

## Problem Set #2

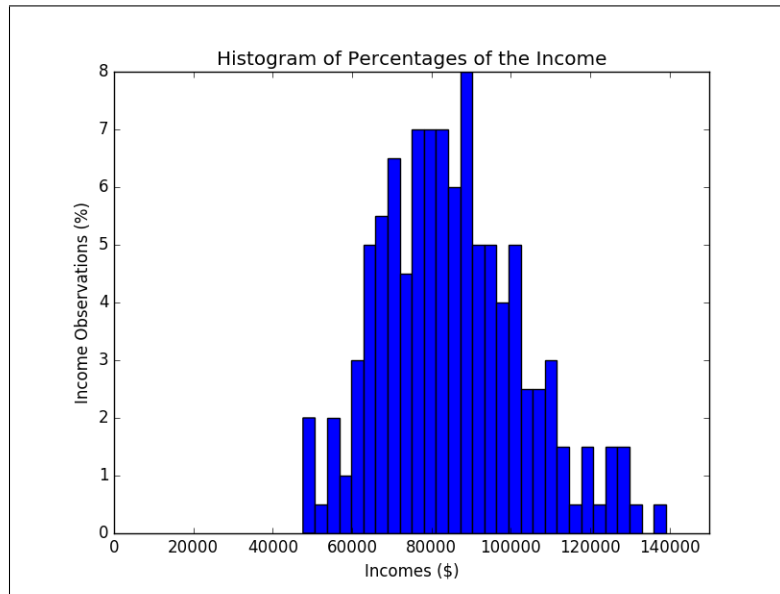
Perspectives on Computational Modeling

MACS 30100, Dr. Evans

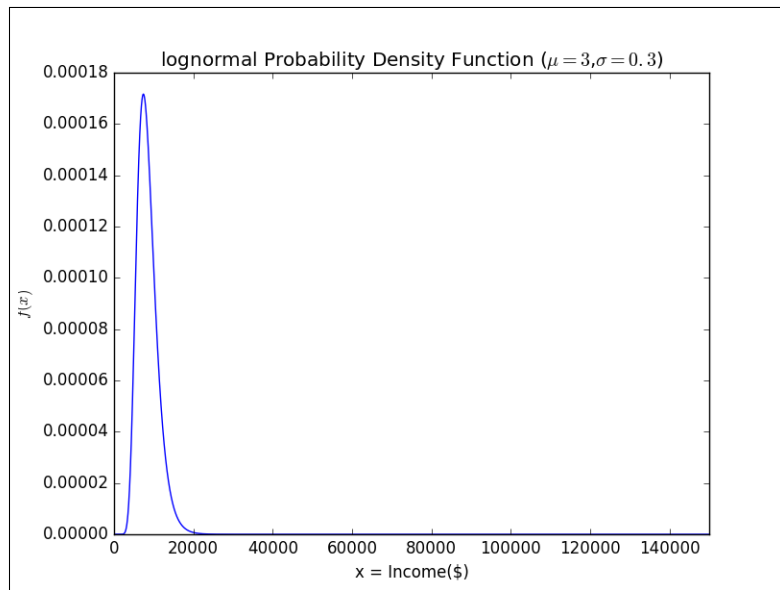
HyungJin Cho

### Problem 1.

#### Part (a). Histogram

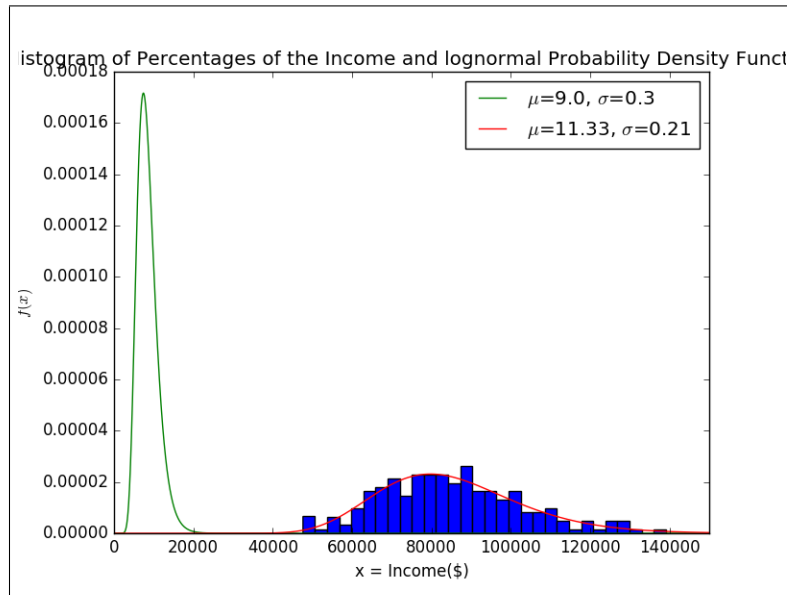


#### Part (b). lognormal PDF



Log-likelihood value = -8298.63695601

**Part (c). MLE**



$\mu$  MLE = 11.3314403326

$\sigma$  MLE = 0.211674580757

Log-likelihood Value = -2239.534744

VCV =  $\begin{bmatrix} 1. & 0. \end{bmatrix}$

$\begin{bmatrix} 0. & 1. \end{bmatrix}$

**Part (d). Chi-square Test**  $\chi^2$  of  $H_0$  with 2 degrees of freedom p-value = 0.0

**Part (e). Inference** The probability that you will earn more than \$100,000 is 19.561800210962077% The probability that you will earn less than \$75,000 is 30.79396097251101%

**Problem 2.**

**Part (a). MLE**  $\beta_0$  MLE = 0.259082991468

$\beta_1$  MLE = 0.0141522942932

$\beta_2$  MLE = 0.389203982613

$\beta_3$  MLE = -0.0106002331579

$\sigma^2$  MLE = 0.0159045883926

Log-likelihood Value = 876.865053329

VCV = [[ 1. 0. 0. 0. 0.]

[ 0. 1. 0. 0. 0.]

[ 0. 0. 1. 0. 0.]

[ 0. 0. 0. 1. 0.]

[ 0. 0. 0. 0. 1.]]

**Part (b). Chi-square Test** $\chi^2$  of  $H_0$  with 5 degrees of freedom p-value = 0.0