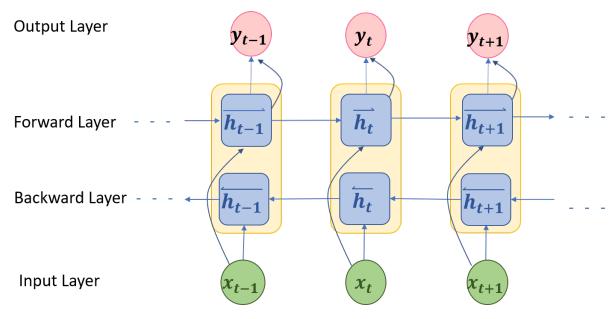


Figure 2.4: A Bidirectional Recurrent Neural Network

write, and reset operations for the memory cell. The gates uses sigmoid as the activation function, where the values of the gates ranges from 0 to 1.

TODO 1: continue LSTM

$$\tilde{\mathbf{c_t}} = tanh(W^{ch} \ \mathbf{h_{t-1}} + W^{cx} \ \mathbf{x_t} + \mathbf{b_c}) \tag{2.6}$$

$$\mathbf{f_t} = \sigma(W^{fh} \mathbf{h_{t-1}} + W^{fx} \mathbf{x_t} + \mathbf{b_f})$$
 (2.7)

$$\mathbf{i_t} = \sigma(W^{ih} \ \mathbf{h_{t-1}} + W^{ix} \ \mathbf{x_t} + \mathbf{b_i}) \tag{2.8}$$

$$\mathbf{o_t} = \sigma(W^{oh} \ \mathbf{h_{t-1}} + W^{ox} \ \mathbf{x_t} + \mathbf{b_o}) \tag{2.9}$$

$$\mathbf{c_t} = \mathbf{i_t} \ \tilde{\mathbf{c_t}} + \mathbf{f_t} \ \mathbf{c_{t-1}} \tag{2.10}$$

$$\mathbf{h_t} = tanh(\mathbf{c_t}) \ \mathbf{o_t} \tag{2.11}$$

Problems with LSTM

TODO 2: Problems with LSTMS

2.2.3 Convolution Neural Networks

TODO 3: CNNs

Now that we have examined neural networks, we move forward to discussing the speech recognition problem in the next section.

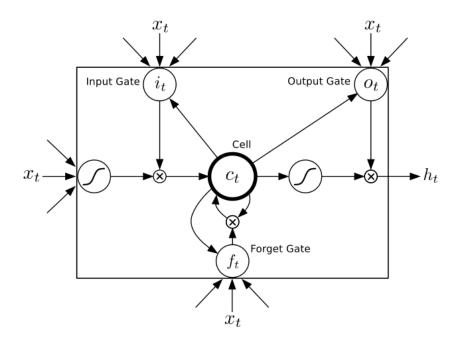


Figure 2.5: An LSTM Cell

2.3 Speech Recognition

The speech recognition problem is defined as follows: given an audio waveform, the task is to find the closest possible transcription to what an accurate human would generate upon listening to that audio. This problem dates back to 1960's, however, the basic Hidden Markov Model (HMM) speech recognition systems originated in mid 1980's. In this section we investigate the mechanics of the ASR systems based on HMMs, moving to the so called "hybrid models" and eventually the growingly popular "End-to-End Systems".

2.3.1 HMM-Based ASR Systems

We begin by demonstrating the main components of an ASR system. As depicted in figure FIGURE, an audio waveform is passed to a "feature extraction" module, which outputs a sequence of acoustic vectors, $\mathbf{Y} = y_1, y_2, ..., y_T$. The audio fragment corresponds to a sequence of words $W = w_1, w_2, ..., w_n$, and it is the objective of the ASR system is to find the most probable word sequence W given a previously unknown audio signal \mathbf{Y} . More formally, the target is to find $W = arg \max_W P(W|\mathbf{Y})$. Using Bayes' Rule, this probability can be broken down into two probabilities as shown in equation 2.12.

$$W = arg \, max_W \, P(W|\mathbf{Y}) = arg \, max_W \, \frac{P(W) \, P(\mathbf{Y}|W)}{P(\mathbf{Y})}$$
 (2.12)

This indicates that we need to find P(W) and P(Y|W) which maximizes 2.12, in order to find the most probable word sequence W. There are two main components in the ASR system, the "language model" is used to compute P(W), which is the probability of observing the word sequence W independent of the audio signal. The second component, which is the "acoustic model" computes P(Y|W) which is the probability of the sequence of acoustic vectors Y, given a word sequence W.

Figure FIGURE illustrates the flow of the ASR mechanics. Firstly, P(W) is computed by the language model, then the word sequence W is passed to a "pronouncing dictionary", which breaks the words into "phones". Phones are distinct units of sounds, and they are specific to every language.

