

Problem Set #2

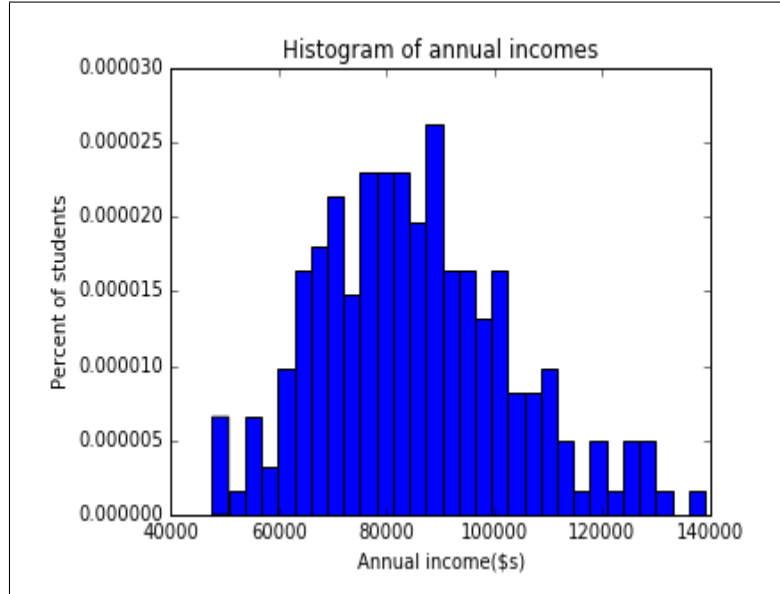
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Problem 1

Part (a). The histogram based on the given data is shown below.

Figure 1: Histogram of annual incomes



Part (b). The lognormal distribution pdf given the provided parameter is shown on the next page. The value of the log likelihood value for this parameterization of the distribution and given the data is -8298.63695601.

Part (c). The three overlaid plots as specified are shown on the next page. The ML estimates for μ and σ are 11.3314403742 0.211674571004 respectively, and the value of the log likelihood function is -2239.534744, and the variance-covariance matrix of MLE estimates is

$$\begin{bmatrix} 1.58680e-06 & 9.80377e-06 \\ 9.80377e-06 & 2.89832e-03 \end{bmatrix}$$

Part (d). After running the hypothesis testing we found the p-value is practically zero, which means that it is not possible that the given data came from the distribution specified in part (b).

Part (e). The probability that I will earn more than \$100,000 is 0.195618045405, and the probability that I will earn less than \$70,000 is 0.307939532566.

Problem 2

Part (a). The MLE value of standard deviation is 0.0164687775806, the MLE values of β_0 , β_1 , β_2 and β_3 are 0.253676099571, 0.0129218826337, 0.400370277848 and -0.0100195586474 respectively. The log likelihood function value using the maximum

Figure 2: Lognormal distribution pdf

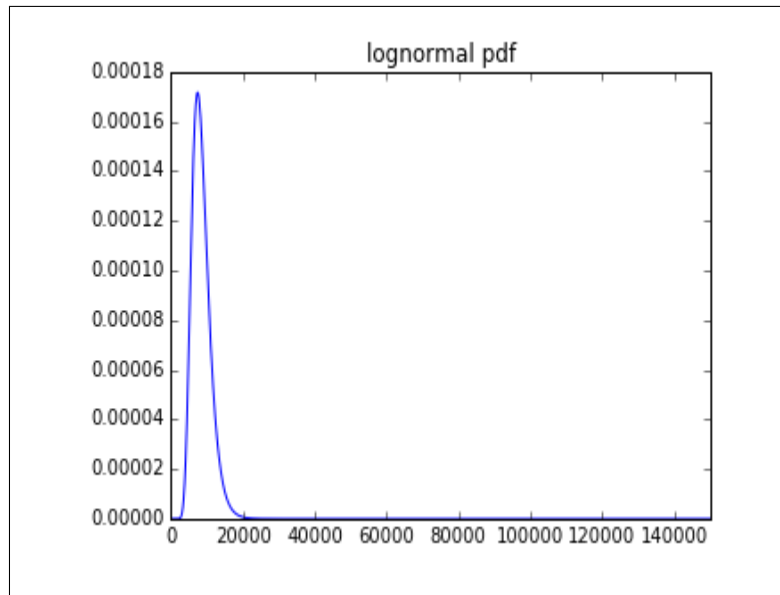
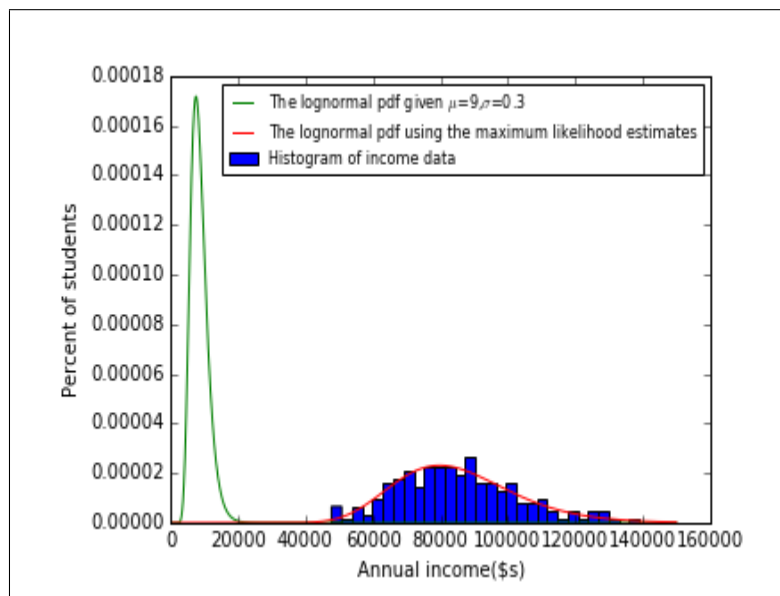


Figure 3: Three overlaid plots for comparison



likelihood estimates is 634.0363498426419, and the variance-covariance matrix of MLE estimates is

$$\begin{bmatrix} 1.0 & 0 & 0 & 0 & 0 \\ 0 & 1.0 & 0 & 0 & 0 \\ 0 & 0 & 1.0 & 0 & 0 \\ 0 & 0 & 0 & 1.0 & 0 \\ 0 & 0 & 0 & 0 & 1.0 \end{bmatrix}$$

Part (b). After running the hypothesis testing we found the p-value is again practically zero, which means it is not possible that the given data came from the linear regression model given the parameters specified in part (b).