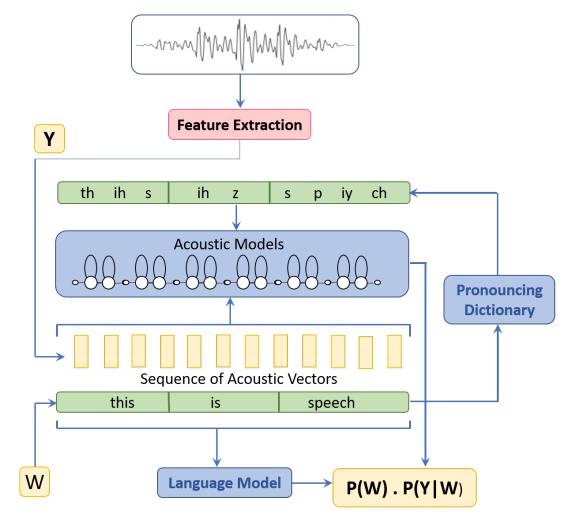


Figure 2.6: An ASR System

For example, English has 44 phones, despite having 26 letters only. That means there 44 different sounds in English. The audio signal is passed to a feature extraction module which outputs numerical features representing the speech signal. For every phone, a statistical HMM model is built, and these models are concatenated together in order to represent the whole sequence of phones making up the utterance using a single model. Then the probability of this model generating the sequence of acoustic vectors Y, given the word sequence W is calculated i.e. $P(\mathbf{Y}|W)$. For every possible word sequence W, this process can be repeated until we get the most probable word sequence, however, this is obviously impractical and more efficient methods are used. The process of searching for the most probable word sequence is referred to as "decoding".

We begin by shedding light on the feature extraction module.

Feature Extraction

The premier step in any ASR system is to extract features. That is to turn the raw speech waveforms into a sequence of numerical vectors. The issue, however, lies in the fact that audio signals are constantly changing. For us to be able to deal with them, we make the assumption that for sufficiently small period of time the signals are stationary. Therefore we sample the signal into 25ms frames, with a step of about 10ms so that the frames are overlapping. Then we apply some operations on each frame to extract features. The most widely used feature extraction method is Mel-Frequency Cepstral Coefficents (MFCC), which we explain in brief.

For each frame, the Fast Forier Transform (FFT) is calculated, in order to move from the time domain to the spectral domain. Human ears cannot distinguish between two closely spaced frequencies, specially for higher frequencies; to mimic this effect, we need to know how much energy exists in

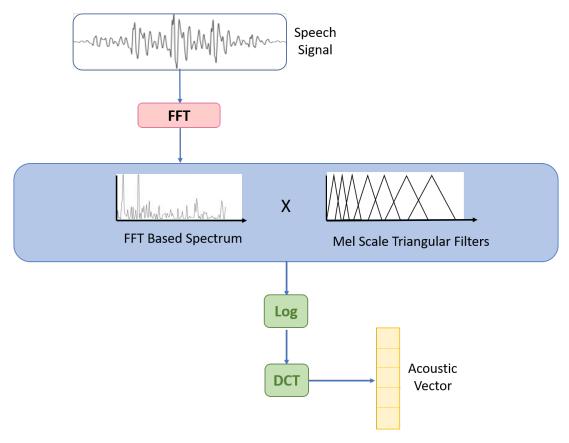


Figure 2.7: MFCC

different frequency regions. This is done by applying special filters called Mel filterbanks. The first filter is the narrowest, and indicates how much energy exists around 0 Hertz. Then the filters become wider as the frequencies get higher because we become less concerned about variations. Afterward, we take the log of the filterbank energies. This is also done to mimic the human ear as we do not hear loudness on a linear scale. Then we compute the Discrete Cosine Transform (DCT) of the log filterbank energies. This is due to the fact that the filterbanks are overlapping, so we compute DCT to reduce the correlation between filter bank amplitudes. The resulting DCT coefficients are referred to as MFCC coefficients. Only 12 coefficients are kept and the rest are dropped, this is proven to improve the ASR performance. These 12 coefficients, together with the normalized energy, they form the feature vector.

Acoustic Model

The acoustic model provides a mechanism for computing the probability of a sequence of acoustic vectors Y given a word sequence w. To be able to do this, each word is broken into its constituent phones using the pronouncing dictionary, and we model each phone as a HMM. HMMs are statistical models that are used to predict a sequence of unknown random variables - hence the name "hidden" - from a set of observed variables. Here the unknown variable is the phones sequence, and the observed variables are the sequence of acoustic vectors. HMMs are Finite State Machines (FSM) based on the "Markov Assumption" which states that, in order to predict the future (next state), all we need to know is the present (current state) only, neglecting the past (previous states). i.e. $P(q_i|q_1,q_2,...,q_{i-1}) = P(q_i|q_{i-1})$. Each phone model has an entry state and an exit state which are used to connect different phone models together forming words, and words to be connected together forming sentences. The states are connected by arrows which represent the probabilities of moving from one state to another. Thus, a_{ij} represents the probability of moving from state i to state j. Each time t, the HMM changes state moving from state i to j with probability a_{ij} , and generating an acoustic vector $\mathbf{y_t}$ with probability $b_i(\mathbf{y_t})$. HMMs are also based on the "Output Independence

Assumption", which states that the probability of an output observation o_i depends solely on the state q_i that generated that observation, not on any other state or any other output observation. From that, the HMM is fully described by:

- 1. $Q = q_1, q_2, ...q_n$ A set of n states.
- 2. $A = a_{11}, ..., a_{ij}, ..., a_{nn}$ A transition probability matrix **A**, where a_{ij} is the probability of moving from state i to state j
- 3. $O = o_1, o_2, ..., o_T$ A sequence of **T observations**
- 4. $B = b_i(o_t)$ A sequence of **output probabilities**, where $b_i(o_t)$ is the probability of state i generating observation o_t
- 5. $\pi = \pi_1, \pi_2, ..., \pi_n$ An initial probability distribution over the states, where π_i is the probability that the HMM will start in state *i*. [17] [18]

For estimating the parameters A and B, there exists an algorithm called "Baum-Welch Algorithm" or "Forward-Backward Algorithm" for training these parameters. We do not go into the details of this algorithm in this literature, and refer to [17] and [3] for understanding this algorithm.

For decoding, *i.e.* searching for the sequence of words which maximizes equation 2.11, there are two main approaches: "depth first" and "breadth first". In depth first approach, the most reassuring branch is inspected until the end of the speech. In breadth first, which is referred to as "Viterbi Decoding", all hypotheses are inspected in parallel. We elaborate the decoding process in more details; formally, the decoding problem is defined as: given an HMM M = (A, B) and a sequence of observations (acoustic vectors) $\mathbf{Y} = y_1, y_2, ..., y_T$, find the most probable hidden state sequence (phone sequence). The Viterbi algorithm used for decoding is a dynamic programming algorithm that uses the dynamic programming trees or trellis. The algorithm goes by handling the observations sequence one by one, from left to right, and filling out the tree nodes as it proceeds. Each node in the tree has a value $v_t(j)$, this value represents the probability of being in state j after the first t observations and taking the most probable state sequence $q_1, q_2, ..., q_{t-1}$. The probability given by the cell value is described formally as: $v_t(j) = \max_{q_1,...,q_{t-1}} P(q_1, ..., q_{t-1}, o_1, ..., o_t, q_t = j | M = (A, B)$). We compute the value of each node by recursively taking the most probable path leading to that node. The value of each cell is computed as given by equation ??

$$v_t(j) = \max_{i=1}^{N} v_{t-1} a_{ij} b_j(o_t)$$
 (2.13)

where:

 $v_t(j)$ = previous path probability computed recursively a_{ij} = probability of transition from state i to state j $b_i(o_t)$ = probability of state j generating output o_t

This method is guaranteed to find the best sequence of phones and thus words, however it takes too much time and space. To overcome this problem, pruning of the search space is performed by using "beam search", where every point in time, highest node value is updated, and any node whose value is greater than the highest value plus the "beam width" is ignored. This way, only subset of the most probable probable state sequences are kept in memory at a time. This modification does not guarantee to find the most probable sequence of phones, however, it saves a lot of memory.

Language Model

The sole objective of the language model is to compute the probability of a word w_k given the previous words $W_1^{k-1} = w_1, w_2, ..., w_{k-1}$. "N-grams", are one of the earliest and simplest, but still efficient methods used for language modeling. As implied by the name, n-grams make the assumption that the probability of a certain word w_k , depends only on the previous n-1 words. More formally, $P(w_k|W_1^{k-1}) = P(W_{k-n+1}^{k-1})$. N-grams are pretty simple to compute; using frequency counts from textual data and storing them in look-up tables simply gets us the probability distribution. They also capture dependencies and semantics and hence are highly suitable for languages like English due to the fact that word order matters a lot and nearest neighbors contribute largely to the contextual meaning of a word. For more compound languages like German, higher order grams would be a more convenient choice.

2.3.2 Hybrid Systems

TODO 6 : Hybrid Systems PROBLEMS WITH HYBRID MODELS THE NEED TO SEGMENT THE DATA

Although RNNs seemed to be the best suit for sequence models, their use in speech recognition has been limited to hybrid models which do not make use of the full capabilities of the RNNs

2.3.3 End-to-End Systems

In 2006, Graves et al. introduced a novel way of using RNNs for labeling unsegmented sequence data which they called Connectionist Temporal Classification (CTC) [10]. We shall demonstrate their paper in this section. The basic idea is to model the RNN outputs as a conditional probability distribution over all possible sequences of labels given a certain input sequence. With that, an objective function is defined that tries to maximize the probability of the correct label sequence. The neural network can then be trained using standard BPTT.

Let L be a finite alphabet of labels and L^* is the set of all sequences over the alphabet L. Likewise, let S be a set of training examples which comprises pairs of sequences (\mathbf{x}, \mathbf{z}) , with $\mathbf{x} = (x_1, x_2, ..., x_T)$ being an input sequence of real-valued feature vectors, and $\mathbf{z} = (z_1, z_2, ..., z_U) \in L^*$ is a target sequence of labels which is at most the same length as the input sequence x. i.e. $U \leq T$. Our goal is to train a classifier h that uses the training examples set S to classify formerly unseen input sequences in a manner that minimizes our "label error rate". Label error rate is defined as the minimum number of insertions, deletions and substitutions required to change the predicted word into the ground-truth word.

The RNN output layer is a softmax layer, consisting of |L|+1 units. The first L units correspond to the probabilities of the L labels of our alphabet, the extra unit correspond to the probability of the output being no label, or "blank". This softmax layer corresponds to the probabilities of the entire possible permutations of labels, hence giving us the probabilities of all possible label sequences for a given input sequence.

For the purpose of investigating the matter in a more formal way, let us define alphabet $L' = \{L \cup blank\}$, and let L'T be all the label sequences of L' of length T, we refer to elements of L'T as "paths" and denote them as π . Also let y_k^t be the probability of the output being label k at time step t. With this, the probability of a certain path, given the input sequence is given by equation 2.14

$$P(\pi|x) = \prod_{t=1}^{T} y_{\pi_t}^t, \ \forall \pi \in L^{T}$$
 (2.14)

2.4. TEXT ANALYSIS

In equation 2.14, it is assumed that the network outputs at different time steps are independent. This is achieved by not allowing any feedback connection from the outputs to the network itself.

The next step is to remove all blanks and repeated labels from every path. This gives us a new set $L^{\leq T}$ which is the set of all possible label sequences having length less than or equal T defined over the alphabet L without the blank. We then can calculate the probability of a given label sequence l by simply summing the probabilities of all the paths producing that label sequence l. Note that after removing all blanks and repeated labels, many paths would generate the same label sequence. Hence, the probability of a certain label l is given by equation 2.15

$$P(l|x) = \sum P(\pi|x), \ \forall \ \pi \ generating \ l$$
 (2.15)

The output of our classifier should be the label sequence with the highest probability $h(x) = arg \max_{l \in L \leq T} P(l|x)$.

There are two efficient mechanisms for finding the most probable label sequence:

1. Best Path Decoding

Best Path Decoding is a greedy algorithm based on the assumption that the most probable path, corresponds to the most probable label sequence. The advantage of Best Path Decoding is that it is remarkably easy to compute; the most probable path is the concatenation of the most probable labels for every time step. The disadvantage is that does not ensure finding the most probable label sequence.

2. Prefix Search Decoding

Prefix Search Decoding works by calculating the probabilities of successive extensions of prefixes of label sequences. Despite Prefix Search Decoding being slower, it is guaranteed to identify the most probable label sequence. The drawback here is that the number of prefixes that must be expanded grows exponentially with the length of the input sequence. To overcome this issue, the authors of the paper make use of an observation which is that the outputs of a CTC network form spikes of labels with strongly predicted blanks. Using this observation, a certain threshold is chosen, and points with blank probabilities higher than that threshold are chosen as boundary points, forming sections or regions. For every region, we calculate the most probable label sequence for each region separately, and then we concatenate the results to get the final label sequence.

2.3.4 Deep Speech 2

TODO: Deep Speech Model

2.4 Text Analysis

Text analysis is defines as the procedure of extracting information and semantics from written text. Some famous text analysis tasks are text classification, document summarization, named-entity recognition and entity-relation extraction. Text classification is a class of NLP tasks which has been significant to many applications such as spam filtering, language identification, sentiment analysis, and email routing. Transfer learning is the process of using information learned from solving one problem in order to solve another different, but relevant problem. Transfer learning has gained great popularity in many fields like computer vision and text analysis due to the massive amount of data and enormous computational resources required in training deep neural models. Regarding text analysis, the main idea is to "pre-train" a large language model, using large amount of unlabeled text

corpora, and then "fine-tune" the model using a smaller labeled dataset to a specific task such as text classification, question answering, etc. The features learned from the first task has to be generic in order to be used in solving the second task, in case of text analysis, features are "word embeddings". Word embeddings map words to a high-dimensional vector space, where different words with similar meanings are grouped together in the vector space. Fine-tuning pre-trained language models liberates us from training from scratch which requires large datasets and long time for the model to converge. In section 2.4.4, we shall discuss Bidirectional Encoder from Transformer (BERT), which is a general language model proposed by google that could be pre-trained once, and fine-tuned for many downstream tasks, but prior to that, we discuss in the following three sections the underlying theory of some components in BERT, starting by the "Encoder-Decoder architecture", and going to the "Attention Model" and the "Transformer" which is the core component in BERT.

Encoder-Decoder architecture has been marked broadly useful in modeling sequence-to-sequence models, where the input is a sequence, and the output is as well a sequence. An example is machine translation, where a model is trained to find an output sentence y which maximizes the conditional probability of y given an input sentence x. We take a closer look at it in the next section.

2.4.1 Encoder-Decoder Architecture

The popular encoder-decoder architecture was first proposed by Cho et al. (2014a) [7] and Sutskever et al. (2014) [22]. This system consists of two RNNs which work together as an encoder-decoder pair (Figure 2.8). The encoder encodes a variable-length sequence (e.g. a sentence) into a fixed-length vector which we call summary vector \mathbf{c} . The decoder then uses this fixed-length vector to generate a variable-length output sequence. The vector \mathbf{c} has information from each data point in the input sequence.

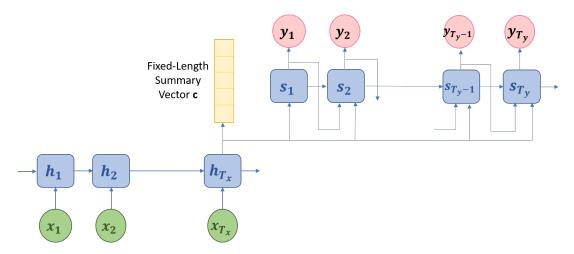


Figure 2.8: An Encoder-Decoder System. The encoder encodes a variable-length sequence into a fixed-length vector \mathbf{c} . The decoder uses the summary vector \mathbf{c} along with the previously generated predicted symbol from the previous time step y_{t-1} and the current hidden state $\mathbf{s_t}$ to generate an output y_t

The encoder is a RNN which has a hidden state $\mathbf{h_t}$ updated at each time step according to equation 2.16, where f is a non-linear activation function; Sutskever et~al.~(2014)~[22] uses LSTMs for this purpose while Cho et~al.~(2014a)~[7] uses a variation of LSTMs instead.

$$\mathbf{h_t} = f(x_t, \mathbf{h_{t-1}}) \tag{2.16}$$

The decoder is also a RNN that is trained to generate the output sequence \mathbf{y} one by one. Its hidden state $\mathbf{s_t}$, which is used to generate the output y_t is calculated according to equation 2.17,

2.4. TEXT ANALYSIS 15

where it is a function of the previously generated symbol y_{t-1} , the previous hidden state $\mathbf{s_{t-1}}$ and the summary vector \mathbf{c} . Similarly, the conditional probability of the target symbol is given by 2.18

$$\mathbf{s_t} = f(\mathbf{s_{t-1}}, y_{t-1}, \mathbf{c}) \tag{2.17}$$

$$P(y_t|y_1, y_2, ..., y_{t-1}, \mathbf{c}) = g(\mathbf{s_t}, y_{t-1}, \mathbf{c})$$
(2.18)

The two components are then trained to maximize the conditional probability of the output sequence $\mathbf{y} = (y_1, y_2, ..., y_{T_u})$ given the input sequence $\mathbf{x} = (x_1, x_2, ..., x_{T_x})$

The problem with this architecture is that the performance deteriorates as the length of the input sequences increases [6]. This is due to the difficulty of cramming all the necessary information into a fixed-length vector. In order to address this issue, the attention mechanism was introduced by Dzmitry *et al.* [2]

2.4.2 Attention Mechanism

Attention is the ability to focus on important details and discard irrelevant information. Dzmitry et al. (2015) [2] proposes modifying the encoder-decoder architecture through arming the decoder with "attention mechanism" which allows it to attend to only parts in the input sentence which are most relevant to the target word in the output sequence. The characteristic feature of this approach is that it doesn't encode all the input sequence into a fixed-length vector as the basic encoder-decoder approach explained in section 2.3.4. Instead, it encodes the input sequence into a number of vectors, and chooses which of these vectors are relevant to the target word in order to make a prediction. This approach performs better on longer input sequences as it is no longer needed to suppress all the information given in the sentence in one fixed-length vector. We demonstrate the model proposed by Dzmitry et al. (2015) [2] starting by the encoder, then the decoder.

I. Encoder

No major modifications were performed on the encoder, however, a BRNN was used instead of a uni-directional one (Figure 2.9). This is done in order to gather left and right context as discussed in section 2.2.2. By concatenating the forward hidden state $\overrightarrow{h_j}$ and the backward hidden state $\overleftarrow{h_j}$ for each word x_j in the sequence, an annotation $h_j = [\overrightarrow{h_j}^T, \overleftarrow{h_j}^T]$ for that word is obtained. The decoder would use these annotations later in the attention layer as we will explain.

II. Decoder

The decoder searches through the input sentence for the most for the most relevant data points when generating an on output. It is composed of a RNN that also uses the hidden state $\mathbf{s_i}$ to calculate y_i . The hidden state $\mathbf{s_i}$ of the decoder is calculated according to equation 2.19, where it uses the previously generated symbol y_{i-1} , the previous hidden state $\mathbf{s_{i-1}}$ and a context vector $\mathbf{c_i}$ in predicting the target symbol. The conditional probability of the target symbol is given by 2.20. The major difference here from the basic encoder-decoder approach is that there is a distinct context vector $\mathbf{c_i}$ for each target word y_i (Figure 2.9). The context vector $\mathbf{c_i}$ is calculated as a weighted sum of the sequence of annotations produced by the encoder as seen in equation 2.21. Each annotation h_i carries information from the entire input sequence with strong emphasis on parts closer to the i-th point of the input. The weights of the annotations are given by equation 2.22

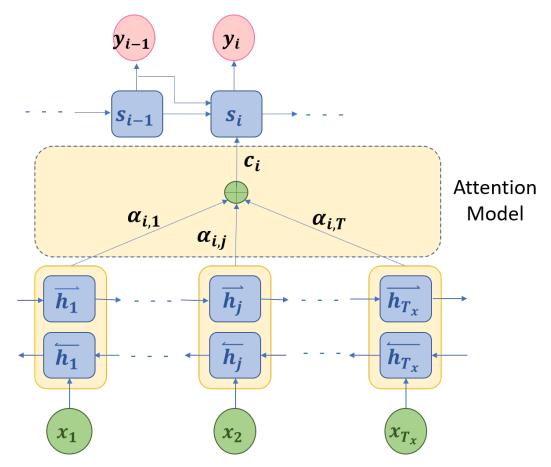


Figure 2.9: The modified encoder-decoder system implementing the attention mechanism. The output y_i has a corresponding context vector $\mathbf{c_i}$ which is a summation of the weighted annotations h_j . The most relevant annotations in the input sentence have the largest weights α_{ij} , while the least relevant annotations have the smallest weights.

$$\mathbf{s_i} = f(\mathbf{s_{i-1}}, y_{i-1}, \mathbf{c_i}) \tag{2.19}$$

$$P(y_i|y_1, y_2, ..., y_{i-1}, \mathbf{x}) = g(\mathbf{s_i}, y_{i-1}, \mathbf{c_i})$$
(2.20)

$$\mathbf{c_i} = \sum_{j=1}^{T_x} \alpha_{ij} h_j \tag{2.21}$$

$$\alpha_{ij} = \frac{exp(e_{ij})}{\sum_{k=1}^{T_x} exp(e_{ik})}$$
(2.22)

where $e_{ij} = a(s_{i-1}, h_j)$ is the attention model, or the "alignment model" which resembles the relevance between the target output at position j, and the inputs around position i in the source sentence. The alignment model a is a simple FNN which is trained with the other components.

Using the attention mechanism, there is no need to suppress all information of the input sentence into a single vector, instead the decoder knows for the output y_i where the relevant information lies in the source sentence through the context vector c_i

In 2017, Google came up with a novel architecture using only the attention mechanism and eliminated the use of RNNs, they called their model "The Transformer" [23] and we explain the idea behind it in the next section.

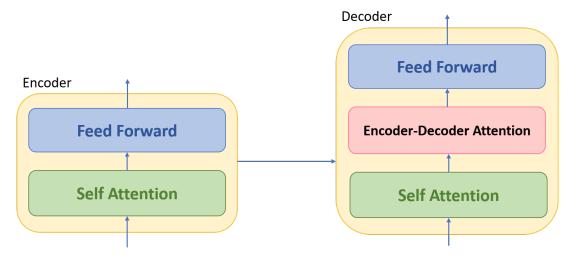


Figure 2.10: The Transformer architecture

2.4.3 The Transformer

Problem with Recurrence

As seen in equation 2.11, RNNs calculate the hidden state as a function of the current data point and the previous hidden state. This sequential nature of calculation largely suits the sequential nature of natural languages, however, this introduces a major problem as it hinders parallelization among the training inputs. This issue is manifested when the input sequences are of longer lengths. The Transformer abandons recurrence in order to achieve more parallelization and efficiency in performance.

The Transformer follows the prominent encoder-decoder architecture, however, introducing major modifications to both the encoder and the decoder. Both of them make use of what is called "Self-Attention" or "Intra-Attention".

I. Encoder

The encoder consists of N layers, each layer made up of two sub-layers. The first sub-layer is called "Self-Attention" sub-layer. This is one of the most influential changes proposed in the Transformer. What self-attention does is that it calculates the relevance of each word in the sequence to every other word in the same sequence. To demonstrate the gain we achieve with self-attention, consider the following example which highlight the problem of linking the pronouns to their antecedents: "The animal did not cross the street because it was too tired." A question very simple to humans such as "what does it refer to: the animal or the street?" isn't that simple to a model implementing no self-attention. This is owing to the fact that it did not learn any link between "it" and its antecedent when encoding the input sentence. Self attention allows the model to attend to other positions in the sequence when processing a certain position, in order to get a better encoding for this word (See Figure 2.12). The second sub-layer is a simple fully-connected feed-forward neural network. A residual connection [11] is applied to each sub-layer, then layer normalization [1] is performed.

II. Decoder

The decoder is made up from N layers as well, with each layer composed of three sub-layers: a self-attention layer similar to the self-attention layer implemented in the encoder, however, modified so that each word can attend only to words earlier in the sequence and not to consequent words, a feed-forward network, and an additional layer which implements the encoder-decoder attention as

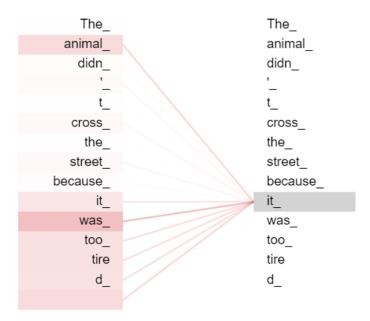


Figure 2.11: Self Attention Weights

explained in section 2.4.1. As in the encoder, residual connections are applied on each sub-layer followed by layer normalization.

Because the Transformer has no RNNs or Convolutional Neural Network (CNN)s, the position of each word in the sequence has to be modeled in some way. For this purpose, "positional encodings" [9] [23] are added to the input embeddings at the encoder and the decoder.

The Transformer model utilizes the attention mechanism in three different ways:

- 1. Self-attention layer in the encoder, where every token in the input sequence attends to every other token in the sequence.
- 2. Self-attention layer in the decoder, where every token in the output sequence attends to every other token up to that position in the sequence.
- 3. Encoder-Decoder Attention, where each position in the decoder attends to all positions in the input sequence. This is analogous to the attention implemented in [2]. (Refer to section 2.4.2)

In 2018, Google released a general-purpose "language understanding" model based on the Transformer and called it BERT (Bidirectional Encoder from Transformer). We demonstrate the idea behind it in the next section.

2.4.4 Bidirectional Encoder from Transformer (BERT)

As discussed earlier, transfer learning in NLP consists of pre-training a model using a large amount of unlabeled text data on a general task such as language modeling - *i.e.* predicting the next word in a sentence. The next step is to then make use of the learned information in solving a downstream task, such as text classification, text summarization, etc. Previously, transfer learning has been limited to context-free word embeddings. That means that for every word, there is a single word embedding generated, regardless of the context. For example: the word "bank" would have the same word embedding in "bank deposit" and "river bank". Limitations like such have motivated the use of deep neural language models that generate "contextual representations". The idea is to train a neural network model that maps a vector to each word taking into consideration the entire sentence, instead of having only one vector for the word regardless the context.

2.4. TEXT ANALYSIS

BERT is a method of pre-training contextual language representations, which has been inspired by similar works like REFERENCE Elmo and REFERENCE ULMfit. The distinctive feature of BERT over these methods is that in these models, words are conditioned either on the left context only, or combining the left context and right context in a trivial way. BERT, in contrast, was described in the paper REFERENCE as "deeply bidirectional", as each word is conditioned on both its left and right context in all layers in a deep neural network. We briefly demonstrate the model architecture and the pre-training tasks.

Model Architecture and Input Representation

BERT is based upon the transformer REFERNCE described in section ?? SECTION, where it consists of a multi-layer bidirectional Transformer encoder. In REFERENCE, two versions of BERT were introduced with different sizes; a relatively small model with 12 layers, 768 hidden size, and a total of 110M parameters, this model was used only for comparison purposes, and the authors refer to it as $BERT_BASE$. The larger model has 24 layers, 1024 hidden size, and a total of 340M parameters, they call it $BERT_LARGE$ and it achieves state of the art results on many NLP tasks.

As seen in figure 2.12, the input represents either a sentence pair, or a single sentence. For sentence pairs, the two sentences are separated by a special [SEP] token, and a sentence A embedding is added to the first sentence tokens, while a sentence B embedding to the second sentence tokens. For single sentences, only sentence A embedding is used. In addition to the segment embeddings, positional embeddings are also added in order to model the sequential nature of text. Instead of using whole words, word pieces are used REFERENCE. The input embedding of a given token is the sum of the corresponding token embedding, segment embedding and positional embedding.

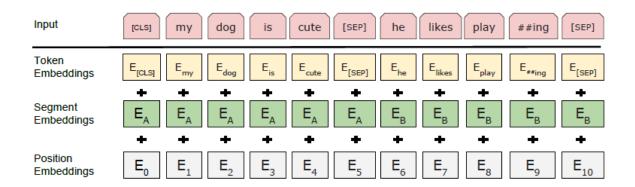


Figure 2.12: BERT input representation

Pre-training Tasks

Methodology

In this chapter, the methodology used to implement the system is illustrated. Firstly, an overview of the system is discussed, along with the datasets used. Secondly, an interpretation of the choice of architecture and decisions is elaborated. Eventually, the system implementation steps are demonstrated in detail.

3.1 System Overview and Datasets

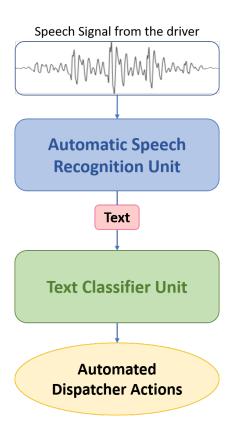


Figure 3.1: Automated Dispatcher Actions System comprising two sub-systems: Automatic Speech Recognition unit taking input as raw speech from the driver. The text output is fed into a trained Text Classifier which issues the proper action accordingly.

As discussed earlier, the main purpose of this study is to implement a system able to issue dispatcher actions automatically when provided with audio signals from the vehicle driver, hence, introducing more automaton in the control-center.

Our system consists of two sub-systems, as shown in figure 3.1, the first sub-system is the ASR unit, which takes as input raw speech waveforms produced by the driver, and produces the information in a text form. Then the text is passed to a trained Text Classifier, which given the text information from the ASR, issues the corresponding appropriate dispatcher action.

TODO IN THE CHOICE OF ARCHITECTURE NLP PROBLEMS TO MAKE AN END TO END SYSTEM

3.1.1 ASR Datasets

End-to-End ASR systems require large amounts of transcribed audio data. For this purpose we make use of three open-source German datasets and clean them. We list the three datasets here with the cleaning operations performed for each.

I. Common Voice

Common Voice is the largest open source, multi-language dataset of voices available for use. It is managed by Mozilla and was collected by volunteers on-line who were either recording samples or validating other samples. Mozilla began work on this project in 2017 and contribution to the dataset continues up till now. For our ASR, the German subset of the dataset was selected. It incorporates 340 total hours, with 325 validated hours and 15 invalidated hours which we excluded. The dataset has 5007 speakers but as we discarded the invalidated utterances we end up with only 4823 speakers. All the utterances were in "mp3" format and sampled using a sampling rate of 44kHz so we converted them to "wav" format and we performed down-sampling to obtain sample rate of 16kHz. We checked for any corrupted files but there were none.

II. M-AILABS Speech Dataset

M-AILABS Speech Dataset is an open-source multi-lingual dataset provided by Munich Artificial Intelligence Laboratories GmbH. Most of the data is based on LibriVox 1 and Project Gutenberg 2 . We make use of the German subset which is 237 hours 22 minutes with a total of 5 speakers. The data is available in "wav" format and sample rate of 16kHz so we perform no modifications. We also check for corrupted files but all of them were healthy.

III. German Speech Data [19]

This open-source corpus is provided by Technische Universität Darmstadt. It has 36 hours read by 180 speakers, and recorded using 5 different microphones simultaneously. They made use of the KisRecord ³ toolkit, which allows for recording with multiple microphones concurrently. Their target was distant speech recognition, thus a distance of one meter between speakers and microphones was chosen. The sentences which volunteers were provided to read were extracted randomly from three text resources: German Wikipedia, German section of the European Parliament transcriptions, short commands for command-and-control settings. Unfortunately, there were some corrupted files in the dataset, which we discarded.

TODO SPEAKER INDEPENDENT CLASSIFICATION

¹https://librivox.org

²https://www.gutenberg.org

 $^{^3 {\}rm http://kisrecord.source forge.net}$

- 3.1.2 Text Classifier Datasets
- I. German Wikipedia Dump
- II. 10K German Articles
- 3.2 Automatic Speech Recognition Unit
- 3.3 Text Classifier Unit

Results

Results

Conclusion

Conclusion

Future Work

Text

Appendix

Appendix A

Lists

NLP Natural Language Processing

NLG Natural Language Generation

NLU Natural Language Understanding

ANN Artificial Neural Network

FNN Feed Forward Neural Network

MLP Multi Layer Perceptrons

RNN Recurrent Neural Network

BPTT Backpropagation Through Time

BRNN Bidirectional Recurrent Neural Network

LSTM Long Short-Term Memory

ASR Automatic Speech Recognition

MFCC Mel-Frequency Cepstral Coefficients

FFT Fast Forier Transform

DCT Discrete Cosine Transform

CTC Connectionist Temporal Classification

HMM Hidden Markov Model

CNN Convolutional Neural Network

FSM Finite State Machines

BERT Bidirectional Encoder from Transformer

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